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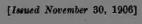
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Jus affectionales SARheldon

BIOMETRIKA.

WALTER FRANK RAPHAEL WELDON. 1860—1906.*

I. Apologia.

It is difficult to express adequately the great loss to science, the terrible blow to biometry, which results from the sudden death during the Easter vacation of the joint founder and co-editor of this journal. The difficulty of adequate expression is the greater, because so much of Weldon's influence and work were of a personal character, which only those who have enjoyed his close friendship can estimate, and which will only to some extent be understood should it ever be possible to publish his scientific correspondence. That correspondence is not only the most complete record of the development of the biometric conceptions, but the amplest witness to Weldon's width of knowledge, keenness of intellectual activity, and intense love of truth. It is marked by an extreme generosity to both friend and foe, which is not in the least incompatible with the use of frankly-perhaps it would be better to say playfully—strong language whenever the writer suspected unfair dealing, self-advertisement, or slipshod reasoning masquerading as science. Any form of publicity was very distasteful to Weldon; in particular he had a strong dislike for all forms of personal biography. The knowledge of this makes the writing of the present notice a peculiarly hard task. Yet Weldon's influence and activity must always be associated with the early history of biometry; if there be anything which can effectively aid younger workers in this field, it must be to realise that at least one man of marked ability and of the keenest scientific enthusiasm has devoted the most fertile years of his life to this new branch of science. Weldon's history is not written in a long series of published memoirs; much of his best work was unfinished at his death, and we can only trust that it will eventually be completed as the truest memorial to his life. But science, no less than theology or philosophy, is the field for personal influence, for the creation of enthusiasm, and for the establishment of ideals of self-discipline and self-development. No man becomes great in science from the mere force of intellect, unguided and unaccompanied by what really amounts to moral force. Behind the intellectual capacity

^{*} I have gratefully to acknowledge much aid from Mr A. E. Shipley in the preparation of certain parts of this memoir. K. P.

there is the devotion to truth, the deep sympathy with nature, and the determination to sacrifice all minor matters to one great end. What after all helps us is not that "he settled *Hoti's* business"...

"Properly based Oun—Gave us the doctrine of the enclitic De,"

but that the Grammarian had the strength of will which enabled him "not to Live but Know."

If there is to be a constant stream of men, who serve science from love as men in great religious epochs have served the Church, then we must have scientific ideals of character, and these do involve some knowledge of personal life and development. It is the abuse of the personal so prevalent in modern life, the mere satisfaction of a passing curiosity, which we have to condemn. But the personal which enables us to see the force of character behind the merely intellectual, is of value, because it moulds our working ideals. We see the environment—imposed and self-created—which favours scientific development, and we can with accumulating experience balance environment against heritage in the production of the highest type of scientific mind. From the standpoint that no man works effectively without a creed of life, that for width of character and healthy development there must ever be a proper balance of the emotional and the intellectual, it would be a distinct loss if the personal were removed from what we know of the lives of Charles Darwin and James Clerk-Maxwell. Science, like most forms of human activity, is occasionally liable to lose sight of its ultimate ends under a flood of controversy, the strugglings of personal ambition, or the fight for pecuniary rewards or less physical honours. The safety of science lies in the inculcation of high ideals among its younger votaries. A certain amount of purely human hero-worship is not to be condemned, and yet this is impossible without some knowledge of the personal. Weldon himself was no more free from heroworship than the best of his contemporaries. Of the men whose influence tended most to mould his life and career—F. M. Balfour, T. H. Huxley, Francis Galton—the personal side was not the smaller element. There was enthusiasm, hero-worship in its best sense, unregarding self-sacrifice in the defence of the man who had become for Weldon not only an ideal thinker, but an ideal character. defence of hero or friend, Weldon belonged to a past age, he was out with his rapier, before considering the cause; it was enough for him to know that one he loved or admired was attacked. A criticism of Huxley was to the end inadmissible; if at any point apparently correct, this appearance of correctness was due solely to the inadequate manner in which the facts of his life had been reported by biographers,—the class who pandered to the public love of the petty. It was in this spirit that Weldon received with delight the request to write for the Dictionary of National Biography, a scientific appreciation of Huxley's work. From Weldon's standpoint that appreciation should have formed the "Life." It is a fine piece of work and it was a labour of love, but those who have ever watched the younger man with the old, will know that the Huxley of the appreciation was not all that

Huxley meant to Weldon; the feeling of affectionate reverence did not spring from intellectual appreciation. It had far more its source in the influence of a strong character on a sympathetic character. And when we turn to Weldon himself, his relation to his friends and pupils was not purely that of a keen strong intellect; his best and greatest influence arose from the strength of character, that subtle combination of force and tenderness, which led from respect for the master, to keenest affection for the man.

If then we are to realise his life, it cannot be by a strict adherence to an appreciation of his published work. Some account of his stock, his early environment, and his temperament becomes needful, and the value of such an account lies in the help with which any life spent in single-eyed devotion to the pursuit of truth provides us, when we have ourselves to form our creed of life, and to grasp that science is something more than one of the many avenues to a competency. It must be in this spirit, therefore, that Weldon's dislike to the biographical is in a certain sense, not forgotten, but frankly disregarded in these pages.

II. Stock and Boyhood.

It would be impossible in a journal like Biometrika, devoted to the consideration of the effects of inheritance and environment, to pass by the striking resemblance of Raphael Weldon to his father Walter Weldon. The facts of Walter Weldon's life are given in the Dictionary of National Biography. It appears to have been a resemblance not only in intellectual bent, but also in many respects in emotional character. Raphael Weldon's paternal grandparents Reuben Weldon and his wife Esther Fowke, belonged to the manufacturing middle class. Their son Walter Weldon was born at Loughborough, October 31, 1832. Of his childhood we know little, he was as reticent as his son about both his childhood and his home surroundings; there is reason to suppose they were not wholly happy, and that shadows from these early years may have cast themselves not only over the father, but in a lesser extent have moulded the thought and life of the son. Walter Weldon married Anne Cotton at Belper, March 14, 1854, and shortly afterwards, leaving his father's business, came to London, starting as a journalist, writing for the Dial and Morning Star. Here he first made the acquaintance of William and Mary Howitt, who proved long and intimate friends of the family. From 1860 to 1864 he edited Weldon's Register of Facts and Occurrences relating to Literature, the Sciences and the Arts, and had as contributors a number of men afterwards well known in the world of letters. Thus while Walter Weldon's real name was to be made in science, his first interests were in literature and art. The steps by which Weldon regenerated the manganese peroxide used in the manufacture of chlorine, and the extensions he made of his chlorine process up to his death have been well described by Dr Ludwig Mond in his address in 1896 to the Chemical Section of the British Association. They brought Weldon comparative wealth, though nothing compared with the three-quarters of a million pounds his process saved They also brought him scientific reputation; a vicethis country annually.

presidency of the Chemical Society, and in 1882 the fellowship of the Royal Society. But for our present purposes the main point is this: that Walter Weldon made his discovery while totally unacquainted with the methods of quantitative chemical analysis and possibly because of this ignorance. He was accustomed to attribute the discovery to a peculiar source, but those who knew well the immense facility of his son for closely observing phenomena out of his own field of research, and rapidly studying their interaction, always probing things, whether in the physical universe, or in mechanism, to their basis in simple laws of nature, will at once realise the source of the father's inspiration, and the heritage to the son*.

If Walter Weldon's discovery brought him wealth, he was generous to a fault. Like his son he appears to have scarcely known the value of money, except as a means of giving pleasure to his friends. His early death in September, 1885, two years after his son's marriage, cut off a career far from completed. But his life had been lived to the full, each instant crowded with physical, intellectual, or emotional activity. It is impossible to regard Walter Weldon's character without seeing whence Raphael Weldon drew much of his nature. The intense activity, the keen sympathy and generosity, the reticence, the creative power in many channels, the artistic appreciation †, were common to father and son. Nay, perhaps to give

* Raphael Weldon delighted during his many voyages in spending days in the engine-room: he made a study of the various types of engines, and his knowledge in this respect was not without service to the Marine Biological Association. He even studied the use of indicator diagrams. His first plan with a new bicycle was to take it part from part, so that he could fully understand its working and the nature of possible repairs. The microscope was not merely an instrument to work with, but a familiar illustration of optical laws, so that he knew at once how to modify each detail to suit special needs. Over and over again, talking over physical problems he would say: "Well, I don't know what you people think, but it has always seemed to me that "-and then would come some luminous suggestion or apt criticism of a proposed investigation in a field wholly outside the biological. A striking instance of this occurred only in the autumn of last year. Many friends had already gone to see the eclipse, most people were talking about it, and Weldon was left in sultry Oxford, fighting out a theory of determinantal inheritance. It was settled that a holiday should be taken, the determinants put on one side and a continuous photographic record made of the eclipse. Neither Weldon nor his colleague knew anything about sun-photography, and miserable were their first attempts. But gradually the objective, the telephoto lens and the focal shutter were worked out; a camera which had done yeoman service in photographing snail habitats became a wonderful structure, and a whole series of colour screens prepared from biological sources were tested and criticised. It was Weldon who obtained the first clean cut photograph showing sun spots clearly and admitting of definite enlargement. But what is more, each developmental stage of his sun camera had been thought out physically, and he knew why he took it. The trained physical astronomer would have found the stages already made, and a posteriori each would have been obvious, but this was the case of a biologist with insight into other fields and a striking power of making things work.

† An interesting illustration of the relationship is given in Mary Howitt, an Autobiography, 1889 (p. 184). The child Raphael, then 10 years, had gone with his father and the Howitts to visit the Wiertz Gallery at Brussels. William Howitt writes: "On our first entrance I was quite startled, I did not think I should at all like the paintings, they appeared so huge, so wild and so fantastic. But by degrees I began to see a great mind and purpose in them...... Little Raphael came and took my hand as we left the gallery, and said: 'Mr Howitt, I think Wiertz could not be a good man.' I asked him why. He answered, 'I think he could not be a good man, or he would not have painted some things there.' I told him he might naturally think so, but that a vast deal was to be allowed for his education. No doubt Wiertz thought all was right, and that many of his pictures contained

expression to a paradox, their volume of life was too great to be compatible with its normal length. There are men—not the least favoured of the Gods—who live so widely and so deeply, that they cannot live long. Discussions on the inheritance of longevity now come back to the memory, wherein Weldon referred to stocks of short-lived but intense life, and the personal experience and its moulding effect on character are now clear, where at the time the mind of the listener ran solely on a correlation coefficient.

In one respect Raphael Weldon differed widely from his father. Walter Weldon turned naturally to the mystical to satisfy his spiritual cravings; he was a Swedenborgian, and ipso facto a believer in intercourse with another world. Whether owing to a difference of training or of temperament, these things were to Raphael Weldon uncongenial. He was through the many years the present writer knew him, like his hero Huxley, a confirmed Agnostic. Sympathetic as every cultured mind must be with the great creations of religious faith; knowing more than many men of religious art—painting, sculpture, and music—he yet fully realised that these things had for him only emotional, no longer intellectual value*. It may be that the difference of training made this distinction between father and son, for the latter's mind was keenly alive to spiritual influences. A solitary fortnight with the beloved Dante was not solely pleasure; the re-perusal of the Inferno left its sombre influence on Weldon's thoughts for long after, testifying not only to its author's supremacy, but to the spiritual impressibility of the reader's nature.

It may be that the difference was due to heritage from the mother's side. Of Anne Cotton we know little, she died in 1881, when Raphael Weldon had just taken his degree. She appears to have exercised a rather stern discipline, which had greater influence on Raphael, than on his brother Dante. She was a devoted companion to Walter Weldon, and a resourceful helpmate in his early struggling days. A daughter Clara born in 1855 died in 1861. Of his childhood Weldon rarely spoke. He was born in the Highgate district, and shortly after his birth his parents removed to a three-gabled house on the West Hill still standing. Here we get occasional peeps of a solitary child who would retire for hours under the dining-room table with his Shakespere, learning whole acts by heart. At six years old he appears in Mary Howitt's letters as staying at Claygate near Esher.

great and useful lessons. His father came up and added that when Raphael was older he would see those lessons more clearly than he could now."

The prophecy was fulfilled, in perhaps rather a different way. The little Raphael became a big Raphael who did not look to art "for great and useful lessons," and who refused to study Ibsen because undiscerning critics made current the idea that his art was subservient to inculcating a lesson.

* The "fulness of life" admitted, nay demanded, many a visit to cathedral service, especially in Italy. Even a study of Gregorian music was entered upon, and the writer recollects many a summer's afternoon spent in visiting the churches of Oxfordshire and Berkshire,—the cycle ride, the keen eye on surrounding nature, not only from the standpoint of the biologist, but of the artist; then the break to the religious past, the "biometric tea" at the village inn; the return journey towards evening and the discussion which touched many things, from Draba verna to the Norsemen in Sicily. The "volume of life" was there, as it was in the midnight talks in Wimpole Street or in the discussions in the study at Merton Lea.

⁺ See R. S. Proc. Vol. xLvi. "Obituary Notice of Walter Weldon," p. xix. et seq.

"We find little Raphael Weldon one of the best of children. Secker is mowing the grass at this moment, and he harnessed like a pony is drawing the machine. The Pater calls him 'Young Meritorious.'" And again:

"[Agnes] and Raphael are the best of friends, and their ringing laughter comes to us in the garden through the open window, as they sit in the dining-room painting the Stars and Stripes and the Union Jack for each other's amusement... Agnes is a little free-spoken American full of fun and dash. Raphael more silent and contemplative. They sit painting pictures together for hours at a time. I feel quite proud of them both."*

In 1870 comes the flying visit to Brussels; in 1872 a still more memorable first visit to Paris, where the destruction caused by the Commune to the Tuileries and other buildings much impressed the boy. The Weldons had moved meanwhile to The Cedars, Putney, and shortly afterwards went to the Abbey Lodge, Merton, near Wimbledon. The visits and the changes give one the impression of a rather broken education. We have no record of what school Raphael Weldon attended, if any, at Highgate. At Putney he had as tutor a neighbouring clergyman. In 1873 he was sent to a boarding-school at Caversham, and from this time onwards the educational career is more definite.

Even before 1870, however, we find in the boy the father of the man. His great pleasure was to organise lectures for his children friends, and the adult population, if it could be procured. The seats were formally arranged, tickets provided, and the boy would discourse on slug or beetle procured in the garden, observation and the scanty literature available providing the material. According to a surviving auditor the lectures were carefully prepared and good so far as they extended.

Of the school at Caversham we have some detailed information. Mr W. Watson, its headmaster, had been a private 'coach' in London to University College students. In 1865 he opened a school at Reading, which was transferred to the hill out of Caversham in 1873†. Mr Watson's daughter Ellen Watson had a brief but brilliant career as a mathematician and pupil of W. K. Clifford's. Her life has been written by Miss Buckland. It is possible that she first stirred Weldon's mathematical tastes, as he spoke with admiration of her powers; she does not, however, appear to have taught in the school. The pupils were chiefly sons of Nonconformists of some eminence. Among the earlier scholars were Viriamu Jones, Alfred Martin, and E. B. Poulton, and among the later pupils Owen Seaman, F. W. Andrewes, P. Jacomb-Hood, and W. F. R. Weldon; names afterwards distinguished in literature, science, or art. The headmaster appears to have been a clever man of wide knowledge and sympathy, but there was little to specially encourage biological tastes in the school. It is reported of one under-

^{*} Loc. cit. p. 162 et seq.

[†] As an illustration of Weldon's reticence I may state that we had passed this house several times together, before he mentioned it as his old school.



Raphael Weldon Aged 10.

		•

master that he protested against the study of insects, asking: "How do you think that such pursuits will put a leg of mutton on your table?" and the ability that proceeded from the school has been attributed by one of its former pupils to the special class from which it drew its chief material.

III. Lehrjahre.

Weldon did not remain fully three years at this school. It was followed by some months of private study and he matriculated at 16 (1876) in the University of London. In October of '76 we find him at University College taking classes in Greek, English, Latin, and French, with two courses of pure mathematics. In the summer term of 1877 physics and applied mechanics were studied. During this whole session he also attended Daniel Oliver's general lectures on botany and Ray Lankester's on zoology. He used to come up to town for Oliver's 8 o'clock lectures, getting his breakfast at a bun-house on the way*. Of his education at University College he especially praised in after years Olaus Henrici's lectures on mathematics. They were he held most excellent, and he considered Henrici the first born teacher under whom he came. Later in the Christmas vacation of 1879, after he had gone up to Cambridge, he researched for some weeks under Ray Lankester, who set him to work out the structure of the gills of the mollusc Trigonia. This completes Weldon's relations as a student to University College.

The difficulty of access, or possibly Walter Weldon's strong views, led Raphael Weldon in the autumn of 1877 to transfer himself to King's College. Here he stayed for two terms attending classes in chemistry, mathematics, physics, and mechanics, beside the zoology course of A. H. Garrod and the biology of G. F. Yeo. Divinity under Barry, at that time I believe compulsory, was also taken. At this time Weldon had the medical profession in view. He was only entered on the Register of Medical Students on July 6, 1878, but there can be no question that his course on the whole was directed towards the Preliminary Scientific Examination of the London M.B. This examination he took in December, 1878, after he had gone up to Cambridge; he was coached for it by T. W. Bridge, now Professor of Zoology in Birmingham, but he had already completed the bulk of the work in his London courses. With the Preliminary Scientific, Weldon's relation to London ceased. His student career there was not of quite two years' duration and it dealt with a variety of subjects, dictated as much by Weldon's catholic tastes, as by the discursiveness of the London examination schedule. But in his case, as in that of others, the grounding he received in physics and mathematics became a valuable asset, and the taste for languages, afterwards so emphasised, was to some extent trained and coordinated with literary knowledge. Yet Weldon's earlier instinct to study biology was not substantially modified either by the choice of medicine as a profession or by the diversity of his London studies. In 1877 he attended the Plymouth Meeting of the British Association, and there he was generally to be found in Section D.

^{*} Weldon states in his applications for the Jodrell and the Linacre Chairs that he commenced the study of zoology under Lankester in 1877.

The presence of a life-long friend, who had already gone to Cambridge, was at least one of the causes which led to Weldon's entering himself as a bye-term student at Cambridge, and probably his choice of St John's College was due to Garrod's influence. He was admitted on April 6, 1878, as a pupil of S. Parkinson's. In the record his father is given as a "Journalist," although the chlorine process had now become a success, and his reference is to the Professor of Mathematics at King's College, then W. H. Drew*.

At Cambridge Weldon soon found his work more specialised and he rapidly came under new and marked influences. His first May term and Christmas term were devoted to his preparation for Little-Go and the London Preliminary Scientific. For the classical part of the former he seems to have worked by himself. After these examinations were over reading for the Tripos was begun and, under the influence of Balfour, Weldon's thoughts turned more and more to zoology, and the medical profession became less and less attractive. During the years 1879 and 1880 Weldon worked steadily for his Tripos; in the first year he was given an exhibition at St John's, and almost the only break in his work was the York Meeting of the British Association. In the second year a little original investigation on beetles was started; in May he took, for a month, Adam Sedgwick's place and demonstrated for Balfour. Overwork led to a serious breakdown, and resulted in insomnia and other ills, which occasionally troubled him again in later life. At the annual British Association holiday, this year in Swansea, Weldon saw for the first time Francis Galton, but an actual friendship was not begun till some years later.

The Tripos work was continued in spite of ill-health, till the Easter of 1881, when Weldon was unable to enter for the college scholarship examinations. By the influence of Francis Balfour, however, Weldon's real ability was recognised and a scholarship was awarded to him. A three months' holiday had become necessary, and Weldon went to the south of France, returning only shortly before his Tripos examination. At the very start of this, in itself all-sufficient, mental strain, Dante Weldon, who had joined Peterhouse, died suddenly of apoplexy. says much for Weldon's self-control that the terrible shock of his brother's death, though it greatly affected him, did not interfere with his place in the first class of the Natural Sciences Tripos. The distress he had felt at his brother's death was redoubled a few weeks later when his mother passed away. She had never recovered from the blow resulting from the tragic death of her Of these things Weldon did not speak, but they undoubtedly influenced immensely his deeply emotional nature. Balfour's untimely death in the following year, and the early death of Weldon's father a few years later, left also their indelible impresses, a certain tinge of melancholy, a doubt whether he too would live to finish his work, and a tendency to take the joy and fulness of life while it was there. Few who saw the almost boyish delight in work and in play, the energy which spent itself for hours at a problem, or cycled eighty or a hundred

^{*} There are errors in the entries in the Register, Weldon's mother's maiden name is erroneously given as Chester, not Cotton. Weldon was actually born at Suffolk Villa, Highgate.

miles in the day, the activity in debate, the vigour in lecture, the flow of thought and talk to the midnight hours, realised that the man was not of iron physique, and had indeed but small reserves of strength. To see Weldon keen over a piece of work was to believe him robust and ready for any fray; but looking back on the past one can see what each piece of work cost him, and the strain on a highly nervous temperament began in even those early Cambridge days.

J IV. Wanderjahre.

With the Tripos Weldon's Lehrjahre closed and, as his nature directed, the Wanderjahre began without any interval of rest. Immediately after his Tripos, Weldon started for Naples to work at the Zoological Station. We have seen that at Cambridge he had been a pupil of F. M. Balfour's, whose death from an Alpine accident in the July of 1882 was the greatest loss British zoology had sustained for years. The charm of Balfour's personality had aroused the affection of all who attended his classes, and had awakened a keen desire to follow, even if but a long way behind, in his footsteps. In those days the stimulus given by Darwin's writings to morphological and embryological researches was still the dominating factor amongst zoologists, and Weldon threw himself at first with ardour into the effort to advance our knowledge by morphological methods. In Naples he began his first published work, a "Note on the early Development of Lacerta muralis" (1), but at the same time did much miscellaneous work on marine organisms. The lizard paper was finished in the winter at Cambridge, Weldon gratefully acknowledging the help of Adam Sedgwick, in whose laboratory he was then working. Anticipation in the publication of some of the results by C. K. Hoffmann, who had been working at the same points, caused a not unnatural disappointment.

In September Weldon was back in England at the Southampton meeting of the British Association. Here Adam Sedgwick, who had succeeded to the teaching work of Francis Balfour, invited Weldon to demonstrate for him. Thus the winter found Weldon in Cambridge again, and from Sedgwick's laboratory was issued the next piece of work: "On the Head-Kidney of Bdellostoma, with a suggestion as to the Origin of the Suprarenal Bodies" (2). Weldon hoped to show that "at all events in Reptiles and Mammals, the connection between the Wolffian body and the suprarenal is much more intimate than has generally been supposed," and he followed the matter up in the next year by publishing his paper "On the Suprarenal Bodies of Vertebrates" (3).

Meanwhile a great change had come over Weldon's personal life. On March 14, 1883, the anniversary of his parents' wedding-day, he was married to Miss Florence Tebb, the eldest daughter of William Tebb, now of Rede Hall, Burstow, Surrey, which formerly, after he left Merton, had been the house of Walter Weldon. The Weldons and Tebbs had been intimate friends for many years, and Miss Tebb had been at Girton while Raphael Weldon was at St John's. At Cambridge the new Statutes had just come into force, marriage was the order of the day, and houses were even difficult to procure. The Weldons on their return from a tour in France

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took Henry Fawcett's furnished house and settled down in Cambridge for the May term. Raphael Weldon still had his scholarship, and he was demonstrating for Sedgwick. He was now compelled to undertake "coaching,"—work which he gave up as soon as his means would allow of it, for his whole heart was then as afterwards in research. Still this coaching work brought him in touch with many men who afterwards distinguished themselves in biological or other fields.

After the death, on the 14th January, 1883, of Forbes, a fellow Johnian, Weldon for four months—June 15 to October 15—acted as locum tenens for the Prosector at the Zoological Gardens, London, and during that time he read the following papers before the Zoological Society: "On some points in the Anatomy of Phoenicopterus and its Allies" (4); a "Note on the Placentation of Tetraceros quadricornis" (5), and "Notes on Callithrix gigot" (6). Weldon did not succeed Forbes—it was rumoured that some of the electors doubted the fitness of his physique for the work and considered that the post was not without danger. But the temporary work into which he threw his usual energy gave him increased insight into vertebrate anatomy and had the further advantage of making him personally known to the active workers in zoology of the metropolis.

In the following year (1884) the paper above referred to on the development of the suprarenal bodies was published in the R. S. Proceedings. Weldon was now demonstrating in comparative anatomy at Cambridge, and the holidays were devoted to collection. At Easter Banyuls was visited, and the summer vacation found Weldon in Naples again for three months preparing his fellowship dissertation. In Naples the cholera had broken out, and the Weldons experienced not only difficulty in getting the precious dissertation back to England, but in returning themselves. This was done by an Orient liner, the last allowed to call. Thus began the long series of holidays in Italy with the sea passage to or fro. The summer heat of Naples seemed to suit Weldon, and he could work and think under circumstances which only allow mere existence to an ordinary Englishman. On returning to Cambridge, Weldon was elected to a fellowship at St John's College on November 3rd, and was shortly afterwards appointed University Lecturer in Invertebrate Morphology. About this time the Weldons took a permanent home at No. 14, Brookside, which soon became a centre for Cambridge workers in biology*. The Weldons' home, whether in Cambridge, London, or Oxford, was always a centre, where not only the right people met, but whence actual profit came by the right people interchanging ideas and planning work.

On his return to Cambridge in November 1884 Weldon had taken up again his invertebrate work. His next memoir "On Dinophilus gigas" (7) dealt with the anatomy and affinities of Dinophilus, at that time a very little known Annelid. A. E. Shipley had been fortunate enough to collect a number of these minute worms at Mounts Bay, Penzance, and had handed them over to Weldon for

^{* &}quot;The house in Brookside in which he lived after his marriage until he left Cambridge was a delightful and hospitable centre, where all sorts of subjects were discussed, attacked and defended until all sorts of hours in the morning." A. E. S.

description. The latter gave a full account of their anatomy and added a careful discussion on the affinities of the genus, expressing his belief that while it is "related on the one hand to *Archiannelida*, it retains on the other many features characteristic of the ancestor common to those groups (especially Chaetopods, Gephyreans, Mollusca, Rotifers and Crustacea) which possess a more or less modified trochosphere larva."

The next few years of Weldon's life were—if it be possible to make any comparative where all were intense-more active than ever. He had now given up coaching, and as he only needed to be in Cambridge two terms of the year, travel and research could occupy the time from the beginning of June to January. On May 8, 1885, Weldon gave his first Friday evening lecture at the Royal Institution on "Adaptation to surroundings as a factor in Animal Development." No report is published in the Proceedings of this lecture, but there are those who still remember the impression caused by the youthful lecturer of 25 years of age. And here may be a fitting place to say something of Weldon's lecturing power. There are two distinct sides to lecture work; the instruction of small or large classes of students and the public oration. Success in the one field does not necessarily connote success in the other. In the former case the eye must be kept on the average student, the lecturer must realise what the individual auditor is feeling, he must expand his exposition or must contract it to meet the carefully observed needs of his audience, for he knows that he can take up the subject again on the next occasion exactly where he has left off. In this form of lecturing Weldon was an adept, it brought out all his force and enthusiasm as a teacher. As a writer in the Times (April 18, 1906), says:

"Seldom is it given to a man to teach as Weldon taught. He lectured almost as one inspired. His extreme earnestness was only equalled by his lucidity. He awoke enthusiasm even in the dullest, and he had the divine gift of compelling interest."

In public lecturing on the other hand, with a time limit and an unknown audience, the personal touch with individuals is impossible. There is no time to elaborate points, the whole matter must be a priori fitted to the time, and if the audience is not grasping an idea, then the lecturer must put both explanation and disappointment on one side; he must make his audience jump gladly, and trust to better luck in his exposition of the next stage of his thesis. Shortly, he must feel his audience with him as a whole and pay no regard to the individual.

Weldon's own intense thoroughness made him only too conscious when a portion of his audience were not following him; his highly nervous temperament made it a necessity that he should have a sympathetic grip on the individual. This made for success in his lectures to students; but it brought also a factor of uncertainty into his public lectures. The most carefully prepared discourse, and no man gave more time and energy than Weldon to preparation*, might be

^{*} Drafts and re-drafts were written, elaborate diagrams painted, or lantern slides made and coloured by Weldon himself.

spoiled by Weldon's consciousness that certain members of the audience were not following him. He would then turn his exposition into explanation of minor points, so that the lecture would not be completed, or he would settle down to speak to the few he realised to be following him, and neglect the audience as a whole. If a portion of his audience were hostile or actively unsympathetic, this always prevented Weldon from reaching his best; it formed a strain on the lecturer's nervous temperament, which could only be realised by those of like fibre, and in some cases left its permanent mark. Thus it came about that the success of a public lecture by Weldon could not a priori be measured; it depended far too much on the audience. Individual lectures at the British Association, the London Institution, at University College or elsewhere were brilliant achievements, but at the same places on other occasions, Weldon was not so successful, for no man was ever more responsive to immediate environment than he was. To do his best and to be at his best he needed essentially a sympathetic environment. Weldon has been spoken of as an eager, ready and dramatic debater, keen to see a weak joint in his opponent's armour and quick in putting his own case with telling effectiveness. This is undoubtedly true, but it needs the qualification that this intellectual readiness when in full action meant a high pressure; it was a strain the less oft repeated the better. A torpedo-boat destroyer is associated with a 26 knot speed, and such speed differentiates it from other vessels of war; but the less it is run at this rate, the longer undoubtedly it will last. Controversy was not an atmosphere in which Weldon rejoiced*; it came to him because he felt bound to criticise what he held to be error, because he must defend a friend, but it was—running the destroyer at 26 knots!

This digression may be justified on the ground that we have reached the period when Weldon began to exercise a personal influence over his students at Cambridge, and the sources of that influence are to be found first in the lecture-room and then in strong personal sympathy. In the lecture-room he always impressed his hearers with the importance of his topic. You could not listen to him lecturing on a flame-cell or on the variations in the carapace of Pandalus annulicornis without sharing his intense conviction of the importance of the matter in hand. He aroused a consciousness in his students that things were worth studying for their own sake, apart from their examination value.

The summer months of 1885 were spent in Guernsey, and the death of Walter Weldon in the September of this year kept Raphael Weldon at other things than research. Christmas, however, found the Weldons at Rome. The Lent and May terms (1886) were spent in Cambridge as usual. In June came a visit to the south of France on Chlorine business, but in July came freedom, the crossing to America and the visit to the Bahamas in August to collect. From his

^{*} Actual experimental work which upset another man's views, Weldon declined to publish. "Yes, I know he is wrong, but I don't want merely to controvert him, I want to get at the truth of these things for myself." And when he had satisfied himself he would pass on to a new point of investigation and never publish at all.

headquarters in the Bahamas Weldon went with two friends to North Bimini in the Gulf stream and enjoyed immensely his first experience of tropical or at least semi-tropical seas. He made considerable collections, but his published results were confined to "Haplodiscus piger; a new Pelagic organism from the Bahamas" (8), and a "Preliminary Note on a Balanoglossus Larva from the Bahamas" (9). Haplodiscus was netted near the Island of New Providence. It is a member of the Acoela, the most simplified of the class Turbellaria, and for some time Weldon's account was one of the most complete we had of any member of this group. Working at the Balanoglossus material in 1887, Weldon found that his results differed from those reached by Professor Sprengel. He accordingly went to Giessen at Easter,-his second visit to Germany, the first having been at Christmas, 1886-and finally handed over to Professor Sprengel the whole of the Balanoglossus material he had collected in the Bahamas. During the Lent and May terms Weldon came up from Cambridge and gave a course on Economic Entomology to the forestry students at the Royal Engineering College, Cooper's Hill. The summer and autumn of this year involved a meeting of the British Association at Manchester, a visit on Chlorine business to France, and later, collecting and working in Guernsey. The Christmas was spent at Plymouth.

In 1888 the buildings of the Marine Biological Laboratory in Plymouth were nearly completed, and the visits to Plymouth now replaced those to Guernsey. To the Marine Biological Association Weldon gave both time and sympathy during the rest of his life. His annual visits of inspection to Lowestoft during the last few years were always a great pleasure to him, and he was preparing for and talking of this year's visit only a few days before his death. Lent and May terms, 1888, were spent as usual in Cambridge, but June to December were given up to Plymouth, with a brief Christmas holiday in Munich. And here we must note the beginning of a new phase in Weldon's ideas. His thoughts were distinctly turning from morphology to problems in variation and correlation. He has left on record the nature of the problems he was proposing to himself at this time and they are summed up as follows:

- (1) The establishment of a new set of adult characters leading to the evolution of a new family has always been accompanied by the evolution of a new set of larval characters leading to the formation of a larval type peculiar to the newly established family; the two sets of characters having as yet no demonstrable connection one with the other.
- (2) The evolution of the adult and that of the larval characters peculiar to a group advance pari passu one with the other, so that a given degree of specialisation of adult characters on the part of a given species implies the possession of a larva having a corresponding degree of specialisation and vice versa.

The next year was to place in Weldon's hands a book—Francis Galton's Natural Inheritance, by which one avenue to the solution of such problems, one quantitative method of attacking organic correlation, was opened out to Weldon;

and from this book as source spring two of the friendships and the whole of the biometric movement, which so changed the course of his life and work. In 1889, the year of the issue of this book, another change also came. Weldon found that his dredging and collecting work separated him from his books for half his time. Accordingly, he applied for a year's leave from Cambridge, and the Weldons settled down in a house of their own at Plymouth. This period of hard work lasted through 1890, and was broken only by flying visits to Dresden in September and at Christmas, 1889, and an autumn visit in 1890 to Chartres and Bourges. intellectual development and the experience and knowledge gained in this period were far more important than the mere published work would indicate. In 1889, Weldon investigated the nature of the curious enlargement of the bladder associated with the green, or excretory, glands in certain Decapod Crustacea, and published in October of the same year his paper on "The Coelom and Nephridia of Palaemon servatus" (10). The result of his investigation was to confirm "the comparison so often made (by Claus, Grobben, and others) between the glomerulus of the vertebrate kidney and the end-sac of the Crustacean green gland." A little later, June 1891, Weldon published the results of more extended researches in this field in what proved to be his last strictly morphological paper. It was entitled: "The Renal Organs of certain Decapod Crustacea" (11). In this he showed that in many Decapods spacious nephro-peritoneal sacs "should be regarded rather as enlarged portions of the tubular system...than as persistent remnants of a 'coelomic' body cavity into which the tubular nephridia open."

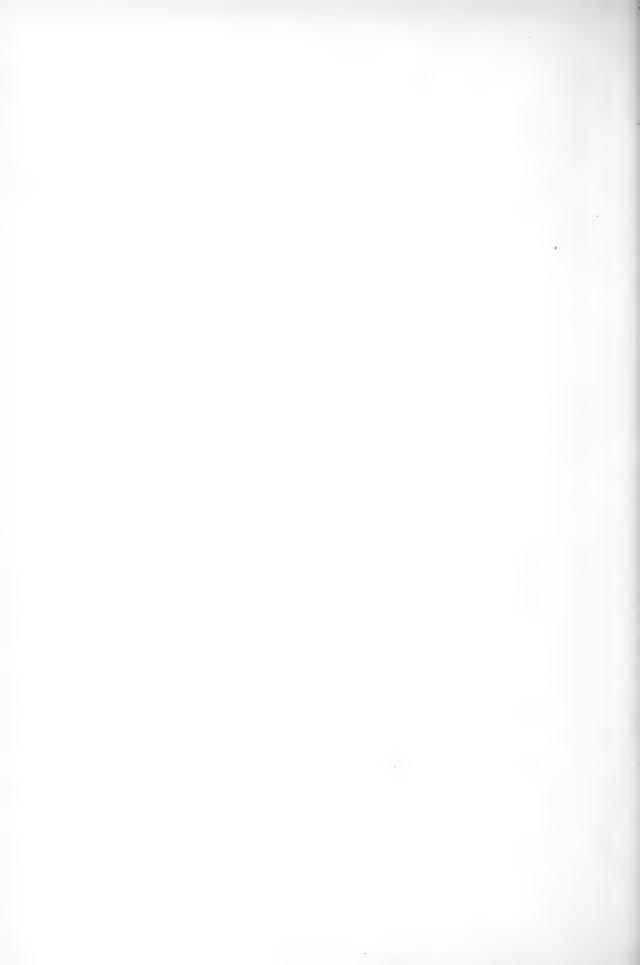
One further paper of a year later may be best referred to here, Weldon's only piece of work on invertebrate embryology, "The Formation of the Germ Layers in Crangon vulgaris" (12). This contains a clear account of the early stages of segmentation and the building up of the layers of the shrimp, illustrated by excellent figures. And here it may be mentioned that Weldon's power with the pencil was not that of the mere draughtsman, accurate in detail, but too often lifeless. Weldon was an artist by instinct, and he had the keenest pleasure in drawing for its own sake. His brilliant blackboard drawings will be remembered by all his students; some correspondents will remember elaborately beautiful sketches sent merely to illustrate a passing question, where a rough diagram would have sufficed; a delicately pencilled shell to please a child friend; carefully copied architectural details to gratify himself and made to be destroyed;—all signs of a real artistic power of creation. And the sense he enjoyed in himself, he appreciated in others. Nothing refreshed him so much as a visit to the National Gallery, or to a lesser extent the sight of more modern art. Weldon, smiling before one of his own pictures, unconscious of his environment, was good to behold, and made one realise how for him pictures were still differentiated from In the last two years of his life, when he had become an ardent photographer, the artistic feeling came to play a prominent part as the difficulties of the craft were one by one mastered.



(a) "L'Apparition: Le Café Orleans."



(b) H. Hortensis, from a letter.



December, 1890, closed the Cambridge work* and concluded the Wanderjahre. Weldon now succeeded Ray Lankester in the Jodrell Professorship at University College. In June he had been elected a Fellow of the Royal Society largely on the basis of his first two biometric papers, which will be considered more in detail in the next section.

It will be seen that the years between Weldon's degree and his first professoriate were years of intense activity. He was teaching many things, studying many things, planning many things. His travels perfected his linguistic powers, and his fluency in French, Italian and German was soon remarkable. But while this added immensely to his delight in travel, it opened to him also those stores of literature, which appealed so strongly to his artistic temperament. From the mediaeval epics to Balzac he was equally at home in French literature; and the Italian historians were read and carefully abstracted, that he might understand Dante without the aid of a commentator, and appreciate Italian towns without the help of a guide-book. In German he had a less wide knowledge of the earlier literature and history, but he spoke the language with an accent and correctness remarkable in an Englishman. In later years he had commenced the study of Spanish, the Romance tongues and literatures being always more sympathetic to him than the Scandinavian or Teutonic. His remarkable thoroughness in science reappeared as a form of scholarly instinct when he approached history and literature, and the present writer remembers Weldon's keen pleasure and exactitude in following up more than one historical enquiry. His delight in knowing spread far beyond the limits of natural science.

V. London and the First Professoriate, 1891–1899.

A word must here be said as to the transition which took place during the Wanderjahre in Weldon's ideas. He had started, as most of the younger men of that day, with an intense enthusiasm for the Darwinian theory of evolution; it threw open to him, as to them, a wholly new view of life with its possibility of seeing things as a connected whole. Weldon realised to the full that the great scheme of Darwin was only a working hypothesis, and that it was left to his disciples to complete the proofs, of which the master had only sketched the

^{*} A note may be added as to the general influence of Weldon at Cambridge. At the time Weldon began lecturing there were a considerable number of students largely attracted to Cambridge by Balfour's fame and remaining there to mourn his loss. Mr W. Bateson of St John's, Dr Harmer of King's, Professor Sherrington of Caius, Professors D'Arcy Thompson and J. Reynolds Green of Trinity, Professor Adami and Mr A. E. Shipley of Christ's, graduated in 1883 and 1884, and all, to some extent, came under his influence. For six years (1884–1890) he gave advanced lectures to the candidates for Part II of the Natural Sciences Tripos. During these few years the number of men in his class who have since done much to advance science was considerable. The following is by no means a complete list. Among botanists, F. W. Oliver, C. A. Barber, W. B. Bottomley; among geologists, T. T. Groom, P. Lake, S. H. Reynolds, H. Kynaston and H. Woods; among physiologists, pathologists and medical men, A. E. Durham, H. E. Durham, J. S. Edkins, W. B. Hardy, A. P. Beddard, E. H. Hankin, H. Head; and among zoologists, H. Bury, G. P. Bidder, W. F. H. Blandford, R. Assheton, F. V. Theobald, T. H. Riches, E. W. MacBride, H. H. Brindley, A. T. Masterman, C. Warburton, and Malcolm Laurie.

outline. Naturally he turned first to those methods of proof, morphological and embryological, which were being pursued by the biological leaders of the period, and it was only with time that he came to the conclusion that no great progress could be attained by the old methods. We have already seen that even before the appearance of Natural Inheritance, Weldon's thoughts were turning on the distribution of variations and the correlation of organic characters. He was being led in the direction of statistical inquiry. The full expression of his ideas is well given in the first part of the "Editorial" with which Biometrika* started:

"The starting point of Darwin's theory of evolution is precisely the existence of those differences between individual members of a race or species which morphologists for the most part rightly neglect. The first condition necessary, in order that any process of Natural Selection may begin among a race, or species, is the existence of differences among its members; and the first step in an enquiry into the possible effect of a selective process upon any character of a race must be an estimate of the frequency with which individuals, exhibiting any degree of abnormality with respect to that character, occur. The unit, with which such an enquiry must deal, is not an individual but a race, or a statistically representative sample of a race; and the result must take the form of a numerical statement, showing the relative frequency with which various kinds of individuals composing the race occur."

It was Francis Galton's Natural Inheritance that first indicated to Weldon the manner in which the frequency of deviations from the type could be measured. A mere catalogue of exceptional deviations seemed to him of little value for the study of Natural Selection. But this description of frequency was only the first stage. How did selection leave the distribution? and How was the intensity of selection to be measured? naturally arose as the next problems. These problems led at once to the even greater question of the influence of selection on correlation. What is the relation between organs in the same individual, and how is this changed, if at all, by the differentiation of species, or at least by the establishment of local races? Nor could the problem of evolution be complete without ascertaining the manner in which deviations were inherited. The modern biometric methods of discussing these problems, if very far from fully developed, were at least suggested in Galton's great work, and that book came as a revelation not only to Weldon, but to others who were preparing to work on similar lines†.

In Plymouth, 1890, Weldon started his elaborate measurements on the Decapod Crustacea and soon succeeded in showing that the distribution of variations was closely like that which Quetelet and Galton had found in the case of man. So far as the present author is aware, the paper "The Variations occurring in certain Decapod Crustacea I. Crangon vulgaris" (13) was the first to apply the methods of Galton to other zoological types than man‡. In this paper Weldon shows that different measurements made on several local races of shrimps give frequency distributions closely following the normal or Gaussian law. In his next paper,

^{*} Vol. 1. p. 1.

⁺ The present writer's first lecture on inheritance was given on March 11, 1889, and consisted of an exposition and amplification of Galton's theory.

[‡] Galton had dealt with the weights of sweet pea seeds, Merrifield with the sizes of moths, but they had not published fitted frequency distributions.

"On certain correlated Variations in Crangon vulgaris" (14), Weldon calculated the first coefficients of organic correlation, i.e. the numerical measures of the degree of interrelation between two organs or characters in the same individual. It is quite true that the complete modern methods were not adopted in either of these papers, but we have for the first time organic correlation coefficients—although not yet called by that name—tabled for four local races. These two papers are epoch-making in the history of the science, afterwards called biometry.

It is right to state that Weldon's mathematical knowledge at this period was far more limited than it afterwards became. The first paper was sent to Francis Galton as referee, and was the commencement of a life-long friendship between the two men. With Galton's aid the statistical treatment was remodelled, and considerable modifications made in the conclusions. But the credit of making the vast system of measurements, of carrying out the necessary calculations (now with the aid of his wife, who was for years to assist in this part of the work), of seeing a priori the bearing of his results on the great problems of evolution, must be given to Weldon. Nor must we forget the rich suggestiveness of these papers. Weldon was on the look-out for a numerical measure of species. He was seeking for something constant for all local races, and although his suggestion that the correlation coefficient was a constant for local races has not been substantiated the "selection constant," the quantity uninfluenced by racial differentiation, being of a much more complex nature—yet his suggestion directly led up to the investigation of correlation in man, animals and plants, and has given us immensely clearer ideas on the inter-relationship of organic characters. And Weldon realised

"A large series of such specific constants would give an altogether new kind of knowledge of the physiological connexion between the various organs of animals; while a study of those relations which remain constant through large groups of species would give an idea, attainable in no other way, of the functional correlations between various organs which have led to the establishment of the great sub-divisions of the animal kingdom*."

The defect in mathematical grasp, which Weldon had realised in his first paper, led him at once to seek to eliminate it. He sought first to 'enthuse' a mathematician with his project of demonstrating Darwinian evolution by statistical enquiries. A visit was paid to Cambridge with this end in view, but it did not lead to the required result. Weldon then set about increasing his mathematical knowledge by a thorough study of the great French writers on the calculus of probability. He did not turn to elementary text-books but with his characteristic thoroughness went to the fountain head. Turning over his papers now, it is astonishing to notice the completeness of his studies as evidenced by his notes and abstracts. He thus attained to a very great power of following mathematical reasoning and this power developed with the years. He never reached a high wrangler's readiness in applying analysis to the solution of new questions, possibly this requires years of training in problem papers; but he was able to follow and

criticise extremely complicated algebraical investigations, and to reproduce and often simplify them for the use of his own students. He had, however, a touch with observation and experiment rare in mathematicians. In problems of probability he would start experimentally and often reach results of great complexity by induction. Thus he was able to find out a number of problems relating to the correlation between a throw of n dice, and the result obtained when a re-throw of m out of the number n was made, and others relating to the mixture of n packs of cards and the throwing out of random portions*. In all these cases Weldon was illustrating by a game of chance a definite biological process.

From 1890 onwards, Weldon's knowledge, theoretical and experimental, of the theory of chance increased by bounds. Weldon and the present writer both lectured from 1 to 2, and the lunch table, between 12 and 1, was the scene of many a friendly battle, the time when problems were suggested, solutions brought, and even worked out on the back of the menu or by aid of pellets of bread. Weldon, always luminous, full of suggestions, teeming with vigour and apparent health, gave such an impression to the onlookers of the urgency and importance of his topic that he was rarely, if ever, reprimanded for talking 'shop.'

It is difficult now, after fifteen years of common work and continuous interchange of ideas, to distinguish where one or other idea had its source, but of this the writer feels sure, that his earliest contributions to biometry were the direct results of Weldon's suggestions and would never have been carried out without his inspiration and enthusiasm. Both were drawn independently by Galton's Natural Inheritance to these problems, but the papers on variation and correlation in shrimps—which in rough outline are types of all later biometry—were published before their friendship had begun.

Weldon's work at University College commenced in 1891. The house in Wimpole Street was taken and, if possible, life became more intense. Easter was spent at Chartres. In the summer came the annual visit to Plymouth, where work on crabs was now to replace that on shrimps. September gave some rest with a sea trip to Malta. In October came the college inaugural lecture for the session, Weldon taking as his subject the statistical treatment of variation. At Christmas there was a break for opera in Munich and Dresden. This year and the next were strenuous years in calculating. The Brunsviga was yet unknown to the youthful biometric school; the card system of correlating variables was still undeveloped, we trusted for multiplication to logarithms and Crelle, and computors trained to biometric work had to be created. The Weldons toiled away at masses of figures, doing all in duplicate. At Easter, 1892, they went to Malta and Naples, and the summer was spent over crab-measurements at the zoological station in the

^{*} In the summer of 1905 a great deal of work was done by the present writer in conjunction with Weldon on mixtures of card packs, the main features of the work having been already outlined by Weldon. The results are summed up in a theory of determinantal inheritance which, it is hoped, will be eventually published.

latter city, and the first biometric crab paper "On certain correlated Variations in Carcinus moenas" (15) was issued in this year. In this paper Weldon confirms on the shore crab his results for the common shrimp. The distributions of characters are closely Gaussian with the exception of the relative frontal breadth, which Weldon considered dimorphic in Naples, a problem which led to the present writer's first paper in the Contributions to the Mathematical Theory of Evolution. It is right to say that Weldon had reached a moderately accurate solution by trial and error before he proposed the problem to his colleague. He does not refer to this fact in his memoir. As for shrimps the correlations again came out closely alike for the Plymouth and Naples races. Weldon was not dogmatic on the point; he considered the constancy as at least an "empirical working rule" and this it has certainly proved.

"The question whether this empirical rule is rigidly true will have to be determined by fuller investigation on larger samples; but the value of a merely empirical expression for the relation between abnormality of one organ and that of another is very great. It cannot be too strongly urged that the problem of animal evolution is essentially a statistical problem: that before we can properly estimate the changes at present going on in a race or species we must know accurately (a) the percentage of animals which exhibit a given amount of abnormality with regard to a particular character; (b) the degree of abnormality of other organs which accompanies a given abnormality of one; (c) the difference between the death rate per cent. in animals of different degrees of abnormality with respect to any organ; (d) the abnormality of offspring in terms of the abnormality of parents and vice versâ. These are all questions of arithmetic; and when we know the numerical answers to these questions for a number of species we shall know the deviation and the rate of change in these species at the present day—a knowledge which is the only legitimate basis for speculations as to their past history, and future fate."

These concluding words were surely epoch-making; they formulated the fundamental principles of biometry. We may criticise the memoir in that the index measurements selected by Weldon overlooked the question of spurious correlation, or because the growth law of the indices had not been previously determined. But these are minor matters compared with the general ideas involved in the memoir. It is a paper which biometricians will always regard as a classic of their subject. It first formulated the view that the method of the Registrar-General is the method by which the fundamental problems of natural selection must be attacked, and that is the essential feature of biometry.

Besides biometry a new bond drew Weldon and the present writer together. Since 1884, a strong movement for the reform of the University of London had been in progress, association followed on association, royal commission on royal commission. Few people had distinct ideas of what they themselves wanted, scarcely any one had a notion of what a real university must connote. At University College, after severe crises, the teaching staff had won direct representation on the governing body, and was beginning to insist upon being heard in the question of university reform. One of the most vigorous protagonists in this matter was Lankester, and his removal to Oxford threatened the little group who had definite notions of academic reform with complete defeat. Luckily Weldon joined us

and his energy and enthusiasm were of immense service. We had to fight our own College authorities as well as outside influences. It is not now the fitting occasion to tell the complete history. A joint letter to the *Times* roused the authorities, there were rumours of dismissal from chairs, and of wiser counsels prevailing solely at the instance of a distinguished Liberal statesman then on the College Council. The authorities were supporting a scheme which would have united King's and University Colleges in a second-rate and duplicate London University to be termed the Albert University, and rebellion had to go to extremes, if this project was to be defeated. Weldon with the help of one or two colleagues circularised every member of the College, and the night before the discussion of the charter a widely signed petition against it was in the hands of every member of the House of Commons; the Albert charter was dead, and the College Council hopelessly defeated.

The destructive attitude was now dropt; at a meeting in Wimpole Street, Weldon, G. Carey-Foster and the present writer drafted the scheme, afterwards accepted with small modifications, of an "Association for Promoting a Professorial University for London." The idea was to bring all the London teachers into one camp, to get them to accept a common ideal, and to enlist support for it among thinking men outside. The ideal was the foundation of a university in which teaching should be done by the university professors only, who should largely control the university; the separate colleges were to be absorbed. The aim was thus expressed:

"The creation of a homogeneous academic body with power to *absorb*, not to federate existing institutions of academic rank, seems the real solution of the problem. An academic body of this character might well be organised so far as teaching is concerned on the broad lines of a Scottish University. Such a corporation may be conveniently spoken of as a professorial university to distinguish it from a collegiate or federal university."

The Association met a real need, the London teachers to our surprise and joy joined readily. We got the support of great names in literature and science. We produced a distinct effect on public opinion and by our witnesses even on the Royal Commission. But we considered that we ought to have a leader of great name, and we asked Huxley to be president. Huxley accepted, and came to us with views diverging to some extent from those of the initiators of the Association. Instead of holding up an ideal of academic reform, his plan was to find the minimum which would be accepted by various opposed interests and compromise on the basis of this. The alternatives were a long campaign to impress the powers that be with true notions of academic life, or the immediate acceptance of a teaching university, which should be an omnium gatherum of all the teaching institutions in London. The present writer resigned the secretaryship of the Association, and was succeeded by Weldon. It was only after very anxious consideration that the open letter of the former to Professor Huxley of December 3, 1892, was sent to the Times*. It was a course which Weldon strongly condemned.

^{*} Personal requests to join the Association had been made to many on the basis of a circular containing the words cited above, the spirit of which was directly repudiated by Huxley.

At a general meeting of the Association held on December 21, 1892, the report of the Executive Committee was received, and after a strong speech from Huxley, adopted. It was then moved by Pearson, and seconded by Unwin: "That the Association trusts that its Executive Committee will persevere in its efforts to establish as far as possibly may be a professorial as distinguished from a federal university." This was carried. At the meeting of the Executive Committee on January 24, 1893, the President presented his own scheme for a teaching University for London; a vague motion to prepare a scheme to be submitted to the Association was, at the instance of Pearson, seconded by Lankester, amended as follows: "That the Committee prepare a scheme to be submitted to the Association in general accordance with the proposals adopted by the Association." This was carried. On January 25, 1893, Huxley wrote withdrawing his scheme on the ground that the amendment moved by Pearson and seconded by Lankester was "incompatible with any progress towards attainable ends." At the following meeting of the Committee in February, Professors Carey-Foster, Rücker, and Pearson were asked to prepare a scheme embodying the principles of the "proposals" of the Association as a basis for the charter of the proposed university. Mr Dickens and Professor Weldon were added to this committee. The scheme was actually prepared and Weldon aided with yeoman service in the drafting of it*. But the influence of the Association was dead; it never recovered from the divisions thus manifested in its executive. The spirit of compromise and the fatal easiness of federation dominated the situation and the present University emerged out of the chaos. No one felt more bitterly than Weldon the contrast between the original ideal and the result achieved. In fact, it is not too much to say that the greatest hopes for the University, and its most progressive steps since its incorporation, lie in the endeavours made to carry out in part the ideal of a homogeneous professorial university, as it was originally developed one Sunday evening in the house in Wimpole Street, and later substantially reproduced in the proposals of the Association.

This account of one movement, however, with which Weldon was closely concerned would not be justified here, did it not illustrate strongly a marked characteristic of the man. He found his great leader attacked, as he and some others believed, unwarrantably. He wrote one very strong private letter on the point, and never referred to the matter again; not the slightest breach was caused in his friendship, and the biometric talks, the common work and plans for work were resumed a day or two afterwards as if no source of friction had for a moment arisen. Yet Weldon always felt deeply, and felt this attack on Huxley more than many men would feel a direct personal attack on themselves.

With the death of Huxley in 1895, the Association practically came to an end. Weldon succeeded his hero in 1896 as Crown nominee on the Senate of the University; here, as on the Board of Zoological Studies of the later reconstituted

^{*} The scheme was printed and adopted by the Association, March 23, 1893.

University, he continued to work and fight for truer ideals of academic administration.

As an administrator and committeeman Weldon combined geniality with strong convictions; he saw at once through flimsy pretexts, and expressed clearly and concisely his own point of view,—"An impulsive loveable man going to the heart of any subject immediately, and always speaking up with great feeling for what he thought right," is how one of his former colleagues aptly describes him. But he lacked several of the essentials which go to make the completely effective committeeman. He was always full of the current piece of research and he grudged all time taken from it; to carry through his own projects he did not adopt the manner of the bull and crush down all opposition; some few men can do this, but it needs not only physique, but its combination with very dominant intellectual power; nor had he the persistency of the corncrake, to wear down his colleagues by continual nagging; nor silent in committee would be molelike be active underneath, "lobbying" his men, and thus more effectually work his will. These types I have known and each was less loved, but more successful than Weldon. He "played the game," threw firmly and well the lance for the cause he thought right, and went his way. He remained to the end the public school or 'varsity lad, whom the idea of "good form" controlled; but unfortunately the type is not so persistent in practical life that it dominates scientific or academic politics. From this standpoint Weldon's death removed from the field a healthy administrator, who acted as a tonic upon weaker colleagues. It was in this sense that he did excellent work, not only on various bodies connected with University College and the University of London, but on the Council of the Royal Society (1896-8), and on its Government Grant and Sectional Committees.

To the biometrician, perhaps, the most interesting committee with which Weldon was associated in these years was that which came later to be called the Royal Society Evolution (Animals and Plants) Committee. It is somewhat difficult to give the full history at present, but some attempt at a sketch of Weldon's connection with it must be made here. Weldon's papers on variation and correlation in shrimps and crabs had brought him closely in touch with Francis Galton, and both were keenly interested in the discovery of further dimorphic forms such as had been suggested by the frontal breadths of the Naples crabs. Weldon was full also of other ideas ripe for investigation. He had started his great attempt at the measurement of a selective death-rate in the crabs of Plymouth Sound; experiments on repeated selection of infusoria were going on in his laboratory; he was gathering an ardent band of workers about him, and much seemed possible with proper assistance and that friendly sympathy which was ever essential to him.

The idea that a group of men can achieve more than a single investigator, if true in some forms of social work, is rarely applicable to scientific committees; but such committees have often been tried in the past, and will no doubt be again attempted in the future. If used as instruments of research, the work done is too

often a compromise between different methods and divergent personalities; if merely administrative they are successful or not, according to the width of view of some dominating temperament. If run in the interests of one school, still more of one individual, a committee may no doubt do good work, but it is likely, at the same time, seriously to damage the reputation of any larger body in whose name it works, by too markedly connecting it with one aspect of a problem or one side of an unsettled controversy. These difficulties of the situation seem only by degrees to have come home to the founders of the Evolution Committee.

The project was first discussed informally by R. Meldola, Francis Galton, and Weldon, at a meeting held on the 9th of December, 1893, at the Savile Club. Francis Darwin, A. Macalister, and E. B. Poulton had expressed themselves willing to assist such a project. It was settled that a proposal should be made to the Royal Society for the formation of a committee "For the purpose of conducting Statistical Enquiry into the Variability of Organisms," the members suggested being F. Darwin, F. Galton, A. Macalister, R. Meldola, E. B. Poulton, and W. F. R. Weldon, to whom "it may afterwards be desirable to add a statistician." It was resolved further to ask for a grant of money to obtain material and assistance in measurement and computation.

A Committee* consisting of these members was finally constituted by the Council of the Royal Society, with Francis Galton as chairman and Weldon as secretary, the Committee being entitled: "Committee for conducting Statistical Inquiries into the Measurable Characteristics of Plants and Animals." The use of the words statistical and measurable, somewhat narrowly, but accurately, defined the proposed researches of the Committee. It went on until 1897, with these members, the same title and scope. Then in the early part of that year its scope was much extended by adding to its objects the "accurate investigation of Variation, Heredity, Selection, and other phenomena relating to Evolution," and W. Bateson, S. H. Burbury, F. D. Godman, W. Heape, E. R. Lankester, M. Masters, Karl Pearson, O. Salvin and Thiselton-Dver were added to its number. But at present our account must deal with the earlier biometric period of the Committee. Looking back on the matter now, one realises how much Weldon's work was hampered by this Committee. It is generally best that a man's work should be published on his own responsibility, and when he is a man of well-known ability and established reputation, grants in aid can always be procured. In this case Weldon had a sympathetic committee, but the members were naturally anxious on the one hand for the prestige of the Society with whose name they were associated, and secondly, they were desirous of showing that they were achieving something †. Both conditions were incompatible with tentative researches such as biometry then

^{*} First meeting, January 25, 1894.

^{† &}quot;Of course these considerations only make the problem more interesting than it was before: and I very much want to solve it. But the committee may say that it requires a problem which is reasonably certain to yield an adequate solution in a fairly short time, and that so risky an attempt as this is not suitable for its present work." Letter of Nov. 13, 1894, relating to the secretion of a specific poison by Daphnia.

demanded. Trial and experiment were peculiarly needful in 1893; the statistical calculus itself was not then even partially completed; biometric computations were not reduced to routine methods, and the mere work of collecting, observing, experimenting, and measuring was more than enough for one man. Weldon with his "volume of life" was eager to do all these things, and run a laboratory with perhaps sixty students as well. He was impatient because the probable errors of biometric constants, on which tests of significant differences depend, were not at once forthcoming; he wanted the whole mathematical theory of selection, the due allowances for time and growth, the treatment of selective death-rates and the tests of heterogeneity and dimorphism settled in an afternoon's sitting. The Committee did not possess a mathematician to put on the brake, and Weldon attempted too much in too short a time. Each week Weldon had new and exciting problems, he thrust them upon his friends, demanded solutions, propounded solutions, and was never discouraged when difficulties were pointed out and time asked for.

One of the first subjects to be taken up by the new Committee was to test whether the method of resolution into two Gaussian curves, which suggested dimorphism in the Naples crabs, would be helpful in confirming a similar dimorphism said to exist in the herring. Several thousand herrings arrived at University College, a measurer was trained to deal with them, and the variability of a wide series of characters determined. The distributions came out skew, and Weldon was intensely hopeful that statistical evidence of dimorphism would be forthcoming. Instead of this, the analysis showed dimorphic Gaussian components to be impossible. This result was a great disappointment to him, and, I believe, to the Committee. I could never understand why. A most extensive and valuable series of measurements had been made, which in themselves were well worth publishing. It had been shown that simple dimorphism of a Gaussian kind certainly did not hold for these herrings; in all probability it was a typical case of skew frequency, which would have been most valuable as adding to the known instances, and aiding statisticians eventually to classify such occurrences, But Weldon, and, I presume, the Committee were disheartened, they had been searching for dimorphism and had not found it. The herring data were put on one side by Weldon, and as far as I know have never been published. It is much to be hoped that they may some day be resuscitated from the archives of the Committee (16).

The next point that I personally became aware of in relation to the Evolution Committee was Weldon's attempt to solve the problem of subraces in the case of the ray florets of ox-eyed daisies. I am unaware who brought the material before the Committee, but it was obviously heterogeneous in the highest degree. There was no evidence at all that any attempt had been made to allow for seasonal and environmental effects, and whatever truth there may be in a tendency of the modes to fall into Fibonacci groups, we now know that varying season and period will produce within a certain range almost any mode in this flower*. To break

^{*} Biometrika, Vol. 1. pp. 305, 309 et seq.

up such a heterogeneity even into Gaussian components was a problem not then solved, and one which has not since been solved. It was cruel fate that thrust such a problem on Weldon, and kept him over it for weeks. He was struggling with most highly complex mathematical difficulties, and actually beginning with a problem which a more highly trained mathematician would certainly have put on one side in the then state of statistical analysis*.

The next portion of the Committee's work was far more successful—the "Attempt to Measure the Death-rate due to the Selective Destruction of Carcinus moenas, with respect to a Particular Dimension" (17). This formed the first report of the Committee, and was presented to the Royal Society in November, 1894. Weldon's general project in this case was, I believe, absolutely novel at the time, and embraces, I consider, the best manner still of testing the truth of the Darwinian theory. It consists in determining whether the death-rate is correlated with measurable characters of the organism, or, as he himself put it, "in comparing the frequency of abnormalities in young individuals at various stages of growth with the frequency of the same abnormalities in adult life, so as to determine whether any evidence of selective destruction during growth could be discovered or not."

Thus stated the problem might appear an easy one, but it is the very reverse. How is the 'abnormality,' i.e. what we should now term the deviation from type, to be measured at each stage of growth? What is to determine 'adult' life? What measure is there of the time during which the individual adult life has been exposed to the selective destruction? Weldon undoubtedly chose the crab because of the facilities it offers for measurement. But its age then becomes an appreciation based merely on the obviously close, but probably imperfect correlation between age and size. Further, the law of growth, complicated rather than simplified by the moults, and the question as to how far the variability of the characters dealt with is affected by growth combine, in the case of crabs, to form an exceedingly difficult problem. It is practically impossible to keep a sufficiently large series of crabs through the whole period of adolescence, and if it were possible, it is far from certain that the claustral environment necessary would not sensibly affect their law of growth.

Looking back now on Weldon's paper of 1894, one realises its great merits; it formulates the whole range of problems which must be dealt with biometrically before the principle of selection can be raised from hypothesis to law. Almost each step of it suggests a mathematical problem of vital importance in evolution, which has since been developed at length, or still awaits the labour of the ardent biometrician. On the whole, I think, Weldon came very near to demonstrating his point, but whether he did or did not scarcely affects the suggestiveness of the paper.

^{*} We now know that some of the most skew distributions are given by the parts of flowers, and the problem propounded to Weldon was to resolve into a number, probably five or six, of such skew components a strikingly irregular frequency distribution for ray florets!

⁺ Reading through the criticisms I communicated to him at the time, criticisms written purely from Biometrika v 4

Unfortunately the paper, as well as the suggestive "Remarks on Variation in Animals and Plants" (18), with its memorable words:—"The questions raised by the Darwinian hypothesis are purely statistical, and the statistical method is the only one at present obvious by which that hypothesis can be experimentally checked "-fell on very barren soil. The paper produced a mass of criticismfolios were written to the Chairman of the Committee, showing how this, that or the other vitiated entirely the results. The very notion that the Darwinian theory might after all be capable of statistical demonstration seemed to excite all sorts and conditions of men to hostility. Weldon, instead of being allowed to do his own work in his own way, had to be constantly replying to letters, some even eighteen sheets long, addressed to the Chairman of the Committee. These letters were not sympathetic and suggestive, but mostly purely controversial. need for further investigation of the law of growth had been frankly admitted by Weldon in the "Remarks" issued at the discussion on the "Report," but the critics declined to wait for answers till further results were published. This attack lasted for the next three years, during which further researches on the selective death-rate and growth of crabs were carried out, and it formed a serious impediment to calm progressive investigation. A further instructive report (19) on the growth at two moults of a considerable number of crabs was made to the Committee in 1897, but I believe has never been published. Later, an account of work on Natural Selection in crabs was given by Weldon in his "Presidential Address to the Zoological Section of the British Association," Bristol, 1898 (20).

In this paper Weldon returns to the problem of whether frontal breadth in crabs is correlated with a selective death-rate, but he now deals with type and not variability. He first approaches the problem from the consideration of whether for this character the crabs in Plymouth Sound are remaining stable, and he shows from measurements made by Sir Herbert Thompson and himself during the years 1892 to 1896, that the population is unstable. He next seeks a cause for this secular change, and he finds it in the turbid state of the water in Plymouth Sound, due to the continual carriage into it of large amounts of china clay and sewage. Direct experiments were then made on the selective death-rate of crabs kept in water with suspended china clay and on another occasion in foul water. In all cases the survivors were found to have a smaller frontal breadth relatively to their carapace length. Confirmatory experiments showed that after the first shock of confinement was passed this selection did not occur among crabs kept in pure sea water. A reasonable explanation of this selective action was provided in the character of a crab's breathing apparatus. Thus, after several

the mathematical standpoint, I still think them valid, but I realise also how much of my own work flowed directly from the suggestiveness of this paper. In fact it was the starting-point of the whole of the work on the influence of selection on the correlation and variability of organs. The sequel to that work, the influence of selection during growth, flows equally from Weldon's paper, but although we know much more than we did ten years ago as to the laws of growth, no sufficiently general formula of growth can yet be applied to allow of the completion of Weldon's work in this direction.





A "Crabbery" at Plymouth.

years of discouragement and much hard labour, Weldon succeeded in demonstrating that natural selection was really at work, and further that it was at work at a very sensible rate*. The labour involved was excessive. One "crabbery" consisted of 500 wide-mouthed bottles, each with two syphons for a constant flow of sea water, and each crab had to be fed daily and its bottle cleaned. During the summer of 1897 Weldon spent the whole of his days at the aquarium, and his wife hardly left him except to fetch the needful chop. The sewage experiment was "horrible from the great quantity of decaying matter necessary to kill a healthy crab." In 1898 the china clay experiments were continued at Plymouth. But in the autumn a rest came. The Address was written and Weldon thoroughly enjoyed his presidency of Section D of the British Association at Bristol.

It may not be out of place here to note the great aid Weldon's artistic instinct and literary training gave to his scientific expression. His papers are models of clear exposition, his facts are well marshalled, his phraseology is apt, his arguments are concise, and his conclusions tersely and definitely expressed. The result, however, was not reached without much labour. I do not mean that it was an effort to him to write well and clearly, but that his standard was so high, that having written a memoir, he would to please his own sense of the fitting rewrite the whole of it and possibly redraw all the diagrams. Nor was the remodelled memoir necessarily in its final form. A third or fourth reconstruction might follow to satisfy his own standard of right expression. To him a paper was a literary whole, which had not only to convey new facts, but to play its part on the scientific stage.—and he was not satisfied until it was in his judgment artistically complete. There was never any artificial brilliancy introduced in the process; rhetoric in the service of science was intolerable to Weldon. It was simply an attempt to choose the suitable form and the right words for a given purpose. It was comparable with Weldon's sense of sound, with his extraordinary gift of appreciating and reproducing the exact intonation of a foreign tongue. Both were the result of observation and experiment—not manifest in the final product—guided by a trained artistic sense.

Considerable changes were soon to take place in Weldon's environment and scheme of work. Lankester had been appointed director to the British Museum (Natural History), and in February, 1899, Weldon succeeded him in the Linacre Professorship at Oxford. In the February of 1897 the Royal Society Evolution Committee received a large increase of membership; it ceased henceforth to "conduct statistical inquiries into the measurable characteristics of plants and animals." It became transformed into an Evolution (Plants and Animals) Committee. At first there were great hopes of achievement, there was a possibility of securing Charles Darwin's house as a centre for breeding experiments, and a considerable sum of money was promised in aid. Francis Galton struggled bravely for a great idea. He wanted to see the numerous bodies engaged in horticulture

^{*} The 60,000,000 years or so, which the physicist then allowed the evolutionist, were at that time a little more of an incubus than they are now!

and zoology coordinated in at least one aspect of their work, and that research of a scientific kind should be introduced into the proceedings of each of them. He strove to make two schools, widely diverse in method and aim, understand each other. He wanted to keep individuals and societies up to their work, and prevent overlappings. But it was not to be. The members were pulling in opposite directions, there was too much friction, and too little compromise. A false antithesis was raised between what was termed "natural history" and any sort of statistical inquiry leading to numerical results. The biometric members ceased to attend regularly and finally resigned towards the end of 1899. Thiselton-Dyer and Meldola also left the Committee, which became from that date confined to one special school and one limited form of investigation. From beginning to end the Committee has, in the opinion of the present writer, been a mistake; not only because at first it distinctly forced the pace and hampered Weldon's work, but because experience shows that such a committee can only work effectually in the interests of one school of ideas, and this, whatever safeguards may be taken, has at least the appearance of destroying the impartiality of the parent body, a matter of very grave importance.

During the eight years of Weldon's London professoriate his development was great; he became step by step a sound mathematician, and gained largely in his power of clear and luminous exposition. His laboratory was always full of enthusiastic workers, and over forty memoirs were published by his students, who included E. J. Allen, E. T. Browne, F. Buchanan, G. H. Fowler, E. S. Goodrich, H. Thompson, E. Warren, and others of known name. The following lines, provided by a friend, graphically recall Weldon in his early London days:—

"In so vivid a personality it is hard to point to the period of greatest mental activity, but of the nineteen years in which I knew him I should select the first few years of his Professorship at University College, London. Fresh from contemplative research at the Plymouth Laboratory of the Marine Biological Association, and with his mind full of the new problems to which the study of marine life had introduced him, he threw himself into teaching with renewed zest. The effect on his students was amazing; most of them began a zoological course as a compulsory but annoying preliminary to a degree; Weldon soon changed that. Without ever forgetting the requirements of examinations, he made the subject alive and absorbing; his advanced classes soon filled up; and while on the one hand, the scholarships at London University were always claimed by his students, on the other the output of original investigation published by his department was one of which no university need have felt ashamed. Besides all this his students loved him; he was so intensely human....Into the question of remodelling the University and the defence of his College, Weldon threw himself as if unencumbered with arduous teaching and research; his notably lofty ideals and vigorous championship were far from being wasted; but his removal to Oxford at the time of the birth of the new University was a severe loss to the cause of real education in London. Gentle with ignorance, he was fiercely intolerant of educational shams and cants."

As the present writer has indicated, the stress during these London years was very great—the struggle with new mathematical processes, the wear of incessant calculation, the worry of unending controversy to a man fully occupied with research and teaching, all told on Weldon. The holidays were more limited in

extent, but were very varied in character. In 1893, Easter was spent in the Sieben Gebirge; the Weldons were up at six, calculating till one, and starting a great tramp at two, from which they returned at eight. The autumn they spent in Venice, going by sea, and the Christmas at Brussels, with opera each night and walks to Waterloo most days. In 1894 it was Siena for the Palio, with a knapsack tour from Stresa to Alagna by Orta and Varallo. In 1895 Easter found them fossil-collecting in the Eiffel, and, after the hard summer at Plymouth, in the Apennines, winding up in Florence. Bicycling was the rule in 1896, even cycling from Wimpole Street to Plymouth, and the only holiday a cycling tour in Normandy. In 1897 there was an Easter visit with architectural sketching to the cathedrals of North-East France, and after the specially hard summer at Plymouth a trip to Perugia and a return from Genoa by sea. The last year in London included a butterfly and moth collecting expedition to Ravenna at Easter, but no summer holiday abroad; the British Association, followed by a study of Wells Cathedral, occupied its place. The restlessness of work seemed to have overflowed into the holidays, and Weldon's friends knew that it was telling upon him, and trusted that Oxford life might be quieter than the London life had been.

VI. Oxford and the Second Professoriate, 1900—1906.

The removal of Weldon from the London field of work, while an incalculable loss to his colleagues, was not without compensation to his nearest friends. They knew that the life of the last few years had been one of great tension, that Weldon's time had been too much encroached upon by committee work, that the separation between the locus of his teaching and of his research work was very undesirable, that even the social life of London involved too much expense of energy. Oxford, in some respects, would present a narrower field of administrative duties; it would provide a roomy and amply equipped laboratory, where experiments hitherto shared between Plymouth and Gower Street could be carried out, and remain under control while ordinary teaching work was going forward. Even the social life in Oxford had more regular hours and was less over-stimulating. It is true that Weldon occasionally regretted the contact with many minds working on kindred topics, and even the stimulus of keen men working on quite different subjects, which is characteristic of the metropolis. He would speak with great affection of "dear old Gower Street, where everybody was working and everybody wanted to work"—and he would be vexed that so many of "these nice Oxford boys" had no res angusta domi to force them from the river and the playing field into the laboratory and the lecture room. "They are so nice, they come to my lectures because they think it would be rude to leave me alone." The lad who would not make a sacrifice to his love of science—accept an Asiatic appointment of the merest bread and butter value, or take passage in a tramp steamer to collect in South America—was anothema to him. He wanted everywhere an infant Huxley, realising the value of tropical or semi-tropical observation and experience and anxious to seize the opportunity of it at any slight personal inconvenience. Weldon did not grasp that it was largely his own personality which had created the band of earnest workers round him in London, and that with time it would be effective in more conservative Oxford. He did not realise that the overstimulus of the London period, with its midnight hours and incessant interchange of ideas, would be better replaced by the more leisurely intellectual and more regulated social life of Oxford.

There is another point which emphasises the value of this change. Weldon's taste, his whole emotional nature, made him essentially a field naturalist. It was no innate taste for figures or symbols, no pleasure in arm-chair work, which drew him to statistical research. Nor was it the influence of any personality. On the contrary, he was impelled to it by the feeling that no further progress with Darwinism could be made until demonstration from the statistical side was forthcoming. His biometric friendships arose from the direction he felt his work must take. He distrusted mathematicians as much as any good Mendelian might do; they were persons who neither observed nor experimented, who had "a true horror of a real measurement." Acceptance of each stage of biometric theory could only be won from Weldon by a tough battle; it had first to justify its necessity, and next to justify its mathematical correctness. He was not drawn into actuarial work by his sympathies or his friendships, he was driven into it by the looseness he discerned in much biological reasoning; he felt an impasse, which could only be surmounted by the stringency of mathematical logic. Those who have known Weldon collecting on the shore, dredging at sea, or in later days sampling ponds and wells for his Crustacea book, photographing snail environments in Sicily, or hunting for Clausilia in the woods at Risborough or Plön, realise that he was in the first place the open-air naturalist. If further evidence be indeed wanting, let the following words provide it:

[April, 1903.]

"Just back, and have just read your letter. I will play with the spanner and talk of it to-morrow.

I did not telegraph because our office was shut. It was a great disappointment to miss you; but the ride was the one thing I enjoyed out of the last three weeks. I have felt nothing like it since the old days when I used to lie in a fishing boat dodging the squalls off Rame Head or the Deadman, when we were all young and arithmetic was not yet. That is all gone. The good old man I used to sail with went to haul lobster pots in one of the March gales, and his boat was found bottom upwards.

He was a good soul. 'Yes, my dear,' he used to say in a breeze; 'we'll shake out all them reefs if you like. You'll get wet, but I'm only a fisherman and wet don't hurt me.' Then he would sing Devonshire songs while the water came over the gunwale, till you went on your knees to him to ask for at least one reef back again.

Really, even Basingstoke railway station looked good with the squalls climbing round it. *Ride* home. It will do you no end of good. Go by Farnham, Basingstoke, not by Guildford. Sandro and I rode home to-day. We had no snow, and no rain, and not half the fun of Monday. A sober, middle-aged ride on a good road in good weather.

Nevertheless, my head is so full of chalk-downs and clouds, and things, I can't write biometry to-night. Always, when I have been with the country, the feeling breaks out that the other folk have the best of it. The other way you live with the country and become part of it; and you

dredge, or fish, or shoot something wonderful, and you describe it, and everyone sees that it is wonderful, and you all enjoy the wonder. And there is no solution, and if there were, it would not be worth the shadow of a shower flying across the country.

And this is all wicked nonsense, and I am going to bed. Yours affectionately,

W. F. R. WELDON."

Weldon was a child of the open air and the breezes, and we hoped that he might have more of them, if not in lowland Oxford, at least on the hills around. There was space and air too for the experimental work that had been so cramped in Gower Street. The Daphnia studies, which had occupied so much energy under unfavourable conditions in London, were at once resumed on broader lines in the ponds and ditches round Oxford. Weldon, with a basket of bottles attached to his cycle handle, and a fishing creel, filled with more bottles, on his back, might be met even as far as the Chilterns, collecting not only Daphnia, but samples of the water in which they lived. His University College work had shown him how widely Daphnia are modified by their chemical and physical environment, and how this modification is largely due to selection. There exist elaborate drawings of the Daphnia from the Oxfordshire ponds, indicating their differentiation into local races, and notes on the peculiarity of their habitat and the chemical constitution of the water:

"In the meantime I have been led into a non-statistical work for the moment. Get out of the library and read Klebs: Bedingungen der Fortpflanzung bei einigen Algen und Pilzen.

By tricks of nutrition, light, etc., Klebs can make simple algae reproduce either a-sexually or sexually, or parthenogenetically, as he pleases. In cases where every textbook tells you that a regular alternation of sexual and a-sexual generation is the rule, he can make *either* form recur as often as he likes.

If one can by similar tricks throw *Daphnia* into this condition, then the measuring machine can again come into play, and one can compare parthenogenetic inheritance with sexual inheritance as often as one pleases.

That is a *Nebensache*.—The *Hauptsache* here is the great variation in the chemical composition (pardon the phrase) of the water in the little rivers. Their percentage of dissolved salts varies enormously, and I hope to go about as I have begun, with a large fisherman's creel tied to the handle-bar of my bicycle, learning the correlation between the salts in the waters and the fauna.—Then again comes the measurement, and the attempt to derive one local form from the other under controlled conditions by direct selective destruction due to the conditions."

This was precisely the same problem which a study of Kobelt's Studien zur Zoogeographie, 1897-9, led him later to take up with regard to land snails. What is the meaning of the slight but perfectly sensible differences in type to be found in shells from adjacent valleys, or even from different heights of the same mountain? Weldon attacked the problem in his usual manner; he spent two Christmas vacations collecting Sicilian snails of the same species from habitats extending over a wide area, the local environments were described, and the snails often photographed with their immediate surroundings. Innumerable shells were brought back to Oxford, and Weldon delighted to discourse on the significant differences in local type, and yet the gradual change of type to type from one spot

to another. No rapidly made measurement on the outside of the shell would satisfy Weldon; the shell must be carefully ground down through the axis, and measurements made on the section thus exposed. Perhaps four or five snail shells could be ground and measured in a day, and at the time of his death, not more than a few hundred of the Sicilian thousands had even been ground. Like the Daphnia, the Sicilian snails remain as an indication of the way—the path of absolute thoroughness—the master would have us follow. "Life is not long enough for biometry," murmurs the superficial critic. But the man of deeper insight replies:

That low man goes on adding one to one,
His hundred's soon hit:
This high man, aiming at a million,
Misses an unit.

But these attempts to get to the kernel of selection in its action on local races were far from occupying the whole of Weldon's thoughts in these early days. In conjunction with his assistant, Dr E. Warren, he had commenced at University College his first big experimental investigation into heredity.

"The Oxford rivers have had to rest during the last few weeks, because of the pedigree moths. These are apparently going on very well indeed. There are at present about 3500 caterpillars, belonging to thirty-eight families forming the third domesticated generation."

The characters to be dealt with consisted of the number of scales in particular colour patches, and the work of counting these was very laborious. A little later (16 July, 1899) Weldon writes:

"The caterpillars are hatching by hundreds and I hope the clean air will help them to do better here than in London. From egg to moth, poor Warren, in spite of magnificent efforts, had a death-rate of over eighty per cent.; and that seems to me a rather serious thing... because one cannot be sure that the death-rate was not partly selective with respect to things in the caterpillar which are correlated with colour in the moth. The influence of climate is shown by the fertility of the eggs.—Warren got forty per cent. of fertilised eggs from his pairing and an average of over one hundred eggs per batch. Nearly all my pairs lay fertile eggs and those I have counted give an average of one hundred and sixty-five eggs per batch."

And again, on the 14th August of the same year:

"I want to come and talk to you, especially about death; but I cannot come till my caterpillars are safely turned into pupae. For the sake of these caterpillars I have, at the risk of personal liberty and reputation, stolen from the roadside one hundred square feet of clover turf, the property of the Lords of various Manors in this neighbourhood. The little ruffians have now eaten all this clover and for the last day or two of their existence have to be fed by hand.—Therefore I have to pluck fresh clover (which is not stealing if you do not do it in an enclosed pasture) every day.—My bicycle is nearly worn out from carrying extra weight. Riding down a steep hill, with your brake smashed, and with five or six feet of heavy turf on your back is like playing at Attwood's machine. You get very near to the theoretical acceleration too!"

In the course of three years many hundreds of pedigree moths were dealt with and the observations were reduced. But no definite inheritance at all of the character selected for consideration was discovered. Weldon, I believe, thought that there had been some fatal mistake in the selection of pairings, and undoubtedly

in some cases parents of opposite deviation had been mated, so that a rather influential negative assortative mating resulted. But from other series of pedigree moth data that I have since seen, it seems to me probable that there is some special feature in heredity in moths, or possibly in those that breed *twice* in the year, and that the vast piece of work which Weldon and Warren undertook in 1898—1901, may still have its lesson to teach us. At the time it formed another link in that chain of apparent failures which for a time, but only for a time, disheartened Weldon.

In these three first years at Oxford, Weldon's intellectual activity was intense. The letters to the present writer, which in 1899 averaged one a week, in 1900 and 1901 reached an average of two, and in some weeks there were almost daily letters. These letters not only teem with fruitful criticism and suggestion with regard to the recipient's own work, but contain veritable treatises—drawings, tables, calculations—on the writer's own experiments and observations. To the pedigree moth experiments was added in the summer of 1900 an elaborate series of Shirley Poppy growings, 1250 pedigree individuals being grown and tended in separate pots; Weldon's records were the most perfect of those of any of the cooperators, and his energy and suggestions gave a new impetus to the whole investigation. They were ultimately published in Biometrika under the title, Cooperative Investigations on Plants, I. On Inheritance in the Shirley Poppy (22). As Weldon himself expressed it, the moths and poppies meant "a solid eight hours daily of stable-boy work through the whole summer, and through the Easter vacation, with decent statistical work between." The autumn of 1899 provided no proper holiday, but Christmas found the Weldons in Rome. After the Shirley Poppies were out of hand in the summer of 1900, the Weldons went to Hamburg and thence to Plön. The object of this visit was to collect Clausilia at Plön and Gremsmühlen for comparison with the race at Risborough. The same aim—the comparison of local races-led Weldon at Christmas to collect land snails in Madeira. Thus he slowly built up a magnificent biometric collection of snail shells-i.e. one sufficiently large to show in the case of many local races of a number of species the type and variability by statistically ample samples. this part of Weldon's work only two fragments have been published, "A First Study of Natural Selection in Clausilia laminata (Montagu)" (23), and "Note on a Race of Clausilia itala (von Martens)" (24). In the first of these memoirs Weldon shows that two races of C. laminata exist, in localities so widely separated as Gremsmühlen and Risborough, with sensibly identical spirals, although no crossing between their ancestors can have existed for an immense period of time, and although there are comparatively few common environmental conditions. At the same time, while no differential secular selection of the spiral appears to have taken place during this period, there yet seems to be a periodic selection of the younger individuals in each generation, the variability of the spirals of the young shells being sensibly greater than that of the corresponding whorls of adults. In other words stability to the type is preserved by selection in each new generation. In the second memoir Weldon sought for demonstration of a like periodic selection in the *C. itala* he had collected from the public walks round the Citadel of Brescia. He failed, however, to trace it, and was forced to conclude that *C. itala* is either not now subject to selective elimination for this character, or is multiplying at present under specially favourable conditions at Brescia, or again, as both young and old were gathered in early spring, after their winter sleep, that elimination takes place largely during the winter, and "that individuals of the same length, collected in the autumn, at the close of their period of growth, might be more variable than those which survive the winter."

Quite apart from the results reached, Weldon's papers are of the highest suggestiveness. Does selection take place between birth and the adult or reproductive stage? This is the problem which everyone interested in Darwinism desires to see answered. But to answer it we need to compare the characters of the organisms at the same stage of growth, for these characters are modified by growth. How is it possible to compare a sample of the race at an early stage, with its adult sample? The problem of growth, to be studied only under conditions of captivity, possibly modifying the natural growth immensely, had made the crab investigation an extremely complex one. Weldon solved the difficulty by the brilliant idea that the snail carries with it practically a record of its youth. If the wear and tear of the outside of the shell to some extent confuses the record there, a carefully ground axial section will reveal by the lower whorls the infancy of the organism. Hence the days given to experimental grinding, the training in manipulation and the final success, and then the steady work, grinding and measuring a few specimens a day, till the necessary hundreds were put together; the laborious calculations not in the least indicated in the papers—the arithmetical slips with bad days of depression, and the completed result: the illustration of how shells may be used-by those who will give the needful toil—to test the truth of the Darwinian theory.

The summer of 1899 found the present writer at Great Hampden on the Chilterns, working at poppies and developing a theory of homotyposis, namely, the quantitative degree of resemblance to be found on the average between the like parts of organisms. Weldon, who came over from Oxford to dredge the ponds and to discover *Clausilia* by the White Cross at Monks Risborough, provided the criticism, suggestion, and encouragement, in which he never failed*:

"You have got hold," he wrote, after returning to Oxford, "of the big problem which all poor biologers have been trying for ever so long. I wish you good luck with it."

The collection and reduction of material were on a larger scale than had been previously attempted, and the memoir was not presented to the Royal Society until the October of the following year (1900). It was soon evident that the attitude of the Society with regard to biometry was undergoing considerable change. The meeting of November 15 and the discussion that took place on the

^{*} His aid in the second part—Homotyposis in the Animal Kingdom, shortly to be published,—was even more substantial.

homotyposis paper was the immediate cause of the proposal to found this Journal. A little later a detailed criticism of the paper by one of the referees was actually printed by the Secretaries and issued to Fellows at a meeting, before the fate of the criticised paper itself had been notified, and before the paper itself was in the hands of those present. This confirmed the biometric school in their determination to start and run a journal of their own.

On November 16 Weldon wrote:

"The contention 'that numbers mean nothing and do not exist in Nature' is a very serious thing, which will have to be fought. Most other people have got beyond it, but most biologists have not.

Do you think it would be too hopelessly expensive to start a journal of some kind?.....

If one printed five hundred copies of a royal 8vo. once a quarter, sternly repressing anything by way of illustration except process drawings and curves, what would the annual loss be, taking any practical price per number?... If no English publisher would undertake it at a cheap rate, the cost of going to Fischer of Jena, or even Engelmann, would not be very great."

This was the first definite suggestion of the establishment of *Biometrika*. On November 29, the draft circular, corresponding fairly closely to the first editorial of the first number (25), reached me from Oxford with the words: "Get a better title for this would-be journal than I can think of!" The circular went back to Oxford with the suggestion that the science in future should be called Biometry and its official organ be *Biometrika*. And on December 2nd, 1900, Weldon wrote:

"I did not see your letter yesterday until it was too late for you to have an answer last night. I like *Biometrika* and the subtitle. Certainly we ought to state that articles will be printed in German, French, or Italian. One may hope for stuff from anthropologers, and —— for instance, ought to be allowed to use his own tongue."

Thus was this Journal born and christened. The reply to circulars issued during December was sufficiently favourable to warrant our proceeding further. A guarantee fund sufficing to carry on the Journal for a number of years was raised at once; good friends of Biometry coming forward to aid the editors. By June of 1901 its publication through the Cambridge University Press had been arranged for, and the sympathetic help of the Syndics and the care given by the University Printers enabled us to start well and surmount many difficulties peculiar to a new branch of science*. Those of us who believe that Biometrika came to stay and to fulfil a definite function in the world of science hope that the name of the man who first formulated a definite proposal for a biometric organ may always continue to be associated with our title-page. During the years in which Weldon was editor he contributed much, directly and indirectly, to its pages. He was referee for all essentially biological papers; and his judgment in this matter was of the utmost value. He revised and almost rewrote special articles. He was ever ready with encouragement and aid when real difficulties arose. For the mechanical labour

^{*} A special feature has been of course the masses of tabulated numbers. It deserves to be put on record that on more than one occasion 15 or 20 pages of figures have been set up without a single printer's error.

of editing, for proof-reading, for preparation of manuscripts and drawings for the press, or for interviews with engravers, he had little taste or time. He was too full of his current problem to undertake work of this kind regularly; proofs might remain for weeks unopened, until the number was printed off, and manuscript might disappear into a drawer, when the co-editor imagined it was safely on its way back to the author! But Weldon was always delightful when such "laches" were discovered; to meet Weldon when he was in an apologetic frame of mind meant that you must apologise to him yourself for the very thought of scolding him! It was all over before he had shaken hands, sat down, and lighted the inevitable cigarette; you were not talking of proofs, but of Kobelt, Mendel, Maeterlinck, the Kritik der reinen Vernunft,—anything and everything but dull editorial matters. And you felt a freshness and a tonic, and a sense of the healthy joy and pleasure of life, and you wondered how it was possible to do anything but love this man and rejoice in the clearness of his vision and the suggestiveness of his thought.

Starting on October 16, 1900, and extending throughout the early *Biometrika* letters, runs a flood of information with regard to Mendel and his hypothesis.

"About pleasanter things, I have heard of and read a paper by one, Mendel, on the results of crossing peas, which I think you would like to read. It is in the Abhandlungen des naturforschenden Vereines in Brünn for 1865. I have the R.S. copy here, but I will send it to you if you want it."

[October 16, 1900.]

Then follows a resumé of the first of Mendel's memoirs, and for months the letters—always treatises—are equally devoted to snails, Mendelism and the basal things of life. It is almost impossible to give an idea by sampling of the crush of keen and vital interest these letters represent. Some attempt must, however, be made:

"Have you ever been up here? It is not at all a bad little country when you are tired.—We started simply to see the architecture at Lübeck, because neither of us knew the North German brick and wood church work. That was very interesting, then we came here for fresh air and quiet—and we found SNAILS.

I have rather more than 5000 snails all properly pickled, with localities recorded......There are so many points about snails, if one could only measure and breed them !...Also I have been greatly impressed with the way in which they are dependent upon conditions of environment, so that one quickly learned to know almost exactly what species one would find in any place one passed through. I think that by going from here, which is almost the eastern limit of several species, to a very different country, such as Oxford, one might almost hope to make a good shot at some of the essential conditions which determine the distribution of some of the species.... It is ridiculous that such abundant material as snails afford everywhere (except at Danby End?) should be left useless because one cannot see how to take advantage of it. Send me some "tips" for trials. (To Oxford,—we go home to-day)."

[Plön, 5/9/90.]

"You ought to see Lübeck some day. You know so much about German art that I suppose the pathetic ugliness of it does not hurt you any more?.....

You can't get a beautiful art in a climate where people must wear clothes. Just as the northern idea of a portrait is a round face stuck on top of a heap of fine clothes, so the northern idea of a building is a thing with all its good simple lines disguised by silly excrescences. If you

want to see really majestic brickwork go to Siena or Pistoja, where you can see naked men and women in the streets on a summer's day. Lübeck is very earnest, and very interesting, and so on and so on, but it is *not* beautiful!...I am sending you a parcel of snails that you may see the sort of thing.

In one beech wood, on the trunks of the trees, we collected rather more than 3000 snails, most of them *Clausilia biplicata* and *C. laminata* (see the parcel), but some *Helix lapidicida*. There are certainly one thousand each of the two *Clausilia* species from this locality, and four or five hundred of each from another wood."

Then follow pages of minute description of each type of shell in the parcel and discussion as to the possibility, by grinding or by taking a melted paraffin cast of the inside, of measuring biometrically this or that character.

"I fancy want of moisture must have more to do with the absence of snails about you than want of chalk. What are you on? Surely you have nearly the same Oolites and Lias that we have here?..... Have you committed the sin of digging up a bit of your moor, and looking among roots?"

[Oxford, 13/9/1900.]

"A happy New Year to you! I send in another envelope specimens of the problematic snail, which has been found in sufficient numbers already. The pattern cannot, I think, be treated as due to lines of growth, and I hope it will be possible to find some way of estimating its variability.—It occurs more or less in a whole series of species here, and here only; and the hills here are so separated by deep valleys, with great climatic differences at different elevations, that there are well isolated local races.

It is rather hard for me to collect many races, because I have to look after my sick laboratory boy, and to teach him sea work, which takes time and produces only isolated examples of pretty museum things, which are a joy to see, although they teach one very little*. To do this and also to find time for a 2000 or 3000 feet climb after snails makes a very good day, and one goes to bed very fit, and full of beautiful remembrances. As one walks up hill, the impression is very absurd. Here the garden is full of bananas and sugar canes; in an hour's climb one gets into a wood of pine trees and heather, and looks down on to all this tropical valley. The contrast is very curious, and I have not got accustomed to it.

It seems rather a bad year for land beasts. The normal rainfall in December and January is said to be about thirty inches; and this year practically no rain has fallen since the spring. I suppose as a result of this every live thing gets under the biggest block of basalt it can find. This makes snail hunting rather exciting, because when you get to the top of a kopje where the beasts are you find the sides so steep that any stone you disturb rolls down, unless you take great care. My first day's hunt resulted in such a roll. A stone which I could only just lift rolled down into a sugar cane bed some three or four hundred feet below. I have never felt so ill as I felt until I found that stone and made sure that it had not smashed up an innocent Portuguese peasant!

* One of the blows to Weldon, which resulted from his biometric view of life, was that his biological friends could not appreciate his new enthusiasms. They could not understand how the Museum "specimen" was in the future to be replaced by the "sample" of 500 to 1000 individuals, not to be looked at through a glass, but to be handled, used, and if necessary used up. They warned his pupils solemnly to give up this sort of fooling and take to the real business of the "biologer," if they wished for success. "I told — about these snails," Weldon wrote on Oct. 11, 1900, "and he wrote me an earnest letter, urging me to return to the pleasant way of describing beasts for the delight of the faithful. That is the real thing if you want to be popular. Go to sea, and have a good time, and bring back a jelly fish which is bright blue."

There is much missionary work yet to be done by biometricians, and Weldon's loss will make it still harder!

If one knew anything about natural history one might do a great service to these people. The whole place is covered with the tracks of a little black ant, introduced with some South American sugar canes five or six years ago. The ant cultivates a number of aphides, which produce serious diseases on all the fruit trees; also it attacks the newly hatched birds and all beasts which shelter under stones. Under a big stone, where some dozen snails have sheltered, about half the shells (which look quite fresh) are eaten empty by ants; so it is with the beetles, grasshoppers, and other things. The only good thing they have done is to eat the cockroaches. Every kitchen is now full of ants, and contains no cockroaches at all.

How snails make their shells here is hard to understand; there is not a scrap of limestone in the place: all basalt and beds of gorgeously coloured volcanic sands. Yet when one finds the right place, one finds that snails swarm and their shells are rather harder than usual!

I should very much like to know whether the habit of hiding under stones is as general in all seasons as it is now. You know Wallace points out that most of the beetles here have lost their wings; and he regards it as probable that flying beetles would be blown out to sea in storms. Now first of all there are practically no storms, and secondly, if there were, the valleys are so deep and their sides so precipitous, that there is abundant shelter against winds. But the loss of wings might well be correlated with the habit of walking under stones to get out of the sun. You find a patch of bare hot sand, so steep that you can hardly stand on it, with a stone here and there, and no sign of any living thing. If you turn over a stone you find a number of snails, a lizard, twenty or thirty beetles, a grasshopper or two, and armies of millipedes...... The man we see most of in this inn is a splendid creature. A captain in the Canadian frontier police, who volunteered for service in South Africa, and is recovering from a bullet through his right lung. Because he has a colonial accent, —— cannot see any merit in him......It is only another sample of the difficulty I feel every day at Oxford. The boys there are so occupied with silly superficial things that one can never bring them to think of fundamental matters."

[Funchal, 29/12/00.]

"I am glad you are disgusted with the Life. I was afraid you were not.—You cannot judge the man from the bits of his letters. I do not think one ought to try to have an opinion about a man's conduct towards his wife, or indeed about his ethical value at all. One cannot possibly get hold of evidence enough, and the little bits of bad journalism which people give one are only sufficient to disturb one's mind. Take the old man as one knows him by his work, without troubling to guess at his motives, and there is not much the matter with him. I quite agree with you in loving Darwin and —— more; but a man may be a great deal lower than these two, and yet be high enough for reverence."

The earlier part of 1901 was chiefly occupied by snails, but a new factor had come into Weldon's many-sided occupations. It was settled that Biometrika should have in an early number a critical bibliography of papers dealing with statistical biology. Weldon undertook this task as his study of Mendel had led him to a very great number of such papers dealing with inheritance, and the section on Heredity was to be published first. Like all Weldon's projects, it was to be done in so thorough and comprehensive a manner that years were required for its completion. A very full list of titles was formed, especially in the Inheritance section, and many of the papers therein were thoroughly studied and abstracted (26). But such study meant with Weldon not only grasping the writer's conclusions, but testing his arithmetic and weighing his logic. Thus Weldon's Note on "Change in Organic Correlation of Ficaria ranunculoides during the Flowering Season" (27) arose from this bibliographical work and the erroneous manner in which he found Verschaffelt and MacLeod dealing with correlation. A further result of this work

was that his confidence in the generality of the Mendelian hypotheses was much shaken. He found that Mendel's views were not consonant with the results formulated in a number of papers he had been led to abstract, and that the definite categories used by some Mendelian writers did not correspond to really well-defined classes in the characters themselves. It was a certain looseness of logic, a want of clear definition and scale, an absence of any insight into how far the numbers reached really prove what they are stated to prove, that moved Weldon when he came to deal with Mendelian work. And his attitude has been largely justified. The simplicity of Mendel's Mendelism has been gradually replaced by a complexity as great as that of any description hitherto suggested of hereditary relationships. This complexity allows of far greater elasticity in the deduction of statistical ratios, but the man in the street can no longer express a judgment upon whether the theory really accounts for the facts, and the actual statistical testing of the numbers obtained, as well as the logical development of the theory, will soon be feasible only to mathematical power of a high order. The old categories are, as Weldon indicated, being found insufficient, narrower classifications are being taken, and irregular dominance, imperfect recessiveness, the correlation of attributes, the latency of ancestral characters, and more complex determinantal theories are becoming the order of the day. If Weldon's papers "Mendel's Laws of Alternative Inheritance in Peas" (28), "On the Ambiguity of Mendel's Categories" (29), and "Mr Bateson's Revisions of Mendel's Theory of Heredity" (30), be read with a due regard to the dates of their appearance, it will be seen that they served, and that they continue to serve, a very useful purpose: they enforce the need for more cautious statement, for more careful classification, and for greater acquaintance with the nature of the inferences which are logically, i.e. mathematically, justifiable on the basis of given statistical data. The need will become the more urgent if the complexity of Mendelian formulae increases at the present rate.

To those who accept the biometric standpoint, that in the main evolution has not taken place by leaps, but by continuous selection of the favourable variation from the distribution of the offspring round the ancestrally fixed type, each selection modifying pro rata that type, there must be a manifest want in Mendelian theories of inheritance. Reproduction from this standpoint can only shake the kaleidoscope of existing alternatives; it can bring nothing new into the field. To complete a Mendelian theory we must apparently associate it for the purposes of evolution with some hypothesis of "mutations." The chief upholder of such an hypothesis has been de Vries, and Weldon's article on "Professor de Vries on the Origin of Species" (32) was the outcome of his consideration of this matter. During the years 1902 to 1903 an elaborate attempt was made to grow the numerous sub-races of Draba verna, with the idea that they might throw light on mutations. The project failed, largely owing to difficulties in the artificial cultivation of some of the species. But for a time all other interests paled before Draba verna.

"Where are you going at Easter? Stone wall country is very good, and if you find a place with delightful old stone villages and pretty churches, *Draba verna* will be there! Come into

this region, with the bike, and learn to know and love the dear Dog!* Also explain to me how without thrashing to teach that same animal that lambs are not made to be eaten by puppies. There must be a way. I have taught him to walk at heel past the most tempting of other dogs, and even past chickens, and I have not yet beaten him at all. Cows and sheep will I suppose make one or two beatings necessary?"

[Oxford, 7/2/02.]

And a little later comes a letter which shall be cited because it may induce another to take up a form of biometric work, which must some day be pushed to a successful issue; in the fifteen years of letters there are many problems like this of *Draba verna*, which are discussed month after month with specimens, drawings, and tables, some merely schemed, but in surprising detail, others reaching the experimental stage, some in part solved, others but records of failure, one and all suggestive.

"Draba verna, or its earliest race is in full flower. I have four model types from a certain wall.

Now can you and Mrs Pearson give us the week end, so that your eyes may see the glory of this plant?

If you can turn up on Friday (I finish lecturing at 6) we can go for a tramp on Saturday, and see *Draba* at home on its walls. A gentle 7 or 8 miles all told, in a decently pretty country, with a variable plant in the middle and a really Perfect Dog all the way makes a very good combination;—only bring some knickerbockers, because Oxford Clay goes over one's ankles in places just now.

We can bring home our spoil, and discuss the very difficult question of descriptive units.

I think it a good and important thing to try. All the problems of treating mixed races come in; and above all I am curious to see what comes of statistical treatment applied to characters which have been chosen by "naturalists." They all say we choose anything which is easy to measure, and neglect the real points of "biological" importance; and there is a little truth in this reproach.

For Draba we want units of "habit," of shape and colour of leaves, of hairiness, of shape and colour of petals, sepals and fruit. We want to treat leaves which are very distinctly differentiated according to their relative time of appearance, and I think having tabulated all these characters, we want to break up the plants on a wall which you shall see on Saturday into about four races.

Do come if you possibly can. I saw one plant yesterday with all its seed capsules ripe and open; so that the first lot of little races will very soon be out of flower.

* The great Borzoi Sandro, henceforward to be a marked feature of the Weldon household, at home and away from home. Sandro pursuing sheep over the Yorkshire moors, Sandro pursuing game in the Buckinghamshire beechwoods, Weldon pursuing Sandro with every tone of affectionate persuasion, on the track the stacked cycles and the co-editor pursuing the deserted biometric problems in solitude, Weldon returning with the unchastised dog, after any interval of from 10 to 40 minutes, the chase being fully completed, the apologies for the Borzoi, his sustentation on chocolate and the human need for cigarettes, the return to the cycles, to the experiment that was to be crucial, to the colour and the sunset, these are all memories, the like of which others will have shared, which helped to form the atmosphere about the man. Sandro achieved his purpose, he kept his master out in the air—such wolf hounds can follow a cycle for miles—and to exercise him was held up as a moral duty. But his limited intelligence led to his own disablement and he had to become a partaker only in biometric "at homes." For two years, however, he was a great feature of our joint expeditions.

As Nebensachen, there are the mice and I very much want you to group the snails* in your own way—to see how far your grouping will bring them into a better form for the curve!

But Draba verna ought to be an example of the whole bearing of statistical methods upon systematic problems. I think it is rather important to begin this spring by collecting material for an analysis of the races round here, and a comparison of these with the types recognised by systematists. Learning these and their variability in this neighbourhood this spring, we can learn cotyledon characters and the characters of the first formed leaves in the Autumn—basing upon these a first set of hereditary correlations.

Again, the statement that each of Jordan's species can be recognised at any stage in the life-history of the plant makes it necessary to work correlations between cotyledon characters, autumn leaf characters, and spring characters. All this is work for lots of folk, and it is most important to get it properly planned now. Therefore, and for lots of other reasons try to come on Friday!

The Dog shall be washed for you!"

[Oxford, 22/2/02.]

The reference in this letter to the mice indicates that that great piece of experimental work in heredity was now started. A study of the work of von Guaita had convinced Weldon early in 1901 that the cross between the European albino mouse and the Japanese waltzing mouse was not one which admitted of simple Mendelian description. In May, 1901, his letters contain inquiries as to Japanese mice dealers. During the summer and autumn the collection of Japanese mice was in progress. These mice were to be bred to test the purity of the stock; during December about forty does had litters, and pure breeding went on until the autumn of 1902, when hybridisation commenced. The work on these mice was for two years entrusted to Mr A. D. Darbishire, but the whole plan of the experiments, the preparation of the correlation tables, and the elaborate calculations were in the main due to Weldon. On Mr Darbishire's leaving Oxford, Weldon again resumed personal control of the actual breeding arrangements, and from second hybrid matings carried on the work to the sixth hybrids' offspring. The work was nearing completion at his death, and through the energy of Mr Frank Sherlock the skins of the 600 pedigree mice forming the stud at that time have been dressed and added to those of the earlier generations. The reduction and publication of this material will, it is hoped, be not long delayed (33). Weldon had this work much at heart, and his letters during 1904 and 1905 give many indications of the points he considered demonstrated. The experimental part of the work would have been nearly completed had not his whole thought and energy been directed from November, 1905, into another channel.

From 1901 it is harder for the present writer to give a detailed account of Weldon's life, the co-editorship of *Biometrika* and common work brought them so continually into contact. In the early part of the summer there had been a hurried visit to Gremsmühlen for young *Clausilia*; Weldon on his return visited his co-editor at Througham in Gloucestershire bringing his Brunsviga†, and there

^{*} H. nemoralis and H. hortensis of which many hundreds had now been collected from various parts of England by Weldon and his helpers.

[†] The familiar mechanical calculator of the biometrician, the grinding sound of which (emphasised by the want of oiling in Weldon's case!) is the music which tells him how much his labours can be lightened.

was calculation and reduction of Clausilia data. Later there was a hurried visit to the Tegernsee and to Munich for opera. At Easter, 1902, there was a noble missionary effort (with the Brunsviga) to Parma; the missionary carried a memoir, which he had spent some weeks in rewriting in biometric form, but his efforts to show that a science of statistics exists were unavailing. In the summer Biometrika was edited from Bainbridge in Wensleydale, and accompanied by Sandro, the co-editors cycled to the churchyards of the Yorkshire dales, collecting material for their joint paper "On Assortative Mating in Man" (34). From Bainbridge the Weldons went to the British Association meeting at Belfast, where an evening lecture on Inheritance was given. At Christmas came one of the above-mentioned visits to Palermo to collect Sicilian snails. An event of this year (1902) was the publication of Mr Bateson's Mendel's Principles of Heredity. The origin of Weldon's first paper on Mendel has been described in this memoir; it was an expansion of a part of the promised bibliography for this Journal, and was written without any arrière pensée or knowledge of Mr Bateson's not then published experimental work. It is impossible for one who has been and again may be a combatant in this field to say more than that the tone of Mr Bateson's defence deeply pained Weldon, and rendered it difficult for a finely strung temperament to maintain—as it did maintain to the end-the impersonal tone of scientific controversy.

In the spring of 1903 Weldon was busy, as were the whole available members of the biometric school, in studying the influence of environment and of period of season on the variation and correlation of the floral parts of Lesser Celandine.

"Give my love to the Brethren who are cooperating in the matter of Celandines, and beseech them to make a better map of their country than the enclosed." [Oxford, 23/2/03.]

Weldon threw his whole energy and love of minute exactitude into the task, and his letters are filled with an account of the almost daily changes in the type and variability of the Celandine flowers from his selected stations. The result of this enquiry was the collection of an immense amount of data showing that environment and period in the flowering season affected the flower characters to an extent comparable with the differences attributed to local races. The reduction of the material has gone on progressively, if intermittently since, and it is hoped that a memoir, which will be a sequel to that issued in Biometrika*, may be published shortly (35). The wider standpoint of this second memoir will be chiefly due to Weldon's initiative and critical mind. At Easter of 1903 a series of mishaps prevented the common holiday, but this was more than compensated for by the summer vacation. The Weldons started with a sea trip to Marseilles and back. They then returned to Oxford, that work on the article Crustacea for the Cambridge Natural History might be carried on, and an eye kept on the mice. But a biometric camp was formed at Peppard on the Chilterns; here the "Consulting Editor" and one of the co-editors had established themselves, and the Weldons took a week-end cottage. The three Oxford members of the party arrived partly on cycles and partly on four

^{*} Vol. II. pp. 145—164, Cooperative Investigations on Plants. II. Variation and Correlation in Lesser Celandine from Divers Localities.

feet, and were often met en route by the residents in the uplands, the numbers being swelled by the addition of biometricians from the London or Oxford schools. Hence arose a series of Friday "biometric teas," for the discussion of the week's work and plans for the next two days. Saturday and Sunday morning were given to steady calculating and reducing work, and much was got through. The data on assortative mating in man collected in the previous year were reduced and a joint paper sent to press; the immense amount of calculation and reduction involved in the mouse-paper was got through; a joint criticism of Johannsen's Ueber Erblichheit in Populationen und in reinen Linien was written by the co-editors under the title "Inheritance in Phaseolus vulgaris" (36); the Huxley Lecture was written with yeoman help from the Oxford contingent, and lastly, a joint study was made, at Weldon's suggestion, of the relationship between Mendelian formulae and the theory of ancestral heredity. It was shown that there was no essential antagonism between the two methods of approaching the subject, and the results were published ultimately as Part XII of the Mathematical Contributions to the Theory of Evolution, Weldon persistently declining to allow it to appear as a joint memoir, because he had taken no part in certain portions of the more complicated algebraic analysis. Christmas found two-thirds of the party reunited in Palermo, and Weldon on the snail quest. His letters thence to his co-editor teem with the freshness of the sky and the joy of open-air work:

"Out between five and six, in the dark, without any breakfast, sunrise up in the hills, a day's tramp on a piece of bread and a handful of olives, and home at seven, laden with snails. Then after dinner to clean the beasts. That is not work, and it makes one very fit, but one gets tired enough to sleep when the snails are cleaned!

The camera works all right, and I think there is a very marked correlation between the general character of the limestones and the character of the shells; but developing in one's bedroom does not make for negatives which will "process"! Also it involves heavy subsidies to such chambermaids as do not understand what new form of madness this particular foreigner has developed!

I have repeated all last year's collections, and have tried hard to get a series of forms, such as Kobelt describes, intermediate between the rounded and the flat keeled forms, but I cannot at present find these. They ought (according to him) to live in a certain wilderness of beautiful mountains twenty miles away. I have several times tramped without any result. I hope to try again. I feel sure something worth having will come out of these shells; they illustrate local races and the general problem of what is a species splendidly. But the question of their markings comes in also; and you, or Galton, or someone, will have to make a scale of patterns for me, I expect. They will be the most perfectly hopeless things to draw!

It is, of course, just conceivable that the intermediate, slightly keeled forms described in 1879 by Kobelt have been exterminated since his time? He is very precise in his localities, and everywhere except in his transitional region I find exactly what he describes, but in this region I find so far only rounded forms.

The only difficulties about tramping in this country are the *carabinieri*. Every high road is patrolled by groups of two or three, so that even in a desolate place, so long as you keep to the road, you are rarely out of rifle shot; but these men come and solemnly warn you that the people round are ruffians, who would cheerfully cut your throat for a soldo; and if you simply grin, they make a great pretence of falling in behind you and guarding you.... Now collecting snails with an armed guard becomes ridiculous after a time and there is no danger at all; the

men only want tips. When one gets off the road into the hills the goatherds and other ruffians are most friendly. They want to see one's camera, and one's knife, and of course they want half one's bread, but they never ask for tips, and my throat is still uncut.

We have so far had two wet days; to-day, and one other.—We have had several inches to-day, and shall have some more; but between we have had the most glorious sun. I look as if I washed in strong coffee every morning." [Palermo, 31/12/1903.]

At the beginning of 1904 the work on the Brescia Clausilia was in progress, the mice were multiplying after their kind and Weldon's thoughts were turning more and more to a determinantal theory of inheritance, which should give simple Mendelism at one end of the range and blended inheritance at the other. Easter was spent in common, one editor at Rotherfield Greys and the other at Peppard, with the usual flow of suggestion on Weldon's part and the bi-weekly cyclings to Oxford to look after the mice. Now and then the fear would strike Weldon's friends that life was being lived at too fast a pace, but the constant intellectual and physical activity was so characteristic of the man that there was no means of calling halt, and to many when Weldon was most active he seemed most fit and well. The summer found the Pearsons twelve miles from Oxford, at Cogges, near Witney, and the Galtons twenty miles further, at Bibury; there was much cycling too and fro, and the plan of a new book by Weldon on Inheritance was drafted, and some of the early chapters written. The vacation was broken by the visit to Cambridge-Weldon cycling in one day from Oxford-for the British Association. The Presidential Address in the Zoological Section was chiefly an attack upon biometric work and methods, and the discussion which followed culminated in the President dramatically holding aloft the volumes of this Journal as patent evidence of the folly of the school, and refusing the offer of a truce to this time-wasting controversy. The excitement of the meeting, as earlier contests at the Zoological and Linnean Societies, seemed to brace Weldon to greater intellectual activity and wider plans, but the torpedo boat was being run at full speed.

The book on Inheritance occupied most of the remainder of the year, and to aid it forward and help those of us who were not biologists to clearer notions, I suggested to Weldon a course of lectures in London to my own little group of biometric workers. The project grew, other departments of the College desired to attend, and ultimately the lectures were thrown open to all members of the University and even to the outside public. Weldon had a good audience of more than a hundred, and enjoyed the return to his old environment. But it may be doubted whether his vitality responded as quickly as of old to the additional stress; there were special elements of difficulty, and I believe now that it would have been kinder and more helpful had we limited the audience to my own small body of sympathetic students.

"It will be a great pleasure to me to come and talk, and to feel that you cared to ask me; the lectures will do far more good to me than to anyone else ... and I owe U. C. L. a bigger effort than this anyhow."

[Oxford, 16/10/04.]

And again:

"It makes me more than ever glad I am coming back to Gower Street where there are live people to talk to! Surely thirty people* is a great many. Try talking for five years to an audience of from three to nine, and see how the thought of thirty will cheer you! And none of these excellent folk are sent by their tutors!"

[Oxford, 7/11/04.]

The letters of Weldon to both Francis Galton and myself during the years 1904 and 1905 are full of inheritance work, the details of the great mice-breeding experiment, the statement and the solution, or it might be the suggested solution, of nuclear problems leading to determinantal theories of inheritance. Occasionally there would be a touch of conscience, and the drawings for the *Crustacea* would be pressed forward:

"I ought to give my whole time to the Cambridge Natural History for a while. They have been very good to me, and I have treated them more than a little badly. I am rather anxious to get them off my conscience." [Oxford, 15/2/05.]

But only the chapter on *Phyllopods* got completed, figures and all, and set up. Many figures were prepared for other parts; beautiful things, which gave Weldon not only scientific but artistic pleasure, he had made, but the text remains the veriest fragment. In the same way but little was absolutely completed of the article on *Heliozoa* for Lankester's *Natural History*. It was not Weldon's biometric friends that kept him from these tasks, it was solely his own intense keenness in the pursuit of new knowledge. It was occasionally with a feeling of great responsibility that the present writer would propound to him an unsolved problem with which he might himself be struggling. There was absolute certainty that if the problem was at all an exciting one, Weldon would leave his scent and follow the new trail with his whole keenness and at full speed. All else would be put on one side, and he could only be recalled to natural history or biometrics by an appeal to his conscience. Like Sandro, the chase must be completed before he returned to the humdrum trot behind a cycle on the highway.

The fascination of inheritance problems kept Weldon, however, for months at a time at the Heredity Book. At Easter, 1905, he went to Ferrara[†], because that place had a university, and as such must have a library, where work could be done. The contents of the library were perfectly mediaeval, a characteristic appropriate in the castle, but hardly helpful in heredity[‡]. Still, portions of the manuscript came to England for comment and criticism, and we were hopeful that the end of the year would see the book completed.

^{*} The number I already knew would certainly attend.

^{† &}quot;The town is worth a lot, and the fields are full of a little speedwell, which varies most delightfully. I have so far resisted the temptation to chuck the wretched book and tabulate the variations of its flowers, and I hope I shall do to the end. But it is a temptation.....I feel out of the world, an absolute blank, with only a slight interest in newts' tails and an even slighter in a statue of Savonarola which looks at me all day through the window."

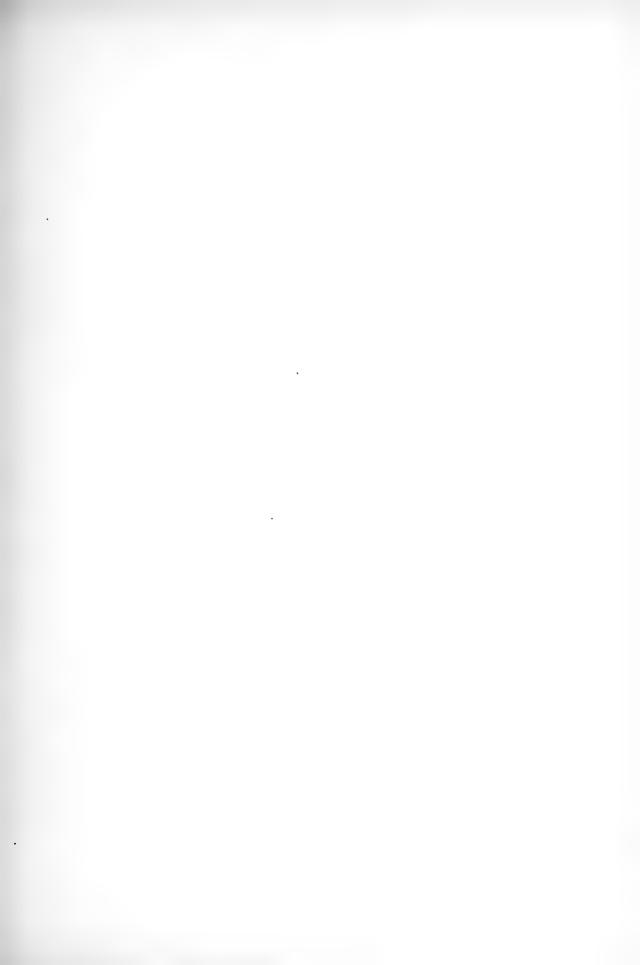
[Ferrara, 3/4/05.]

[‡] From Ferrara came back if not the speedwells, masses of silkworms' eggs of different local races, but providentially they failed to hatch out in sufficient numbers owing to the May frosts and no new scent took Weldon off the book and the mice during the summer.

It must not be thought for a moment that Weldon was desultory in his work. As E. R. Lankester says in a letter to the writer: "His absolute thoroughness and unstinting devotion to any work he took up were leading features in his character." He pursued science, however, for sheer love of it, and he would have continued to do so had he been Alexander Selkirk on the island with no opportunity for publication and nobody to communicate his results to. He never slackened in the total energy he gave to scientific work, but having satisfied himself in one quest, he did not stay to fill in the page for others to read; his keen eye found a new problem where the ordinary man saw a cow-pasture, or a dusty hedgerow, and he started again with unremitted ardour to what had for himself the greater interest. The publication of his researches will show that it is not we who are the losers, because he went forward, regardless of publication and finality of form. The true function of such a man is not to write text-books or publish treatises, it lies in directing and inspiring a school, which will be trained by completing the work and carrying out the suggestions of its master. The curse of the English educational system is that it leaves such men to solitude, and throngs the chambers of those who cram all nature into the limits of the examination room.

In the summer the present writer was at East Ilsley, some seventeen miles from Oxford, and there was cycling out several times a week; the writer's chief work was on other than biometric lines and broken by other claims on his time, but there was steady joint work on the determinantal theory of inheritance as outlined by Weldon, and it is hoped that it is sufficiently advanced to be completed and published (37). Weldon had in August, 1905, given to the Summer Meeting of the University Extension in Oxford a lecture on *Inheritance in Animals and Plants* (38), and this had taken up some of his energy during the summer vacation. On the whole, however, he worked persistently at the Inheritance Book. It is too early yet to say definitely how far it can be considered ready for press, but a considerable number of chapters are completely ready, and there are drafts for several others. We can only hope that this, the work he was in many respects best fitted for both by direct experiment and by study of the labours of others, will be issued in his name and show the full measure of his activities during these last few years.

It cannot be denied that those who were often with Weldon during the last two years were occasionally anxious—the pace had been too great—but at no time had one definitely realised that there was an immediate anxiety. His intellectual activity was never apparently diminished, and his long cycling rides were maintained to the end. It was an occasional, but never long persistent, lack of the old joyousness in life which was noticeable. At East Ilsley he was full of keenness over his photographic work; he enjoyed an antiquarian investigation into the probable final locus of the bones of St Birinus with a view to testing a local legend; we examined carefully a human skeleton dug up from under a sheepfold, the authorities having determined that no inquest was needful, the bones being those of an old man who died "hundreds of years ago." "And you think?" said



To the Editor of Biochamicle

Sin, - In the loop number of your most instructive Norwall you probled neadows to towns up the horsels treets by this account, and to know materalists of Greek. It may been in tret to some of your namerous an account ghe way in which Snails are cotacted by he energetic possibling of the way in which smalls grow up bygge they are collected.

to you, Sir, know very wale, a smail is unlike most of the avoinable found Thing like the drawing in the maryin, which is means can be dividization to balous, which are curiously alice. Byour take a in the neighborshood of Brush, in its chape. Hot Rot of his animals in to be like haf a cay for, and pur the other by edge of the decerning against a Colone glage, the The Brush collection, thatien 1806s, or Buterpless, or Creap finhes, on others,

But except the two balues of to brain, and its eyes, the tops Edition Hands are like cochother. Ches the other tolk of the coastist. Are the legs of a cay forh are on pairs, as so have have are notife and ly less, as curered like lack other as

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and one or two other agains on it bead, the partiga

for your consideration a few deep rame indicating the office of this upon Self; and I travelyn will not think me wanting in rospect if I sulais nght. band side nearly dis appears. Two ld ask you to consider, Sir, what the expert of such a mode of growth would it upon gon Editival ride grows very much parter than its right hand side, so that the your person

y is belonged than left side, a at least thuston You see that the effect would be 15 make from legs the leg which is now on your right ride look as paint forwards, towards you beach, and to make is tie the test of he other tog.

In the region of your wasis took you would have a most uncompatable proclains, which I apologice for suggesting

6

had y us just as gan can on a cray-fith. Out as it grows up, is lefthered to guile young, which is egg-sheet, you can recognise a notif and a last graws up trail as not arranged in praise in his way. When a shall

Now a shall navor has any Egs; hut it has a number of pained organs, right and Egt, in he hides part of its look, uten is is formy. As it spores, it this to he him ead of its lood, formands or I have described; and while I is don't him, has organs which Eg on its Egy rides, its Egy kidnesy, the Egy half or its heart, and other hims, disappear. So that it and has one kidney, and the puece of its heart which Egon its right seat often it would say the form it would be and then it was found and motive to had not got after got a

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Frail weld you can sowifely understand it.

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Weldon on our homeward way. "Having no anatomical training I think they are those of ——." "A young woman, who has not been buried so very long," he interrupted, with a responsive twinkle in his eye. "Let us have a smoke and consider the scientific education of the English medical profession." His sense of humour was always keen, whether with word or pencil, and it remained with him to the end. The joy of life which in the early days led him to dance and sing on the completion of a heavy bit of work, made him in later manhood ripple over with quiet humour in talk and letter when problems were going well.

Thus to Francis Galton:

"I enclose the best I can do with one of the negatives you were kind enough to let me make. Please forgive me for caricaturing you in this way.—You know enough about the lower forms of man to know that respect and affection show themselves in strange ways:—look upon this as one of them and pardon it."

[Oxford, 27/7/05.]

Nor did he spare a quiet joke at a friend:

"Your work on dams has filled the Italian papers with horror. They say you threaten the safety of all existing dams, however long they have stood." [Ferrara, 7/4/05.]

In November, 1905, Weldon was unfortunately taken off from the work on his inheritance book by the presentation to the Royal Society of a paper by Captain C. C. Hurst: On the Inheritance of Coat-Colour in Horses. He had had no proper summer holiday, but he threw himself nine hours a day into the study of The General Studbook*.

"I can do nothing else until I have found out what it means...The question between Mendel and Galton's theory of Reversion ought to be answered out of these. Thank God, I have not finished that book. There must be a chapter on Race Horses!"

Weldon felt himself in a difficult position; as Chairman of the Zoological Committee, he had at once directed the printing of Hurst's paper. But the subject being one in which he personally was keenly interested, he had immediately attacked the original material and to his surprise came to views definitely opposite to those of Hurst. He felt bound to report this result at once to the Society, and he did so on December 7, when the original paper was read. His results were provisional, as could only be the case considering the short period of preparation that had been possible. He promised to communicate a note to the Society involving more details of his inquiry. This was done on January 18, 1906 in a "Note on the Offspring of Thoroughbred Chestnut Mares" (39).

^{*} I cannot resist citing a last illustration of Weldon's humour: "What volumes of Weatherby have you? I have found in Bodley 17—20. To show you what Bodley is, I looked in the catalogue vainly under: Weatherby (found here and not under Racing, Racing Calendar), Jockey Club (found here pamphlets about the J. C. but not its own publications), Horses, Race Horses, Racing, Studbooks (found here only Clydesdale Studbook, Pigeon Studbooks, and Dog Studbooks), Turf, Sport, Race, all suggested by assistants in the Library. For a whole day I raged, and came back despairing. Next day I raged worse, and captured a man who knew something. He smiled and said: 'Oh, Yes, The General Studbook is entered under General of course.' I said, 'Why not under The?' and he thought that unseemly!'

"The object of the present note is partly to fulfil my promise and partly to call attention to certain facts which must be considered in the attempt to apply any Mendelian formula whatever to the inheritance of coat-colour in race-horses."

It is impossible at present to say more on this point, for the whole subject is likely to be matter for further controversy. Even one authenticated case of a non-chestnut offspring to chestnut parents is sufficient to upset the theory of the 'pure gamete,' but if studbooks are to be taken as providing the data, the whole question must turn on whether one in sixty of the entries of the offspring of chestnut parents can be reasonably considered as a misprint or an error in record.

Here it can only be said that Weldon took up the subject with his usual vigour and thoroughness. But he was overworked and overwrought and a holiday was absolutely needful. He went to Rome, but the volumes of the Studbook went with him:

"Will you think me a brute, if I take the Studbook to Rome? I really want a holiday, but I cannot leave this thing unsettled."

And then from Rome:

"I think it will be worth while to deal for once with a whole population, not with a small random sample. Only I could find it in my heart to wish one need not do it in Rome! To sit here eight hours a day or so, doing mere clerk's work, seems rather waste of life?"

And again:

"I have really been working too hard to write, or to do anything else. I have seen nothing of Rome....I want to know what these horses will lead to, but it would not interest me at all to know that my paper on them would or would not be printed. More important is the enormous time these horses will take. It seems clear that one ought to carry these arrays back to another generation of ancestors—and that means a very long job. I wish I had a pupil! A mere clerk would be no good, but a pupil, such as one had in good old Gower Street, would help with the drudgery, and then he might stick his name all over the paper, if he liked."

[February, 1906.]

The letters are filled with Studbook detail till Easter, there is hardly a reference to anything else. Re-reading them now one sees how this drudgery with no proper holiday told on Weldon. Hundreds of pedigrees were formed and a vast amount of material reduced. At Easter the Weldons went to the little inn at Woolstone, at the foot of the White Horse Hill, and his co-editor came down later to Longcot, a mile away, for the joint vacation. Weldon was still hard at work on the Studbooks, but he was intellectually as keenly active as of old; he was planning the lines of his big memoir on coat-colour in horses (40) and showing how they illustrated the points he had already found in the mice. He was photographing the White Horse, and rubbing mediaeval idlers' scrawlings on the church pillars. He projected the despoiling of a barrow, and planned future work and rides.

On Sunday, April 8, he rode into Oxford to develop photographs, and the present writer rode some miles of the way with him; the joint ride terminated with the smoke by the roadside and Weldon's propounding the problem which

was to be brought solved for him on Tuesday. On Tuesday I found him in bed, with what appeared to be an attack of influenza. He had expressed himself tired after his ride on Sunday, an almost unique admission. But on Monday he went a long walk over the Downs, getting home late. He came down to breakfast on Tuesday but had to return to bed. In the afternoon when I came he insisted on smoking and wanted the solution of the problem, saying he was better. I begged him, as one still closer did, to stay in bed on the morrow and give up a projected journey to Town. But there was a dentist to be seen, preparations for a visit to the M.B.A. Laboratory at Lowestoft to be made, and a wonderful picture-gallery to be visited to free him from the atmosphere of the Studbooks, His will was indomitable; he went up to Town and went to the pictures on Wednesday, he went to the dentist on Thursday, but from the dentist's chair he had to be taken to a doctor's, and thence to a nursing home. The summoning telegram reached his wife on the same afternoon, and he died of pneumonia on Good Friday, April 13. So passed away, shall I say not unfitly—for it was without any long disabling illness and in full intellectual vigour—a man of unusual personality, one of the most inspiring and loveable of teachers, the least self-regarding and the most helpful of friends, and the most generous of opponents.

As for his life, I think it was to him what he would have wished it. There were moments of discouragement and depression, he felt occasionally a want of sympathy for his life-work in some of his former colleagues, and while he was born to be the centre of an enthusiastic school, he found at times somewhat scanty material for its maintenance in pleasure-loving Oxford. But every stone he lifted from the way became gold in his hands; each problem he touched became a joy which absorbed his whole being. The artist in his nature was so intense that he found keen pleasure in most men and in all things. Only meanness or superficiality fired him, and then, considering how the world is built, sometimes to almost an excess of wrath. But he had no personal hate; he could make the graceful amend, and had he ever a foe, that foe, I veritably believe, could have won Weldon's heart in the smoking of a cigarette.

If we pass from himself to those whose fortune brought them in close contact with him—to his friends and pupils—their loss can only be outlined, it is too intimate and personal for full expression. There was a transition from respect to reverence, a growth from affection to love; to such a tenderness as some bear for a more delicate spiritual nature, to even such feeling as the Sikh is reputed to hold for the white man's child in his charge.

And lastly as to science, what will his place be? The time to judge is not yet. Much of his work has still to be published, and this is not the occasion to indicate what biometry has already achieved. The movement he aided in starting is but in its infancy. It has to fight not for this theory or that, but for a new method and a greater standard of logical exactness in the science of life. To those who condemn it out of hand, or emphasise its slightest slip, we can boldly reply, You simply cannot judge, for you have not the requisite knowledge. To the

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biometrician, Weldon will remain as the first biologist who, able to make his name by following the old tracks, chose to strike out a new path—and one which carried him far away from his earlier colleagues. It is scarcely to be wondered at if those he joined should wish to see some monument to his memory; for he fell, the volume of life exhausted, fighting for the new learning.

Is what he gave science small? That depends on how it is measured. He was by nature a poet, and these give the best to science, for they give ideas. They follow no men, but give that which another generation may study from and be inspired by. He was the enthusiast, but the enthusiasm was that of the study, trained to its task; and when the time comes that we shall know, or that those who come after us shall know, whether Darwinism is the basal rule of life or merely a golden dream which has led us onwards to greater intellectual insight, then the knowledge, so biometricians have held and still hold, will be won by those actuarial methods which he first applied to the selection of living forms. If there be aught else to be said, let another say it.

Step to a tune, square chests, erect each head,
'Ware the beholders!

This is our master, famous, calm and dead,
Borne on our shoulders.

Description of Plates.

Plate I. W. F. R. Weldon.

Plate II. Raphael Weldon, aged 10.

Plate III. (a) Rapid pencil caricature by W. F. R. W. "Apparition: Le Café Orleans."

(b) Sample of Illustration to letters. Description of bands of H. hortensis in letter to a lady collector. "Has it occurred to you that a lady of artistic ability, and so enlightened that she likes snails, would have great joy and do great service by drawing them? There is a good inexorable severity about their lines which one would enjoy, I should think, if it were not so unattainable (to me!) on paper. And it would be nearly as good fun as real engraving to get all their lights and shadows put in with curved lines which also indicate the growth lines on the shell? Think how Bewick liked it."

Plate IV. A "crabbery" at Plymouth.

Plate V. Contribution to a manuscript magazine run by a youthful friend.

LIST OF MEMOIRS, ETC., BY W. F. R. WELDON.

- Note on the early Development of Lacerta muralis. Q. Jour. Mic. Sci. Vol. XXIII, pp. 134—144, 1883.
- (2) On the Head-Kidney of Bdellostoma, with a suggestion as to the Origin of the Suprarenal Bodies. Q. Jour. Mic. Sci. Vol. xxiv, pp. 171—182, 1884.
- (3) On the Suprarenal Bodies of Vertebrates. Q. Jour. Mic. Sci. Vol. xxv, pp. 137—150, 1885.
- (4) On some points in the Anatomy of *Phoenicopterus* and its Allies. *Proc. Zool. Soc. Lond.* 1883, pp. 638-652, 1883.
- (5) Note on the Placentation of Tetraceros quadricornis. Proc. Zool. Soc. Lond. 1884, pp. 2-6, 1884.
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VARIATION IN CHILOMONAS UNDER FAVOURABLE AND UNFAVOURABLE CONDITIONS.

By RAYMOND PEARL.

For some time past it has seemed to the writer that much of value for the elucidation of the problems of morphogenesis might be gained by quantitative investigations which should give more precise information than we now have of the effects of different environmental conditions on the formative activities of protoplasm. It is, of course, well known that in general the form of an organism is directly influenced by the environment in which it lives. Further the brilliant investigations of such experimental morphologists as Driesch, Herbst, and Morgan, for example, have shown for individual organisms the particular qualitative change which follows a given definite change in the environment. Such investigations can only be regarded as of the highest value and importance, and the field they open up is likely to be one of the most fruitful in biology. Furthermore it seems to me to be a field in which much of fundamental significance may be brought out by the application of the methods of biometry. It is not the place here to enter upon a general discussion of the grounds for this opinion. The time for such a discussion is after a respectable body of objective results have been gleaned by biometric investigations in the field of experimental morphology. It will not, however, be out of place to outline very briefly the nature of some of the problems of morphogenesis which seem especially to need biometric treatment, as in this way the standpoint from which the writer's work in biometry is being done may most easily be made clear. One such problem is this: to what extent and in what manner is the relative constancy of form production capable of modification? Thus, to take a concrete instance, are "lithium" sea-urchin larvae reared under uniform conditions relatively more or less constant (or, if one pleases, less or more variable) in form than are normal larvae reared under uniform conditions? Driesch has strongly emphasized that one of the most fundamental problems which biology presents is that, to use his own term, of the "Lokalization morphogenetischer Vorgänge," His own work has served the admirable purpose of very sharply and clearly defining the nature of this problem. For its solution, however, he has turned to a teleological principle the "entelechy" of the system. But before taking such a radical step it seems not undesirable to investigate more thoroughly than has been done the nature and laws of this "Lokalization." After all, how precise is it? Driesch has frequently cited as one of the most striking of the phenomena which led him to adopt a vitalistic hypothesis, the proportionate division by constriction of the intestine of a sea-urchin larva into three parts. Whether the larva develops from a normal egg, a half-blastomere, or a quarter-blastomere, the proportionality of the three regions of the intestine so marked off is said to be constant. But how constant is it? Is there really as great precision in the relative localisation of the constrictions in the embryo from a half-blastomere as there is in the embryo from the normal egg? For Driesch's point of view an affirmative answer to this question seems to me to be vitally important. But clearly it is a question which cannot be answered by general inspection of individuals, nor by the measurement of a comparatively few isolated cases. Its answer must depend on the accurate determination of the probable errors of what must in the nature of the case be absolutely very small differences*. To answer satisfactorily such a question we must, it seems to me, turn to the biometric method of attack. It is, then, in connection with such problems of morphogenesis as these outlined that I believe much is to be gained by the application of the methods of biometry.

From this general orientation we may turn to the specific problem in connection with which the present work was done. During the past three years I have been engaged on an investigation (in connection with some of the students in biology at the University of Michigan) of the effect of environmental conditions on the form of the body in the Protozoa. An experimental study of certain phases of the problem has been made on Paramecium, of which a preliminary report has been published (Pearl and Dunbar, 1905). The results of that work made it seem desirable to get similar data for some other protozoan, where the environmental differences should be such as appear in the course of the normal life of the organism, rather than those experimentally induced. It was desirable to compare the variability and correlation shown by a population living under the most favourable natural conditions with the same characteristics of a population living under extremely unfavourable natural conditions. To present the results of such a comparison for the flagellate infusorian Chilomonas is the purpose of this paper. It has seemed best to publish these results in advance of the complete paper on Paramecium, as it is likely to be some time before that appears and the present results lend themselves readily to separate treatment.

The particular protozoan chosen for the work, Chilomonas paramecium, seems especially well adapted for biometrical studies. It has a definite and constant form; its protoplasm is relatively dense, and hence little affected by osmotic changes in the surrounding medium, a point of practical importance in quantitative work on Protozoa; and it can be had everywhere in abundance. It may perhaps be well to recall very briefly some of the facts regarding the biology of the form. Chilomonas is a very minute infusorian, which commonly appears in great numbers in cultures containing decaying plant material. The body forms an elongated ovoid with an asymmetrically situated depression or notch near the anterior end. From

^{*} Of course in the particular case cited of the proportional division of the intestine the *practical* difficulties in the way of measuring may be insuperable, but this in no way affects the point of principle that in this and similar cases quantitative treatment of the problems of morphogenesis is necessary if real advance is to be made.

the base of this notch spring two flagella (cf. Fig. 1, p. 56). Its nutrition is saprophytic and the usual method of reproduction is by longitudinal fission. An excellent account (with figures) of this organism has been given by Bütschli (1878).

Material and Methods.

The material on which this study is based was taken from two cultures set in the ordinary way for rearing Protozoa with pond-water and decaying plant material. One of the cultures was made with dry hay and pond-water (Culture B), and the other (Culture A) with dead and decaying water-plants from the same source as the water itself. The source of the water in both cultures was the same. Both of these cultures ran the ordinary course, rising to a maximum of animal and plant life and then gradually falling off. Both passed through a stage in which Chilomonas was especially abundant. The associated organisms were in general the same in both cultures, the most abundant forms, in point of numbers, being Paramecium caudatum and a large Spirillum. In the hay culture Chilomonas was extremely abundant and very evidently in a flourishing condition when the samples were taken for measurement. Judged by the standards of (a) abundance, (b) size of individuals, (c) appearance of the protoplasm, and (d) activity, it could only be concluded that the environmental conditions in Culture B at the time the samples were taken were at an optimum for Chilomonas. The series taken from this culture, which will be designated throughout the paper as Series B, may, then, be considered to represent the prevailing condition (for this particular race, of course) of Chilomonas growing under favourable circumstances.

On the other hand, when the samples were taken for measurement from Culture A the conditions were very different. This culture had at that time passed the optimum for infusorian life, and all the organisms were rapidly disappearing. All the Paramecia, which had previously been abundant in the culture, had disappeared, and the numbers of individuals of Chilomonas and Spirillum were being rapidly reduced. Some notion of the rapidity with which this reduction was going on may be gathered from the fact that on the day following that on which the samples were taken one could only with difficulty find specimens of Chilomonas, while on the second day after the sampling careful search failed to obtain any specimens. The culture had apparently completely "run out" as far as infusorian forms were concerned. The series taken from this culture (Series A) may be considered to represent the character of the local race of Chilomonas when living under the most unfavourable environmental conditions which the individuals were capable of withstanding in the active state. It will thus be seen that the individuals of Series A were in a sense practically the ultimate "survivors" of the progressively worsening conditions of the culture. But it must be understood that this does not mean that they were survivors in any process of destruction of the Chilomonas, in common with most other infusoria, encysts when the environmental conditions become so unfavourable that it is unable to withstand them any longer in the active condition. The cysts of Chilomonas have been figured by Bütschli (1883–87, Taf. XIV, Fig. 9 c). When the infusorian life begins to disappear from a culture it usually means that the organisms are encysting rather than dying. That this is the case is clearly shown by the fact that by appropriately changing the culture medium they may be induced to reappear again in the active condition. This fact is, of course, well known to all who have worked to any extent with Protozoa.

For the present purpose it is not of immediate consequence to know what the optimum conditions for infusorian life are, or, on the other hand, in what manner the cultural conditions become so unfavourable as to lead to the encystment of these organisms. It is of course a well-known phenomenon that laboratory cultures usually and normally pass through both these stages. The important investigation of Peters (1904) in this field indicates clearly that the basis of the matter lies in the changing chemical constitution of the culture medium. From the present standpoint it is sufficient to note that the "favourable" conditions of Culture B and the "unfavourable" conditions of Culture A were in no way artificially or experimentally induced, but appeared in a normal way in the undisturbed cultures.

With reference to the technique used in the collecting and measuring the following may be said. Samples were taken from each of the cultures with a clean pipette quite at random. These samples were then killed with Worcester's formol-sublimate fluid (Pearl, 1903). This fluid has been used by the writer in a number of biometric studies on Protozoa, and has proved very satisfactory for the purpose. With Chilomonas it is possible to prove that killing with this fluid when properly performed produces no measurable distortion of the organism. After killing, the specimens were measured by the camera lucida method which has been used by the writer and his students in other similar studies. (Cf. for description of methods, Pearl and Dunbar, 1903, and Pearl, 1906.) The magnification used in the present instance was such that 1 mm. on the cards on which the dimensions were pricked with a needle point corresponded to 1.45 mikrons (= × 689.7 linear). The measurements are given in mikrons.

The characters measured were length (C—D) and greatest breadth (A—B) of the body as shown in Figure 1. An attempt was made to measure the flagella, which

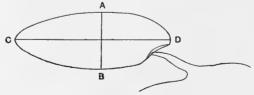


Fig. 1. Outline of Chilomonas to show measurements taken.

appear with perfect distinctness in specimens killed with the formol-sublimate fluid, but it was not feasible on account of the too frequent curvature of a flagellum either up or down in the line of sight. In addition to the absolute length and

breadth dimensions, the variation in the length-breadth index has also been studied.

Series A included 201 individuals and Series B 175 individuals. Larger numbers would have been measured but for the fact that the work on *Chilomonas* was interrupted by other work which had to be carried on while the material was available. With the degree of variation exhibited by *Chilomonas*, however, these numbers lead to reasonably small values for the probable errors of the constants and hence we are able to reach definite conclusions.

In the calculation of the constants the ordinary biometrical methods were followed. Sheppard's corrections for the moments were used in all cases.

The work was done in the Zoologisches Institut at Leipzig, and it is a pleasure to express my thanks to Professor Carl Chun and Professor Otto zur Strassen for so kindly placing the facilities of that laboratory at my disposal. I am also greatly indebted to the Carnegie Institution for a grant, during the tenure of which this investigation was carried out.

Results.

The data for the length and breadth of the individuals measured are exhibited in Tables I and II. Table I gives the data for Series A, that is, the individuals living under unfavourable conditions, while Series B including the individuals living under favourable conditions is given in Table II.

TABLE I.

Length and Breadth of 201 Individuals of Chilomonas paramecium. Series A. Unfavourable conditions.

Breadth in mikrons.

		6.9 -9.9	4.2 -0.2	7.5-7.9	7.8 -0.8	6.2 - 6.8	7.6 -0.6	6.69.6	7.01-0.01	6.01-9.01	7.11-0-11.4	6.11-2.11	13.0—13.4	Totals
Length in mikrons.	$\begin{array}{c} 14\cdot0-14\cdot9\\ 15\cdot0-15\cdot9\\ 16\cdot0-16\cdot9\\ 17\cdot0-17\cdot9\\ 18\cdot0-18\cdot9\\ 19\cdot0-19\cdot9\\ 20\cdot0-20\cdot9\\ 21\cdot0-21\cdot9\\ 22\cdot0-22\cdot9\\ 23\cdot0-23\cdot9\\ 24\cdot0-24\cdot9\\ 25\cdot0-25\cdot9\\ 26\cdot0-26\cdot9\\ 27\cdot0-27\cdot9\\ 28\cdot0-28\cdot9\\ \end{array}$	1 1	1 1 2 1 2 —————————————————————————————	1 1 1 4 1 1 - -	- - 4 2 3 3 - - -								- - - - 1	$\begin{array}{c} 1 \\ -1 \\ 4 \\ 13 \\ 12 \\ 33 \\ 23 \\ 26 \\ 29 \\ 18 \\ 18 \\ 15 \\ 5 \\ 3 \\ \end{array}$
	Totals	2	7	9	12	27	51	37	26	11	10	8	1	201

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TABLE II.

Length and Breadth of 175 Individuals of Chilomonas paramecium. Series B. Favourable conditions.

T)	3 . 3		* 7		
Brea	dth	ın	m_1	ron	S.

		6.1 -9.1	7.8 -0.8	6.8 - 9.8	7.6 -0.6	9.2— 9.8	4.01-0.01	10.5—10.9	7.11-0-11.7	6.11-2.11	7.21-0.21	12.5—12.9	7.81-0.81	13.5—13.9	7.71-0.71	14.5—14.9	7.90-12.4	Totals
Length in mikrons.	$\begin{array}{c} 17.0 - 17.9 \\ 18.0 - 18.9 \\ 19.0 - 19.9 \\ 20.0 - 20.9 \\ 21.0 - 21.9 \\ 22.0 - 22.9 \\ 23.0 - 23.9 \\ 24.0 - 24.9 \\ 25.0 - 25.9 \\ 26.0 - 26.9 \\ 27.0 - 27.9 \\ 28.0 - 28.9 \\ 29.0 - 29.9 \\ 30.0 - 30.9 \\ 31.0 - 31.9 \\ 32.0 - 32.9 \end{array}$	1 1 	1 1	1 1 - 1 - - -	1 1 1 2 2 2 1 1 -						- - 3 - 1 1 2 - 1 1 1 1 1 1 1 1 1				1		1	1 1 5 5 9 19 33 35 18 15 16 8 6 3 —
	Totals	2	2	3	10	27	30	29	28	17	15	4	5	1	1	_	1	175

We may first consider the variation in length and breadth for the two series from the analytical standpoint. In Table III are given the chief analytical constants of the distributions. The moment-coefficients are given in units of 1 mikron for the lengths, and of 5 mikron for the breadths.

TABLE III.

Analytical Constants for Variation in Chilomonas.

Constant	Serie	es A.	Series B.				
Constant	Length	Breadth	Length	Breadth			
μ_2 μ_3 μ_4 β_1 $\sqrt{\beta_1}$ β_2 $\beta_2 - 3$ κ_1 Skewness d	6·9137 -·0494 122·6396 ·000007 ·0027 2·5657 -·4343 -·8685 -·000006 -·00198 -·0052 mikrons	4·4534 ·3113 62·1412 ·0011 ·0331 3·1332 +·1332 ·2632 ·0022 +·0153 ·0161 mikrons	6·4739 2·9056 133·9061 ·0311 ·1763 3·1950 +·1950 ·2966 +·0793 +·0805 +·2048 mikrons	5·5237 5·5862 118·4789 ·1852 ·4303 3·8831 +·8831 1·2107 ·1209 +·1592 +·1870 mikrons			

This table brings out a number of points of interest, but before considering it in detail it is necessary to have before us the values of the probable errors of certain of the constants, on the assumption that all the distributions obey the normal or Gaussian law. The formulae for these probable errors have been given by Pearson (1905 and elsewhere), and it is unnecessary to repeat them here. In Table IV are given the values of the probable errors of the four constants which are of the most importance in testing whether a distribution significantly differs from the normal law, viz., $\sqrt{\beta_1}$, β_2 , skewness, and the "modal divergence," d.

TABLE IV.

Probable Errors of Constants for Normal Distribution.

Constant	Series A. N=201	Series B. N=175
$ \sqrt{\beta_1} $ $ \beta_2 $ Skewness $ d $ Length $ d $ Breadth	$\pm .1165$ $\pm .2331$ $\pm .0583$ $\pm .1532$ mikrons $\pm .0615$,,	$\pm .1249$ $\pm .2498$ $\pm .0624$ $\pm .1589$ mikrons $\pm .0734$,,

Examining the values given in Table III in connection with those for the probable errors in Table IV we see at once a number of differences between Series A and Series B. Considering first the question of the symmetry of the distributions, it is evident, from the values of $\sqrt{\beta_1}$ and of the skewness, that for Series A the distributions of both length and breadth are symmetrical within the limits of the errors of random sampling. In both distributions the skewness and $\sqrt{\beta_1}$ differ from their theoretical value (if the distribution be truly symmetrical) of zero, by only small fractions of their probable errors. With Series B the case is different; here both the length and breadth distributions give values for $\sqrt{\beta_1}$ and skewness which differ from zero by more than their probable errors. In the case of the breadths this deviation rises to more than twice the value of the probable error. It is probable that we have to do with real skewness here, and not simply with an effect of random sampling. An examination of the "modal divergence" leads to the same result: namely, in both the length and breadth distribution of Series A the mode does not significantly differ from the mean, while in Series B the value of d is for both distributions greater than its probable error. For the breadths this divergence of d from zero is about 2.6 times its probable error. The skewness is positive in both of the Series B distributions, or the mean is greater than the mode.

Turning to the kurtosis (cf. Pearson, 1905, p. 173) measured by the quantity $\eta = \beta_2 - 3$, it is seen that for the lengths in Series A it has a value of -4343, with a probable error (if the distribution were truly mesokurtic) of ± 2331 . We conclude then that the distribution is probably significantly leptokurtic (i.e. is less flat-topped than the normal curve), and that we shall get better results if we

graduate with some curve, which, while still remaining symmetrical about the mean, has a sharper peak than does the normal curve. The breadth distribution for Series A is sensibly mesokurtic, with a value of $\eta=1332$ and a probable error of ± 2331 . The same is true for the length distribution of Series B, though in this case the value of η is somewhat larger. The breadths in Series B give a value for η of ± 8834 with a probable error of ± 2498 ; the distribution is significantly platykurtic.

Putting all the results together we conclude that the individuals of Series A vary symmetrically about their type condition, while those of Series B exhibit skew variation. For the character length this skewness is slight and taken by itself could not be considered significant, but considering that the length and breadth distributions of this series (B) exhibit deviations from normality in the same direction with respect to all constants we may safely conclude, I think, that we are dealing with a case of real skewness. This conclusion is of interest when it is recalled that Series A represents the extreme of unfavourable environmental conditions, and Series B the optimum environment. This point will be more fully discussed farther on in the paper.

From the values of κ_1 and κ_2 , β_1 and β_2 , it is clear that the length distribution of Series A calls for a curve of Type II; the breadth distribution of Series A for a normal curve; while both length and breadth distributions of Series B demand curves of Type IV.

The frequency distributions and their fitted curves are shown graphically in Figures 2 and 3. The equations to the curves are:

Series A, Length.

Type II.
$$y = 28.5889 \left(1 - \frac{x^2}{81.69698}\right)^{4.4084}$$

Origin at mode = 22.555 mikrons.

Series A, Breadth.

Normal.
$$y = 37.9978 e^{-.4491 x^2}$$

Origin at mode = 9.479 mikrons.

Series B, Length.

Type IV.
$$y = 4.7077 (\cos \theta)^{45.7771} e^{12.8514\theta}$$

$$x = 15.9676 \tan \theta$$

Origin at 19.973 mikrons.

Series B, Breadth.

Type IV.
$$y = 14.5990 (\cos \theta)^{15.3703} e^{4.9594 \theta}$$

 $x = 7.7502 \tan \theta$
Origin at 9.375 mikrons.

Considering the small number of observations these curves give very good graduations. The skewness of the Series B distributions is very apparent in these

diagrams. They also show clearly to what a marked degree the type of the individuals in favourable conditions differs from that of the individuals living under unfavourable conditions. The exact amount of this difference is however more directly brought out by a comparison of the chief physical constants of the distributions, to which we may now turn.

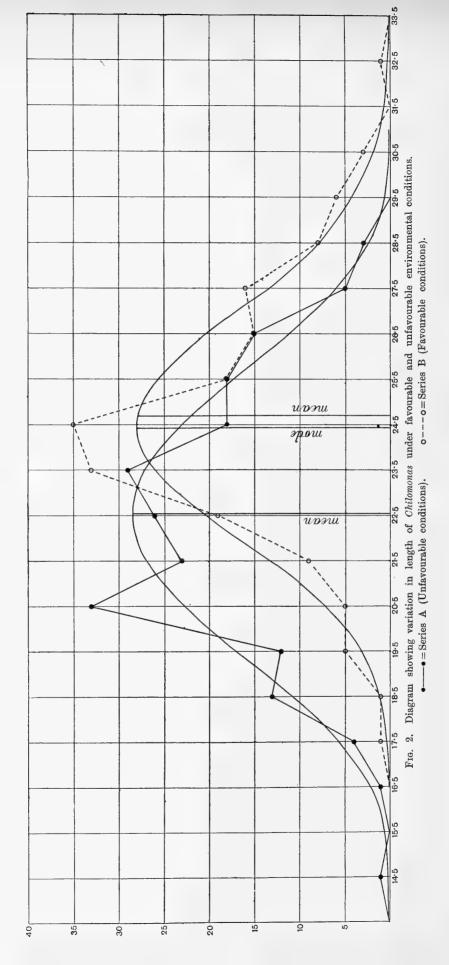
In Table V are given the means, standard deviations, and coefficients of variation, for the characters length, breadth, and index, in the two series. In order to facilitate comparison I have also tabulated the absolute differences (with their probable errors) between the corresponding constants of the two series. The differences are given the plus sign when the Series B constant is the greater and the minus sign in the opposite case.

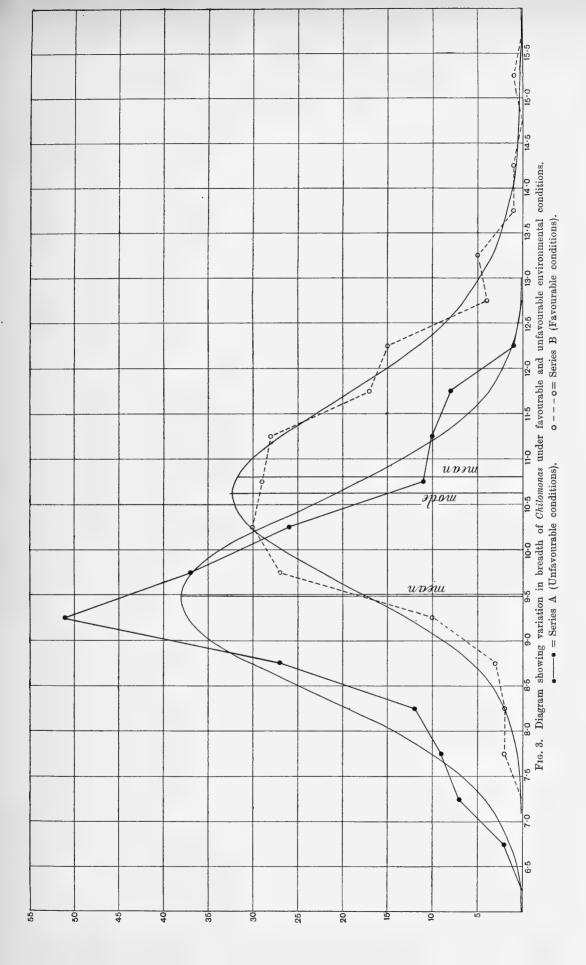
TABLE V.

Comparison of Type and Variability of Chilomonas Living under Favourable and Unfavourable Conditions.

Character	Series	Mean	Standard Deviation	Coefficient of Variation
Length	B, Favourable conditions A, Unfavourable ,, Difference	24.660 ± .130 mikrons 22.555 ± .125 ,, +2.105 ± .180 ,,	2·544±·092 mikrons 2·629±·088 ,, -·085±·128 ,,	10·318±·376 11·658±·397 -1·340±·547
Breadth "	B, Favourable conditions A, Unfavourable ,, Difference	10·813 ± ·060 mikrons 9·479 ± ·050	$ \begin{array}{c} 1.175 \pm .042 \text{ mikrons} \\ 1.055 \pm .035 & ,, \\ +.120 \pm .055 & ,, \end{array} $	10.868 ± .396 11.132 ± .379 264 ± .548
Index	B, Favourable conditions A, Unfavourable ,, Difference	44·060 ± ·203 °/。 42·137 ± ·191 °/。 +1·923 ± ·279	3·972±·143°/。 4·006±·135°/。 034±·197	

It is seen at once that the differences between the two series in respect to type are large. The individuals living under favourable conditions are longer and broader both absolutely and in proportion to their length than are those living under unfavourable conditions. There can be no doubt that these differences between the means are significant in comparison with their probable errors. This result shows clearly that even in such a form as *Chilomonas* the conditions of existence which are favourable to rapid multiplication are also favourable to large size of body. Such a relation is, of course, to be expected in an organism reproducing sexually, but it is not so obviously necessary a priori in an organism reproducing by fission. In fact, it might on general grounds be maintained that when the conditions were such as to lead to very rapid reproduction by fission, the average size of the individuals would diminish, on account of fission taking place before the maximum growth possible had occurred. The present data show that such is not the case, however.





In view of the striking difference in type between the two series it is somewhat surprising to find them so nearly alike in variability. For none of the characters can the differences in the variation constants be said to be significant. It is worth noticing, however, that, with a single exception (the absolute variation in breadth) the differences between the variation constants, both absolute and relative, are negative. That is to say, the individuals of Series A, living under unfavourable conditions, are slightly more variable than those of Series B, living under favourable conditions. The differences are so small in comparison with their probable errors, however, that no particular stress is to be laid upon this fact. The conclusion to which we must come from the present data is that there is no marked difference in variability between individuals living under conditions which in the one case were very favourable and in the other case very unfavourable to the continued existence of the race in the active condition. What slight preponderance exists is in favour of greater variation under unfavourable conditions.

We may next examine the correlation between length and breadth of body for the two series. The raw material is given in Tables I and II, whence, calculating the coefficient of correlation by the usual formula $r = \frac{S(xy)}{N\sigma_{c}\sigma_{c}}$, we get:

Series A (Unfavourable conditions)
$$r = .683 \pm .025$$

Series B (Favourable conditions) $r = .617 \pm .032$
Difference = $.066 \pm .041$

These values of the coefficients are high, indicating a closer relationship between length and breadth of body in this simple protozoan than would have been predicted, I think. Just as in the case of the simple variation, however, there is no certainly significant difference between the two series in respect to degree of correlation. What difference there is is in favour of higher correlation under unfavourable conditions, but no great stress is to be laid on the difference.

Since biometric investigations on Protozoa are as yet not especially numerous, it seems desirable to examine the regression for these two characters, length and breadth, to determine whether it is linear or not. The equations to the regression coefficients are as follows:

Series A, Length on breadth.

$$b_1 = \frac{2.6294}{1.0552} \times .6832 = 1.7024.$$

Series A, Breadth on length.

$$b_2 = \frac{1.0552}{2.6294} \times .6832 = .2742.$$

Series B, Length on breadth.

$$b_1 = \frac{2.5444}{1.1751} \times .6168 = 1.3355.$$

Series B, Breadth on length.

$$b_2 = \frac{1.1751}{2.54444} \times .6168 = .2849.$$

From these values we easily obtain the following characteristic equations, in which L signifies "length of body" in mikrons, and B "breadth of body" in mikrons.

Series A {Probable
$$L = 1.7024 B + 6.418$$

Probable $B = .2742 L + 3.295$

Series B {Probable
$$L = 1.3355 B + 10.219$$

Probable $B = .2849 L + 3.787$

The means of the arrays and the fitted regression lines are shown in Figures 4 and 5.

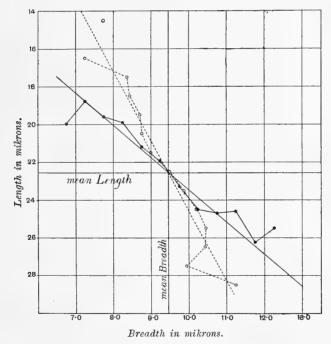


Fig. 4. Regression lines for Series A (Unfavourable conditions). \bullet — \bullet = Regression of length on breadth. \circ – – \circ = Regression of breadth on length.

It is evident that the regressions are very closely linear. This result is in accord with what has been found for the other Protozoa for which this point has been determined, namely Arcella (Pearl and Dunbar, 1903) and Paramecium (Pearl,

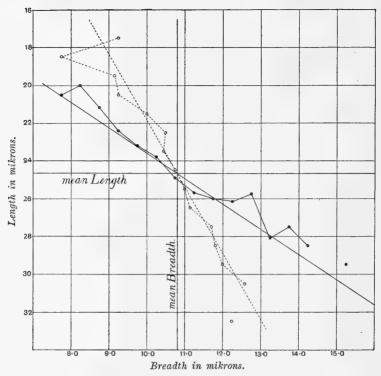


Fig. 5. Regression lines for Series B (Favourable conditions). \bullet — \bullet =Regression of length on breadth. \circ – – \circ =Regression of breadth on length.

1906). It seems to me to be a result of considerable significance that in organisms representing three of the important types of protozoan structure (namely the Rhizopoda, Flagellata, and Ciliata) the regression between size characters is substantially linear. Biometric work on a variety of multicellular organisms has shown that in such forms linear regression between size characters in the fully developed (i.e. adult) organism is practically the universal rule. To find the same thing true of Protozoa seems to me to be definite quantitative evidence that the factors concerned in regularity of form production, if not the same, at least operate in fundamentally similar ways in unicellular and multicellular organisms.

We may next examine the index correlations. It is of considerable theoretical interest to know what degree of correlation exists between the length-breadth index and each of the characters entering into it. We shall then have a measure of the extent to which size of body and shape of body are associated in their variations. These correlations may be determined from formulae which are readily deduced from the fundamental theorems regarding the variation and correlation of indices given by Pearson (1897). The particular formulae used in the special case with which we have to do here are given in another paper by the present writer (1906), and need not be repeated. The values found for the index correlations of *Chilomonas* are given in Table VI.

TABLE VI.

Index Correlations in Chilomonas.

Series	Characters	Gross (ρ)	Spurious* (ρ_0)	Net* $(\rho - \rho_0)$
A (Poor conditions) B (Good ") A (Poor ") B (Good ",)	Index and Length ", ", Breadth ", "	- '446 ± '038 - '389 ± '043 + '407 ± '040 + '426 ± '042	- ·723 ± ·023 - ·689 ± ·027 + ·723 ± ·023 + ·689 ± ·027	+ '277 ± '044 + '299 ± '046 - '317 ± '043 - '263 ± '047

In this table the column headed "Gross" gives the observed correlations between the designated characters; the column headed "Spurious" gives the value which this correlation would take if the organic correlation between length and breadth did not exist; and finally the column headed "Net" gives the portion of the "gross" coefficient which is due to the existence of an organic correlation between the index and the particular character under consideration.

From the values in Table VI we see that:

- (a) The net organic correlation between the length-breadth index and length is positive, while the correlation between the index and breadth is negative. Thus the net correlations are opposite in sign to what the gross correlations are. The sign of the gross coefficients is in each case what we should expect it to be for arithmetical reasons, because the length is the denominator and the breadth the numerator of the index fraction.
- (b) The net coefficients are of considerable magnitude, and represent clearly a sensible real correlation between the index and the absolute dimensions. They show that there is a definite correlation in this form between shape and size of body. The theoretical bearing of this result will be discussed farther on in the paper.
- (c) The index correlations are of sensibly the same magnitude in both series, as are the correlations for absolute size characters (cf. supra, p. 64).
- (d) The index is correlated more closely with breadth than with length in Series A, where the environment was unfavourable, while the opposite relation prevails in Series B, with a favourable environment. The differences are small, however, and no great stress is to be laid on them.

Without at this time entering upon any discussion of the matter, I should like merely to call attention to the fact that the values for the variation and correlation constants for *Chilomonas* agree very well with what we have found for similar characters in other Protozoa. From Table V we see that the coefficients of

* The probable errors in the "spurious" and "net" columns are calculated from the usual formula for the probable error of a correlation coefficient, P.E. $r = 67449 \frac{1-r^2}{\sqrt{n}}$. This assumes that the probable error of these constants is the same as it would be if they had been determined from the product moment. The error involved in this assumption is probably insignificant.

variation for length and breadth in *Chilomonas* have values ranging roughly between 10.5 and 11.5. There is no sensible difference in relative variability between length and breadth of body. For Arcella we have for the diameter of the shell a coefficient of variability of 10.27, and for the diameter of the "mouth" opening a coefficient of 13.66 (cf. Pearl and Dunbar, *loc. cit.*). The mean value of the coefficient of variation in length of body for a series of Paramecia reared under various environmental conditions and including all told 4900 individuals is 8.45 (cf. Pearl, *loc. cit.*). All these values cluster well together, and point to a value of roughly 10 per cent. for the coefficient of variation in size characters of this kind in Protozoa.

Discussion of Results.

It now remains to consider the meaning of the facts set forth in the preceding sections. These facts may be summarily stated as follows: comparing two populations of the same local race of the flagellate Infusorian *Chilomonas paramecium*, one of which populations was living under the most favourable of environmental conditions and the other under the least favourable conditions, we find:

- (1) That in respect to absolute length and breadth of body and in shape of body as measured by the length-breadth index, the *types* of the two populations are significantly different. Those living in the least favourable conditions are smaller and relatively slenderer than the individuals in an optimum environment.
- (2) In respect to the characters dealt with, both populations are equally variable, and have their parts correlated to an equally high degree. There is a slight tendency for the individuals living in the unfavourable environment to be more variable and more highly correlated, but in view of the probable errors the differences cannot be said to be certainly significant.
- (3) The individuals living under unfavourable conditions vary symmetrically about their typical condition, while the group from the optimum environment exhibit an unsymmetrical or skew variation about the type.
- (4) There is a sensible correlation between the absolute size of the body and its shape as measured by the length-breadth index.

The first of these results is exactly what we should expect to find, on general grounds. There can be little doubt that one of the chief factors which induce saprophytes like *Chilomonas* to disappear from a culture is that the medium no longer furnishes proper food (either in amount or kind, or both). The Series A individuals are in all probability to be regarded as "starved." We should in consequence expect them to be smaller than the flourishing individuals of Series B. Similar cases of diminution in size in organisms living in unfavourable environments have recently been described by Dimon (1902) for *Nassa*, and by Warren (1902) for *Hyalopterus*.

It is of more interest to find that in spite of the great change in the type between the two populations there is no marked difference in the amount of variation. That is to say, relatively equal degrees of aberration from the typical condition are, on the whole, produced with equal frequency in the two populations. Thus there is apparently nothing like a selective process in the encystment of this form. The last individuals to "survive" in the active condition are as variable as the general population.

The third result appears to be worthy of notice. For both length and breadth there is a positive skewness in the variation of the individuals in the optimum environment. That is to say, the mean falls to the right of the mode, or the curve tends to "tail out" more on the side of large individuals than in the opposite direction. This indicates that the conditions which are favourable to the production of large size of body in the population as a whole, are also more favourable to the production of exceptionally large than of exceptionally small individuals. In other words, the direction of the skewness is the same as the direction in which the type is changing. May not this relation be generally true when a change of type is brought about by direct environmental action rather than by selection, the distribution finally becoming symmetrical when the possible limit of direct modification of the type is reached? The results from both series of *Chilomonas* are in accord with such a view, but of course are altogether too meagre to base more than a suggestion upon. The question will be more definitely tested on Paramecium material collected ad hoc.

The result that shape of body as measured by the length-breadth index is sensibly correlated with absolute size seems to me to have such important theoretical significance that it appears desirable to discuss the matter in some detail. At the outstart I may say that the results from *Chilomonas* on this point are by no means an isolated case. I have elsewhere shown (1906) on material comprising a number of fairly long series that the same thing is true for Paramecium, with, of course, differences of detail in the values of the constants. The following table gives the values of the net organic correlations between index and length and breadth of body in three lots of Paramecium, comprising altogether 544 individuals. Other data are given in the paper referred to, but these will be sufficient for comparison in the present instance.

TABLE VII.

Correlation of Index with Absolute Dimensions in Paramecium.

Series*	Characters	Net Correlation $(\rho - \rho)$
A C	Length and Index Breadth ,, ,, Length ,, ,,	*4134 ± *0386 - *2246 ± *0442 *3692 + *0410
Ë	Breadth ,, ,, Length ,, ,, Breadth ,, ,,	$ \begin{array}{r}2497 \pm .0445 \\3556 \pm .0513 \\2964 + .0535 \end{array} $

^{*} The letters designating the series are those used in the original paper.

Comparing these values with those for *Chilomonas* in Table VI above, we see that the signs of the correlations are the same in the two cases: the index is positively correlated with length and negatively with breadth. In Paramecium the correlation is distinctly higher between length and index than between breadth and index, a relation which apparently does not exist in *Chilomonas*. These differences are, however, not of importance for our present purpose. The essential fact is that in these two unicellular organisms there is a significant correlation between shape of body and absolute size.

Now Driesch (1900, 1901 and elsewhere) has stated as one of the most fundamental laws of morphogenesis that the *proportionality* of the parts in a differentiated system is absolutely independent of the size of the system. Thus in the case which has already been mentioned (p. 53) he holds that the proportions of the three regions into which the intestine of a sea-urchin larva is divided are constant whatever the size of the larva.

The following quotations will make Driesch's position clear. He says (1900, p. 397): "Dieses Faktum lehrt uns zugleich die vollständige Proportionalität der inneren Ausbildung bei Keimen aus isolirten Blastomeren im Vergleich zu Normalkeimen kennen: erstere sind durchaus ein verkleinertes Abbild letzterer. In meinen Betrachtungen über die Lokalisation morphogenetischer Vorgänge spielt die Wahrung der Proportionalität bei verkleinerten Gebilden bekanntlich eine grosse Rolle." Again in his Organischen Regulationen (1901, p. 176): "Das aber ergiebt als Schluss:

$$\frac{x}{q} = A *.$$

Für eine bestimmte Organbildung bleibt also in jedem Experimentalfall das Verhältniss ihres Abstandes vom Ausgangsende der Messung zur Gesammtlänge konstant." Regarding the "constant" A, Driesch says (loc. cit., p. 178): "In dem 'A' unserer Formel ist nämlich Dasjenige verkörpert, was seit Alters 'Substantialität der Form' genannt worden ist, was man aber auch, mit aristotelischem Ausdruck, Entelechie nennen könnte. Die Formsubstantialität tritt nun in der Formel x = g.A als in elementarer Weise massgebend für das Geschehen in jedem Falle auf." And again (loc. cit., p. 179): "Unsere Grösse A wird dem analog, was im Physikalischen eine Konstante ist. Der Satz: 'dieses hier vor uns liegende äquipotentielle System (dieser Keim) hat die Entelechiekonstante A' heisst: wie gross das System auch sein mag, das Entwickelungsgeschehen an ihm muss in einer Weise vor sich gehen, dass eine endliche Konfiguration bestimmter Art und Proportionalität an ihm auftritt. Ebenso bleibt die Konstante eines homogenen Stückes Metall für elektrische Leitfähigkeit dieselbe, mag das Stück gross oder klein sein."

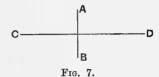
The point may be stated in its most general form in the following way: Let AB, BC, and CD (Fig. 6) be any three dimensions of an organism. Then according to the position maintained by Driesch the ratios $\frac{AB}{AD}$, $\frac{BC}{AD}$, $\frac{CD}{AD}$, etc., are

^{*} Where x and g correspond to AB and AD in Fig. 6, below.

each a constant regardless of the absolute size of the individual dimensions themselves. In other words, it is contended that these ratios are not sensibly



correlated with the absolute size of the system. From this assumed independence Driesch deduces rather far-reaching generalizations, as the quotations show. But, as has been brought out above, when the matter is subjected to quantitative test it is found that, in the case of two protozoan forms at least, there is a sensible and definite correlation between such a ratio $\frac{AB}{CD}$ (Fig. 7) and the



absolute size of the system. Now clearly the ratio $\frac{AB}{CD}$ is an index of the proportionality of the two chief dimensions of the body, or, in a word, of the shape of the body. It seems to me that the facts given demonstrate that in Paramecium and Chilomonas size and form of body are correlated, and hence, in so far, experience does not agree with Driesch's generalization. It is probable that the same thing will be found to be generally true. It has been demonstrated for the principal indices of the human skull by Miss Fawcett (1902) and Macdonell (1904). Unpublished material on other and widely different organisms gives the same result. If it holds generally that the proportionality of the parts and the absolute size of a differentiated system are sensibly correlated, it seems to me that the analysis on which Driesch's first "proof" of the "Autonomie der Lebensvorgänge" is based will have to be considerably modified.

Summary.

A comparative study of variation and correlation in the flagellate Infusorian *Chilomonas paramecium* when living on the one hand under the optimum environmental conditions, and on the other hand under extremely unfavourable conditions, has led to the following results.

- 1. The individuals in the unfavourable environment are markedly smaller than those in an optimum environment.
- 2. The individuals under the two sets of conditions are significantly different in shape, those living under poor conditions being relatively narrower.
- 3. There is no marked difference in variability or correlation between the two groups, though there is a slight preponderance for both variability and correlation in the group living in the unfavourable environment.

- 4. The distribution of variation is skew in the case of the individuals from the optimum cultural condition, and symmetrical in the case of the other group.
- 5. The skewness is positive, or in other words, the majority of the population are *larger* than the modal individuals.
- 6. There is a considerable degree of correlation between length and breadth of body in *Chilomonas* (coefficients > 6). The regressions between these characters are linear.
- 7. The values for the coefficients of variation and correlation in *Chilomonas* are of the same general order of magnitude as those which have been determined for other Protozoa.
- 8. There is a distinct correlation between the shape of the body and its absolute size in *Chilomonas*. The bearing of this result on Driesch's first "proof' of the "Autonomie der Lebensvorgänge" is discussed.

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THE NON-INHERITANCE OF SEX IN MAN.

By FREDERICK ADAMS WOODS, M.D.

The appearance of several recent articles summarizing our knowledge concerning sex determination has suggested the possibility of an inheritable influence in the distribution of the sex of offspring. According to this view there should be some families in which males predominate, and some in which females appear in exceptional numbers. Although not presenting satisfactory statistics this belief was held by Lorenz (2) (p. 364), Lenhossék (1) (p. 56), and Orschansky (5) (pp. 18, 126), who considered sex subject to hereditary influences. Orschansky (p. 126) states: "Als Hauptresultat unserer Beobachtungen über die Entstehung des Geschlechts beim Kinde: ergiebt sich, dass die Entstehung des einen oder des anderen Geschlechts in gewissen Grenzen eine erbliche morphologisch-physiologische Funktion des gesamten Organismus, und hauptsächlich der Sexualorgane der Eltern ist."

If it is true that a purely inherited tendency is of any moment whatever in governing sex distribution, then the parents of "fraternities" in which there is a marked departure from the normal proportions, should themselves belong to "fraternities" which, on the average, show something of the same departure. That this is not the case and that there is no correlation in sex-producing power between mother and daughter, or father and son, I believe to be conclusively proved by the following statistics.

I have used the records contained in Dr K. von Behr's "Genealogie der in Europa regierenden Fürstenhäuser. Zweite Auflage," Leipzig, 1870. This large and authoritative work contains excellent material for such a research. Within its pages is to be found the full genealogical tree of every reigning house in Europe; and the birth and sex of every infant born is recorded with the utmost care. I have collected a portion of my material from this book, and within certain rigid limits, have included all the individuals mentioned. Taking one family after another, I have started with the last generation, the first child of which was born before the close of the eighteenth century. A count was made of the number of males and of the number of females in this generation. I then looked up the record of the mother of these children. She, almost invariably, being also of royal blood, was to be found recorded somewhere in the book under the heading of the

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house from which she came. The sexes of children which her mother gave birth to were thus obtained, and were placed in the columns at the right of the columns containing the figures for the younger generation. Next, the sexes of the children in the father's generation were recorded and can be seen in the left-hand columns just below the children's (see Table I). This record was repeated for every generation back to the beginning of the seventeenth century. All the families, touched upon at all, have been studied completely, and are in general the same houses the records of which I used in a study "Mental and Moral Heredity in Royalty." These families are to be classified among the more famous branches of royalty, the genealogical and biographical records of which are seldom difficult to obtain even on the female side. Several families in von Behr's genealogy have been entirely unutilized in this research. I have omitted them merely to save time. They are such families as have made frequent alliances outside the strictly royal houses, and consequently one could not find the maternal records in von Behr. This omission should have no effect on the general averages.

In the illustrative table below we see the distribution of sex among the children of different fraternities for several generations. Thus the figures within the block for the Hapsburgs (page 208 of "von Behr") give us the history of the sex distribution in that house during two centuries. In the upper left-hand corner we see the figures 1 and 3. This means one male and three females were born in the last generation which this family produced prior to 1800 A.D. These children were Maria Theresa, her one brother and two sisters. Their mother was Elizabeth of Brunswick who was found to have been one of four sisters. This fact is recorded in the figures 0 and 4 just to the right of 1 and 3. Their father was Charles VI of Austria, of a family of three boys and eight girls, which fact is recorded just below the figures 1 and 3. The ancestry of Charles VI's fraternity of 3 boys to 8 girls was next taken up and so on back to the parents of the fraternity reading 6 and 9, which was the most ancient studied. In the first three fraternities 1-3; 0-4; and 3-8, we see an apparent inherited tendency towards the birth of girls. Our averages and correlation coefficient show, however, that this is but a meaningless accident.

In order to obtain material sufficient to give me a low probable error, I added to the facts drawn from von Behr, some statistics taken from Burke's "Peerage and Baronetage," 1895. Here I have utilized the records of the two most recent generations, taking first the numbers of males and females in the very latest generations, and compared these fraternities with the fraternities of their fathers and mothers. I have taken only those families in which the eldest child was born prior to 1880. I have also left out of consideration those fraternities whose mothers were not also born in the peerage, because it would be very laborious to look up the ancestry of such mothers. It is really surprising how many peers of to-day marry the daughters of commoners, making it often necessary to turn over many pages of Burke to find a case where the maternal ancestry is recorded in this same book of the élite.

TABLE I.

Sample Table from von Behr's "Genealogie."

von Behr page	of sex	bution among nildren	of sex the m	bution among other's ernity	von Behr page	of sex	bution among aildren	of sex the m	bution among other's crnity	von Behr page	of sex	bution among ildren	of sex the me	bution among other's rnity
	3	ç	3	9		ð	9	3	9		đ	9	đ	9
146	4 2 3 2 2 4	3 0 2 3 3 0	3 7 2 10 2	5 6 3 4 2	168	8 5 6 6	5 2 6 8	3 2 2 —	3 2 5 —	192	$\begin{array}{c} 1 \\ 1 \\ 1 \\ 3 \\ 4 \\ 2 \end{array}$	0 2 0 6 6 1	$ \begin{array}{c} 1\\ 4\\ 5\\ 1 \end{array} $	2 6 3 3
147	4 5 13 2 12 10 2	0 2 6 6 6 1 3	4 4 2 5 0 6 6	4 1 1 7 1 4 5	184	8 5 5 9 2 1	4 1 4 6 1 1	2 7 2 5 —	3 4 5 - 2	192	2 4 4 3 2	0 1 3 0	1 3 4 — 0	$\begin{array}{c} 7 \\ 6 \\ 6 \\ \hline \\ - \\ \hline \end{array}$
150	5 5 4 3 10	5 2 4 5	3 9 4 3	4 6 9 4	185	1 2 3 2 1 3	1 1 0 2 7 5	$\frac{1}{2}$	$\begin{bmatrix} 1 \\ - \\ 4 \\ - \end{bmatrix}$	196	2 3 3 2 1	6 4 5 3 2	1 4 1 1 -	1 7 1 4
155	5 4 4 6	5 5 8 4	$\begin{array}{c} 1\\4\\3\\-\end{array}$	5 6 3	187	3 1 1	$egin{array}{c} 3 \\ 2 \\ 1 \\ 7 \end{array}$	5 4 5 5	2 1 4 3	199	0 3 1 5	$\begin{matrix} 1\\0\\7\\4\end{matrix}$	6 6 3 —	5 2 4 —
158	4 2 2 4 1 1 4 6	3 4 2 9 1 4 6 4	8 1 5 2 — 2 5	7 5 8 6 9 7	188	2 2 5 3 3 3 3	1 0 2 4 8 0 0 3	6 7 5 6	1 6 8 - 5 3 5	201	6 7 5 4 6 3 4	3 3 5 2 4 6 3	2 1 1 3 - 4 8 1 2	4 3 4 9 6 7
166	5 7 2 5 2	4 3 2 8 2	$\frac{1}{2}$ $\frac{3}{2}$	3 2 - 3	190	2 3 8 6 4	0 3 6 7 3	$\frac{4}{7}$	2 8	208	5 5 4 1 3	1 4 3 8 2	9 0 9 4	7 8 - 4 8 4
					191	6 7 6	6 10 7	8 5	6 11 —		4 6 4	3 9 11	6 5	4 2 -

TABLE II.

Sample Table from	Burke's " Peerage."	Distribution of the sexes.	(Youngest Generations.)
1	U	J	

Burke's Peerage 1895 page			sex among of sex among of sex among the mother's the		of sex	Distribution of sex among the father's fraternity		Distribution of sex among the children		Distribution of sex among the mother's fraternity		Distribution of sex among the father's fraternity	
	8	9	8	Ŷ	\$	Ŷ		♂	Ŷ	ð	9	₹	Ŷ
1 8 9 29 30 35 51 58 71 109 114 119 144 170 180 181 182 199 217 222 232 237 250 270 271 271 274 282	6 3 5 1 2 4 5 5 1 4 4 5 5 5 1 4 4 0 6 2 1 5 1 3 1 1 6 3 2 2 0 1	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 4 2 2 5 7 4 2 7 3 7 5 4 2 6 6 8 2 2 7 4 1 3 3 3 3	1 3 4 4 4 5 7 7 2 8 2 3 6 7 4 5 3 2 4 3 7 2 5 3 5 6 2 5 2 3	6 3 2 3 3 1 2 2 1 1 1 3 5 4 4 3 2 2 1 6 4 4 1 3 3 2 2 3	7 3 3 4 4 4 2 1 3 0 0 1 6 2 4 4 3 3 6 0 0 4 4 2 1 1 1	304 308 308 310 316 323 337 343 344 347 355 366 384 402 403 411 416 417 434 440 447 470 471 479 483 557	1 2 4 1 4 3 3 4 5 3 6 6 2 2 3 4 4 8 6 0 6 2 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 0 1 1 0 1 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 1 0 1 1 0 1 1 0 1 0 1 0 1 0 1 1 0 1 1 0 1 0 1 1 0 1 0 1 1 1 0 1	0 3 3 3 1 6 3 3 5 3 1 0 5 2 0 2 3 3 3 5 3 6 6 6 6 6 7 6 7 8 7 8 7 8 7 8 7 8 7 8 7	3 0 2 4 5 0 2 1 3 2 4 2 0 4 0 7 4 6 2 1 4 2 4 3 6 6 6 6 7 7 4 6 6 7 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7	3 1 6 1 8 1 5 6 4 4 5 5 4 1 3 1 6 4 3 7 3 7 2 4 1 7 7 3 7 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8	2 4 4 4 2 2 3 5 5 3 1 1 6 3 2 2 2 1 1 2 1 1 5 8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3 7 7 8 7 3 2 6 1 0 1 6 1 2 4 1 1 1 2 4 1 7 0 0 2 3 4 1 1 2 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6

Following the tables recording these facts are the records of the distribution of sex obtained by the same method, for the next to the latest generations, in the male lines; and parallel to them the records of the distribution of sex in the fraternities of their fathers and mothers.

I then sought to find a correlation in the distribution of sex in the fraternities of all the children, and the distribution of sex in the fraternities to which their parents belonged.

I have divided all the fraternities into two classes, first those with an excess of males, and second those without an excess of males. By this means I could utilise those cases which frequently occur, in which the proportion of males and females is equal.

The four-fold correlation table shows us at once, that the inheritable influence in the tendency to produce an excess of males must be very slight. Working it out carefully we find the coefficient, r, practically zero, and well within the probable error.

Parental.

		Fraternities showing an excess of males	Fraternities showing no excess of males	Totals
Filial.	Fraternities showing an excess of males Fraternities showing no excess of males	291 303	423 448	714 751
	Totals	594	871	1465
	h = 2392224,	H = 3876579,		

k = .0316591

K = 3987424.

This gives the equation:

 $006628 = r + 003787r^2 + 003787r^2 + 00008r^3 + \dots$ the root of which is $r = 00066 \pm 00008$.

I have also selected those cases in the foregoing tables in which an excess of males happened on both sides of the house in the ancestral (parental) generations, and have sought to find if here an excess of males might not be shown among their children. Instead of an excess of males there were but 334 males against 351 females born in such families. Similarly the families with an excess of females in both sides of the ancestry produced but 357 female children against 402 males.

Thus we may conclude that the determination of sex, in man at least, can be shown to be unaffected by hereditary influence. This agrees with the statistical conclusion of Simon Newcomb (4) obtained by a different method.

Nor does it seem probable that any Mendelian principles control the determination of sex in man, for then we should expect some correlation in the distribution of the sexes in successive generations due to the union of dominants with each other, and also due to the union of recessives with each other.

These statistical proofs which lead us to a definite conclusion of non-inheritance have an important bearing upon several theories regarding the determination of sex. If sex is largely determined by agencies acting upon the young and supposedly indifferent embryo, even if these were largely external (nourishment, temperature, etc.), the constitutional peculiarity of the mother would have, under ordinary circumstances, a large share in forming these differences of environment. As we know that constitutional peculiarities are to a measurable degree inherited and capable of giving us a correlation coefficient, and as we here find no such coefficient, we see an argument in favour of the view that sex is not determined during gestation.

There are moreover many other considerations which lead to the belief that sex is not influenced after impregnation, but is already determined at that time or before (conf. Lenhossék (1) and Morgan (3)). Many writers who favour this theory nevertheless believe that parental organisms have considerable influence on the proportion of males to females, although this influence is exerted prior to impregnation. This question is discussed in its many relations in Orschansky (5). His statistics are, however, far from convincing. On page 122 we find the following: "Die Beobachtungen an kranken Familien ergeben die augenscheinlich paradoxe Thatsache, dass ein Erzeuger mit der schwächsten Konstitution eine grössere Neigung als ein gesunder äussert, sein Geschlecht auf seine Kinder zu übertragen."

If it be true that sex is dependent on any constitutional or nutritional influence exerted during the formation or ripening of the ova or spermatozoa, then like other constitutional differences it should be inherited. My own figures tend to show that neither the soma of the father nor the soma of the mother have any influence, at least in man, in the determination of sex, nor is the proportionate distribution of sex in any degree subject to hereditary influence.

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ON THE INHERITANCE OF THE SEX-RATIO.

By DAVID HERON, M.A.

It has been suggested that the approach to equality in male and female births is an illustration in some mysterious manner of Mendel's theory of heredity. Observers have actually counted the number of males and females born in divers species with the conception that the approach to equality thus rendered manifest illustrates in some way Mendelian principles. I am not prepared to say it does not, because I have failed to grasp the manner in which those principles are applied to this case. If the demonstration depends, however, on the equality of the male and female births, their sensible inequality* in the case of man requires some further explanation; it is a case wherein environment or a priori, perhaps, race causes permanent and fairly constant deviations from equality. The aim of the present paper is to show that, as far as the writer can judge, there is no inheritance, Mendelian or other, of the sex-ratio. So far it confirms the results of Dr F. A. Woods stated in the previous paper, but the method of approaching the problem differs from his. No assumption is made as to the existence of a Gaussian distribution for the frequency, and the sex-ratio for the family of each individual is directly calculated and tabled. The paper further deals with the case of horse as There is no difficulty in extending the investigations to cattle and dogs from the herd and studbook returns, but the negative results provided by two such different species seem sufficient to demonstrate that the non-inheritance of sex is fairly widespread.

The material is the following:

(i) Data from a series of schedules on the size of families issued by Professor K. Pearson. Unfortunately this material proved less ample for this special purpose than we had anticipated. For although marriages must have existed at least 15 years in both generations for a schedule to be filled in, it happened in a very large number of the cases that the families in both generations did not provide the number (four) of children which seemed the least upon which a determination of sex-ratio could be made. Only 348 cases were taken from this source.

^{*} See C. J. and J. N. Lewis: Natality and Fecundity, 1906.

- (ii) Data drawn from *The Whitney Family of Connecticut and its Affiliations* (1649—1878), by S. Whitney Phoenix, 3 vols., Newport, 1878. This work contains a very great deal of genealogical information with regard to American families connected nearly or remotely with the Quaker Family of Whitney. In this case no family in both generations of less than four members was used to determine the sex-ratio, 2197 such families were extracted.
- (iii) Data drawn from *The General Studbook*, 20 vols., J. E. and T. P. Wetherby. In this case 1000 thoroughbred mares were taken at random and the sex-ratio of their produce and that of their dam calculated. Both mother and daughter must have had at least eight foals to be included in the list.

Some word must be said as to what has been understood by sex-ratio in the course of the work. It has been taken to represent the fraction: number of male offspring divided by total number of offspring. This point must not be forgotten in the following investigation. Thus, in dealing with the father's sibship, there must always be one male, and, considering the average size of human families, it is extremely unlikely that the sex-ratio as defined above should fall between '00—'05, it would in fact require at least 20 children. Again, in the mother's sibship there is always one female, and thus it is unlikely that the sex-ratio should fall between '95 and 1.00; this would again require at least 20 children. It will be seen that in the sex-ratio of the offspring's sibship we have a tendency for the frequency to lump up in these terminal groups, although their range is only half that of the other elementary frequency groups. This is almost entirely due to families in which there are no males or no females. Undoubtedly certain individuals tend to produce offspring all of one sex, either per se or because they are mated with a special type of consort. The latter reason seems the more probable, because, in the case of thoroughbred horses, where the matings change there appears to be no similar tendency for produce all of one sex to occur. A special study of cases in man and other animals in which for the same mating there is constancy of sex would be very instructive. It is probably due, as the tendency shows no sign in our tables of inheritance, to some physical characteristic of the individual which remains wholly dormant until it is affected by a corresponding characteristic in the mate. In working the moments and products, the frequency has been centered at the middle of the elementary range. This is probably not true in the case of the extreme elements in the offsprings' sibships in Tables I. and II., but the actual centering was found to have little influence on the correlations, and made no modification in the fundamental significance of the results. Sheppard's corrections were used.

In Tables I. and II. the sex-ratio of a family is correlated with that of the father's and mother's sibships respectively. It may be said: Why not, when dealing with the latter sibship, leave out father and mother successively in calculating the sex-ratio? A somewhat similar method has been adopted by Francis Galton for another purpose, and is justified in his case if we may assume that the chance of male or female is practically one-half for each family. It does

TABLE I.

Correlation of Sibships of Father and Offspring. Whitney Data.

Sex-Ratio of Offspring's Sibship.

Sibship.		90. —00.	91. —90.	.1525	.2535	9798.		29. —22.	92 29.	28. —21.	26. —28.	.95—1.00	Totals
Sex-Ratio of Father's Si	.00— .05 .05— .15 .15— .25 .25— .35 .35— .45 .45— .55 .55— .65 .65— .75 .75— .85 .95—1.00	 1 2 6 4 1	- 1 1 3 2 4 6 1 1	4 6 14 17 23.5 15.5 8 4.5 0.5		1 5 16 28 31 40 31 17 5 7	5:5 12*5 39 50 46 40:5 19:5 11 8	$ \begin{array}{c c} & - \\ & 1 \\ & 7.5 \\ & 5.5 \\ & 30 \\ & 34 \\ & 41 \\ & 31 \\ & 17 \\ & 12 \\ & 6 \end{array} $	3·5 6 19 27 27 29·25 10·75 11·5 6·5	$\begin{array}{c} -\\ -\\ 2\\ 7 \cdot 5\\ 11\\ 24\\ 35\\ 22 \cdot 25\\ 6 \cdot 75\\ 2 \cdot 5\\ 4 \cdot 5\\ \end{array}$	- - - 6 4 3 3 - 3 2	$\begin{array}{c c} - & 2 & 2 & 6 & 3 & 7 & 7 & 2 & 5 & 5 & & & & & & & & & & & & & &$	$\begin{array}{c} -2\\ 31\\ 64\\ 170\\ 215\\ 266\\ 207 \cdot 5\\ 96 \cdot 5\\ 61\\ 44\\ \end{array}$
	Totals	14	19	93	115	181	232	185	140.5	115.5	21	41	1157

TABLE II.

Correlation of Sibships of Mother and Offspring. Whitney Data.

Sex-Ratio of Offspring's Sibships.

Sibship.		90. —00.	9190.	28. —91.	.2535	2498.	9997.	.5565	2429.	.7585	96. —98.	.95—1.00	Totals
Sex-Ratio of Mother's Si	.00— .05 .05— .15 .15— .25 .25— .35 .35— .45 .45— .55 .55— .65 .65— .75 .75— .85 .85— .95		 1 3 1 0.5 	1·5 2 9 9·5 18·5 22·5 15·5 3·25 2·25 0·5 —	0·5 4 13 11·5 21·5 21·5 17·5 9·25 4·25 1·5	2 4 9·5 17·5 39 23 29 16 6 3	1 5 18 36 54 37 36 15 7	1 2 12 21 44 44 32 12 5 —	0·5 3 8·5 18·5 27 22 23 11·25 2·75 2	0·5 5 13 15 22 23 21 4·25 4·75 —		2 4·5 5·5 5 9 10 4·5 0·5	7 29 88·5 141·5 250 212 190 78·5 33·5 10
30	Totals	29	6	84.5	104.5	149	212	173	118.5	108.5	14	41	1040

not a priori seem justified in the present investigation, for one of the points involved is, admitting the average sex-ratio for the race to be not very far from 5, does this ratio vary significantly from individual family to individual family, as we should expect if it were inherited? Thus, if we leave mother or father out in calculating the sex-ratio of their sibship, we may be diminishing or emphasising

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the possibly slight tendency of that sibship to femininity or masculinity. The exclusion of even one individual can produce very sensible effects in the case of the small families which occur with human beings, although it is of less significance in the case of horses or many other mammals. It will thus be seen that the vertical and horizontal means and standard deviations of our Tables I. and II. could not be expected to be in accordance. To test whether this peculiarity has any influence on the result, Table III. was formed. This gives the correlation between sibships in the filial generation and all parental sibships. It would seem from this table that there really exists a marked difference between the distribution of the sex-ratio in the two generations, families which tend wholly or largely to one sex being much under-represented in the mated population.

TABLE III.

General Correlation, Parental and Filial Sibships. Whitney Family.

Sex-Ratio of Filial Sibships.

Sibships.		20. —00.	9190.	.15— .25	.2535.	54. —58.	99. —94.	<i>59.</i> — <i>55.</i>	.75	.7585	26. —28.	.95—1.00	Totals
Sex-Ratio of Parental Si	.0005 .0515 .1525 .2535 .3545 .5565 .5565 .7585 .8595 .95100	$ \begin{array}{r} $	1 2 6 3 4 6.5 1.5 1	1·5 2 13 15·5 32·5 39·5 39·18·75 10·25 5 0·5	0·5 4 13·5 18 33·5 44·5 51 27·25 13·75 9 4·5	2 5 14·5 33·5 67 54 69 47 23 8 7	1 5 23·5 48·5 93 87 82 55·5 26·5 14 8	1 3 19·5 26·5 74 78 73 43 22 12 6	0·5 3 12 24·5 46 49 50 40·5 13·5 6·5	0·5 5 15 22·5 33. 47 56 26·5 11·5 2·5 4·5	$ \begin{array}{c c} - & \\ 1 & \\ 2 & \\ 12 & \\ 6 & \\ 4 & \\ 5 & \\ 0 & \\ 5 & \\ 3 & \\ 2 & \\ 35 & \\ \end{array} $	2 6·5 7·5 11 12 17 11·5 7·5 2 5	7 31 119·5 205·5 420 427 456 286 130 71 44

In Table IV. another method of investigating the problem is considered, based also on different data. A sort of mid-parent was used. A joint-parental sibship was formed by combining mother's and father's sibships together and taking the sex-ratio for the total array. The result is precisely the same as in the previous cases.

In Table V. we have a wholly different method of approaching the problem. Here the sex-ratio of the produce of a thoroughbred mare—often reaching 14 to 18 foals—has been determined and correlated with the produce of one of her fillies selected at random. In this case the produce is usually due to a very considerable number of sires, or forms a half-sibship, some individuals, however, being possibly whole siblings. This method enables us to determine whether the individual has any tendency to produce one or other sex which is inherited by

TABLE IV.

Correlation of Joint Parental with Filial Sibships. Schedules.

Sex-Ratio of Filial Sibship.

Sibships.		50. —00.	.05—.15	25. —2I.	32- 32	3798.	29. —97.	<i>29.</i> — <i>22.</i>	2229.	28. —22.	.85— .95	.95—1.00	Totals
Sex-Ratio of Joint Parental	.00— .05 .05— .15 .15— .25 .25— .35 .35— .45 .45— .55 .55— .65 .65— .75 .75— .85 .85— .95 .95—1.00		1 1 3 2 1		0·5 4 6·5 9·5 6·5 3·5 4·5	1 12 26 15 5 3 —	2·5 8·5 11 18 22 9 3·5 0·5	- 2 4·5 13·5 17·5 16 5 1·5 -					9 27·5 56·5 111·5 92 34·5 16·5 0·5 —
Se	Totals	7	8	20	35	62	75	60	46	25	5	5	348

TABLE V.

Correlation of Sex-Ratios of Mother and Daughter Mares' Produce.

Thoroughbred Horses.

Sex-Ratio of Mother's Produce.

Produce.		9000	91. —90.	22. —21.	.25— .35	<i>37.</i> – <i>92.</i>	29. —97.	.5565	22. —29.	28. —22.	.85— .95	.95—1.00	Totals
Sex-Ratio of Daughter's E	00— 05 05— 15 15— 25 25— 35 35— 45 45— 55 65— 75 75— 85 85— 95 95—100			0.5 0.5 6 10.5 9 19 12 3 1 —	1.5 1.5 7 20.5 25 27 25 14 3 1	1 3 11 23 58 61 51 18 6 2	1 6 8 35 60 72 52 21 10 2	$\begin{array}{c} -\\ 2\\ 7\\ 30\\ 41\\ 47\\ 38\\ 19.5\\ 6.5\\ -\\ -\\ -\\ \end{array}$	$\begin{array}{c}\\ 5\\ 12\\ 13\\ 20\\ 11\\ 5\\ 2\\ 1\\\\ \end{array}$	1 3 5 5 6 3			4 13 46·5 136·5 222 257 199 85·5 29·5 6
$S_{\rm e}$	Totals	2	24	61.5	125.5	235	267	191	69	23	2		1000

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her offspring, and is, perhaps, more satisfactory than the human determination. Reducing this material, we obtained the following results:

TABLE VI.

Mean and Standard Deviation of Sex-Ratios.

Group	Mean	Standard Deviation
Mother's Sibship, Man	$\begin{array}{c} -589 \pm \cdot 004 \\ \cdot 456 \pm \cdot 003 \\ \cdot 526 \pm \cdot 003 \\ \cdot 522 \pm \cdot 004 \\ \cdot 520 \pm \cdot 005 \\ \cdot 521 \pm \cdot 003 \\ \cdot 504 \pm \cdot 007 \\ \cdot 521 \pm \cdot 005 \\ \cdot 463 \pm \cdot 003 \\ \cdot 478 \pm \cdot 003 \end{array}$	$\begin{array}{c} \cdot 178 \pm \cdot 002 \\ \cdot 167 \pm \cdot 002 \\ \cdot 185 \pm \cdot 002 \\ \cdot 208 \pm \cdot 003 \\ \cdot 218 \pm \cdot 003 \\ \cdot 210 \pm \cdot 002 \\ \cdot 193 \pm \cdot 005 \\ \cdot 130 \pm \cdot 003 \\ \cdot 148 \pm \cdot 002 \\ \cdot 151 \pm \cdot 002 \end{array}$

Now, if we examine this table, we cannot in the case of thoroughbred horses assert that any difference exists in the variability of the sex-ratio for the two generations. But in the case of man there certainly is a significant difference in the variability. While there is no significance in the difference of the variabilities denoted by the row numbers 4, 5, and 6, and possibly not in 7, there is a difference more than six times the probable error of the difference between these variabilities and that of 3. There is, however, no difference in type between 3, 4, 5, 6, 8, and possibly, but not certainly, 7*. These figures demonstrate the point referred to above, that in the free mating of man, families with a preponderance of female or male elements are not drawn upon equally with families in which the sexes are more equally balanced. In the controlled mating of horses this result is not apparent.

We have already noted that in the sibships which are not selected so as to have at least one male or one female, the type is fairly constant and gives a sexratio of about 522, which corresponds to 109 male births as compared with 100 female births, a quite good result. We next ask how does this agree with the values found for sibships which must have at least one male or female? Let n be the average number in a sibship, and s be the sex-ratio. Then if we choose sibships in which there is at least one male, we might expect the sex-ratio to be

$${1+(n-1)s}/n,$$

and that for sibships with at least one female to be

$$(n-1) s/n$$
.

^{*} The data for 7 include a Cornish fishing village where the sex-ratio is far more nearly one of equality than elsewhere in this country; owing to the persistence of large families in this district, it therefore figures disproportionately in the results.

Equating these respectively to '589 and '456, the sex-ratios for paternal and maternal sibships, we find:

n = 7.62 and s = .526.

The latter value is precisely the value found for all sibships of the parental generation. The former should represent the average number in a sibship of the parental generation. It cannot be very far from its true value, because all sibships without at least one male (or it may be one female) have been by the nature of the case excluded, and further, no sibship has been used with fewer than four members. It will thus be seen that our human data are in good accordance with each other.

So far as we can judge, in the second generation of thoroughbred horses under consideration there was a preponderance of mares born, the sex-ratio being 478, and differing from 500 by at least seven times the probable error. In the first generation, since there must be one filly in the produce at least, we have

$$(n-1) s/n = .463,$$

and if n lie between 10 and 15 as it does, this gives s = .5 within the probable error. In other words, the sex-ratio between the two generations appears to have fallen from equality to about .48, a substantial alteration.

Turning now to the main portion of the present enquiry, we have:

TABLE VII.

Correlation between Sex-Ratios in Successive Generations.

Nature of Sibships	Correlation
Sibships of Father and Offspring, Man	·053 ± ·020
Sibships of Mother and Offspring, Man Sibships of Parent and Offspring, Man Joint Parental Sibship and Offspring, Man	001 ± 021 021 ± 014 043 + 036
Produce of Mother and Daughter, Thoroughbred Horse	034 ± 021

It is true that all these correlations are positive, but not one of them is definitely significant, having regard to its probable error. Thus on rather wider data—in horse as well as in man—Dr Woods' position is confirmed; there is no inheritance, or at least no sensible inheritance, of sex. The persistent and sensible differences from '5 which occur in various races for the sex-ratio are therefore not racial in the sense that they are an inherited characteristic of the race; they must be in some manner associated with environment, nutrition, or habit. They appear to be a more universal, if less marked, result of such causes as lead certain species which usually reproduce parthenogenitively to occasionally reproduce sexually. It is conceivable that the sex-ratio of produce may not exhaust all the characters associated with an individual which are not subject to the general rule of inheritance.

A SECOND STUDY OF THE ENGLISH SKULL, WITH SPECIAL REFERENCE TO MOORFIELDS CRANIA.

By W. R. MACDONELL, LL.D.

(1) Introductory.

I now publish the detailed measurements of the series of English (Moorfields) skulls to which reference was made passim in my paper in Biometrika, Vol. III. pp. 191—244. The collection is in the possession of Professor G. D. Thane, of University College, London, and I have again to thank him very cordially for granting my fellow-workers and myself every facility for measuring and studying the skulls. I have also to express my gratitude to him for the great aid he has given in preparing the description of the anatomical peculiarities of the skulls provided in the "Remarks" to my Tables of Measurements. The collection is much smaller than the Whitechapel series, the subject of my former paper; it is too small, for instance, to allow of a satisfactory determination of coefficients of correlation, and I have therefore not worked them out except in two or three cases; but in other respects this series is quite as interesting as the former one. The preservation of the crania for scientific purposes was due in the first place to the energy of Mr S. Jacob, at that time working in the Biometric Laboratory at University College, London. Only an Indian appointment prevented him from carrying out the biometric investigation of the material, which I then undertook, starting de novo to avoid the influence of personal equation.

(2) Material and History of the Site.

Professor Karl Pearson and I examined the site together, and compared the old maps, and he has kindly drawn up for me the following notes. We have to thank Mr Welch, of the Guildhall Library, Mr Wood-Hill, Engineer of the North London Railway, and the staff of the Map and Print Departments of the British Museum, for assisting us in our inquiry.

The problems as to the date and mode of interment of the Moorfields remains are, as in the case of the Whitechapel bones, rendered very complex by the fact

that no proper archaeological investigation was made at the time of their discovery. The remains were found in excavating for a street latrine, since constructed, at the West End of Liverpool Street, and were already collected into heaps before any complete investigation could be made of them in situ*. The bones were found uncoffined and apparently lying in great disorder. In the Report of the Medical Office of Health (City of London, No. 61, 1903) it is suggested that the very large number of skeletons which were found when the Broad Street Station of the North London Railway was built may have been collected and reburied at the place where the excavations for the underground latrine were made in 1903. This solution of the problem does not seem to me probable, for the following reasons: That even if Liverpool Street were broadened at the building of the station, the bones were discovered in the middle, or south of the middle, of the existing street; it is extremely improbable that exhumed bones would have been reinterred under an existing thoroughfare, or that the permission to place them under the newly made part of such a thoroughfare would have been given. It is far more probable that the roadway was carried, whenever it was broadened, across an existing deposit of human remains. Now we know that Bethlem Burial Ground once occupied the sites of Broad Street Station and of the station yard. It is so marked on the large scale modern ordnance map of this part of the City. It would therefore be reasonable to suppose that the original burial ground extended to the centre of the present Liverpool Street, and that on widening that street a portion of the old burial ground was covered by the roadway. Stow remarks, concerning Bethlem Burial Ground:

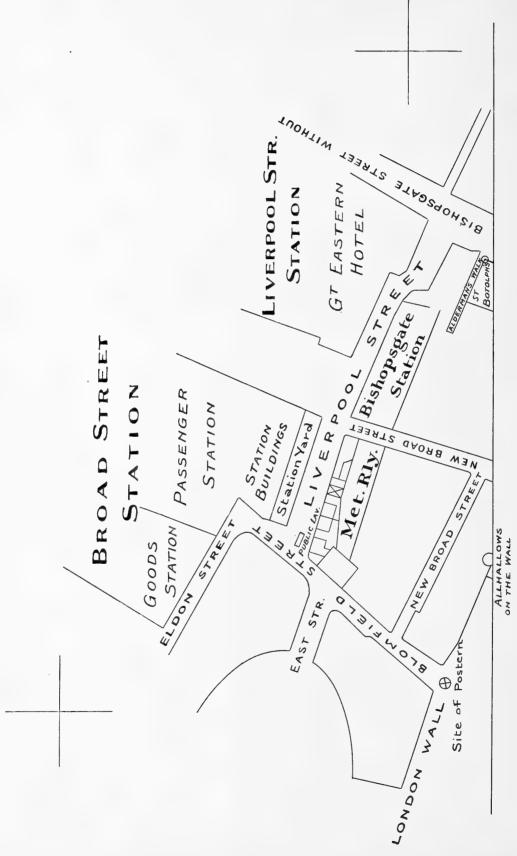
"In the yere 1569. Sir Thomas Roe Merchant Taylor Mayor, caused to bee inclosed with a "wall of bricke, about one acre of ground, being part of the said Hospitall of Bethelem, to wit, on "the west, on the bancke of deepe ditch, so called, parting the said hospitall of Bethlem from the "More field: this he did for burial, in ease of such parishes in London as wanted ground, "convenient within their parishes. The Ladie his wife was there buried (by whose persuasion "he inclosed it) but himself borne in London, was buried in the parish church of Hackney."

Now it might be thought that the exact position and dimensions of a burial ground of this importance could hardly fail to be known, but unfortunately no plans or title-deeds seem to exist in the City Archives, and we are thrown back upon the evidence of the maps of the City and its environs at different dates. Unfortunately, most of these maps are very diagrammatic in character, few are drawn even approximately to scale ‡, and even such an important map as Ogilby's of 1677 is quite unreliable for this district, as far as giving the accurate dimensions of streets and intervening plots is concerned. The first map which seems at all accurately drawn to scale with correct angles and capable by proper reduction of being fitted fairly closely to the modern ordnance map is Rocque's of 1746.

^{*} A brief Act of Parliament ought to be passed compelling all building operators to at once summon a local officer, and a competent archaeologist, before proceeding further, when antiquities of any kind are reached in excavating.

[†] A Survay of London, Octavo Edition, 1599, pp. 127-8.

[‡] If different pairs of definite base points be taken and two maps reduced to a common scale, the fit, or want of fit, is often wholly different.



Reduced from 60 inch Ordnance Map.

polityrae A to 18 a, so yrin swogr yra id bi yrin sid f wodo dara tairiciah it isawin alf Al buo Latin'i A Jai'

Traced from Rocque's Map of Oct. 1746.

This map is to superpose map on p. 88 of Biometrika, Vol. v, Parts I and II, the crosses registering with those below. 345 31×0×004218 BROAD STR BUILDS 133872 133872 Burying Ground a RPOAB Moon

Traced from Rocque's Map of Oct. 1746.

NEW

Postern

BOLTOPHS P

1810er Waln's Walk S

BROAD

NEW

In Rocque's and earlier maps the present Liverpool Street is termed Old Bethlem, and this street runs from the modern Blomfield Street, then bounding Moorfields, to the site of the original Bedlam. Now if Rocque's map and the Ordnance Survey be reduced to a common scale,—and in doing this we have taken the north-east corner of St Botolph's Church and the old Moorfields postern in the city wall, which are marked on both maps—it will be found, as shown in the accompanying reproduction, that Old Bethlem coincided with the southern half of the modern Liverpool Street, and that the site of the latrine excavation was immediately on the left of the entry into Old Bethlem from Moorfields. If then, the bones were from interments in Sir Thomas Roe's Burial Ground, that ground must originally have extended to the corner where the centre line of the Liverpool Street of to-day runs into Blomfield Street. The available maps appear to provide no confirmation of this view. It is true that maps of the 18th century give most diverse forms to the ground, and there can be little doubt that in the latter half of that century and the beginning of the next, buildings encroached largely on the original space*. Not only Rocque, however, but Ogilby of 1677 show a distinct enclosure or a building, falling exactly in the south-west corner of the plot, the centre of which is marked Old Bethlem Burial Ground. In Horwood's map of 1799, this enclosure, separated from the burial ground, still remains of much the same shape as in Rocque's. In W. Faden's map of 1813, the road between Moorfields and the Burial Ground is termed Brokers' Row—the modern Blomfield Street—and the separate enclosure in the south-west corner is called No. 1. This house stands apart from the others, and I think there is little doubt that No. 1 Brokers' Row, in 1813, stood almost on the site of the modern latrine, and since it is marked as a separate enclosure as early as 1677, was not one of the encroachments on the original burial ground to which reference has been made. Strong confirmation of this view will be found in Morden and Lea's map of 1690. In this we find that the space marked churchyard did not extend on the west fully up to Brokers' Row, or on the south to the street marked Old Bethlem. There were at that date strips of intervening land.

To account for this, I think we have only to turn back to the original condition of affairs. The hospital of St Mary Bethlem was founded by Simon Fitz-Mary in 1246 as a priory of canons with brothers and sisters. The mayor and commonalty of London, in the year 1546, purchased the patronage thereof and all the lands and tenements belonging thereto. In the same year King Henry VIII. gave the hospital to the city, and the church and chapel were removed in the reign of Elizabeth, and houses built there by the Governors of Christ's Hospital. Now if we look at Aggas' map of London in the reign of Elizabeth (from 1560), before Roe's enclosure, we see that north of St Botolph's a row of houses stretched along to the road leading north from the Moorfields postern (i.e. the later Brokers' Row) and that the road passed under an archway into some sort of a quadrangle. Within

^{*} This is very clearly indicated in the copy of part of the "deposited" plan of the North London Railway, 1861, kindly provided by the Engineer to the Company.

this quadrangle was a tower, like a martello tower, with a flag attached to it. This tower remains after the archway disappears, and serves to identify the quadrangle. It appears, for example, in Ryther's map of 1604, and we see that it was in the centre of the plot, which in maps of somewhat later date is marked as Old Bethlem Burial Ground. There can be little doubt accordingly, that Sir Thomas Roe fenced in a portion of the Bethlem quadrangle as the burial ground, and that this burial ground was originally separated by the buildings terminating in the archway (over Brokers' Row as it was called later) from the street afterwards termed Old Bethlem, which indeed may have partially covered the site of these houses. Thus from the very founding of the burial ground it is improbable that it ever covered the south-west corner of the plot. It would be difficult to determine when these houses disappeared, but they were gone before the middle of the 17th century, and from this time to Hollar's map of 1706 we find the western and southern boundaries of the Bethlem plot are marked as separate enclosures.

The improbability that the bones are directly due to interments in Old Bethlem Burial Ground is increased by the fact that they were uncoffined. Even in excavating for Broad Street coffined bones were only found on a portion of the excavated site*. Such burials are characteristic not of ordinary interment, but of interment during an epidemic, and the want of any arrangement noted in both 1863 and 1903 tends to confirm the view that on the borders of Sir Thomas Roe's ground plague pits were dug at one or another period.

If we turn to Defoe's Journal of the Plague Year we find that he gives a long list of plague pits, and there is little doubt that although he was a child at the time, he was still able as a man to get recent and authentic information. After enumerating various spots where there were pits, he continues:

"Besides this, there was a piece of ground in Moorfields, by the going into the Street which is now called Old Bethlem, which was enlarged much although not wholly taken in on the same occasion†."

This description seems to fit well the spot where the bones were found, i.e. the corner where Old Bethlem ran into Moorfields, and further accounts fully for the uncoffined mass of bones without arrangement extending from 4 to 8 or 10 ft. below the surface.

It is not of course possible to assign dogmatically a definite date and character to these Moorfields crania, but we may hold with a high degree of probability that they were drawn from the plague pit referred to by Defoe, and accordingly date from 1665.

Those who incline to believe that they originally came—as in the case of a clearance pit—from the burial ground, can assign any date from 1569 to about 1750, the ground being probably in most use not very far from the plague pit date.

^{*} See Notes and Queries, August 1, 1863.

⁺ Morley's Edition, p. 295. The "not wholly taken in," clearly refers to the already existing Bethlem burial ground alongside.

Accepting this view would only mean somewhat greater scatter in time round about the same mean date, and we may consider ourselves fortunate, in most cases of large cranial finds, if it is possible to fix the date of the bulk of the material with anything like certainty within a hundred years.

(3) Measurements and Methods of Measurement.

All the detailed measurements given in my former paper are given here except G_1 , the length of the palate from the base of the *spina nasalis posterior*, and the same symbols and methods of measurement were adopted as before. There were no mandibles in the collection.

Certain additional characters are given, viz.:

- (j') Length from nasion to bregma (S_1) .
- (k') Length from bregma to lambda (S_2) .
- (l') Length from lambda to opisthion (S_3).

These three were measured with the steel tape.

- (l'') Length from lambda to opisthion (S_3') , measured with the callipers. S_2 , S_3 and S_3' were frequently difficult to measure on account of difficulty in determining the lambda precisely.
 - (x) Greatest length of foramen magnum (fml).
 - (y) Greatest breadth of foramen magnum (fmb).
 - (ν) Foraminal Index $\left(100 \frac{fmb}{fml}\right)$.
- (π) Ratio of radius of curvature of the cerebellum (from lambda to opisthion) to S_3' (CC); this measure of cerebellar curvature equals $\frac{S_3}{S_3'}\sqrt{\frac{S_3}{24(S_3-S_3')}}$ very nearly*, and will be termed the Cerebellar Index.

The Cerebellar Index, which measures the convexity towards the inion, seems useful as giving some indication of the capacity of the cerebellum. A low Cerebellar Index is a sign of large convexity. The Cerebellar Index of men is lower and less variable than that of women, to judge from the first investigation of it now made in this paper.

I have to thank Dr Alice Lee for help in calculating this ratio. I am also greatly indebted to Miss Winifred Gibson for the foraminal measurements and also for calculating the angles A, N, and B on the trigonometer.

TABLE I. Cranial Means and Variability.

Comparison of Moorfields English with Whitechapel English.

MALE.

Character			Moorfie	elds English			Whitech	apel English	
and Referenc Letter		No.	Mean	Standard Deviation	Coefficient of Variation	No.	Mean	Standard Deviation	Coefficient of Variation
(b) F (c) L (d) L' (e) B (f) B'	4	22 45 44 19 46 47 46 34	$\begin{array}{c} 1473 \cdot 82 \pm 19 \cdot 01 \\ 186 \cdot 88 \pm & \cdot 59 \\ 189 \cdot 15 \pm & \cdot 57 \\ 188 \cdot 00 \pm & 1 \cdot 02 \\ 143 \cdot 02 \pm & \cdot 53 \\ 98 \cdot 47 \pm & \cdot 41 \\ 129 \cdot 84 \pm & \cdot 75 \\ 113 \cdot 78 \pm & \cdot 47 \\ 98 \cdot 54 \pm & \cdot 52 \\ \end{array}$	$\begin{array}{c} 132 \cdot 18 \pm 13 \cdot 44 \\ 5 \cdot 90 \pm \cdot 42 \\ 5 \cdot 58 \pm \cdot 40 \\ 6 \cdot 57 \pm \cdot 72 \\ 5 \cdot 31 \pm \cdot 37 \\ 4 \cdot 12 \pm \cdot 29 \\ 6 \cdot 45 \pm \cdot 53 \\ 4 \cdot 69 \pm \cdot 33 \\ 4 \cdot 57 \pm \cdot 37 \end{array}$	$\begin{array}{cccc} 8.97 \pm & 92 \\ 3.16 \pm & 22 \\ 2.95 \pm & 21 \\ 3.50 \pm & 38 \\ 3.71 \pm & 26 \\ 4.19 \pm & 29 \\ 4.97 \pm & 41 \\ 4.12 \pm & 29 \\ 4.64 \pm & 38 \\ \end{array}$	72 138 137 72 135 132 122 135 119	$\begin{array}{c} 1476 \cdot 94 \pm 9 \cdot 73 \\ 187 \cdot 35 \pm \cdot 35 \\ 189 \cdot 06 \pm \cdot 36 \\ 187 \cdot 76 \pm \cdot 45 \\ 140 \cdot 67 \pm \cdot 31 \\ 98 \cdot 02 \pm \cdot 25 \\ 132 \cdot 04 \pm \cdot 34 \\ 114 \cdot 59 \pm \cdot 25 \\ 101 \cdot 60 \pm \cdot 25 \\ \end{array}$	$\begin{array}{c} 122 \cdot 37 \pm 6 \cdot 88 \\ 6 \cdot 17 \pm & \cdot 25 \\ 6 \cdot 27 \pm & \cdot 25 \\ 5 \cdot 64 \pm & \cdot 32 \\ 5 \cdot 28 \pm & \cdot 22 \\ 4 \cdot 20 \pm & \cdot 17 \\ 5 \cdot 56 \pm & \cdot 24 \\ 4 \cdot 28 \pm & \cdot 18 \\ 4 \cdot 13 \pm & \cdot 18 \end{array}$	$8 \cdot 28 \pm \cdot 47$ $3 \cdot 29 \pm \cdot 13$ $3 \cdot 31 \pm \cdot 13$ $3 \cdot 00 \pm \cdot 17$ $3 \cdot 75 \pm \cdot 15$ $4 \cdot 29 \pm \cdot 17$ $4 \cdot 21 \pm \cdot 18$ $3 \cdot 73 \pm \cdot 15$ $4 \cdot 07 \pm \cdot 18$
(k') S_2 (l') S_3		37 40 32 44 43 40	$\begin{array}{c} 527 \cdot 08 \pm 1 \cdot 60 \\ 378 \cdot 50 \pm 1 \cdot 28 \\ 305 \cdot 41 \pm 1 \cdot 49 \\ 129 \cdot 34 \pm 56 \\ 128 \cdot 72 \pm 78 \\ 120 \cdot 50 \pm 90 \\ 98 \cdot 09 \pm 63 \end{array}$	$\begin{array}{c} 14.45 \pm \ 1.13 \\ 12.01 \pm \ .90 \\ 12.54 \pm \ 1.06 \\ 5.55 \pm \ .40 \\ 7.61 \pm \ .55 \\ 8.48 \pm \ .64 \\ 5.94 \pm \ .45 \\ \end{array}$	2·74± ·21 3·17± ·24 4·11± ·35 4·29± ·31 5·91± ·43 7·04± ·53 6·05± ·46	131 131 115 — —	524·25± ·88 377·11± ·81 307·93± ·72 ————————————————————————————————————	15·02± ·63 13·69± ·57 11·40± ·51	2·87±·12 3·63±·15 3·70±·16
$\begin{array}{c} (n) \ G'H \\ (o) \ GB \\ (p) \ J \ \dots \\ (q) \ NH \\ (r) \ NB \end{array}$	2	20 15 7 20 18	$\begin{array}{cccc} 68 \cdot 12 \pm & \cdot 62 \\ 93 \cdot 87 \pm & \cdot 77 \\ 129 \cdot 00 \pm & 1 \cdot 19 \\ 50 \cdot 37 \pm & \cdot 39 \\ 24 \cdot 03 \pm & \cdot 30 \\ \end{array}$	$\begin{array}{cccc} 4.08 \pm & .43 \\ 4.45 \pm & .55 \\ 4.65 \pm & .84 \\ 2.60 \pm & .28 \\ 1.90 \pm & .21 \end{array}$	5·99 ± ·64 4·74 ± ·58 3·60 ± ·65 5·16 ± ·55 7·91 ± ·89	75 55 43 79 70	70·17 ± ·30 90·87 ± ·45 130·05 ± ·57 51·22 ± ·20 24·29 ± ·17	3·86± ·21 5·07± ·32 5·57± ·40 2·60± ·14 2·16± ·12	5·50±·30 5·58±·36 4·28±·31 5·08±·27 8·89±·51
(A) O T	2	20 18 20 18	$\begin{array}{cccc} 41.80 \pm & .23 \\ 42.28 \pm & .22 \\ 32.82 \pm & .32 \\ 32.83 \pm & .34 \end{array}$	1·51 ± ·16 1·42 ± ·16 2·12 ± ·23 2·12 ± ·24	3·61 ± ·38 3·35 ± ·38 6·47 ± ·69 6·46 ± ·73	63 68 67 69	43·06± ·15 42·99± ·16 33·46± ·15 33·42± ·18	1·81 ± ·11 2·02 ± ·12 1·88 ± ·11 2·22 ± ·13	4·20 ± ·25 4·69 ± ·27 5·61 ± ·33 6·65 ± ·38
$\begin{array}{cc} (u) & G_1 \\ (v) & G_2 \end{array}$	1	17 15	48·12± ·69 39·73± ·41	4·25 ± ·49 2·36 ± ·29	8·84±1·03 5·94± ·73	69 66	48·27 ± ·22 36·78 ± ·24	2·74 ± ·16 2·85 ± ·17	5·68 ± ·33 7·75 ± ·46
(w) GL	3	17	95·03 ± ·67	4·12 ± ·48	4·33 ± ·50	73	95:93 ± ·35	4·49 ± ·25	4·68 ± ·26
(-1) L I		36 34	35·44± ·32 29·74± ·21	2·86 ± ·23 1·82 ± ·15	8·08 ± ·65 6·10 ± ·50	_		_	_
(cc) N ∠ (dd) B ∠	i	15 17 17 17 17 14	$\begin{array}{c} 84^{\circ} \cdot 50 \pm & \cdot 69 \\ 72^{\circ} \cdot 35 \pm & \cdot 61 \\ 66^{\circ} \cdot 56 \pm & \cdot 58 \\ 41^{\circ} \cdot 09 \pm & \cdot 44 \\ 29^{\circ} \cdot 39 \pm & \cdot 53 \\ 11^{\circ} \cdot 64 \pm & \cdot 43 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		63 69 69 69 59 59	$\begin{array}{c} 86^{\circ} \cdot 09 \pm \cdot 33 \\ 73^{\circ} \cdot 38 \pm \cdot 28 \\ 65^{\circ} \cdot 19 \pm \cdot 29 \\ 41^{\circ} \cdot 43 \pm \cdot 20 \\ 28^{\circ} \cdot 71 \pm \cdot 22 \\ 12^{\circ} \cdot 92 \pm \cdot 29 \end{array}$	$\begin{array}{c} 3.92 \pm .24 \\ 3.41 \pm .20 \\ 3.52 \pm .20 \\ 2.50 \pm .14 \\ 2.53 \pm .16 \\ 3.34 \pm .21 \end{array}$	
 (β) 100 B/L (γ) 100 H/L' (δ) 100 H/L 	2	18 42 17 31 32	$\begin{array}{cccc} 75 \cdot 08 \pm & \cdot 52 \\ 75 \cdot 52 \pm & \cdot 31 \\ 68 \cdot 24 \pm & \cdot 51 \\ 68 \cdot 37 \pm & \cdot 42 \\ 90 \cdot 55 \pm & \cdot 56 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4·35 ± ·49 3·97 ± ·29 4·59 ± ·53 5·07 ± ·44 5·16 ± ·44	69 131 69 120 116	$\begin{array}{cccc} 75 \cdot 17 \pm & \cdot 24 \\ 74 \cdot 34 \pm & \cdot 19 \\ 70 \cdot 40 \pm & \cdot 22 \\ 69 \cdot 97 \pm & \cdot 20 \\ 94 \cdot 31 \pm & \cdot 29 \end{array}$	2·97 ± ·17 3·26 ± ·14 2·67 ± ·15 3·22 ± ·14 4·58 ± ·20	3·95 ± ·23 4·38 ± ·18 3·80 ± ·22 4·61 ± ·20 4·86 ± ·21
$ \begin{array}{c} (\theta) \ 100 \ G'H/\ell \\ (\kappa) \ 100 \ NB/N \\ (\lambda) \ 100 \ O_2/O_1, \\ (\lambda') \ 100 \ O_2/O_1, \\ (\mu) \ 100 \ G_2/G_1 \end{array} $	$egin{array}{c c} H & 1 \ L & 2 \ R & 1 \ \end{array}$	14 18 20 17 13	$\begin{array}{c} 72 \cdot 79 \pm & \cdot 86 \\ 47 \cdot 58 \pm & \cdot 66 \\ 78 \cdot 52 \pm & \cdot 64 \\ 77 \cdot 35 \pm & \cdot 69 \\ 82 \cdot 73 \pm & 1 \cdot 05 \end{array}$	$\begin{array}{cccc} 4.77 \pm & .61 \\ 4.13 \pm & .46 \\ 4.27 \pm & .46 \\ 4.16 \pm & .48 \\ 5.59 \pm & .74 \end{array}$	6·55 ± ·84 8·68 ± ·98 5·43 ± ·58 5·37 ± ·63 6·76 ± ·90	53 70 63 68 61	$76.52 \pm .50$ $47.55 \pm .37$ $77.86 \pm .32$ $77.69 \pm .38$ $76.26 \pm .55$	5·39 ± ·35 4·58 ± ·26 3·78 ± ·23 4·66 ± ·27 6·40 ± ·39	7·04±·46 9·64±·55 4·86±·29 6·00±·35 8·39±·52
(ν) 100 fmb/fr	nl 3	34	84·20 ± ·77	6.64 ± .24	7·89 ± ·65	-	_	_	
$\langle \pi \rangle$ CC	4	40	58·52 ± ·23	2·15 ± ·16	3.68 ± .28		_	_	_

TABLE I.—(continued). Cranial Means and Variability.

Comparison of Moorfields English with Whitechapel English.

FEMALE.

Character		Moorfie	lds English			Whitech	apel English	
and Reference . Letter	No.	Mean	Standard Deviation	Coefficient of Variation	No.	Mean	Standard Deviation	Coefficient of Variation
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	31 65 63 23 62 64 47 59 46	$\begin{array}{c} 1365 \cdot 31 \pm 13 \cdot 68 \\ 182 \cdot 45 \pm & \cdot 52 \\ 183 \cdot 36 \pm & \cdot 51 \\ 182 \cdot 50 \pm & \cdot 86 \\ 137 \cdot 60 \pm & \cdot 45 \\ 95 \cdot 16 \pm & \cdot 34 \\ 123 \cdot 58 \pm & \cdot 46 \\ 109 \cdot 38 \pm & \cdot 38 \\ 95 \cdot 89 \pm & \cdot 43 \\ \end{array}$	$\begin{array}{c} 112 \cdot 93 \pm 9 \cdot 67 \\ 6 \cdot 24 \pm \cdot 37 \\ 6 \cdot 02 \pm \cdot 36 \\ 6 \cdot 14 \pm \cdot 61 \\ 5 \cdot 28 \pm \cdot 32 \\ 4 \cdot 05 \pm \cdot 24 \\ 4 \cdot 72 \pm \cdot 33 \\ 4 \cdot 39 \pm \cdot 27 \\ 4 \cdot 34 \pm \cdot 31 \end{array}$	$8 \cdot 27 \pm \cdot 71$ $3 \cdot 42 \pm \cdot 20$ $3 \cdot 28 \pm \cdot 20$ $3 \cdot 37 \pm \cdot 33$ $3 \cdot 84 \pm \cdot 23$ $4 \cdot 25 \pm \cdot 25$ $3 \cdot 82 \pm \cdot 27$ $4 \cdot 01 \pm \cdot 25$ $4 \cdot 53 \pm \cdot 32$	80 143 140 57 140 147 124 143 122	$\begin{array}{c} 1299.87 \pm 8.51 \\ 180.14 \pm .36 \\ 180.36 \pm .35 \\ 180.07 \pm .57 \\ 134.68 \pm .27 \\ 93.12 \pm .23 \\ 124.56 \pm .30 \\ 109.21 \pm .25 \\ 95.34 \pm .24 \\ \end{array}$	$\begin{array}{c} 112 \cdot 80 \pm 6 \cdot 01 \\ 6 \cdot 38 \pm \cdot 25 \\ 6 \cdot 22 \pm \cdot 25 \\ 6 \cdot 33 \pm \cdot 40 \\ 4 \cdot 77 \pm \cdot 19 \\ 4 \cdot 23 \pm \cdot 17 \\ 4 \cdot 93 \pm \cdot 21 \\ 4 \cdot 50 \pm \cdot 18 \\ 3 \cdot 91 \pm \cdot 17 \\ \end{array}$	$\begin{array}{c} 8.68 \pm .47 \\ 3.54 \pm .14 \\ 3.45 \pm .14 \\ 3.52 \pm .22 \\ 3.54 \pm .14 \\ 4.55 \pm .18 \\ 3.96 \pm .17 \\ 4.12 \pm .16 \\ 4.11 \pm .18 \\ \end{array}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	56 53 42 53 52 49 49	$\begin{array}{c} 512.68 \pm \ 1.53 \\ 365.58 \pm \ 1.26 \\ 293.07 \pm \ 1.16 \\ 125.75 \pm \ .57 \\ 123.60 \pm \ .68 \\ 116.98 \pm \ .87 \\ 95.91 \pm \ .59 \\ \end{array}$	17·02±1·08 13·56± ·89 11·11± ·82 6·17± ·40 7·29± ·48 9·01± ·61 6·09± ·41	$\begin{array}{c} 3.32 \pm .21 \\ 3.71 \pm .24 \\ 3.79 \pm .28 \\ 4.91 \pm .32 \\ 5.90 \pm .39 \\ 7.70 \pm .53 \\ 6.35 \pm .43 \end{array}$	136 130 122 — — —	503·84± ·85 362·76± ·84 293·97± ·71	14·70± ·60 14·16± ·59 11·67± ·50 —	2·92±·12 3·90±·16 3·97±·17 —
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	27 18 18 27 26	$\begin{array}{cccc} 64.15 \pm & .47 \\ 86.86 \pm & .79 \\ 122.00 \pm & .69 \\ 48.02 \pm & .36 \\ 23.40 \pm & .25 \end{array}$	$3.66 \pm .34$ $4.99 \pm .56$ $4.32 \pm .49$ $2.76 \pm .25$ $1.92 \pm .18$	5·71 ± ·53 5·75 ± ·65 3·54 ± ·40 5·74 ± ·53 8·21 ± ·77	62 58 33 67 64	65·93 ± ·40 84·86 ± ·41 120·27 ± ·58 48·68 ± ·22 23·19 ± ·14	4·71 ± ·28 4·59 ± ·29 4·97 ± ·41 2·70 ± ·16 1·64 ± ·10	7·14±·43 5·40±·34 4·13±·34 5·55±·32 7·06±·42
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	22 25 22 25 25	$\begin{array}{ccccc} 40.93 \pm & .24 \\ 40.90 \pm & .23 \\ 32.84 \pm & .34 \\ 32.60 \pm & .27 \end{array}$	$\begin{array}{c} 1.64 \pm & .17 \\ 1.67 \pm & .16 \\ 2.34 \pm & .24 \\ 2.03 \pm & .19 \end{array}$	4·02 ±·41 4·09 ±·39 7·11 ±·73 6·22 ±·60	57 62 64 64	$\begin{array}{r} 41.17 \pm & 13 \\ 40.95 \pm & 14 \\ 33.59 \pm & 12 \\ 33.73 \pm & 13 \end{array}$	1.45 ± .09 1.64 ± .10 1.45 ± .09 1.51 ± .09	3·53±·22 4·00±·24 4·31±·26 4·47±·27
(u) G_1 \dots (v) G_2 \dots	20 22	45·92 ± ·43 37·04 ± ·40	2·83 ± ·30 2·80 ± ·28	6·15 ± ·66 7·55 ± ·77	57 58	45·13 ± ·26 35·22 ± ·24	2·95 ± ·19 2·70 ± ·17	6.53 ±.41 7.68 ±.48
(w) GL	25	92·14± ·76	5.66 ± .24	6·14±·59	58	90·42 ± ·40	4·47 ± ·28	4·95 ± ·31
$ \begin{array}{ccc} (x) \ fml & \dots \\ (y) \ fmb & \dots \end{array} $	50 50	$34.29 \pm .24$ $29.01 \pm .23$	2·49 ± ·17 2·43 ± ·16	7·26 ± ·49 8·39 ± ·57			_	_
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	19 26 26 26 26 19 19	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} 2 \cdot 26 \pm & \cdot 25 \\ 2 \cdot 29 \pm & \cdot 21 \\ 2 \cdot 82 \pm & \cdot 26 \\ 2 \cdot 67 \pm & \cdot 25 \\ 2 \cdot 15 \pm & \cdot 24 \\ 2 \cdot 36 \pm & \cdot 26 \end{array}$		52 57 57 57 57 50 50	$\begin{array}{c} 87^{\circ} \cdot 13 \pm \ \cdot 27 \\ 73^{\circ} \cdot 90 \pm \ \cdot 29 \\ 64^{\circ} \cdot 70 \pm \ \cdot 23 \\ 41^{\circ} \cdot 39 \pm \ \cdot 27 \\ 28^{\circ} \cdot 11 \pm \ \cdot 24 \\ 13^{\circ} \cdot 13 \pm \ \cdot 34 \\ \end{array}$	2·85 ± ·19 3·31 ± ·21 2·53 ± ·16 2·98 ± ·19 2·51 ± ·17 3·60 ± ·24	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	21 57 20 44 44	$\begin{array}{cccc} 75 \cdot 38 \pm & \cdot 30 \\ 75 \cdot 05 \pm & \cdot 21 \\ 67 \cdot 07 \pm & \cdot 41 \\ 67 \cdot 17 \pm & \cdot 28 \\ 89 \cdot 93 \pm & \cdot 40 \end{array}$	2·02± ·21 2·36± ·15 2·75± ·29 2·78± ·20 3·96± ·28	2.68 ± ·28 3.14 ± ·20 4.10 ± ·44 4.14 ± ·30 4.40 ± ·32	55 130 55 117 115	$ \begin{array}{c} 74.62 \pm \ \cdot 27 \\ 74.73 \pm \ \cdot 18 \\ 69.05 \pm \ \cdot 26 \\ 69.13 \pm \ \cdot 18 \\ 92.35 \pm \ \cdot 24 \end{array} $	3·01 ± ·19 2·98 ± ·12 2·91 ± ·19 2·83 ± ·12 3·84 ± ·17	$4.03 \pm .26$ $3.99 \pm .17$ $4.21 \pm .27$ $4.10 \pm .18$ $4.16 \pm .18$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	26 22	$\begin{array}{cccc} 73.55 \pm & .64 \\ 48.73 \pm & .52 \\ 80.34 \pm & .84 \\ 79.76 \pm & .75 \\ 81.24 \pm & .71 \end{array}$	4·01± ·45 3·96± ·37 5·83± ·59 5·53± ·53 4·62± ·50	$5.46 \pm .61$ $8.12 \pm .76$ $7.26 \pm .74$ $6.93 \pm .66$ $5.69 \pm .62$	54 64 57 62 51	$77.94 \pm .57$ $47.79 \pm .33$ $81.70 \pm .38$ $82.46 \pm .37$ $77.69 \pm .62$	6·26 ± ·41 3·90 ± ·23 4·23 ± ·27 4·33 ± ·26 6·62 ± ·44	$8.04 \pm .52$ $8.16 \pm .49$ $5.18 \pm .33$ $5.25 \pm .32$ $8.52 \pm .57$
(ν) 100fmb/fml	-	84·45 ± ·60	6·12 ± ·43	7·25 ± ·51	_	_		
(π) CC	49	59·24 ± ·28	2·90 ± ·20	4·90 ± ·33		_	_	_

(4) Capacity.

Circumstances prevented me from measuring the capacity of the skulls, and this laborious piece of work was most kindly carried out by Miss M. Radford and Professor Karl Pearson, by the method of weighing and comparing with Professor Thane's standard skulls which I had previously adopted.

After many preliminary trials, they decided to use as their standard the "crâne étalon," which I called " α "*, and finally determined the constant for reducing to volume the weight of mustard seed contained in the skulls as $\frac{1000}{766.55}$, which agrees fairly closely with my determination $\frac{1000}{768.33}$.

(5) Mean Value and Variability.

Table I. gives the means, standard deviations and coefficients of variation, with their probable errors, of the characters, and will enable us to see to what extent the Moorfields and Whitechapel series agree with each other. If it can be established that they agree very closely, it will be unnecessary to institute an elaborate comparison between our present series and other races, such as I made in the case of the Whitechapel skulls, as the same conclusions will apply to both. I will therefore confine myself to a somewhat detailed comparison of our two London series.

TABLE II.

Capacity and Lengths. Means.

MA	ALE	Female		
Moorfields	Whitechapel	Moorfields	Whitechapel	
1474	1477	1365	1300	
189·1	189·1	183·4	180·4	
143.0	140·7	137·6	134·7	
98.5	98·0	95·2	93·1	
129·8	114.6	123.6	124.6	
113·8		109.4	109.2	
98·5		95.9	95.3	
	Moorfields 1474 189·1 143·0 98·5 129·8 113·8	1474 1477 189·1 189·1 143·0 140·7 98·5 98·0 129·8 132·0 113·8 114·6	Moorfields Whitechapel Moorfields 1474 1477 1365 189·1 189·1 183·4 143·0 140·7 137·6 98·5 98·0 95·2 129·8 132·0 123·6 113·8 114·6 109·4	

In males the chief difference is in *LB* (length of skull base from nasion to basion); also in height and maximum breadth the series differ, the Moorfields being broader but less high; the other characters are closely alike.

The Moorfields female skull is markedly more capacious, being longer, broader, and higher.

I consider in the second place the circumferences.

^{*} Biometrika, Vol. III. p. 204.

TABLE III.

Circumferences. Means.

	M	ALE	FEMALE		
Character	Moorfields	Whitechapel	Moorfields	Whitechapel	
U	527.1	524.2	512.7	503.8	
\mathcal{S}	378.5	377.1	365.6	362.8	
Q	305.4	307.9	293·1	294.0	

The male skulls are strikingly alike, while in the female skulls the larger U was to be expected in the Moorfields group, owing to their greater length and breadth.

We next come to characters of which the frequencies in the Moorfields series are very few, and the comparison is thus less satisfactory.

TABLE IV.

Face Measurements. Means.

Character	M	ALE	Female		
	Moorfields	Whitechapel	Moorfields	Whitechape	
G'H	68.1	70.2	64.1	65.9	
GB	93.9	90.9	86.9	84.9	
J	129.0	130.0	122.0	120.3	
NH	50.4	51.2	48.0	48.7	
NB	24.0	24.3	23.4	23.2	
O_1L	41.8	43.1	40.9	41.2	
O_1R	42.3	43.0	40.9	40.9	
O_2L	32.8	33.5	32.8	33.6	
O_2R	32.8	33.4	32.6	33.7	

The only important differences are in G'H and GH (upper face height and face breadth) the former of which is shorter, the latter broader in the Moorfields skulls, both male and female.

As regards the palate, the two series agree in length, but differ considerably in breadth, in males and females, but breadth of palate I have again found a somewhat unsatisfactory character to measure*.

^{*} Biometrika, Vol. III. p. 202.

The two series, in both sexes, agree closely in the angles A, N, and B of the triangle whose apices are the nasion, basion, and alveolar point*. The profile angle, P, is the larger in Whitechapel females.

TABLE V.

Chief Indices. Means.

	MALE		FEMALE		
Character	Moorfields	Whitechapel	Moorfields	Whitechapel	
100 B/L	75.5	74.3	75.0	74.7	
$100~\dot{H}/L$	68.4	70.0	67.2	69.1	
100~H/B	90.5	94.3	89.9	92.3	
$G'H/\dot{G}B$	72.8	76.5	73.5	77.9	
NB/NH	47.6	47.5	48.7	47.8	
$O_2/O_1,\ L$	78.5	77.9	80.3	81.7	
$O_2/O_1, R$	77:3	77.7	79.8	82.5	
G_2/G_1	82.7	76.3	81.2	77.7	

Here, as we should expect, there are differences between the two series where B, H, G'H, GB, and G_2 are involved.

In order to compare the variability of the two collections, I will now give side by side the standard deviations of the chief characters.

TABLE VI.

Capacity and Lengths. Coefficients of Variation.

	M	ALE	FEMALE		
Character	Moorfields	Whitechapel	Moorfields	Whitechapel	
C	8.97	8.28	8.27	8.68	
L	2.95	3.31	3.28	3.45	
B	3.71	3.75	3.84	3.54	
B'	4.19	4.29	4.25	4.55	
H	4.97	4.21	3.82	3.96	
OH	4.12	3.73	4.01	4.12	
LB	4.64	4.07	4.53	4.11	

The general agreement is close between the two series.

^{*} Biometrika, Vol. III. pp. 211 and 213.

TABLE VII.

Circumferences. Coefficients of Variation.

Character	Mai		FE	MALE
Character	Moorfields	Whitechapel	${f Moorfields}$	Whitechapel
U	2.74	2.87	3.32	2.92
S Q	$\frac{3.17}{4.11}$	3.63	$\frac{3.71}{3.79}$	3·90 3·97

Here again the two series agree very well.

The frequencies of the remaining characters are too few in the Moorfields group to enable us to make a satisfactory comparison; I give, however, in the following Table the figures for face measurements.

TABLE VIII.

Face Measurements. Coefficients of Variation.

	M	ALE	FEMALE		
Character	Moorfields	Whitechapel	Moorfields	Whitechapel	
G'H	5.99	5.20	5.71	7.14	
GB	4.74	5.58	5.75	5.40	
J	3.60	4.28	3.54	4.13	
NH	5.16	5.08	5.74	5.55	
NB	7.91	8.89	8.21	7.06	
O_1L	3.61	4.20	4.02	3.53	
O_1R	3.35	4.69	4.09	4.00	
O_2L	6.47	5.61/	7.11	4.31	
O_2R	6.46	6.65	6.22	4.47	

The most important difference is in G'H (upper face height) and in the breadth of orbit, in females, but the smallness of the Moorfields frequencies has to be kept in mind.

The coefficients of variation in palate measurements are markedly different in the two series in males, but in females they are about the same.

The following Table gives the coefficients of variation of those indices, for which the frequencies are over 30 in the Moorfields series.

TABLE IX.

Indices. Coefficients of Variation.

Characters	М	ALE	FEMALE	
	Moorfields	Whitechapel	Moorfields	Whitechapel
100 B/L	3.97	4.38	3.14	3.99
$\begin{array}{c c} 100\ H/L \\ 100\ H/B \end{array}$	5·07 5·16	4·61 4·86	4·14 4·40	4·10 4·16

The agreement is seen to be fairly close.

An examination of these Tables will, I think, establish the conclusion that the Moorfields and Whitechapel skulls are strikingly similar both as regards means and variability, and that the peculiar features on which I dwelt when discussing the Whitechapel crania are present in the Moorfields also. Moorfields females show even greater average length than Whitechapel, and in spite of their greater breadth the cephalic index, 75, is much less than that assumed for modern English*. The above conclusion is confirmed by an examination of the abnormalities of the present series, which will be given later on.

I add a specification of the Moorfields crania, for purposes of comparison.

TABLE X. Specification of Moorfields Crania.

	Cla	D 1	
Character	\$	ę	Remarks
100B/L	Mesocephaly	Mesocephaly	Close on border of doli- chocephaly, sexes practically alike
100 <i>H/L</i>	Chamaecephaly	Chamaecephaly	Sexes nearly alike; well within borders of chamaecephaly
Profile Angle	Mesognathy	Mesognathy	Sexes alike, tending towards prognathy
Upper Face Index	Narrow faced	Narrow faced	Sexes nearly alike
Zygomatic Upper Face Index+	Leptoprosopy	Leptoprosopy	♂ 52.8, ♀ 52.6
Orbital Index	Chamaeconchy	Chamaeconchy	In both eyes practi- cally the same in each sex, but female rounder
Nasal Index	Mesorrhiny	Mesorrhiny	Male near leptorrhiny
Palate Index	Mesostaphyline	Mesostaphyline	Female tends to lep- tostaphyline
Alveolar Index†	96.44	96·10	Sexes alike

^{*} Biometrika, Vol. III. p. 209.

[†] These indices are the ratios of the means of the characters; the former is $100\,G'H/J$, the latter $100\,GL/LB$.

(6) Photographic Study of the Moorfields Skulls*.

A photographic study of the Moorfields crania brings out even more markedly than the numerical measurements the wide divergence of the English skull of the Londoner of two centuries ago, and possibly of his successor of to-day, from the types of our nearest continental neighbours. A magnificent cranium like that on Plate XVII. is exceptional, although it also shows the very prevalent bathrocephaly; crania like those on Plates XIII. to XVI. are far more frequent, and one recognises at once features of a somewhat primitive or debased type. It seems urgently necessary that a large series of crania from another part of the kingdom, and if possible from a rural district, and of about the same period, should be examined. Is it possible that the contents of plague pits in a city like London only provide us with a debased sample of the population? Or again, is the Londoner of to-day really different from this man of two centuries ago? If he be, is the change the result of selection, immigration, or altered environment? One must confess to a certain feeling of unrest, so long as the two largest series of English skulls, of which we have complete measurements, namely the Whitechapel and Moorfields series, give the English these not very flattering cranial characters.

The remainder of our photographs have been selected to preserve records of special abnormalities for future comparison and reference. Plate IX, gives a fine example of an ossicle of the bregma; Plate VI. completes our English series of tripartite interparietals, the ossa triangularia being detached and the os pentagonale fused; compare Biometrika, Vol. III. p. 220 and Plates XXXVI.—XXXIX.; Plates VII. and VIII. illustrate double and triple ossicles of the lambda and should be compared with Plate XXXIV. of the Whitechapel memoir; Plate X. provides a striking instance of supernumerary condyle with articulating facet; Plate XII. shows the post-coronal depression frequently referred to, and is besides an illustration of the very common receding forehead; and Plate XI. reproduces a remarkably symmetrical pear-shaped norma verticalis. Such pear-shaped domes often curiously regular and smooth in texture—will be familiar to all craniologists as occurring in a small percentage of cases in most cranial series. to this characteristic might possibly be taken as follows: The skull being adjusted to the horizontal plane on the craniophor, mark on the sagittal circumference the points in which the vertical planes through the greatest breadth (B) and through the minimum forehead breadth (B') meet this circumference; let the horizontal distance between these points be $D\uparrow$. Then 100 (B-B')/D is the suggested index. It might perhaps be termed the Pyroid Index. I suggest that the Pyroid Index will be found to be of some racial and sexual value, and I hope that a study of it at least in English crania will soon be published.

^{*} I have to thank Professor Karl Pearson very cordially for the great trouble he has taken in photographing the skulls.

[†] Easily measured with the spanner described in Biometrika, Vol. 1. p. 415.

(7) Special Crania*.

In the 120 skulls which form the subject of this paper, 264 anatomical peculiarities were noted, on an average 2.2 for each skull, as against an average of 96 for each skull in the Whitechapel series. Of the total 120 skulls, 50 were adjudged male, with 107 peculiarities; the average number of peculiarities to each male skull was therefore 2.14, while in the Whitechapel series it was 91; the number considered to be female being 70, with 157 peculiarities, the average number to each female skull was 2.24, compared with 1.0 in the Whitechapel collection. In both series it will be observed that the female skull has a somewhat greater tendency to abnormal variation than the male.

This high frequency of abnormal characters, although some of them, it is true, are very slight, tends to confirm the general conclusion arrived at from an examination of the Whitechapel series, that the English skull is probably remarkable for abnormal variations. The increase of the percentage in the case of the Moorfields crania is to some extent, but I think not wholly, due to still closer examination.

I shall now draw attention to some of the individual cases of abnormality, adopting the classification used in the Whitechapel paper.

(i) Peculiarities of Form,

Post-coronal constriction occurred in only 2 skulls, 1 male and 1 female. When localised about the bregma, we have noted this peculiarity as post-coronal depression, and it occurred in 33 skulls, 17 male and 16 female: in 11 of the 17 males and in 9 of the 16 females, it was noted as slight or faint. The cases of constriction are remarkably few when compared with those of the Whitechapel collection, where 19 cases occurred (mostly in female crania) in a total of 292 crania; but taking constriction and depression together we observe that the cases are relatively about twice as frequent in the present series, the figures being 35 in 120, as compared with 46 in 292.

Two female skulls showed post-coronal flattening, and 2 others pre-coronal depression.

Two female skulls present a *metopic ridge*, associated in one case with a metopic suture (see below).

Flattening of the obelion was noticed in 7 skulls, 2 male and 5 female, and depression of the obelion also in 7 cases, 2 male and 5 female. In 4 crania (all female) the obelion is grooved, while 7 others (3 male and 4 female) show posterior sagittal grooving, and 1 male presents a slight mid-sagittal groove. A coronal ridge was found in 1 male skull, and a sagittal ridge in 3 skulls (2 male

^{*} I have again to thank Professor Thane for his unfailing readiness with help and correction.

[†] Biometrika, Vol. III. p. 217.

[#] Biometrika, Vol. r. p. 217.

and 1 female). Post-parietal flattening is recorded in 3 skulls (2 male and 1 female); 1 female skull is noted as showing parietal bulging; and another shows parietal expansion with slight right parieto-occipital flattening.

Skulls with protuberant occiput have been specially noted in this series; of these 5 males are recorded as having the occiput prominent or protuberant, and 7 males as presenting the same condition in a slight degree. For females, the corresponding figures are 11 with prominent, and 8 with slightly prominent occiput. Bathrocephaly occurs in 13 skulls, 5 male (of which 4 are slightly and 1 markedly bathrocephalic), and 8 females (of which 6 are slightly and 2 markedly bathrocephalic). This shows a percentage twice that of the Whitechapel series. In 2 of the male and 10 of the female cases of bathrocephaly it is noted that there are no ossicles in the lambdoid suture, while in two other female cases the lambdoid suture is obliterated.

Two cases of receding forehead are noted in male skulls, one of which has the calvaria depressed, while the other is recorded as doubtfully microcephalic. One female is recorded as having an infantile upper face. Only 1 male and 1 female skull are noted as plagiocephalic; and 1 female skull is rather pear-shaped in the norma verticalis (see Plate XI.). In 1 female skull left occipital flattening occurs; and in another marked occipital asymmetry.

A marked inion is noted in 5 skulls, 4 male and 1 female. A torus occipitalis occurs, with varying degrees of prominence, in 28 skulls, 15 male and 13 female; the proportion is much higher than in the Whitechapel skulls, in which this peculiarity was met with in only 13 out of 292.

A linguiform process of the occipital bone is noted in 5 skulls, all female.

In only 2 female skulls were two *precondylar eminences* noticed, one pair small, the other minute. In this respect the collection is in marked contrast to the Whitechapel series, in which 14 skulls with these eminences were recorded.

In 1 female skull a facet is noted on the anterior margin of the foramen magnum, on another a small articular facet on the left jugular process, and in a third a right paroccipital process for articulation with the atlas. (See Plate X.)

The following peculiarities are also recorded: 1 case (female) of a median parietal foramen; 1 (female) of foramen jugulare spurium; 1 of bilateral pterygospinous bridge, also female; 2 cases of a horizontal foramen in the spinous sphenoid, 1 (male) on the left side, the other (female) on both sides; and four instances of porus crotaphitico-buccinatorius (1 male and 3 female), as compared with only two in the Whitechapel skulls.

(ii) Anomalies of the Sutures.

Eight skulls are metopic, 5 male and 3 female (in one of the females there is also a metopic ridge, see above). Although the instances are few, it may be of interest to make up a Table as was done for the Whitechapel skulls, showing

how the mean maximum head breadth and minimum forehead breadth of these 8 metopic skulls compare with the means for the whole series.

TABLE XI.

Comparison of Metopic and General Skulls.

Character	Male	Skull	FEMALE SKULL		
	General	Metopic	General	Metopic	
Maximum Head Breadth Minimum Forehead Breadth	143·0 98·5	144·2 103·7	137·6 95·2	138·6 101·0	

These figures, so far as they go, show that the conclusion drawn from the Whitechapel measurements was well within the mark*, viz., that a persistent frontal suture may allow of a 2 to 3 mm. increase in the minimum forehead breadth, but probably influences the maximum head breadth only very slightly.

Traces of a transverse occipital suture passing between the upper and lower inial eminences occurred in one female skull; also vestiges of this suture, on both sides, in one male skull. A distinct masto-squamosal suture was noticed in a female skull, and in another female an infraorbital suture on the face.

A fronto-squamosal articulation, by means of a more or less developed frontal process of the squamous temporal, was met with in 6 skulls, 2 male (bilateral) and 4 female (2 bilateral, 1 right, 1 left).

(iii) Interparietals.

On close examination it has turned out that interparietals are very rare in this series. In addition to the two instances of vestigial transverse occipital suture mentioned above, there is only one case of a tripartite interparietal, in which the os pentagonale is fused with the supraoccipital, while the ossa triangularia, right and left, are distinct. (See Plate VI.)

(iv) Ossicles and Wormian Bones.

Ossicles of the bregma were noted in 3 cases (2 male and 1 female); of the lambda in 8 (4 male and 4 female); of the asterion in 2 female skulls, and of the pterion in 9 cases (3 male and 6 female). There were 4 cases, all female, of ossicles, usually triangular, in the parietal notch of right and left temporal.

Ossicles or Wormian bones were recorded in *sutures* as follows: 21 cases in the *lambdoid* (11 male and 10 female); 2 in the *parieto-mastoid*, both female; and 1, a female, in the *occipito-mastoid*. In all, 36 skulls (17 male and 19 female), or 30 per cent., had anomalous ossicles in one or more of the regions indicated.

^{*} Biometrika, Vol. III. p. 220.

(v) Teeth.

Teeth were present in only a few skulls, but in these the following peculiarities were noted, all in female skulls: in one case the left canine has descended behind the lateral incisor (as in the Whitechapel skull No. 7041); in another, the premolar and molar ranges were markedly convex downwards; and in a third, there was a retained and displaced canine.

The result of this examination, I venture to think, is that, in spite of the paucity of examples of precondylar eminences and interparietals, which were so remarkable a feature in the Whitechapel skulls, our present series has a peculiar interest of its own, owing to the great number of abnormalities of one kind or another which it displays.

(8) Frequency Distributions and Correlation of Cranial Characters.

Owing to the shortness of the Moorfields series I have not calculated the frequency distributions, and for the same reason a determination of the numerous correlations which were given in my Whitechapel paper is not attempted here; but it may be of some interest to show the correlations of head length, breadth, and height in female skulls, as there are considerably more of them than of males. These are shown in the following Table:

TABLE XII.

Correlation of Cranial Characters. Female Crania.

Pair of Characters	No.	Moorfields English	No.	Whitechapel English
$egin{array}{c} L \ ext{and} \ H \ L \ ext{and} \ B \ ext{and} \ H \end{array}$	44	$^{\cdot 239 \pm \cdot 096}$	120	·425 ± ·051
	57	$^{\cdot 619 \pm \cdot 055}$	130	·350 ± ·052
	44	$^{\cdot 293 \pm \cdot 093}$	115	·340 ± ·056

The differences are somewhat considerable, although in the first and last case within the range indicated by once to twice the probable error. The high correlation between L and B in the case of the Moorfields crania is remarkable, and exceeds considerably the values hitherto obtained. If not due to some special disturbing source in the sample, e.g. the preservation of some very small female skulls, it shows how little weight can be laid on the correlation values obtained from small series of crania.

(9) General Conclusions.

The general conclusions to which I was led by a detailed study of the Whitechapel skulls and a partial examination of the Moorfields series were given in my former paper*, and are confirmed by the fuller investigation contained

^{*} Biometrika, Vol. III. pp. 206-7, 217, 240-244.

in the present memoir. Fortunately we are now in possession of much more information regarding the Long Barrow Skulls than when I first wrote: I refer to Mr E. H. J. Schuster's paper on the Long Barrow and Round Barrow skulls in the Oxford Museum*. With the aid of his results I am able to construct the following Comparative Table, which is an enlargement of Table XIX of my Whitechapel memoir†.

TABLE XIII.

Comparison of Moorfields and Whitechapel with Long Barrow Skulls.

	Male				Female							
Character	Mod	orfields	Whit	echapel	Long	g Barrow	Mo	orfields	Whit	echapel	Long	g Barrow
	No.	Mean	No.	Mean	No.	Mean	No.	Mean	No.	Mean	No.	Mean
L'	19	188.0	72	187:8	8	191.9	23	182.5	57	180.1	3	185:3
L	44	189.1	137	189.0	16	190.6	63	183.4	140	180.4	13	182.6
F	45	186.9	138	187.3	17	187.1	65	182.4	143	180.1	12	184.0
B_{r}	46	143.0	135	140.7	18	142.4	62	137.6	140	134.7	12	138.6
B'	47	98.5	132	98.0	16	98.9	64	95.2	147	93.1	11	94.1
H	34	129.8	122	132.0	12	137.8	47	123.6	124	124.6	9	135.1
OH	46	113.8	135	114.6	9	120.7	59	109.4	143	109.2	3	118.0
LB	35	98.5	119	101.6	11	101.9	46	95.9	122	95.3	8	96.8
fml	36	35.4	_		11	35.7	50	34.3			6	34.5
fmb	34	29.7	101	F04.0	11	27.7	50	29.0	100		6	30.2
$egin{array}{c} U \ S \end{array}$	37	$527.1 \\ 378.5$	131 131	524·2 377·1	16 13	534·9 384·8	56 53	512·7 365·6	136 130	503·8 362·8	7	518.7
	40 32		,	307.9	9			293.1	122	294.0	8	382.0
$Q \\ G'II$	3z 20	$\frac{305.4}{68.1}$	115 75	70.2	13	321.8	42 27	64.1	62		3	312.0
GB	$\frac{z_0}{15}$	93.9	55	90.9	12	95.9	21 18	86.9	58	65·9 84·9	4	66.7 92.7
J	7	129.0	43	130.0	3	134.0	18	122.0	33	120.3	4	132.5
$\stackrel{m{J}}{NH}$	20	50.4	79	51.2	15	49.4	27	48.0	67	48.7	7	47.0
NB	18	24.0	70	24.3	15	24.1	26	23.4	64	23.2	7	22.8
GL	17	95.0	73	95.9	9	95.3	25	92.1	58	90.4	4	92.6
100B/L'	18	75.1	69	75.2	8	74.4	21	75.4	55	74.6	3	74.3
100 B/L	42	75.5	131	74.3	16	74.9	57	75.0	130	74.7	12	76.3
100H/L	31	68.4	120	70.0	11	72.7	44	67.2	117	69.1	8	74.0
100~G'H/GB	14	72.8	53	76.5	9	71.4	18	73.5	54	77.9	1	81.0
100 NB/NH	18	47.6	70	47.5	15	49.0	26	48.7	64	47.8	6	49.1
P $^{\prime}$	15	84.5°	63	86·1°	5	83 · 0°	19	84.8°	52	87·1°	_	_

An examination of this Table and of the other comparative tables given in this and the former paper amply justifies me, I think, in re-affirming my main propositions, viz. that the Whitechapel and Moorfields skulls with which we have been dealing represent the typical London skull of two centuries ago, and that notwithstanding some differences, especially in height measurements, the type can be described as approaching that of the Long Barrow men.

^{*} Biometrika, Vol. iv. pp. 351-362.

 $[\]dagger$ I do not include eye and palate, as Mr Schuster and I have not adopted the same method of measurement; probably also in measuring Q our methods would lead to somewhat different results.



Moorfields Crania. Special Skull. Tripartite Interparietal with os pentagonale fused. Ossa triangularia free.

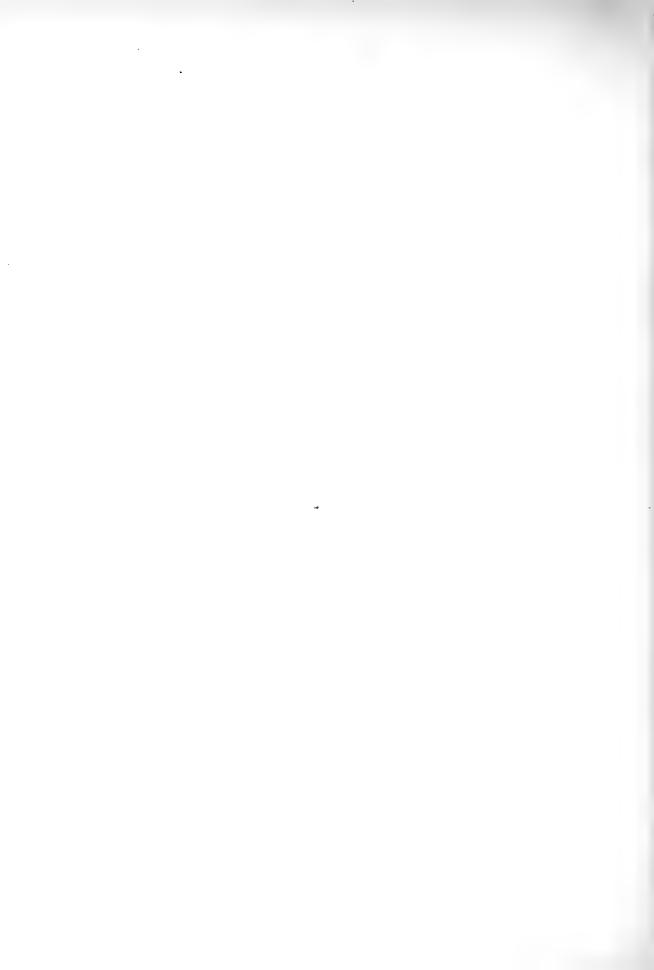
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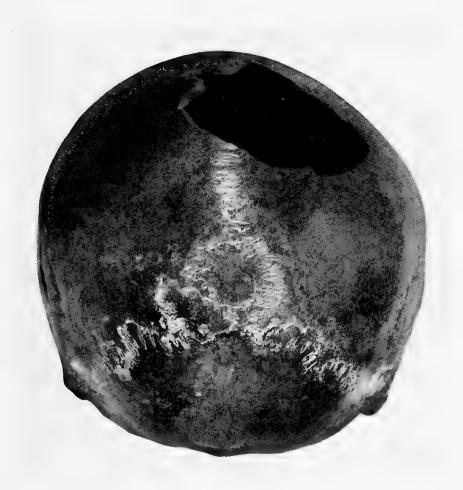




Moorfields Crania. Special Skull. Double Ossicle of Lambda.

L. S. 36.

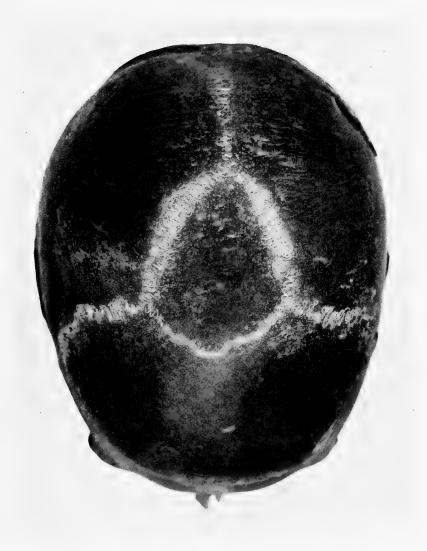




Moorfields Crania. Special Skull. Triple Ossicle of Lambda.

L. S. 56.

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Moorfields Crania. Special Skull. Ossicle of Bregma.

L. S. 66.



Moorfields Crania. Special Skull. Paroccipital Process articulating with Atlas.

L. S. 36.





Moorfields Crania. Special Skull. Pear-shaped in Norma Verticalis.

L. S. 97.

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Moorfields Crania. Special Skull. Showing receding Forehead and post-coronal Depression.

L. S. 120.

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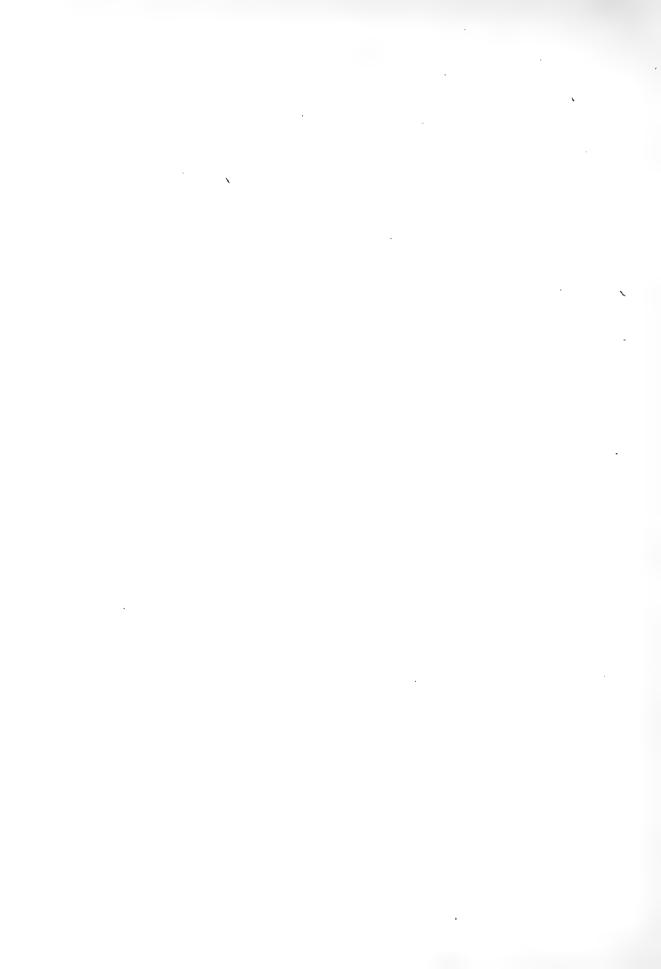
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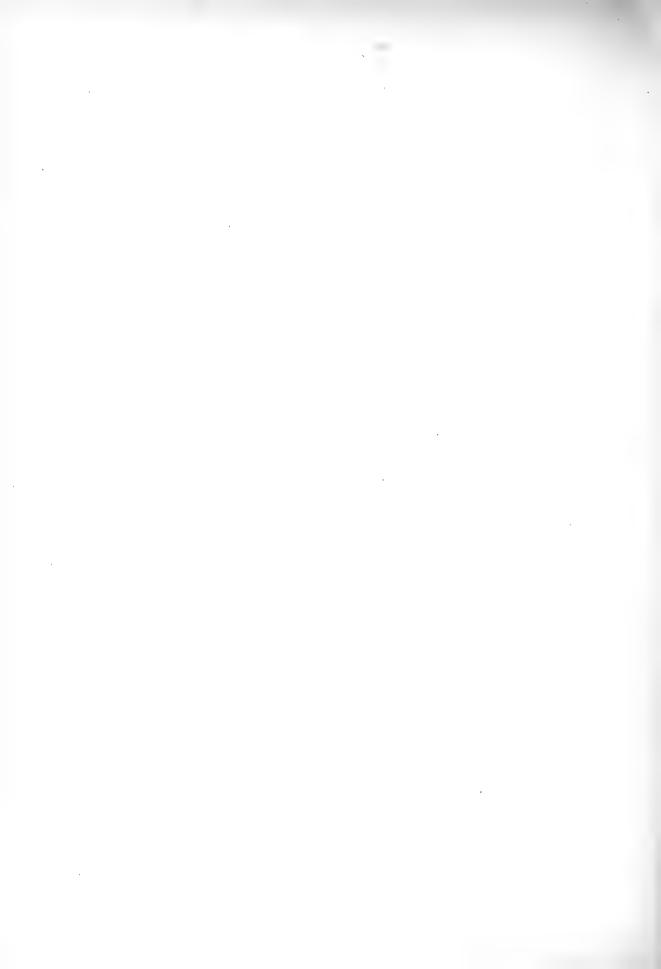


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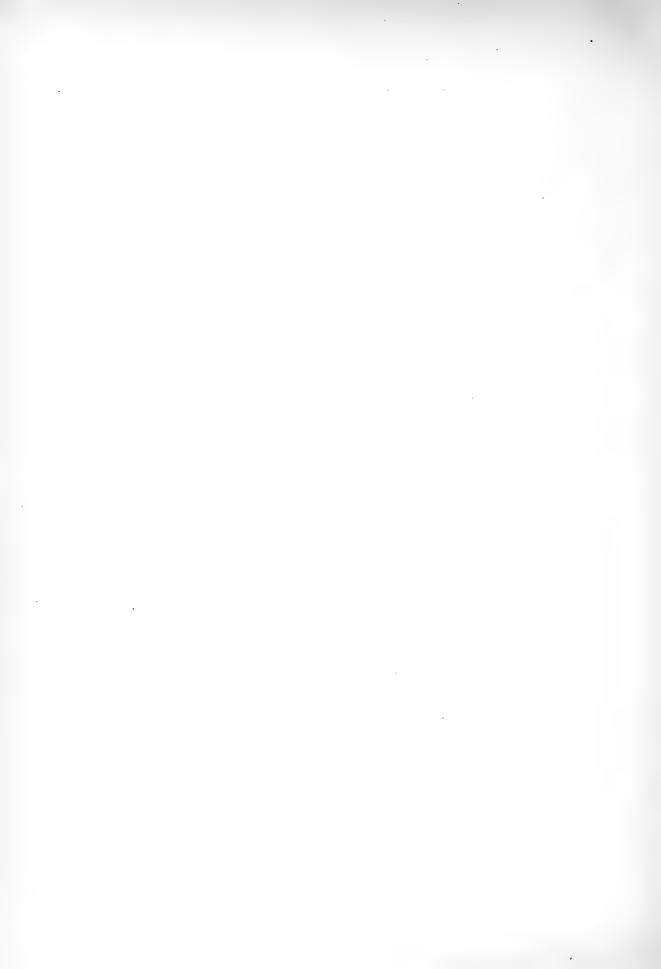












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1 1	1605	197	197	197	140.5	104	130	117	101 5	552	380	34 1	120 14	1 110	101	61.5	73	93 5 1	34 5 5	2 5 2 3	40 5	41	33	32	44 5	3× 5	74 4	(h)	71.4	69	107.7	78 I	43'8	81 5	78	86.5	91.5	bo 5 79	5 44	14	10	59.5	3 : 3	; ;2 >	s6 7	cal. ad. ossicle of bregma 18 × 12 mm. l. ossicle of pterion, coronal ridge, protuberant occipital. torus occipitalis
, 2 6	1427	151	157.5	185	1.5 3	93	127	108	43	522	374	208	123 12	5 126	1 ;	55.4	625	101	1	2 7	41.5	41 5	12	32	50	34	77 12	fig 2	77 3	64-6	1126	61.0	57	77 1	77 1	78	59.5	67 73	413	q	31	N2	\$ 20	3 21 7	70.4	cal ad. r. zygomatic defect, interparietal pentagonal fused with supra occipital r. and l. triangular distinct. post parietal flatten-
3 -	1247	182 5	151	185	142	101	E 24,	105	qu	518	303	207	123 [1	2 128	100	55.9	-	97 1	1,7		43.5		14 5	-		.ş(·	77 2	70-1	70.8	69 7	110.1	_		79.3									3 54	} 00 - 8	7 3	ing faint post coronal degression, marked inion. See Plate VI eal, old, face very defective, r. ossiele of pterion 43 mm, long, extending back in squamous siture. Battening of obelion
4 :		120		15%		1(*)	127 %	111 /	101		375		127 12	3 125	1-4	(4)														67.8	- 1	_					- 1						32,	2 70 5	130	cal. f. ad (2 young). large busul and r. lateral defects, tri- angular ossiele 15 x 18 mm, in parietal notch of l. temporal.
5 ± 6 ₹	1425 ²³ 1559 ³	15q 191 q								528 534														-			_			71.7													3 51	3 45 S)8 G	faint post coronal de-pression cal - f ad. (2 young) with ethinoidal defect. flattening of obelion cal. f. ad (7 young), spheno-ethinoidal defect, protuberant
7	1399	152	184	155	130	45	120	103	105	505	745	2h 9	107 12	5 115	0.2	55 2	70	915 1	25 ,	23	42.5	43	35	6;	47.5	37 5	75	15.2	74 1+	01.0	114 0	70 5	45.1	89.4	55.4	75.9	101	7 7 :	5 31	ç 15	30	51	3 51	3 01 7	0.0	occipital and marked union cal, ad base fractured, slight post coronal depression, slight probaberant occipitat
8 2	1476	107.5	195	145 3	141	1:=;	129	11	104	534	373	200	140 F	0 113	+2	55.2	6.5	89	1	5 22	11.5	14	35	34	45	40	72 3	66-1	72.1	60	109 3	71'9	4 ,	78 ti	77 3	533	115	94 79	37	1)	25	28	4 07	14 7	77.1	cal ad, both zygomata defective, trs. fracture of base, slight depression of obelion, slightly prominent occuput
9 1		179		1,40	1 17	40	112,	107.57	. 14	\$110						l	55.5	52"	10	2.2	\$		3		Ίt	37.5			76-1	65 6	16.1	67'7	4- /	Ю		11.5	76 6	02 77	5 4	7		Ī		₹ -5		cal, ad large occipital and r temporal defect, apex of occipital prolonged (linguiform process), obelion grooved faint post
10 :	1450	173 5								452 510							64	-	4	23		11	,;	32			73			09.2 65.2			5	53.5	78	-	30 · [1	25 75	40					2 15 7	1.4	coronal depression. two small precondylar emmences cal. ad. very defective cal. f. with left orbit. ad. slight post coronal depression.
																İ																														ussicles in lambdoid software (horizontal foramen in 1, spinous spheroid, imperfect porus crotaphetico-buccinaturius), slight torus accinitai
12 2		175	150-5	180	132.5	145		112		\$ 1/2	1/1-1	2 = 3 = 1	123 110	122	102 4	100 8		1.	ω.		:>		,				73.4		23.5		-			~ ",									, 35			cal f. with orbits. ad (? young) with large basal defect slight sagittal ridge and linguiform process on occipital. slightly
13 14	1425	185	10-1	190 S 184	139	13	1 122 5	110 115	1,5	522	357	217	123 13	125	101	50-3	72 62		42	25		42 41		32 5 20 5			73.2	(13	`3	04.3	113.5	_	13.1		77.4 71.9		h7 5 (01.5 72	5 \$10	17.5	25 ,	in .	321	2 73 S		protuberant occiput cal. ad. left half of face wanting. faint post coronal depression, cal. ad. very imperfectwhole base. post coronal flattening on
15 16		176.5		178	136 \$	110		104 h		4/3	3.47			111	**	\$0 x													20.7	- 1	_	_					- 1					-				r side dome. ? old. marked groove of obelion, protuberant occupat dome. ? old. occipital torus
17	1480 3	177	176	177	150 5		123		QI	52.1			132 11			- 1	62		41	5		40		32.5			85 5								81.2	1	yti 5 7	5 5 66	35	5			3 4			cal, ad, left half of face wanting and l, occipital defect, post- coronal depression, slight form accipitalis
18 =	,	152		185	112	*A-4	1 %	1117		- 1			125 17			59.0								- 1						73'5 11	105 1	_						-					,01	2 53 /	- 1	cal f. ad. large 1 fronto-temporal defect, metopic, sharp occupital torus two osaicles in right extremity of lambdoid suture
19 3		175	,		142	N ₁	13.5		(5.5	505			125	104	-,	.~ ,	, -	,	ta 11	24		٠.		12 5	45	ا ه.			24.3	73.5	inta		fo		75.6	٠	. 1.	45 75					١.		- 1	calf. ad. very imperfect base prominent occuput, traces of ossicle of \(\lambda \)
20																									,,,					,,,	,		,-		7,1		~ [~ 7 / / 7	, 42				•	42 41		eal. ad. (° old) r. parietal, l. temporal and l. malar defects post coronal depression. ossiele of asterion in part fused and triangular ossiele 15 × 12 mm. in parietal notch of temporal both
21		121						110 %		\$110		201			25	· 1										İ			-21	05 5 1	05 3					- 1							3 50	70 7	Sign	on r. side (masto-squamosal suture) cal f. ad. with sphenoidal defect, slight post coronal con- striction, post parietal flattening, slightly protuberant occipat
22 9 23 d 24 9	1070	178 187 185		189	155	104	143	112 h 122 h 107 h	c/b	470 545 512	172	3.3	(2) 13 (3) 12	102	17	102 4			_					-		-	-	-	82	71'2 1 70 4 1	10.2						-						3 39 3 82	3 23 - 50 1 91 - 70	0.2	cal. f. ad. fronto-sphenoidal defect, shightly protuberant occipital cal. f. ad. ossicles in lambdoid soture dome. ad. 7 old. shight flattening of obelion. slight forus
25	140∞	155		151	136	4	12)	La	55 ,	515	374	285	125 12	7 124	24.5	5' 4											-			65.2 1		_				- 1							: ta :	: 55 70	- 1	occipitalia esl. f. child. distinct post coronal depression. numerous ossioles
1																											1																, ,,,		,	in lambdoid sature, on r. side one of 12 and one of 16 mm, triangular essible in parietal notch of r. temporal, l. ossiele of
26		190	5	104	E42	1000	125	1134	Qr s	5 5 5 1	374	355	22 12	124	955	55 3											- 1	_	74.7	65'8 1	13%	_					- 1	_					1.70	02 7		pterion, imperfect porus erotophilico-buccinatorius and horizontal foramen in spinous sphenoid both sides cal - f. ad. with fronto-ethmoidal defect, rather prominent
27	7 1207	157	150	180	1345	14	122	102	100	512	370	250	(26 - 12)	115	945	55.8	66		54	2.1	41		11			37 5	71.2	04.2	71'2	64'5 1	10.2		48	80 5		9	14 6	5 75	5 39 5	7.5	30	- 1		70 54	- 1	occipital cal ad r. malar, temporal, occipital and l. zygomatic defects.
28	1470	101		191	14"	47	118	114 h	**3	537	335	302	127 13	125	2.1	57.7				Ì							-	- 1	76-4	61.8 1	23.8	_											3 47	79 5		distinct post coronal constriction. slight depression of obelion. flattening of post parietal region. slightly plagrocephalio call - f. old. prominent comput. traces of ossiele of A and
29 30	-	192 182		195 186	131	100	131	108 h	1 3	505			122 120 116 130		41	57.5								-						70'2 1								-			-		3 27 3	(OI ; 92	2	considerable wormian in l. lambdoid suture. shallow groove of obblion domo. ad. posterior sagitt. grooving cal f. ? old. with large fronto-sphenoidal defect. faint post coronal depression

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74'3	112.2	_
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D			1			į				ı																					1	1						,-3								r. ossicle of pterion 35 : to mm r. paroccipital proces long articulating with atlas, on l. jugular process articular facet, teeth present r. lat meisive canne, tooth descending behind lateral unciaer (cf. Whitechap post sagittal groove r. nearly complete purus crou
37	1121	170	169 17	0 130	92	117	101	90 4	S1 34	27	8 11	6 113	111	90"	5 58.3	60 5	82	114.2	43'5	21 .	μ.	41-5	32 5 3	2	39 3	5 7	7'2 6	9°2 76	·8 68	.2 111	6 73	8 4	18.3	79°3	77'ı So	8 86.	5 67	73°	40°	12°	28°	85^	3 13	2 62	83.7	buccinatorius. See Plates VII and X cal. old. shight post coronal depression. r. foramen spartum
38	1541	188	188 18	9 152	98	121	111.2	96 5	40 37	6 31	5 13	1,0	115	917	5 56.8	66.2	96	- '	52.2	28'5	10.2	415	33 3	3.2	4	15 8	0.8 6.	4.4 80	4 64	123	6' 69	3 5	5473	31,2	80.7 -	911	5 05.2	73°	41.2°	14°	27'5'.	87	3156	3 04	S5-4	cal. y. ad. l. zygoma defective. frontal process l. slight bathrocephaly. 4 wormans in lambdoid suturo. of asterion. premolar and molar range markedly conveyands.
39	1394	184	183 18.	1 136	95		109					4 108	140			69.5	99	122'5	50	25 4	0	10.2	32 5 3	2	47 3	5 7	1'3 7	0°5 73	'9 70	1 105	·5 70	-2 5	ю :	2.18	79 79	b 977	68°	70-5	41.2	10.2	31,	S1°	3,03	2.72	1,06	varus cal. ad, small posterior parietal and maxillary defects o slight depression of obelion
41 4		187	- 18	142	91	129 1	112 h	91 5	15 36 25 38	5 30	57 -		110	95		_	-	-	-	-	-		_	-	- !		- :	- 79 - 75	5 68	6 (110	1		-	_	-	- -		_	1	-	-		3°73 3°25		81 '8 97 '2	cal f. ? old fronto-ethmoidal defect
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43 °		154	190	1	() ()1	٠,	151		15 1 36	5 -	- ? 13:	9	?	?		75)3	- ,	51	22 5 4	ا د	13.5 3	. 3. 3.	- I,	 55 .	- .	_ ! :		. _	-	50	. . 7 49	 02 2	b7 2 + 3	- -	100	- bb's	1 70'5'		-	_	-	_		-	nised in lambdoid suture dome old slight bathrocophily lambdoid suture cose cal 7nd, extensive defect of hinder part and r. sido. In
45	?	181	- 18	149.7 1.12	95	_		_	- 1 18 18 35	-	- 13	122	125	101	57 6	-		-		- '					- -	- [1 -		. , -	- 1		1 -	- 1	- 1	- , -	.		-	-		_	_		_	_	coronal depression. It ossiele of pterion dome. ad.
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53		1837		7 1 153	94	136 1	12 h (00 S	- 39	12		, ,	135	011	e8 2						_			1		·	- -	- '		í –	_				- ' -	1 -	1	-		-	_	- [-	-	- 1	dome. ad. ? young. post coronal depression. linguifo cess to occipital. slight torus occipitalis
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57 î	1405	185	186 5 187	1 13715	, g5 i	126 t	11 : 6													•	1	1					-7 5-1				,									- 1				_		cal. ad. large occipital and r. temporal defect and defect of triple ossicle of \(\) collectively 40 < 30 mm. individually 25 × 15, 15 < \(\) mm. bilateral ossicle 10 × 12 mm. at or of lambdoid. See Plate VIII
58 9		193	195	137			14 k									_			_		1			- 1	, Jo	. /3		70°	2 61:	8 1121	2 77 9	5 40	in 8	921 . 8	4°1 76	93.5	670	70'5"	42'5"	13"	39.20				- 1	cal ad traces of osselvs in lambdaid, retained and d. r. caume, slight torus occipitalis
59 1		184	1186	145 5	_		_	- 1				122				_	- 1	-	-				_		_	. .	- -	_ / _	_		_	1		_		_		_		1	. 1	- 1			- 1	calf. y. ad. spheno-ethroidal defect. bathrocephaly, rous ossicles in iambdoid and r. masto parietal sutures
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62	1531	197	197'5 198	. [] 140°5	1 94 1	136 121 1	1		6 38	7 291	142	125?	125?	00		04.5	82 1	25 2	1"_ 1	23 (4	1 1 2	0.6 5	9 29	5 5	5°05 41	5 -	- -		1		6712			_	0.3 85.	-	-	- 1	-	-		- 1	3.85 2	'95 7 '62 8	76·6 82·6	cal. ad. greater part of calvaria wanting dome, y. ad. with smull part of base
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- metopic ridge inion, trace of nces al defect, pre-
- obelion. pro-
- A 25 30 mm process 12 mm, rocess a small nine, I. canin-itechapel 7041), as crotaphitico-
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- ecta un l. aide.
- parietal, post on both sides, tal suture on
- to be recog-
- crosed lo. faint post
- e. slight de
- 35 mm. long
- 23 × 10 mm.
- guiform pro-
- cture, small
- slight r. post
 mal depression
 elect of vertex.
 duality 25 × 20,
 at outer end
- and displaced
- haly, nume-
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- phaly. small (
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LDS CRANIA.

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2 6	67°2	107.5	68.
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6°2	70.7	107.4	_
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6.9	73'1	105.3	_
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72.9	67.5	108	_
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71.7	64.7	111	_
76.9	68.7	112	
77.6	70.7	109.6	-
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66	1425		_				575	?	_	97		10 30		077	7	7	116		,,,	60 3 1	-	-	-	-	-	-		-		_	-		-	-	-	- 7	76	-		-		-	-	-						- 1	-	-	-	3.08	2 94	79 9	ossicle of bregms 63 * 50 mm. nearly symmetrical, mostly be- twees parietals r. ossicle of pterion. See Plate IX
68 .	z 1×1		185	186	14375	96) 12:	- I	:10	94		10 38 14 36		04	127	7	?		2	-		-	120	5			40.2	-	- 3.	5 !		_	-	77.6	65	9 7	7"1	65°6	117.6				86-4	_	_	-					-	_	-	3*37	2.93	86'9	dome ad slight bathrocephaly, no ossicles in λ, faint torus occipitalis slight post coronal depression cal, f, ad, with l, orbit bathrocephaly, numerous largo ossicles in lambdoid, suggestion of torus occipitalis
69 · 70 · 71	, 1227	_	179		142.5					101	1	. 35	1	_	130	135	117		-	_ 56 7	70	91	12	5 5	- 1	26°5	41		3				32 5 41	75 7	1 -		5 7	6;	112)	70 9		19'5	85'4	77 I 814	S ₇ :	1	5 65.				-	20-5 31°5° {		2.35 3160		Sg 3	ed ad depression of oteller it frintes plant si, contact' Lossiele of pterion
72 . :	1643		202			104			117			\$ 40			ł I					- 1		91				28				2 1	32.2			1				65.8	110'5	73.6	,	57'1	7414	78.3	72 1	97	5 68	72	2*5 3	9*5 1	12.2	27 '	85	3145	2.95	85.5	faintly ridged and posterior faintly grouved), trace of occipital forms cal. ad. slight temporal defects trilateral, slight occipital promin
73 74 75 3	1313	186	186	186	134	97 115 92	119	5 1		n5 92	51	* 37 - 35	13 25	57		 6*1 120	113		6 10	61 n 56 b	61.5	R9.5	120	-	í	23 S	11	1,	3	1	32 —	48	36	72	67	- 2 7	6	(; , 65	1 -7 -2 116:8	68 7		52.2	75.6	78	75_	95	5 69	74	- 3	7^		- Ks	ر اد اد		2 1-9	82 8519	ence dome, ad, with small part of base tal ad, faint pre coronal depression dome, ad, with occipital, slight occipital prominence, sagitful
76 (1 77 2	1048		5 130 5	5 197	141 2		- (5 5 1	17	94 102		- 36 in su			T ₁ O	? 128.3	7	[]	?	55.	(7.5	02		- 5	- o ;	22.5	ĮE j	45	5 1		32 5	51	14	72	(-)		4'4	555	-115	- 73 4	ı		75.		, , ,		5 05	79	5 5 3	/3	15	,	١,	3.77	3125	86°2 79 5	faintly grooved posteriorly dome 2 obt with occipital tal od 17 78g ma defective costete of \$ 15 13 mm slight term seep 55 mm
78 79 80 81	1170	173 191 179	174 174	174 193 181	147	102	1 1 2	1 8	17 n 10 h	, 104	15.	17 12 15 13 37 12 35	ъ .	_	140	120	1.20	16	12	51 1 61 2 57 8 58 5	57	80	110	- 1	0 \{ 		39.5	1)		_	32 29 5 —		1.4		07	- 17	3 7 3 0 0 2	_	_	71 2	1	55 1	74_1		\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	7 90	- []	2 79 3 77	, ·	5.5		27.3 27.3 —	85	३ छ। -	2 (9)	1 -	ent v ad bregmatic and t malar defect cal. ad suggestion of occupital terms, marked occupital asymmetry dome, ad, slight terms occupitalis cal f. ad.
83 8	1237	/ 184	187		149 5		5 115		01	97	5	3.5			129		117	.	. 17	50 5	62			-	6	_	-			_	7.2	-	-	-	61	-	_		115.9				_		-	-				1	_	- 1	_ !	3.21	3 10	\$8.3	cal f. ad. large fronto sphenoidal defect. slight prominence of occiput. faint post coronal depression, traces of ossicle 20 × 20 mm. in r larabdoid
84 3 85 8	1399	? 178 178	5		140	100	133	1		90	1	5 37	1 32	22		131			4.5		-,	-	-	-	_	-	_	٠.		-	-		-	ļ -	-	1	6.9	,	102.3	-			_	-	į -	7.	-	- '.	_	- 1	,	-	_	ľ	2.74	7770	cal. old. I. half face parietal and basal defects. shallow posterior sagittal groove. protuberant occiput. See Plate XV cal. f. y ad. small r. temporal defect. slight bathrocephaly small wormians in lambdoid. trace of torus occiputalis
86 67 88	1217	186	5 179	150	133.5	91	125	. 10	00	1 63	5 40	8 35	6 1 28	85 21	124	124	115	10		1-2 2	71 -	86 92.5 74		5	1	21.	4.1	1.2	- 3	1	1.2	3815 50 35 1	136	25.0	75	-	0.4	74.5	102 [70°0	5	52.7 46 I 52 5	75.0	76.2	96 1	1 Sc 101 78	0 5 04° 0 5 06 0 04	5 73	35 4	0	13	25° 27 29	71 56 5 57	3 11	2.05	97 1	dome, ad. cal yad occupital rather prominent tal, ad inhibiteral zygomatic defects slight torus computation cal shill about 5 or 6 years, faint post coronal depression, teeth in vitor 7 and 2 temps moders each side lat permanent
89 2 90 - 8	1440	158	'5 — —	194 189	141.5	102	131	i	16 h	97		9 39			135					56°9	-	-	, -		_	_	-	_	-	-	-			-	-	- 7	2.9	67.5	108	-		-	-		-	-	- -	- .	-	-	-		_	3'36	3.30	9812	molar and mesial incusor just coming down calf. ad. small ethmoidal defect. metopic, slightly promi- nent occiput. faint post coronal depression
91 92 9	-	152	, –	154	132	97	110		07 S h	98		- 36	0 28	8ς	115	122	120	10		610			1		_		_			.				-	:	7	17	_ (4.7	111			_				-	-	-		_	_	-	_	3 05	2 66	87.2	dome, ad, slightly prominent occipital, small ossedes in lamb- doid suture cal, f ad, l tempore-sphenoidal defect post coronal de- pression, protuberant occipital
93 8	1415		189	1591	147	96	1 1 1 2 2		18	95	-	4 17 5 18									62		1	1	451	22	11.2	14"		3.2	32	18.2	30	1	1		16°0 17 6				1	171	78 3	71.9		1 91	'5 69°	5° 7:	2° 13	85	125	26^	84 5			St .5	cal. ad, r malar defective. faint post coronal depression ossicle in parietal notch of r, temporal
94) 8	1415	154	157	187	140	95	127	7 10	04	97	5 51	8 37	3 29	90	124	126	123	1 9	9 1	57 4	7415	103	-	- 5	3	23.2	43	44	3	3		51	41	7419					110 2		3	1413 - 1	76.7		802	101	70'	·5° 6	5°5° 4	40	10 50	33.20	76°	3.20		-	and small l. frontal defect cal ad 2 zyomatico and occupito-temporal and r. maxillary defective. bilateral frontal process of squamous temporal.
95 96	7 1506		5	1901	141	92	*5 j 140	1 1	10 h	931		7 15							13 1					- i - 5	,	 27	- 43			_		42 5	1	72 0	,		74 72 0	63	117*5		1	52.9	70 7		J			Ì				İ	52	3'57	3 13	°5 3	prominent inion. slight occipital prominence
97 , 8 98 8	1582	- 1	1104	- >7	14315	to3		1		96		9 40 1 36							5 .	~ I		89				22.2		41	3	215		1	36-5	1	68	, ,	74	ris.	108 7	70*				78	82	9 92	67	7-	4^	g^	13	20	87^	3 33	2 68	So-5	(? microcephalic)
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[&]quot; Not taken into account, except for angles.

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RANIA.

		Ind	ICES
B/L	H/L	B/H	G'H/G
6.4	69.4	110.2	76.1
4.9	66.5	112.7	_
0.8	67.9	104.3	_
7.1	68.6	112.3	_
5.8	66.7	113.6	_
9.2	66.8	118.6	-
 7 [.] 7 9	65.6	118.2	71.3
3.4	66.3	110.7	_
74.5	65.8	113.5	73.2
	_	_	
		113.2	_
75.7	66.3	114.1	69.1
_	_	110	_
72.7	67.6	107.6	-
71.6 73.5	70.4 66.1	111.1	69.1
75°3	_		
79.6 73.7 76.4	60.5	121.8	75

MEASUREMENTS OF MOOFFIELDS CRANIA.

	İ		1	ENGTHS			- 1			Ci Time	FRENCES						\mathbf{F}_{A}	CE			- 1	PALATE					Innics	.8				1	1		Ахоы	KB			FORAME	2.	
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99 , 8	ŀ	92 5 -	193 148	97	134 119	9 11 9	0 544	4 401		3. 1				65.2	90	- 4	9 20	5 42 5	43	32.2	2.2	ı6	-	- -	76.7	69 4	110-5	76-1	41.8	76.2	75.6	93	66.50	71°	42°5°	- , -		3:42	2 2.65	77.5	cal. ad. r. temporal absent. coronal ridge, marked bathro- copbally, ossich of a with series of large ossicles in lambdoid
100 , , 121	12 1	75'5 177	177'5 133	92	118 98	8'5 9	o 498	S 346	268	121 1	1187 10	o7 ? S	7? 58 1	68		- 5	0 5 22	_	40	- :	5	_ .	75"	1 66 7	74'9	60.2	112.7		43.6	_] :	87-5	Sı	60	73°5°	46'5° I	3° 133	5° 86.5°	3.81	1 3 21	84.2	suture. See Plate XVII cal. ad. l. malar defective, posterior sagnital groove pair of
101 2 144	45 7	Só _	190 134	5 94'5	129 11	3 h 0	6 517	7 376		151 1	128 11	16 10	0 63.8	67.5	_		0 26	42	_	38	_ :	io -			70.8	67.9	104'3	_	52	90 \$	_ .	97	70'5"	68.50	310	_ .	_	3187	7 1'22	81'2	minute precondylar eminences cal. ad 1 temporal and r. malar defective slightly grooved onel.on
102 1 8 15	26	S4 187	188 145	96.5	129 1 105	S o	g 528	S 375	300 (E32 1	126 11	17 0	t 55.8			_	_			1	_ [_	77'5	5 69	771	68.6	112:1	_ 1	_			1_	1 _	1 _			_	1	5 3'00	_	prominent occiput traces of ossicle of pterion See Plate XIV cal f. ad. with l. malar bone. post coronal depression. slight
103 2 17	01	04	198 150	104	132 117	7.5 / 0	8 5 548	8 205	27.4	1.2	172 77	71 10	a 56.6			_	_ _		_	_	_		1		75.8	66 7	1126	_ !	_					[i		_	1	S 1:02		mid, sugittal groove, slight bathrocephaly, no wormins cal f. ad. metopic, post coronal depression, slight bathro-
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		81 182 5	183 144						272 300 (4 5′ 4 O 5 , 59 7	64.5	90 5	- 1	115 25	43	44	31 3	2 .	6 , 35	7912	2 70 7		65 6 70'5	118.5	71'3	48.3	721	72 7 , 76	1 05	69	72	39	7 32	79°		6 2 94 3 3 0 l		cal. 1. ad. faint posterior sagitta, groove. saght toras occipitalis cal. ad. 1. zygomatic defect, slight coronal ridge, bilateral
108 7 12	95 7 1	53.5	152 5 134	94.5	121 108	8 h 1 9	3 5 510	0 374	280	125	127 11	19 9	5 50%		_		_		_		-	_			73.4	66.3	110'7	_	_ 1	_			1	1	_			3 35	5 3'01	8a*8	fronto-temporal junction protuberant occupital cal f. ? old ethn.osphenoidal defect, prominent inion, slight
109 9 133	30 1	81 183	184 137	92	121 104	15 9	6 505	5 358	287	123	9	7	,	05.5	, 69 5	124	2 24	42	42.5	33	13.5	17 40	5 73 9	Q 66 I	74.5	65.8	113'2'	73'2	16.1	77 6 1	78 8 86	2 05 5	60.5	70'5	ın'	1	_	1	_ -		post coronal flattening cal. old. plagiocephalic, l. occipital flattening, slightly de-
110	_		140	801	116	ù h	-	1			١.	_				_				. 1	_	" _				_	_			1"		77.3		1,23	40	-			, .		pressed obelion (? fronto-temporal junction) donie. ad defective, metonic
111 3	- 1	50.5	158.2 142	100 -	- 1116	6 h	537	7	"	131	124			69	7	- !	1 24	417	, 42 5	30	11.5	515 -		-	75.6	_	1		47.1	72 3	741		-		_	_ , -			. -	-	cal ad. large occipital and I, temporal defect, metopic, turus
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113	. 1 1	52 15 5	181 137	N.)	Q) 167	7 0	0 513	2 1 252	200	120	126 -	9 9	4 650	0015	8715	124)	h 5 22	·5 39	38	3115	;o .	H 37	75	o 5615	75.7	66 3	TT4 T	69.1	48.1	1808	78 o ¹ 84	1 95	681	75.5	365 1	11.5 25	° 87	3.5	4 5 14	88.7	eat, y sd 3rd moler in plan infantile upper face post
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			149		130	471	~	_	302 1	, ,	134 1:	22 10	115 5910		-		- -		_		-		-			_	110	~		-		-	-					3149	9 2 95	84.5	calf. ad. large frontal defect protuberant occipital, slight turus occipitalis, faint post coronal depression
	193 1	104	1 105 1134	5 94 (125 [110	0 n g	14.4 210	0 359	287	120	9	+)	. –	-		-		-		-	-	-	-	. -	72.7	67.6	107 6	-		-	- -	-	-			- -		3 15	5 2.33	74	cal - f. ad. with ethmoidal defect, faint torus occipitalis.
	285	192 182 1825	103 134	101 5	121 10	7 / Lin 7 Lin	01 5 540 03 508	n 159 S 302					n 5 60°5	6.1	92	126 .	1 25	427	4115	2015	1015	1 51 42		e 1 66 s		70 ‡		69.6	euro I	6014	 		6=0	1-60	1-0	e, ten	0 0 0				cal. f ad large I temporo-spacno.dal defect. metopic cal. nd. (Tyoung), small r. frontal defect, post coronal depression.
'			1		1	1					*		, ,,					7	, 4- ,	-/,	"	, 4	3 / / / /	, , , , ,	733			09.0	34.3	09.4	/11 03	3 90	107	170	37	0 29	04	3 00	13 2 35	02.0	parietal expansion, slight r parieto eccipital flattening bi-
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		73.51	174 138		.15	- i ·	491	3 351		110 1	119 11	13 9	175 5778	1	-	,									70 6	1]							_			_	parietal foramen. luguiform process to occipital 25 × 41 ium. dome. ad l. upper parietal defect [See Plate XII]
121		1815	182 (3)	18	125 (1		6 518	8 379	300 -	L _i	132 EI	10 9	7 58 0 4° 02'0	72.5	b2	1105	14.5 25 17 24			37 3215 3	30 5 ' 32 .	44.5 41 47.5 37	5 73					75 6	40 2 52'I		71°I 77	3 91	72.5	60 5		35		3 8.	2 2 54	74'3	ad r malar defect. post cororal depression receding for head, ad, (feld). I. temporo-parietal defect. slight bathrocephaly.
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TABLE IV.

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ON THE RELATIONSHIP OF INTELLIGENCE TO SIZE AND SHAPE OF HEAD, AND TO OTHER PHYSICAL AND MENTAL CHARACTERS.

BY KARL PEARSON, F.R.S.

- (1) Introductory. In two earlier memoirs* my co-workers and I have dealt with certain of the present problems. The methods then used by us were such as are suitable for dealing fairly rapidly with large masses of material, and by those methods the conclusions drawn were:
- (a) that there is a slight correlation between size of head and general intelligence †,
- (b) that this correlation is not sensibly increased by allowing for the size of the body relative to the size of the head;
- (c) that the correlation is so small that it would be absolutely idle to endeavour to predict the intellectual ability of an individual from his or her head measurements. On the other hand, if a population were divided into those with large and those with small heads, we should expect to find a very slight balance of average intelligence in the former group.

The present more precise and extended investigation is based upon the more elaborate statistical reductions carried out during the last few years in my Biometric Laboratory.

The material dealt with is the same, namely:

- (i) The head measurements of upwards of 1000 Cambridge graduates. I have already expressed my thanks to the Cambridge Anthropometrical Committee for this material, and to Mr W. H. Macaulay of King's College, and the University Registrary for supplementing the measurements with ample particulars of the examinational standing of each graduate.
 - * R. S. Proc. Vol. 69, pp. 333-342, 1902; R. S. Proc. Vol. 71, pp. 106-114, 1902.
 - + R. S. Proc. Vol. 69, p. 339.
 - ‡ R. S. Proc. Vol. 71, p. 112.
- § R. S. Proc. Vol. 69, p. 340. See also a series of letters to the British Medical Journal, Jan. 27—March 17, 1906, and Biometrika, Vol. III. p. 391 et seq.

Biometrika v

(ii) The measurement and observation of considerably more than 5000 school children. This material was collected by the aid of many teachers, and with assistance from the Government Grant Committee*.

The present investigation deals with the girls as well as the boys, who alone were considered in the earlier papers. Further, it gives the results in as complete a form as they admit of being tabulated in, and reduces them therefore by a more ample theory than was previously possible. We have investigated the mean and variability of each grade of intelligence for each measurable character. From these means we have deduced the fundamental constant, the correlation ratio η , which becomes identical with the coefficient of correlation when the regression is linear[†]. The value of η must of course depend to some extent on the nature of the intellectual grading, but the results now obtained are: (i) in good agreement with those of the preliminary papers deduced by a totally different statistical process, (ii) in good accordance with each other.

While they largely extend, they yet in every respect confirm our previous main conclusion that: While there exists a slight but sensible relation between size of head and intelligence, there is no possibility of using this relation to make even rough individual predictions.

In the present memoir the full results are for the first time published, and there will be found some discussion of each character taken in order.

(2) On the Expression of Intelligence by a Quantitative Scale.

In dealing with the Cambridge graduates we classified our material into four grades only: (i) First Class Honours, (ii) Second Class Honours, (iii) Third Class Honours, and (iv) Pass Degrees.

In the case of the school data we classified into (i) Quick Intelligent, (ii) Intelligent, (iii) Slow Intelligent, (iv) Slow, (v) Slow Dull, (vi) Very Dull.

Now, for the purposes of determining the correlation ratio between intelligence and the physical characters, it is unnecessary to make any assumption as to the extent to which these grades fit into any quantitative scale. But in order to exhibit the results graphically, it is needful to have some scale of intelligence to plot our average physical characters to. We have accordingly selected, as the normal scale of intelligence, that which would be given if the frequency distribution of intelligence followed the normal or Gaussian curve of errors. Whatever the true scale may be, it can only be a more or less—probably less—distorted form of this scale. Such horizontal distortion has no effect on the value of the correlation ratio for the plotted physical character, and an a priori justification of

^{*} Fuller particulars as to the schedules and method of collecting will be found in my Huxley Memorial Lecture: see *Biometrika*, Vol. III. pp. 131—190.

^{+ &}quot;Mathematical Contributions to the Theory of Evolution, XIII, On the Theory of Contingency and its Relation to Association and Normal Correlation," Drapers' Company Research Memoirs, Dulau and Co.

the scale may be found in the fact that the plotted points of the regression curves are for a number of pairs of characters, within the limits of random sampling, on a straight line when such a scale of intelligence is used. It is convenient to put the plotted values of the physical character in each case along the centroid value of the frequency of the corresponding grade.

In the Cambridge graduates the median ability lies fairly closely on the boundary between third class honours and pass degrees. In the school children the median division is closely in girls, and less closely but still approximately in boys, between the intelligent and slow intelligent groups. The following, indeed, will be found to give roughly the equivalent grading:

This equivalence of grouping is a fairly satisfactory result, but it suggests that, in future, it would be better to break up the intelligent class into two sub-groups, and to differentiate further those who take pass degrees. We might then form the following scale of intelligence:

- (α) Specially Able, (β) Capable, (γ) Intelligent, (δ) Slow Intelligent, (ϵ) Slow, (ζ) Slow Dull, (η) Very Dull and Mentally Defective. The first three groups would then correspond approximately to first, second, and third class school and University honours*.
- * To the teacher trained by many generations of pupils these divisions will provide almost unconsciously an appreciation of classes. For those who have not this experience it is difficult but necessary to attempt a verbal description. The following definitions are based on those provided in the schedules for the inquiry as to school children, and for a further research on adults in progress.
- (a) Specially Able: a mind especially bright and quick both in perception and reasoning about not only customary but novel facts. Able and accustomed to reason rightly about things on pure self-initiative.
- (β) Capable: a mind less likely than the specially able to originate inquiry, but quick in perception and in reasoning rightly about the perceived.
- (γ) Intelligent: a mind ready to grasp and capable of perceiving facts in most fields. Capable of good reasoning with a moderate effort.
- (δ) Slow Intelligent: a mind slow generally, although possibly more rapid in certain fields, but quite sure of knowledge once acquired.
- (ϵ) Slow: a mind advancing in general, but very slowly; with time and considerable effort not incapable of progress.
- (ξ) Slow Dull: a mind capable of perceiving relationship between facts in some few fields with long and continuous effort, but not generally, or without external aid.
- (η) Very Dull: a mind capable of holding only the simplest facts, and incapable of grasping or reasoning about the relationship between facts; the very dull group covers but extends somewhat further up than the mentally defective.

If we pass to the quantitative measurement of these groups, we may compare them either (i) by equivalence of variability, or (ii) by equivalence of class.

These two methods of approaching the matter are indicated in Tables I and II.

If we take σ_i the standard deviation of intelligence as unit, we obtain the three scales given in Table I, and we see that the scale differs somewhat for girls, boys, and men.

TABLE I. Relative Scales of Intelligence with the Standard Deviation σ_i as Unit.

Class	School Girls	School Boys	Graduates	Class
Median Individual downwards	$007\sigma_i$ below top of Slow Intelligent Group	$^{\circ}113\sigma_{i}$ below top of Slow Intelligent Group	$046\sigma_i$ above bottom of 3rd Class	Median Individual downwards
Median Individual upwards	$^{\circ}853\sigma_{i}$ above bottom of Slow Intelligent Group	$^{\cdot 733\sigma_{i}}$ above bottom of Slow Intelligent Group	$^{\cdot 436\sigma_{i}}$ below top of 3rd Class	Median Individual upwards
Range of Slow Intelligent	$^\circ 860 \sigma_i$	$\cdot 846\sigma_i$		
Range of Slow	$\cdot 642 \sigma_i$	$^{\circ}722\sigma_{i}$	From $046\sigma_i$ below median	Range of Pass
Range of Slow Dull	$^{\circ}640\sigma_{i}$	$\cdot 725\sigma_i$	to ∞	Degrees
Range of Very Dull	From $2.135\sigma_i$ below median to ∞	From $2.180\sigma_i$ below median to ∞)	
Range of Intelligent	$1.033\sigma_i$	$1.108\sigma_i$	$1.077\sigma_i \begin{cases} .482\sigma_i \\ .595\sigma_i \end{cases}$	Range of 3rd Class Range of 2nd Class
Range of Quick Intelligent	From $1.040\sigma_i$ above median to ∞	From $1.221\sigma_i$ above median to ∞	From $1.031\sigma_i$ above median to ∞	Range of 1st Class

The divergence, however, is probably not wholly due to a difference of variability. The bulk of the girls were observed by women-teachers, and of the boys by men-teachers, while the estimate of the graduates was formed in a wholly different manner, namely, by examination tests. Apart from this, women and men are not equally variable in any actually measurable character, and there is no reason to suppose they are necessarily so in intelligence. I have therefore rearranged the scales on the assumption that our common unit is the "Intelligent" group, and that this is the same for boys and girls and equal to the range of the

third and second classes of graduates. Table II exhibits this result, and Fig. 1 gives the corresponding scales.

TABLE II.

Relative Scales of Intelligence with the range of "Intelligent" taken as Unity.

Class	School Girls	School Boys	Graduates	Class
Median Individual downwards	·007 below top of Slow Intelligent Group	·102 below top of Slow Intelligent Group	·043 above bottom of 3rd Class	Median Individual downwards
Median Individual upwards	·826 above bottom of Slow Intelligent Group	'662 above bottom of Slow Intelligent Group	'405 below top of 3rd Class	Median Individual upwards
Range of Slow Intelligent	.833	·764		
Range of Slow	*622	.652	From '043 from median to ∞	Range of Pass
Range of Slow Dull	·620	*654	median to ∞	Degrees
Range of Very Dull	From 2.066 below median to ∞	From 1.967 below median to ∞		
Range of Intelligent	1.000	1.000	1.000 {.448	Range of 3rd Class Range of 2nd Class
Range of Quick Intelligent	From 1.007 above median to ∞	From 1·102 above median to ∞	From '957 above median to ∞	Range of 1st Class

Thus, as we might have anticipated, to suppose the intelligent to give unit range on the intellectual standard provides us with far more concordant results than estimating the variability to be the same for boys, girls, and graduates. In fact, an examination of Fig. 1 shows for this sort of enquiry surprisingly close results. It is clear that the median character is very close to the frontier between slow intelligence and intelligence, or between honours and pass in the Cambridge academic standard. There is clearly a little shifting of the boundaries of the "dull group" between boys and girls, but the mean values of the limits may well be taken as within the limits of the probable error.

After much consideration, I would tentatively suggest the following scale of intelligence:

I divide the range of the "Intelligent" into a hundred units, which I propose to term *mentaces*. It is clear that we can have no absolute measure of the intelli-

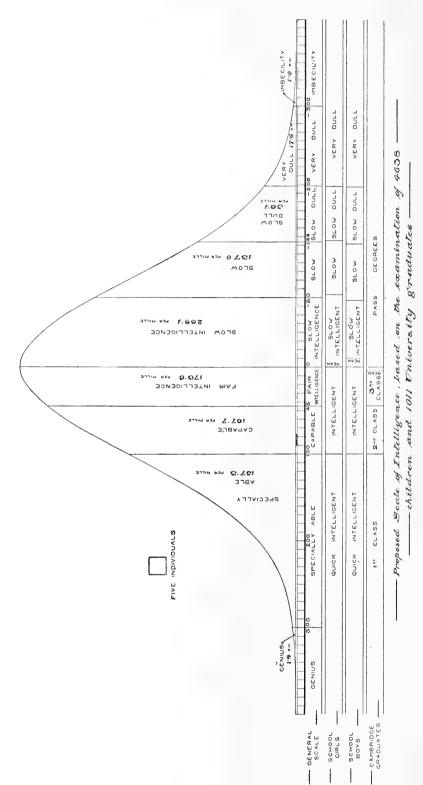


Fig. 1. The scale immediately under the normal curve is the scale of mentaces.

gence of the median individual*, hence intellectual grades will be measured by a plus or minus number of mentaces above the median. The median individual must be looked upon as one whom, if a child, an experienced teacher would hesitate to class in the intelligent or slow intelligent groups, or who would be considered a doubtful honours candidate at Cambridge. Clearly 100 mentaces is not far from the standard deviation of intellectual power in man†.

The following is the suggested classification:

- (i) Genius[†], more than + 300 mentaces. This corresponds to individuals of more than three times the standard deviation from the mean.
- (ii) Specially Able, +100 to +300 mentaces. This corresponds to quick intelligent children and first class University honours.
- (iii) Capable, + 45 to + 100 mentaces. This corresponds to second class University honours.
- (iv) Fair Intelligence, +0 to +45 mentaces. This corresponds to third class University honours. Groups (iii) and (iv) cover the ground occupied by the school teacher's classification of "intelligent," and comprise about one-third of the total population.
 - (v) Slow Intelligent, -0 to -80 mentaces.
 - (vi) Slow, -80 to -144 mentaces.
 - (vii) Slow Dull, -144 to -208 mentaces.
- (viii) Very Dull, -208 to -300 mentaces. This group passes into the mentally defective. Groups (v) to (viii) occupy the range corresponding to pass men from the academic standpoint.
 - (ix) Imbecile, less than -300 mentaces.

We may look upon the whole scheme from another standpoint, corresponding more closely to Francis Galton's decile arrangement, though unfortunately we can only *a posteriori* determine our class indices, and cannot make them suitable round numbers.

Taking 1000 individuals and arranging them in intellectual order: The first, one man in a thousand, would be a genius, then follow 157 specially able men, next 168 capable men, then 174 of fair intelligence; this covers the 50 per cent. above the average. Below the average we have first 288 of the slow intelligent type, then 137 slow persons, next 56 slow dull, followed by 18 very dull including mentally defective individuals, and finishing with one imbecile; thus completing the 50 per cent. with less than average intelligence.

This scale is represented in the upper part of Fig. 1.

- * He can hardly have more than 350 to 400 mentaces, for at a negative position of -350 to -400 on the scale we have passed through the very dull group into imbecility and complete absence of reasoning power. The child whose low grade of intelligence occurs only 3 or 4 times in 100,000 cases, must be sought in the idiot asylum.
- † The standard deviation of school girls is 96.8 mentaces, of school boys 90.3, and of graduate males 92.9, or an average of 93.3 mentaces. The females thus appear more variable than the males in intelligence.
 - # This is of course, purely arbitrary, the simple quantitative idea of "one man in a thousand."

Naturally I do not insist on any particular part of this scale. The numbers are entirely round numbers, and are based on the "normal" distribution of the frequency of intelligence. Still, it is deduced from three series covering the classification of between 4000 and 5000 cases, and the three separate results are in general accord. It will, I think, be possibly useful for other enquirers, and it endeavours to give quantitative expression to our verbal definitions of the intellectual categories. One or two points are suggestive. While the specially able men, the first class in academic judgment, are fewer than either the capable men or the fairly intelligent men, they cover a range double the extent of that of both these two classes added together. In other words, the differences among the specially able are far more marked than in the case of "intelligent" men. This is of course a universal experience, but it is of interest to see its approximate quantitative value.

In the same way the Very Dull minds, although only one-third as numerous as the Slow Dull, and hardly more than one-eighth of the Slow minds, yet occupy a range 50 per cent. greater than that of either of these groups. Thus we see again the source of the great differences in mental stupidity. The apparent want of continuity in the ranges of genius or of imbecility, which must arise when few individuals are spread over a large range, thus enables us to comprehend how it is possible to look upon these things as anomalies and mutations*.

(3) On the Relation of Intelligence to Age.

On the hypothesis that intelligence is very sensibly correlated with either brain-weight or head-size, we might not unnaturally anticipate that growth, which modifies largely the physical characters, would influence the intellectual. It seemed of importance accordingly to enter very fully into the relationship of age to intelligence. Unfortunately the material provided by the Cambridge graduates does not lend itself to an age investigation. It is true that we have the ages provided, but the material consists in great bulk of young men measured in their 19th or 20th years. A certain number of resident "dons" are available in the Cambridge Anthropometric Committee's material, but this group of older men is a stringently selected group, only the men of considerable intellectual achievement from the academic standpoint remaining in residence. Neither in the Cambridge data nor elsewhere did it seem possible to find the material requisite to settle the problem of the relationship of intelligence to age in adults. We are forced, therefore, to confine our attention to the influence of age on general intelligence in childhood.

^{*} For the actual quantitative treatment of this form of discontinuity, see Biometrika, Vol. 1. pp. 385-399.

⁺ When is the intellectual 'prime' in man? His prime in stature is about 27; his prime in head measurements probably two or three years earlier; his prime in brainweight in the teens and probably early in the teens. We know how many inches of stature, how many mm. in head diameters and how many grs. in brainweight he loses yearly after his physical primes. How many mentaces does he lose each year after his intellectual prime? We have no knowledge at present. Yet these very sensible changes which follow physically after the different primes are of the same magnitude as those differences between individuals upon which relations between intelligence and physique are based; they are, however, tacitly put on one side by writers on this subject.

Table III gives the age and intelligence grade for schoolboys; Table IV the same characters for girls.

TABLE III.

Age and Intelligence. Boys.

Age	Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
4	1	2	1	2			6
4 5	2	5	5	4	1		17
6	6	12	15	4	3		40
7	19	25	25	4	6	4	83
8	20	60	39	30	7		156
9	24	57	60	34.5	7.5	6	189
10	33	76.5	72.5	35	21	2	240
11	35	96.5	105	42.5	11	5	295
12	39	110	120.5	51	12.5	3	336
13	27	107.5	108.5	57.5	25.5	11	337
14	29	84	70	39.5	16	3.2	242
15	16	66.5	68.5	19	16	2	188
16	14	39	43	28	9	2 3	135
17	9	24	24	8	4	3	72
18	3	16.5	11.5	8		_	39
19	2.5	5.5	2	2		_	12
20	_	1	2	-			2
	200 5				-		
Cotals	279.5	788	771.5	369	139.5	41.5	2389

TABLE IV.

Age and Intelligence. Girls.

Age	Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
3	_	1	_	_		_	1
4	1	5			<u> </u>	_	6
4 5	$\frac{4}{7}$	5	9	1			19
6	7	13	14	4	3	_	41
7	16	27	20	6 .	6	2	77
8 9	20	40	33	15	4 7	2 2	114
9	20	74	61	22	7	2	186
10	27	91	69	23	9	3	222
11 1	38	106.5	90.5	23	10	4	272
12	44	106.5	84.5	36	18	5	294
13	38	93	80	40	10	3	264
14	32.5	64	60	29.5	13	4	203
15	22	64.5	75	33.5	13	7	215
16	19	48	54	27	7	4	159
17	18.5	34.5	21	8	8	2	92
18	14	20.5	14.5	10	5	1	65
19	2	3	4	3		_	12
20	1	1	3	$\frac{3}{2}$			7
rotals [324	797.5	692.5	283	113	39	2249

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From these Tables the following constants were calculated:

TABLE V.

Variability and Mean Ages of Mental Groups.

Group		GIRLS		
oronp	Mean Age	Standard Deviation	Mean Age	Standard Deviation
Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	12·01 12·48 12·49 12·46 12·52 12·50	$ \begin{array}{c c} 2.964 \\ 2.872 \\ 2.766 \\ 2.833 \\ 2.755 \\ 2.764 \end{array} $ $ \begin{array}{c} 2.867 \\ 2.873 \\ 2.784 \\ 2.764 \end{array} $	12·67 12·45 12·64 13·17 13·03 13·27	$ \begin{array}{c c} 3 \cdot 214 \\ 2 \cdot 978 \\ 2 \cdot 985 \\ 2 \cdot 970 \\ 3 \cdot 077 \\ 2 \cdot 878 \end{array} $ $ \begin{array}{c c} 3 \cdot 059 \\ 2 \cdot 975 \\ 2 \cdot 975 \\ 2 \cdot 878 \end{array} $
Whole Population	12·43 yrs	2·839 yrs	12.67 yrs	3·028 yrs

Examining the means of each intelligence grade first, and taking the boys to start with, we note: That if we omit the quick intelligent group, the mean ages of each intelligence group are essentially the same. With the girls, dullness seems to increase somewhat with age. If we examine the broken vertical lines Fig. 2, we can see, I think, a differentiation between boys and girls; the duller girls have a greater average age. Now the lesser age of the Quick Intelligent boys is, I think, due to the fact that bright children are allowed to go to school rather sooner than dull. But the differentiation between boys and girls is most probably due to the fact that the elder girls, 13 to 15, are commencing a period of life when physical demands upon them introduce very often a temporary and protective intellectual inertia. In the case of boys and girls, the influence of age on the extreme grades of intelligence scarcely amounts to six months at the most; and if we consider the facts that bright children go early to school, and leave early, while dull children go late and leave late, and again that the elder girls are especially apt to feel intellectually the burden of physical development, I think we may safely assert that there is no substantial change of intelligence with age.

The actual correlation ratios are:

for boys: $\eta = .054 \pm .014$; for girls: $\eta = .081 \pm .014$;

and these mark a sensible, but extremely slight, *decrease* of intelligence with age. This decrease is explicable on the grounds just referred to.

We may consider here whether intelligence or dullness is the more scattered character. Turning to the columns of standard deviations, we notice: That for both girls and boys the maximum variability falls to the group of quick intelligence. This is probably due to the fact already noted, that the group is not so homogeneous as the other groups, containing a larger proportion of very able children sent young to school.



Fig. 2.

Taken as a whole, the intelligent group for both sexes appears to be more variable in age than the dull group; but the differences are too slight to be given much weight. If we leave out the quick intelligent group, the difference still appears, but is extremely slight*. We can only say that there possibly exists a small physical tendency for dullness to be concentrated more than intelligence on certain years of childhood.

The matter of change of intelligence with age is so important that I have approached it from another standpoint. I have enquired what is the average intelligence at each age, instead of what is the average age of each grade of intelligence. This might seem the more reasonable method of approaching the problem. But the first method, since age is quantitative, admits of direct determination of the means of the arrays; in the second method we can only find the mean intelligence of each age group by assuming the previously discussed "normal" scale of intelligence. Still the matter is of such interest that it is worth reconsidering from this standpoint. I have accordingly determined the mean intelligence of each age group. This was done as follows: The ratio in which the mean divided the groups Intelligent and Slow Intelligent taken together was determined for each array on the basis of a normal distribution of intelligence. This group covers on our scale a range of 180 mentaces. We are thus able to give the deviation from mediocrity of each age array in mentaces. This is exhibited in the following table:

TABLE VI.

Influence of Age on Intelligence in School Children.

	Boys		GIRLS	
Age Group	Division of Intelligent + Slow Intelligent Range into two parts in ratio	Mentaces from zero of standard scale	Division of Intelli- gent + Slow Intelligent Range	Mentaces from zero of standard scale
3— 7 8— 9	50 to 50 62 to 38	-10 -12	46 to 54 54 to 46	+17 + 3
10—11 12—13	59 to 41 65 to 35	$-6 \\ -17$	51 to 49 56 to 44	+ 8
1415	62 to 38	-12	61 to 39	-10
1617	66 to 34 59 to 41	- 19 - 6	57 to 43 55 to 45	- 3 + 1
General Population	62 to 38	-12	55 to 45	+ 1

Supposing we take 350 to 400 mentaces as the full mental equipment of the average individual (see foot-note, p. 111), it will be clear that these age variations are comparatively slight. It will not, however, do to consider them solely as variations of no account due to the chance deviations of random sampling.

^{*} Boys: Intelligent 2·819, Dull 2·784; Girls: Intelligent 2·982, Dull 2·975.

Random sampling irregularities obscure the results, but there is a fundamental resemblance between the variations in boys and girls which does not allow of our attributing the results wholly to such irregularities. We see that both boys and girls start with greater ability in infancy; their ability then falls between the ages 8 to 9—a period possibly when teeth troubles are more marked; it rises again from 10 to 11 in both cases, but only to make a more exaggerated dip from the ages 12 to 17 during oncoming puberty. After this the tendency is to steadily rise, probably more steeply in men than in women, although the influence of oncoming puberty seems more prolonged in boys than girls. Diagrammatically both sexes combined give a result of the following kind, where the deviations are measured from the mean of each sex (Fig. 3).

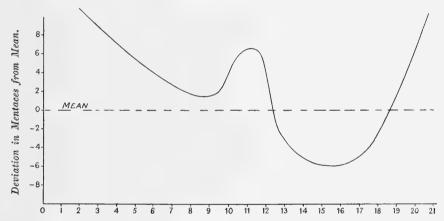


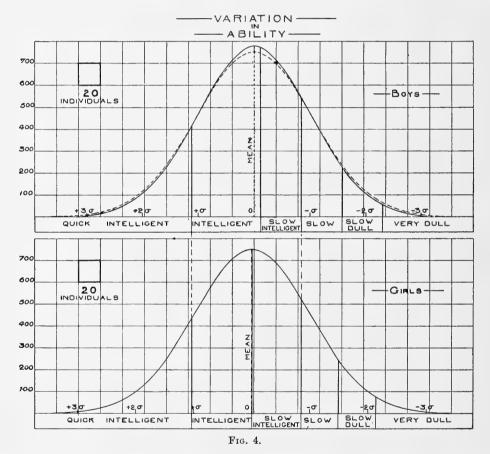
Fig. 3. Rough Diagrammatic Representation of Change of Intelligence with Age.

Now it must be noted that these variations in intelligence are very slight as compared with the total mental outfit of the average individual, perhaps 2 p.c. in boys and 4 p.c. in girls. Generally we must conclude that while there are sensible slight variations in intelligence with growth, these variations are such that they do not affect broad statements based on a consideration of the intelligence-classes of children at different ages, i.e. while the physical characters are rapidly altering and are so highly correlated with age that it is absolutely necessary to allow for this change, the mental characters are far more stationary, the changes which take place in them are by no means always in one direction, and are associated rather with growth difficulties at various stages than with a uniform development with age. Of course in any such considerations as these, we must take, as I have endeavoured to do, a scale of intelligence which is not based on a test of knowledge or training applied to children of all ages without regard to the length of their school career.

The points discussed in this section are illustrated graphically in Fig. 2. The vertical scale is one of intelligence, the horizontal one of age. The upper part of the diagram gives the results for girls, the lower for boys. The upper approximately vertical broken line shows that the duller girls are on the average

slightly older; the lower approximately vertical broken line shows that age is very little dependent on the mental class in boys, when we exclude the very intelligent group. The approximately horizontal broken lines show the direct influence of age on intelligence. Their close approach to horizontality indicates how slight is the relationship; the variations are extremely small as compared with the whole mental range. But we see the parallelism of the variations in the two sexes; the general changes being shown in an exaggerated diagrammatic manner in Fig. 3.

The general results reached in this section, for example, the correlation ratios, are not dependent on the choice of a normal distribution scale, but that scale enables us to plot our results in a manner which indicates conveniently their graphical validity. A further graphical illustration is given in Fig. 4. Here



the normal curves for the school-boys' and school-girls' intelligence distributions are drawn, the total range of Intelligent + Slow Intelligent is taken as unit and the boys' and girls' distributions placed under each other on this basis. It will be seen from this standpoint that the girls' mean is slightly in excess of the boys', and if the girls' curve be now placed on top of the boys' (dotted curve of upper

diagram), then it falls at the terminals slightly outside it, or very intelligent and very dull girls are more frequent than the corresponding boy classes. This greater relative variability of the girls appears confirmed by a comparison of Table V, where in each intellectual class there is more variety in the girls' than the boys' ages. To further test this, I have drawn up a table of the standard deviations in intelligence of each age group of boys and girls. These standard deviations have been calculated in terms of the Intelligent + Slow Intelligent range as the equivalent of 180 mentaces. Here again the girls appear on the whole slightly more variable.

TABLE VII.

Variation of each Age Group in Ability.

Age	Standard in Me	
Group	Boys	Girls
3— 7	103	95
8-9	99	88
10-11	94	83
12-13	90	95
14-15	89	98
16—17	97	100
18—20	84	119
Mean of 7 groups	93.7	96.9

Personally, I should lay no stress whatever on this difference, except to assert the important point, that no inequality exists between the mental variability of girls and boys. Boys are not more variable intellectually than girls. I have tried the fundamental data by all sorts of processes—not here recorded—and always with the result, that in the mass there is no sensible difference in intellectual variability between boys and girls. But the age classes do seem to indicate a difference in the distribution of this variability. While both sexes fall in variability from the earliest years of life, the girls much more than regain the lost variability by 20; on the other hand, the boys may possibly regain it—if we exclude the 18–20 group as not fairly representing boys of this age, many of whom have left school—yet they do not appear to increase rapidly beyond the infantile variability, as the girls do. The matter is deserving of a further special investigation.

(4) On the Relation of Ability to the Size of the Head.

Having shown that to a first approximation the grade of intelligence as estimated in the school observations is not markedly affected by age, I turn now to the relation between ability and the size of the head. In the case of the

school children, all the measurements were reduced to a standard age of 12 by aid of the average growth curves. The substantial legitimacy of this process is demonstrated by the close agreement of the results with those for the Cambridge graduates. In the Appendix Tables XIV—XXIV give the tabulated measurements. These tables differ from those published in the preliminary papers, in that they no longer give mere fourfold divisions but contingency classifications showing the total distributions of head measurements for each mental grade. The method of reduction used throughout this part of the memoir was that of the correlation ratio η^* .

This ratio η is a true measure of the divergence from independence of the two variables, whatever be the nature of the regression. If the regression be really linear, η passes over into the well-known correlation coefficient. The four-fold tabulation and the discovery of the correlation coefficient were adopted in the preliminary investigations already published.

In the accompanying Table VIII the correlations between shape and size of head are given, and Fig. 5 shows the same results exhibited in a graphical form.

TABLE VIII.

Correlation Ratio between Shape and Size of Head and Ability[‡].

Intelligence and	Cambridge Graduates	School boys at Twelve Years	School girls at Twelve Years
Cephalic Index Length of Head Breadth of Head Auricular Height	$ \begin{array}{c c} (1011) &061 \pm .021 \\ (1011) & .111 \pm .020 \\ (1011) & .097 \pm .021 \\ \hline \end{array} $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

Having regard to the magnitude of the probable errors, it is obvious that:

- (a) The correlations are, with the exception of the cephalic index, in every case uniformly of one sign and sensible.
- (b) They are so small that they are in every case of no service for the purposes of prediction.
- (c) Within the limits of the probable error, the results for adults and for school children are in good agreement. The divergences for each character within the three populations are practically within the limits assigned by the probable error of their differences.

These conclusions are based upon a far larger number of measurements than any hitherto published, and are, I think, convincing as to the small part played by head size in determining the grade of intelligence. I have shown in another

^{*} Drapers' Company Research Memoirs, Biometric Series II. Dulau and Co.

⁺ Phil. Trans. Vol. 195 A, pp. 1-47.

[#] The numbers in brackets give populations dealt with.

paper* that no sensible modification is made in this result if allowance be made for either weight or stature. I shall now proceed to consider the data more in detail.

I shall first inquire what amounts of intelligence can on the average be accounted for by differences in head measurement. The average correlation between head length or head breadth and intelligence is 11; that for auricular height is distinctly lower, and we may leave it out of consideration. The variability σ_i in intelligence for all three classes is somewhat under 100 mentaces. The variability σ in a head measurement is roundly 5 to 6 mms. Hence the regression coefficient = $r_{iH} \sigma_i / \sigma_H = 2$ mentaces per millimetre. Now the intellectual range from the average slow man to the average specially intelligent is (see Fig. 1) at least 200 mentaces, or we should require a difference in head measurement of at least 100 mm. to account for this intellectual difference. Now in adults there is at most two millimetres difference between the head measurements of the average slow and the average especially able classes. In children, for some measurements, the average difference between the Quick Intelligent and the Very Dull may amount to 5, but is more usually 2 to 4. Even if we add together the result of two or three separate measurements, supposed independent, we shall not obtain a difference of more effect than 6 to 10 mm., and this depends upon our neglecting the sensible correlation of head measurements. Thus, at a maximum, size of head might account for 12 to 20 mentaces out of the 350 which separate the mean of the specially able group from the mean of the very dull group. The millimetre which separates the head measurements of the slow boy from that of the intelligent corresponding to 2 mentaces,—or if supposed additive for several measurements, to 6 or 10 at most,-is of no effectiveness or value for purposes of prediction compared with the other causes which lead to an average difference of 120 mentaces. Differences in size of head will not account for at most $\frac{1}{12}$, and probably not as much as $\frac{1}{20}$, of the observed differences of capacity whether between adults or between children.

These results are to some extent exhibited graphically in Figs. 5 and 6. In Fig. 5 we see a drop of about 2 mm. in head length and one of about 1 mm. in head breadth in the Cambridge graduates as we pass from one end of the scale to the other. But the mean head measurement of first class honours men has for length a variability of 5.89 mm., or a quartile of about 4 mm. In other words, while 25 per cent. of able men have head lengths under 191 mm., 25 per cent. of slow men have head lengths over 197 mm. The average specially able man is 195 mm. and the average slow man 193 mm. Or again, some 44 per cent. of very able men have heads smaller than the average slow man and some 44 per cent. of slow men heads larger than the average specially able man. This order of numerical relationship holds for the whole range of the characters dealt with, and in view of it we see how idle it is to assert that head measurements can be of any service in the prediction of intelligence. In the case of Fig. 6, we see that for

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both boys and girls the slow increase of intelligence with size of head is quite sensible, but the variability of each group is such that some 25 per cent. of the dull have larger heads than the very intelligent, and some 25 per cent. of the very intelligent have heads smaller than the dull average. It is again impossible under such conditions to use head size as a basis for judgment as to intelligence. Of course all this is merely stating in other words what is obvious to the biometrician, when he finds a low correlation, but possibly, although I am hardly hopeful, it may help to convince the anatomist and old school anthropologist that head measurements are not of real service as intelligence tests*.

In Table IX are placed the mean and variability of each array of head measurements corresponding to different intelligence groups in the case of the Cambridge graduates. In Table X we have the same data for the school children.

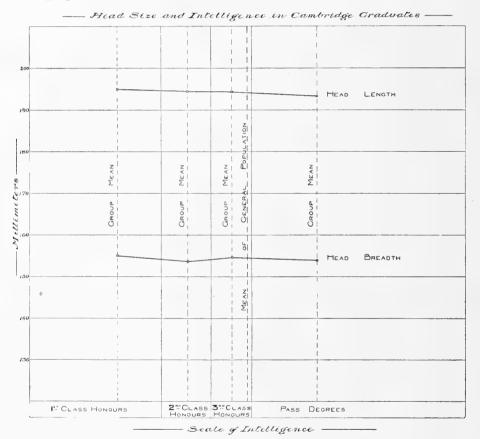


Fig. 5.

^{*} Nurture, exercise and nourishment—shortly environment and class—district or local race, influence extensively the anthropometric measurements. We cannot compare pauper imbeciles or hospital postmortem results with middle class students or professors. We cannot measure agricultural labourers and men of science and point triumphantly to great differences in head volumes as marking widely separate intellectual grades. See the *British Medical Journal*, March 3, p. 536, and March 17, p. 651, 1906.

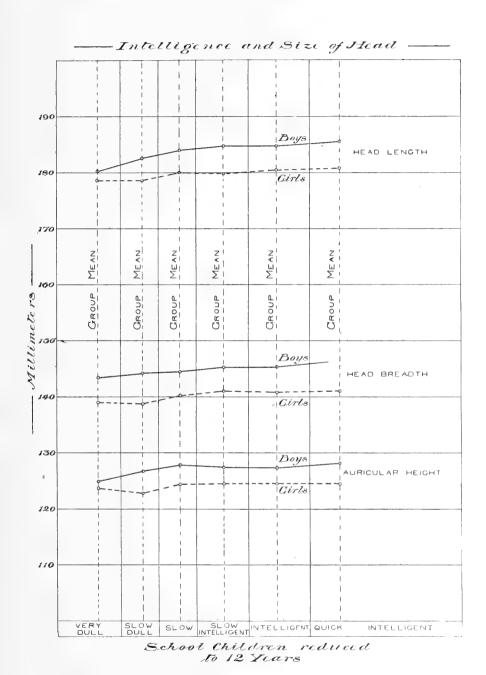


Fig. 6.

TABLE IX.

Cambridge Graduates. Head Measurements.

Grade of Ability	Head	Length	Head	Breadth	Cephal	ic Index
Grade of Ability	Mean	Standard Deviation	Mean	Standard Deviation	Mean	Standard Deviation
Honours, 1st Class " 2nd Class " 3rd Class Poll Men	195·07 194·51 194·38 193·33	5·890 6·026 6·214 6·113	155·07 153·73 154·66 153·95	4·690 4·708 5·247 4·845	79·57 79·22 79·62 79·71	2·995 3·129 3·019 2·827
General Population	194.00	6.121	154.21	4.899	79.58	2.954

The measurements are in mm.

TABLE X.
School Children. Head Measurements at Twelve.

Grade of Ability	Head I	ength	Head B	readth	Auricula	r Height	Cephali	Index
Boys	Mean	S. D.	Mean	S. D.	Mean	S. D.	Mean	S. D.
Quick Intelligent	185.45	6.237	146.40	5.822	128.11	6.418	78.96	3.201
Intelligent	184.70	6.288	145.39	5.814	127:30	6.786	- 78 92	3.360
Slow Intelligent	184.67	6.279	145.31	5.329	127.44	6.519	78.83	3.125
Slow	183.93	6.804	144.45	5.835	127.76	6.619	78.68	3.087
Slow Dull	182.25	7.463	144.23	5.810	126.66	6.467	79.12	3.325
Very Dull	180.19	7.048	143.36	6.023	124.84	6.924	79.48	3.145
General Population	184.44	6.514	145.23	5.700	127.43	6.630	78.88	3.222
Girls								
Quick Intelligent	180.83	5.988	140.97	6.069	124.44	6.800	78.50	3.754
Intelligent	180.35	6.202	140.86	6.337	124.54	6.505	78.43	3.927
Slow Intelligent	179.89	6.305	140.85	6.621	124.52	6.777	78.57	3.861
Slow	179.87	6.517	140.19	6.140	124.40	6.847	78.46	3.800
Slow Dull	178.61	5.962	138.72	6.802	122.86	6.177	77.74	3.871
Very Dull	178.57	6.976	136.55	9.173	123.69	7.232	76.96	4.597
- General Population	180.14	6.260	140.58	6.505	124.40	6.699	78.43	3.885

It is very difficult to draw any definite and safe conclusions from the very irregular distribution of variability. Taking first the Cambridge graduates, we see that the probable error of the standard deviation is in round numbers about '2 for the first three classes and '1 for the poll men in head length; about '15 to '1 for the same groups for head breadth and about '1 for the first three classes and '06 for the poll men in the case of the cephalic index. It is difficult, on the basis of such probable errors, to assert any sensible differences in the class variability. Looking at the series as a whole, we might say with hesitation that possibly 2nd and 3rd class men are more variable in a very slight degree in their head measurements than either brilliant honours men or pass men.

Turning to the school children we again see differences in variability which are often within the probable error of the differences, but occasionally we note considerable divergences. They are difficult to account for, and they do not in any case run parallel with those of the Cambridge graduates. But one general result holds, with two exceptions out of 16 cases, the quick intelligent boys and girls are less variable, and very dull boys and girls more variable than the general population. The exceptions are the very dull boys' cephalic index and the quick intelligent girls' auricular height. Even in the latter case the variability of the very dull girls is sensibly greater than that of the quick intelligent girls. We may therefore say that with a single exception, and that within probable error limits, the quick intelligent are less variable than the very dull. Turning to the Cambridge graduates, we see that with the same exception—cephalic index—the 1st class men are less variable than the poll men. It would accordingly seem probable, that intellectual brilliancy is a more closely selected class than special dullness. Or, perhaps, it would be safer to say that intellectual power is more closely associated with one physical grade than dullness, which is compatible with a wider range of head measurements.

Generally it will be seen, on looking at Tables IX and X or Figs. 5 and 6, that the length of head is more closely associated with intelligence than the breadth, and the breadth than the auricular height. Thus the statement of certain anatomists, that the auricular height is probably the most important head measurement in regard to intelligence is seen to be without statistical basis. The fact that the girls differ from both male children and adults in the nature of the relationship between intelligence and cephalic index is remarkable. I have tested this result in several ways, for example by deducing the intelligence and cephalic index correlations from those of breadth and length with intelligence, but I reach the same conclusion that there is a real change of sign between this correlation for the two sexes, although some methods give the correlation in the girls' case very small and positive, while for the boys it remains between – '04 and – '05.

(5) On the Relationship of Ability to other Physical and Mental Characters.

While the relationship of ability to size and shape of the head has been shown to be very small, it seems worth while to compare it with the values obtained for

the correlation with other physical and mental characters. My school measurements enable results to be obtained for the following series:

Physical Characters Mental Characters Athletic Power Temper Health Popularity Head Length Self-Consciousness Head Breadth Shyness Head Height Conscientiousness Cephalic Index Quiet Habits Hair Colour and the psycho-physical character Eve Colour Handwriting Curliness of Hair Age.

But the method by which the relationship between intelligence and these characters can be best obtained must be varied with the completeness of classification which it is possible to apply. Thus where one quantity, as in the case of the head measurements and age, is quantitative the correlation ratio η has been deter-Where no quantitative measurement is available but a fairly numerous system of classes as in the case of the relation between intelligence and handwriting, health and hair colour, the method of mean square contingency has been adopted*. Even when one of the characters has only a threefold division, as in the cases of temper, curliness of hair and eye colour, the contingency table gave an 18-fold grouping. In the remaining cases with only two alternatives for one character, we were perforce thrown back on the fourfold division table. But even here many tests were made by dividing the intelligence grouping at more than one point. The chief question is whether the slow intelligent shall in the fourfold division be classed with the intelligent or dull groups. In the case of the boys all the fourfold tables were worked out both ways, and the mean taken of the results, but the labour proved excessive and was abandoned in the case of the girls, the division being taken as nearly as possible through the median—which gives the least probable error—i.e. the quick intelligent and intelligent were taken as a single group.

It will be of value to compare some of the results obtained by different methods.

First, we may take as a comparison of correlation ratio and correlation coefficient found by a fourfold table method:

Boys' Breadth of Head and Intelligence $\begin{cases} \text{Correlation Ratio} = \cdot 109 \pm \cdot 014. \\ \text{Correlation Coefficient} = \cdot 084 \pm \cdot 024. \end{cases}$

Next as a comparison of contingency and fourfold method:

 $\mbox{Boys' Handwriting and Intelligence } \left\{ \begin{array}{l} \mbox{Mean Square Contingency} = \cdot 283. \\ \mbox{Correlation Coefficient} = \cdot 312. \end{array} \right.$

A more complete comparison may be taken in the case of temper and intelligence in girls. Here four fourfold tables were worked out; the good-natured

^{*} Drapers' Company Research Memoirs. Biometric Series I. Dulau and Co.

group were put first with the quick and then with the sullen, and the slow intelligent first with the intelligent and then with the slow.

Girls' temper and intelligence.

Correlation Coefficients (a)
$$\cdot 162$$

(b) $\cdot 304$
(c) $\cdot 140$
(d) $\cdot 279$
Mean $\cdot 221$.

Mean Square Contingency = 192.

Thus while the variation in the correlation coefficient shows that the distribution is not normal, the mean of several fourfold tables gives a result of the same order as, indeed, within the limits of the probable errors, equal to that of mean square contingency.

This is, however, rather an extreme example of variation. Take the following as better illustrations of the double grouping of the slow intelligent:

Boys' Intelligence and Conscientiousness.

Fourfold Table: Correlation Coefficient (a) '464. (b) '463.

Boys' Intelligence and Popularity.

Fourfold Table : Correlation Coefficient (a) '233.

(b) ·220.

Thus we have, I think, reached a reasonably close approximation to the intensity of the relationship between the characters dealt with. It is not contended that the numbers obtained are anything more than a first scale of the relationship between intelligence and the other mental and physical characters. But the general accordance between the results for boys and girls is, even so, remarkable, and the whole series in Table XI may serve as a guide for more complete

TABLE XI.

On the Correlation of Ability with Various Mental and Physical Characters.

Character	(Both sexes)	Boys	Girls
Conscientiousness	 •45	*46	•43
Handwriting	 .29	.28	.30
Popularity	 .26	.22	.30
Athletic Power	 .22	.20	.24
Temper	 •21	.19	.22
Health	 .18	.17	•19
Head Length	 -11	.14	•08
Head Breadth	 ·11	·11	.11
Hair Colour	 ·10	.10	.09
Shyness	 ·10	.03	·18
Self-Consciousness	 .07	.10	.03
Eye Colour	 .07	*08	.06
Tead Height	 .06	(07	.05
lge	 .06	.05	-08
Quiet Habits	 -06	.04	.09
Tair Set	 .06	.04	-09
Cephalic Index		- ·04	.07

future investigations on special characters. Judging the series as a whole, it seems impossible to use any of the physical measurements to estimate intelligence from. Hair colour is practically as good as head length or breadth, and eye colour as good as auricular height, and even all these are more important than the age influence. Health and temper have more relation to intelligence than any of the physical measurements we have made, while the intelligent child is athletic, popular and above all markedly conscientious. Handwriting is doubly as good a test of intelligence as any head measurement. If it be argued that this is merely a schoolmaster's measure of intelligence, then the reply must be that this remains to be proved*. If good handwriting be the schoolmaster's standard of intelligence, it appears also to be-as will be shown on another occasion-his standard of health and popularity. For handwriting, we find, is fairly closely correlated with a number of mental and physical characters. It is interesting to observe that, as far as our data go, the handwriting character-readers ought to be able to predict more closely than the anthropometers not only the amount of intelligence in an individual but also his grade in a variety of other mental and moral characters!

Looked at broadly our table seems to justify fully current common-sense methods of estimating intelligence. Give weight to health, temper, physique, popularity, handwriting and above all conscientiousness, in seeking friend, assistant or servant, and in doing this you will most probably obtain intelligence also. If you wish to take anthropometric characters into account—and they are not worth much—hair and eye colour will be as valuable as head measurements, and you need not produce the callipers in order to observe them! I am not denying that in the future other anthropometric characters may possibly be discovered which will be found to be more closely correlated with intelligence. By all means let them be sought for and investigated biometrically; let all types of head measurements and indices be taken and correlated with ability and achievement; it is worth doing even if it leads to purely negative results. But let us hesitate on the ground of slender, or worse than slender, unscientific evidence to proclaim close association between intelligence and external physical measurements +. So far there is nothing to encourage belief in such association; and if we are consistent and apply any of the dogmatic views currently held to the problem of interracial

^{*} As far as the non-expert can judge, the classification of the handwritings is a fair one. It is proposed to place the 5000—6000 specimens of handwriting with the ages of the children before an expert and obtain his classification of the whole material.

[†] Some years ago I was struck by the widespread medical opinion that mentally defective children have peculiarly shaped palates. I asked an exponent of this view for the statistics bearing upon the subject, but I could not find that there had ever been a thorough study of the palate in mentally normal children. In the American Journal of Insanity, Vol. Lxi. pp. 687—697 will be found a preliminary report of Drs Walter Channing and Clark Wissler: "Comparative Measurements of the Hard Palate in Normal and Feeble-Minded Individuals." They show biometrically that "the absolute size of the palate as measured by the three specified dimensions [height, length and breadth from casts] seems to be the same for feeble-minded and normal individuals," p. 695. It is most unfortunate that quantitative tests so rarely precede the spread and acceptance of very dogmatic opinions in a certain section of the medical profession.

intelligence, we are led to very remarkable conclusions! I do not propose to discuss this point on the present occasion, nor am I urging the view that the material I now put before the reader for his judgment is to be considered final. I think, however, that it has far more weight than some recent criticisms would admit it to have*. Perhaps, only one who was in continual communication with the collaborators during the measurements and observations can appreciate the conscientious care given to the task, and he alone can estimate the value of the preliminary trials and later tests which were made of the categories and measurements.

In regard to the association of mental and physical characters, the correlation coefficient may in certain cases screen relationships which are more emphasised by examining the material from other standpoints. I have already pointed out how the correlation ratio and the coefficient of contingency help us in this matter. The regression may indeed not be linear, or there may be, as in the case of hair colour, no scale arrangement beyond criticism. For such cases I have found the old idea of percentages not without value. In the case of intelligence, I take a normal scale as my base line and plot up the percentage of the character for each grade of intelligence along the centroid vertical of the corresponding range, drawing a horizontal line to represent the mean percentage in the population at large. We thus obtain a diagram, which I will venture to term an analograph †.

If the percentage increases or decreases continually with intelligence (or with the base character, whatever it may be), I term the relationship homoclinal; if the percentage does not reach its maximum with the maximum or minimum of intelligence, I term the diagram heteroclinal. There may of course be more than one maximum in heteroclinal analographs; the difficulty will be to distinguish true percentage maxima from the 'peaks' due to random sampling. They can, however, be tested in any particular case by the probable errors of the percentages. The advantages of this rough percentage method are: (i) that it enables us to see relationships of a heteroclinal nature, which are screened by a fourfold table method of finding correlation—especially in those cases where neither a correlation ratio nor a coefficient of contingency is calculable on the available data, e.g. in the case of alternative psychical characters, such as noisiness and quietness; and (ii) that it provides a graphic method—more impressive to some minds than any numerical representation—available in cases where it is quite impossible to construct a regression curve.

I propose to deal with the relation of intelligence to other psychical and to non-measurable physical characters in this manner. The data upon which the analographs are based have been collected in Table XII for boys and Table XIII for girls. The small number of children recorded as *Very Dull* leads to a large probable error in the percentages of this category. I have accordingly classed the

^{*} A reply to the criticisms of G. U. Yule will shortly be published.

[†] ἀνάλογον + γράφω, the former from Euclid, Book V., and the contraction is tolerable as in ἀμφορεύs.

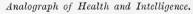
TABLE XII. Percentage Changes in Boys' Characteristics.
Intellectual Grade.

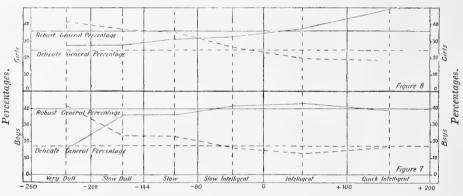
				ctual G	200001			
		Q. I.	I.	S. I.	S.	S. D.	V. D.	Totals
Eye Colour								
Light		41.41	40.28	36.00	36:34	45.74 (42.7 3	32.91	38.59
Medium		40.27	37.28	42.14	42.03	29.84 (34.72		39.76
Dark		18:32	22.44	21.86	21.62	24.42 (22.5		21.65
——————————————————————————————————————								
~		82.98	83.49	05.05	82:31	04.20 (94.4)	4) 84·62	83.89
Smooth Wavy		13.20	13.04	85·25 11·05	14.40	84·39 (84·44 12·64 (12·68	3) 12·82	12.63
Curly		3.52	3.47	3.70	3.29	2.97 (2.88		3.48
Health								
		80.00	1001		2 00	07 10 (00 5)	2) == 0.4	00.00
Robust		38.82	42.34	41.16	35.90		9) 15.24	39.68
Normally Healt Delicate		$\frac{44.36}{16.82}$	44.66 13.00	42.65	40.95	41.36 (41.8) 23.16 (27.40		43.20
Delicate	•••	10.82	13.00	16.19	23.15	23.16 (27.46	0) 41.47	17.11
Hair Colour								
Red		2.66	3.53	4.74	3.43	1.65 (3.5)	7) 8.51	3.82
Fair	***	39.54	35.79	32.50	36.79	33.68 (31.46	0) 25.53	34.96
Brown		31.56	30.12	33.94	36.05	37.81 (37.9)		33.05
Dark	•••	26.24	30.56	28.82	23.73	26.86 (27.08	8) 27.66	28.20
Conscientiousness								
Keen		89.90	79.67	64.15	46.41	37.79 (36.4	5) 31.76	67.24
Dull		10.10	20.33	35.85	53.59	62.21 (63.5		32.76
CII.		50.50	F0.10	F0.40	50.50	F0-00 /F0-4	0) 01.04	#0.00
Shy Self-Assertive		58.52 41.48	59·19 40·81	58·48 41·52	58·72 41·28	58.86 (59.4) 41.14 (40.5)		58.82 41.18
			40 01	41 02		41 14 (40 0		
Self-Conscious		54.42	48.98	50.45	45.04	33.03 (34.3		48.27
Unself-Consciou	ıs	45.58	51.02	49.55	54.96	66.97 (65.6	4) 60.56	51.73
Noisy		30.82	36.32	34.71	37.59	39.34 (38.8	9) 37:35	35.48
Quiet		69.18	63.68	65.29	62.41	60.66 (61.1		64.52
D		00-0*	04-20	70.47	HE: 47	61.06 /60.0	0) 67.07	00.53
Popular Unpopular	• • • •	89·65 10· 3 5	84·38 15·62	79·47 20·53	75·47 24·53	61.06 (62.2 38.94 (37.7		80.51
TT	_		-		1			
Handwriting		00.70	40.00	90.00	20 = 1	24-41 (01.0	4) 11.00	47.0
Good	• • •	63.16	48.32	36.20	29.74	24·41 (21·0 48·12 (48·7		41.07
Moderate Bad	• • • •	30·89 5·95	39.50	44·31 19·49	42:00 28:26	27·47 (30·1		$41.21 \\ 17.72$
Bad	***		12.18	10 40	20 20	21 41 (50 1	1) 51 00	11 12
Temper								
Quick	***	21.07	20.56	19.32	12:39	14.89 (15.0		18.46
Goodnatured		74.38	71.89	67.84	68.59	55.75 (53.0		68.88
Sullen	•••	4.55	7.55	12.84	19.02	29.36 (31.9	5) 39·74	12.66
			T 2.00	05.45	01.41	47.71.415.0	G) 44.44	67.21
Athletic		77.62	72.09	65.47	61.41	45.51 (45.2)	0) 44-44	() / //

		_	~ -				
	Q. I.	I.	S. I.	S.	S. D.	V. D.	Total
Eye Colour	-						
* * * * .	. 36:31	34.82	32.04	33.33	36.28 (35.	48) 33:33	34.09
M . 1'	45.00	42:37	45.08	42.61	43.36 (42.		43.7
Dark		22.81	22.88	24.06	20.36 (22.		22.17
Dark			22 00	24 00	20 90 (22	20) 21 00	221
Hair Set					1		
Smooth	. 62.32	64.25	66.77	66.10	64.86 (65.	10) 65·79	65.01
Wavy	. 28.26	25.14	23.25	19.89	18.02 (17.	45) 15.79	23.83
Curly	. 9.42	10.61	9.98	14.01	17.12 (17.	45) 18·42	11.16
Health							
D -1	. 49.70	36.41	32.88	31.18	27.68 (27.	74) 27·91	36.0-
Normally Healthy	31.72	43.70	40.86	33.80	35.27 (33.		39.17
Delicate	10.50	19.89	26.26	35.02	37.05 (38.		24.79
II							
$egin{array}{ll} Hair\ Colour & \dots & \dots & \dots \end{array}$	6.14	3.99	3.36	2.15	3.69 (3.	99) 4.76	3.88
Fair	00.01	34.32	38.09	34.79	37.33 (38.		36.48
Brown	DE 0E	39.47	35.34	41.95	36.63 (36.		38:02
Dark	7 M - F O	22.22	23.21	21.11	22.35 (20.		21.63
Conscientiousness							
	0.0.2.2	00.00	00.00	F F O 7	20.22 /22	0E) 00 ===	F O (1)
Keen	10.05	83.62	68.69	55.21		05) 28·75	72.85
Dull	. 13.85	16.38	31.31	44.79	60.67 (63.	95) 71.25	27.15
Shy	48.52	62.42	70.02	72.24	63:37 (61:3	35) 56.25	64.01
Self-Assertive	F 7 40	37.58	29.98	27.76	36.33 (38.		35.99
	_						-
Self-Conscious		48.77	48.62	52.64	54.69 (54.4		49.51
Unself-Conscious	. 51.98	51.23	51.38	47:36	45.31 (45.5	52) 46·05	50.49
Noisy	38.59	32.26	28.10	28.95	30:36 (32:4	04) 36:17	31 49
Quiet	01.41	67.74	71.90	71.05	69.64 (67.5		68.21
Popular		84.70	79.58	67:04	59.55 (53.2		79.59
Unpopular	9.46	15.30	20.42	32.96	40.45 (46.7	(5) 63.24	20.41
Good	59.88	51:39	39.23	26:40	23.47 (22.3	39) 19:44	43.50
Moderate	20.00	36.71	44.62	48.28	43.88 (42.5		39.56
Bad	10.00	11.89	16.15	25.32		07) 41·67	16.94
0 1	9.4+01	20.26	15:65	1.4.1.4	10.93 (11.3	31) 12·65	15.00
0 1 / 1	40.01	20·26 68·78	15.65 69.68	$\frac{14.14}{64.14}$	10.93 (11.3 57.38 (56.2		$17.90 \\ 67.43$
Sullen	= =0	10.96	14.67	21.72		16) 32·53	14.67
Athletic	69.21	62.10	54.06	44.57	36.78 (37.0	07) 37·93	56.71
	30.79						

Slow Dull and Very Dull together and calculated the corresponding percentages in the heavy bracketed figures*.

Health and Intelligence. We see that for both boys and girls we have sensibly homoclinal systems. The robust children among dull and slow children are much below the general percentage, and rise above it for the able children. Conversely the delicate children are below the general percentage on the intelligent side, and rise much above it on the dull side. There is one peculiarity which, I think, is not an irregularity of random sampling, but a sexual difference. Among the Quick Intelligent boys there is a smaller percentage of robust and a larger percentage of delicate than among the Intelligent boys. Thus, while ability is associated with health, a certain number of weakly boys are markedly intelligent. With the girls, on the other hand, the Quick Intelligent have the largest percentage of robust cases. And this is, perhaps, what one would, from the standpoint of national efficiency, prefer—i.e. the closest association of strength and intelligence. A further sexual difference is that the percentage of robust girls is smaller and the percentage of delicate girls is larger than in the case of boys.





Scale of Intelligence in Mentaces.

Pigmentation and Intelligence. Both hair and eye colour clearly provide heteroclinal systems, but it is difficult to trace any nomic relationship in either the numbers or the graphs. Thus, while brown-haired boys give a fairly smooth homoclinal graph, showing decreasing percentages with increasing intelligence, there is no corresponding feature in brown-haired girls, the deviation from the

 * The following are sufficiently closely for practical purposes the mean values of each intellectual grade:

Mentally Defectiv	e - 317 :	mentaces.	Fair Intelligence	+ 22	$\mathbf{mentaces.}$
Very Dull	-238	,,	Capable	+ 71	,,
Slow Dull	-170	,,	Specially Able	+151	,,
Slow	-108	,,	Genius	+317	,,
Slow Intelligent	- 38	11			

general percentage being very irregular. Dark-haired children of both sexes have a maximum in the Intelligent to Slow Intelligent, there being fewer than the normal number of both the very able and the very stupid. The analographs for dark boys and girls run very parallel, and I think there can hardly be a doubt that the very dark are not up to the average in either extreme ability or extreme dullness. While the total of brown and dark boys is closely equal to the total of brown and dark girls, there is a sensibly larger percentage of dark boys than girls in these records. The total percentages of red-haired children is strikingly alike for the two sexes. There appears, as far as the slender material enables us to judge, however, a sexual difference in their distribution of intelligence. Disregarding the distinction between Slow Dull and Very Dull, as the numbers are too scanty to use apart, we find that red-haired boys are most numerous among the Slow Intelligent, while red-haired girls have a reversed heteroclisy, being most frequent among the Quick Intelligent or the Very Dull. To some extent these results are confirmed by the data for eye colour; in the case of both boys and girls the Quick Intelligent group contains less than the general percentage of dark-eyed children. The fair children, on the other hand, are in excess in the Quick Intelligent and the total Dull group. Thus light-eyed children have a slight tendency to the extremes and dark to mediocrity.

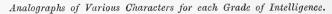
As a whole, while I note some traces of relationship of intelligence to pigmentation, there is not enough to justify any sweeping assertions. While not very hopeful, I think it would be worth while making a much finer classification with actual eye and hair scales; it would be a laborious piece of work, but there is just the indication that it might lead to more definite relationships.

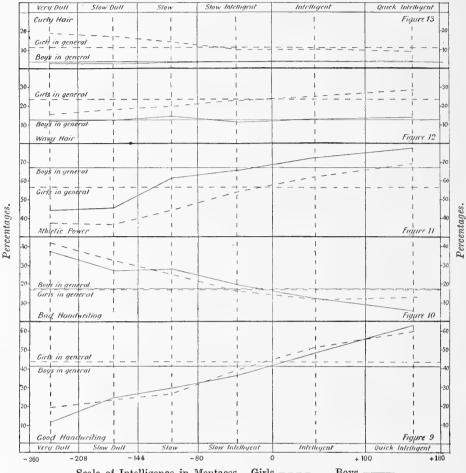
Hair Set. Here again we have some rather marked sexual differences. Curliness in boys decreases as we pass from the intelligent to the dull end of the scale. In girls it is precisely the opposite; curly-haired girls are three times as frequent as curly-haired boys, but the percentage of curly dull girls is twice that of curly and quick intelligent girls. On the other hand, wavy hair, which is heteroclinal for boys, has a well-marked homoclinal analograph for girls, intelligent girls having more frequently wavy hair than dull girls. These points are indicated in Figs. 12 and 13.

I now pass to a series of characteristics which are on the borderland between the psychical and physical—Handwriting, Athletic Power, and Temper—all of which have well-marked homoclinal analographs.

Handwriting. Figs. 9 and 10 indicate how markedly, for both boys and girls, good handwriting decreases and bad handwriting increases with the transition from intelligence to dullness.

Athletic Power. Fig. 11 shows how the percentages of both non-athletic boys and girls are more than doubled as we pass from the quick intelligent to the dull groups. The athletic character in children, at any rate, is markedly associated with intelligence.





Scale of Intelligence in Mentaces. Girls ----. Boys -----

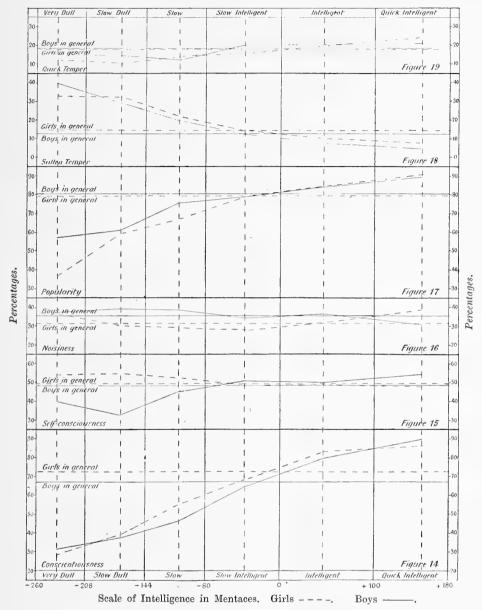
Temper. Fig. 18 indicates the great rise in sullen temper when we turn from intelligence to dullness. If we consider the analographs for Quick Temper (Fig. 19), we see that the ablest children are the most Quick Tempered; but there is a tendency to a heteroclinal system, more marked in boys than girls, the dull having again a tendency to quick temper.

In the more purely psychical alternatives of our observations, there are certain marked relations and certain noteworthy sexual differences.

Conscientiousness. Fig. 14 shows that intelligence is homoclinal to conscientiousness, there being in both sexes a reduction to about a third of the percentage between the very intelligent and very dull classes.

Shyness. This character seems to have no relation to ability in boys; in girls it is sensibly related to slowness, the intelligent and the dull being alike wanting in their due proportion of shyness.

Analographs of Various Characters for each Grade of Intelligence.



Self-consciousness. Here there is a marked sexual difference; while self-consciousness is not closely related to intelligence, still it is the clever boys and the dull girls who are self-conscious in the higher degree: see Fig. 15.

Quiet Habits. The analograph for the girls is heteroclinal, the able and the dull being noisy and the slow being quiet. The relationship is less marked in boys, but the intelligent boys are quieter than the dull boys.

Popularity. While the percentage of popular children is almost exactly the same for both sexes, and the intelligent children are more popular than the dull ones, yet the relationship is more marked in girls than boys: see Fig. 17.

To sum up, then: While no characters in school children so far dealt with show very high correlation with intelligence, we may yet say that the intelligent boy is markedly conscientious, is moderately robust, athletic, and popular; he tends rather to quick than to sullen temper. He is more self-conscious and quieter than the dull boy; he has a *slightly* bigger head, and possibly lighter pigmentation than those of more mediocre intelligence. His hair has a larger percentage of curliness.

The intelligent girl also is markedly conscientious, moderately robust, athletic, and popular. She, too, tends to quick rather than sullen temper. She is less self-conscious than the dull girl, and noisier than the girl of mediocre intelligence. It is the slow girl who is quiet and shy. The intelligent girl has a slightly bigger head than the dull girl, and her hair is more likely to be wavy and much less likely to be curly.

It may possibly be hinted that these results are of little significance, and, had they not been so, they could still have been deduced—without elaborate statistics—from the impressions of a careful and observant teacher. It may be so, but much of science is the verification or refutation of impressions and opinions, and the mainly negative conclusions of this paper place at any rate on a sounder quantitative basis the view that even for the mass, and therefore much more for the individual, little can be judged as to intelligence from the more obvious anthropometric measurements and the more easily noted psychical characteristics of children.

The onus of proof that other measurements and more subtle psychical observations would lead to more definite results may now, I think, be left to those who a priori regard such an association as probable. Personally, the result of the present enquiry has convinced me that there is little relationship between the external physical, and the psychical characters in man. Future papers from my laboratory, while showing certain definite relationships, will serve to confirm this view, as far as the present material is concerned.

In the tables with which this memoir concludes, we have the full classification possible of the raw material. The tables for the three diameters and intelligence in the case of girls are due to my friend Dr M. Greenwood; that for cephalic index and intelligence in Cambridge graduates is due to Miss A. Barrington. The remaining 42 tables are due both in construction and reduction to Dr A. Lee. I have not only to thank her for so much aid, but also to acknowledge heartily the generosity of the Worshipful Company of Drapers, which has rendered it possible for my statistical laboratory to retain the services of such an efficient computator and assistant.

APPENDIX.

A. CAMBRIDGE GRADUATES.

TABLE XIV. Length of Head in inches.

Biometrika v

	6.9	0.2	1.2		7.3	4.2	2.2	9.2	2.2	8.2	6.2	0.8	1.8	8.8	∞ ∴	7.8	8.5	9.8	Totals
1st Class Honours 2nd Class Honours 3rd Class Honours Poll men	67	22 23	00 02 10 10	28 57 29 19	10 8 11 26	10 12 12 48	18 29 31 76	26 39 37 82	29 27 22 85	22 22 26 56	14 19 16 39	11 10 14 17	စဆမာဂ	-1 00 100	1 1 2 7	1		1-11	153 182 189 487
Totals	62	5	17	37	55	82	154	154 184 163	163	126	88	52	29	12	4	1	1	1	1011

Intellectual Grade.

TABLE XV. Breadth of Head in inches.

23 8 3 2 — — 13 5 2 3 — — 16 10 2 5 1 1 50 20 5 4 1 — 102 43 12 14 2 1
23 8 3 2 13 5 2 3 16 10 2 5 4 50 20 5 4 102 43 12 14
23 8 3 13 5 2 16 10 2 50 20 5 102 43 12
23 8 13 5 16 10 50 20
23 13 16 50 102
19 29 29 65 142
40 33 39 105 217
31 47 44 106 228
14 28 22 70 70
9 11 11 40
34 34
1 1 2
03 03
1st Class Honours 2nd Class Honours 3rd Class Honours Poll men

TABLE XVI. Cephalic Index.

Totals	153 182 189 487	1011
92	1	1
16	1111	
90	1 1	2
89	1 1 2	ee
88	5 5	3
87	.5 3 3	œ
98	3.5 2.5 4.5 5.5	16
85	3.5 3.5 3	22
48	9 7 2.5 22.5	41
83	8.5 9 17 35	69.5
83	15 8.5 17 32	72.5
81	12.5 16.5 20.5 57	106.5
80	23 27 26·5 74·5	151
79	24 23 22·5 76·5	146
78	18 28 28 59	133
2.2	$\begin{array}{c c} 11 \\ 21 \cdot 5 \\ 14 \\ 56 \cdot 5 \end{array}$	103
92	10 14 11 22.5	2.19
75	5 7 10 14	36
7.4	6 9	26
73	2.5 5.5 1	10
23	ع ن ^ي ن ^ي	4
	1st Class Honours 2nd Class Honours 3rd Class Honours Poll men	Totals

Intellectual Grade.

SCHOOL CHILDREN. HEAD MEASUREMENTS. REDUCED TO 12 YEARS OF AGE. m.

TABLE XVII.

Boys' Head Length in cms.

Totals	276·5 737 758·5 345·5 137 43·5	2298
9.907-9.407	67	23
9.402-9.202	1	23
g.&0&—g.00&	1 8 2 5 1 1	6.5
\$.00%—\$.86I	4 6 5 5 4 6 7	22.5
\$.86I-\$.96I	5 7.5 16.5 9	38
£.961—£.761	9 20 17.5 12 5.5 1	65
2.761-2.761	14 29 39 9.5 2.5	96
\$.76I_\$.06I	18 54 57·5 26·5 8	165.5
g.06I—g.88I	27 78·75 72·75 31 12·5	223
9.88I-9.98I	44 82·75 83·75 26·5 11	249
g.08I—g.78I	36 96·5 93 33 14·5	274
g.481—g.281	41 111 90·5 53·75 13·75 7·5	317.5
g.781—g.081	21.5 72 88 34.75 11.25	235.5
G-08IG-811	17.5 64 68 27.5 13.5 6	196.5
G-821	16.5 39 47.5 30 10 3.5	146.5
9.921—9.721	9.5 26.5 31 15.5	91.5
2.711-9.211	3.5 13.5 15.5 8 4	29
G-&71 - G-071	4.5 15.5 14.5 5.5 9.5	52
£.021—£.891	1.5 9.5 6 10.5 4	32
9.891—9.991	1.4.1.5.1.1	œ
9.991—9.791	01-1-1-	5
g.†9I—g.z9I	61 =	ಣ
	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	Totals

Intellectual Grade.

TABLE XVIII.

Girls' Head Length in cms.

Totals	316·5 780·5 664·5 276·5 109 41	2188
9.008-9.861	-	1
g.861—g.961	67 - 12 - 1 - 12	8
9.961—9.761	6.5	19.5
9.761—9.261	5.5 10.5 6.5 3 1	27.5
g.@6I—g.06I	9.5 21 10.5 8 1	20
g.061—g.881	10.5 35 23 14.5 1	68
g.881—g.981	17 52°5 57 14 2	146.5
g.981—g.481	31 66°5 51 18 3°5 4	174
g.481—g.781	33 86 73 36 9.5	246.5
g.28I—g.08I	44 98.5 79.5 13	292
G-08I—G-82I	47 107.5 101 33.5 19	309
9.821—9.921	49.5 96.5 76 37 10.5	276.5
9.921—9.72I	24 71 65 28·5 111·5	207.5
g.721—g.221	13 45 35 5 19 5 15 20 5	130.5
9.821-9.021	11.5 35 30 12.5 7.5	97.5
9.02I—9.89I	7.5 20 18 9 2.5	29
9.89I—9.99I	12 12 12 3 3	41.5
9.991—9.791	1 12.5 5 2 1	32.5
9.491-9.291	1.5	4.5
9.291—9.091	1 2.5	4
g.09I—g.89I	1 2 1 1 1 2 1	3.5
	Quick Intelligent Intelligent Slow Intelligent Slow Very Dull Tery	Totals

Intellectual Grade.

Boys' Head Breadth in cms.

Totals	276·5 733·5 762·5 348 135·5 43	2299
2-191-2-691	84411	15
9-691-9-291	984-6	22
g.191—g.191	10 12 10 10 7.5	41.5
g.ggI—g.ggI	10.5 23 27 11 3	2.22
g.ggI—g.IgI	17 56 42.5 16.5 1	140
9.191-9.671	32.5 76 76 28 8.5 3.5	224.5
2.671—2.171	41.5 92.5 108 42 10.5 3.5	298
9-141-9-941	35.5 104 104 47 21 4	315.5
9.541—9.841	40.5 96 104 45 22.5 8	316
9.871-9.171	28 85.5 102.5 47 14 3	280
g.171—g.681	23 76 85.5 36.5 17	243
g-681—g-281	38.55 38.55 11.55 4	126
9-121-9-921	4.5 27 28.5 19 3	68
9.981-9.881	ი 10 10 10 ო ო	52
9.881-9.181		26
9-181-9-681	121 4 22 1	23
9.62I—9.12I	64 85 85 -	6
9.2%1—3.9%1		73
9.9%1-9.8%1		1
g.821—g.121		П
	Quick Intelligent Intelligent Slow Intelligent Slow Oull Very Dull	Totals

Intellectual Grade,

TABLE XX.

	Totals	312 768 664·5 276 105·5 39	2165
	9.29I—9.09I		1
	9.091—9.891	2 2	3.5
	9-89I—9-99I	1.5	3
	9:991—9:491	1.5	9.5
	9.431—9.231	485161	28
1	g.zgI—g.0gI	13 13.5 3.5	39
,	g.0g1—g.8†1	18·5 39·5 33 7·5 3	102.5
	g.87I—g.9 7 I	25 74.5 60 25 6.5	191
	9.941—9.441	34.5 74 70.5 21.5 8	214.5
	9.441—9.241	42.5 1111.5 86.5 24 14.5	2.622
cms.	g.z†Ig.0†I	35 104.5 103 40 13 5.5	301
in	9.07I—9.8EI	32.5 103.5 72.5 50.5 9	273
Breadth	g.881—g.981	43.5 73 60 45.5 17	241
Head I	g.98I—g.78I	22 38°5 45°5 23°5 8°5	138
ls' H	9.781—9.881	18.5 44.5 27.5 8 6 3.5	108
Girls'	9.781-9.081	14 30 30 8 6 6	92.2
	9.081-9.881	6.5 41 5.88 5.88	48
	9.871—9.971	1.5 6.5 9.5 2.5 1	56
	9.971—9.471	1.5	18.5
	9.421-9.221	4004 H	13
	9.221-9.021	8 8 4 81 81 ic io	15
	2.021—2.811	w 4 w	10
	9.811-9.911	1.5	4.5
	9.911-2.711	63 1	ಣ
	9.711—9.211	nt: nt	: 21
		Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	Totals

z—81 Intellectual Grade.

TABLE XXI.

Boys' Auricular Height in cms.

Totals	276 730·5 760·5 346 135·5 41·5	2290
9.141-9.941	1 1	2
9.971—9.871	3 4.5 1 1	15
9.871-9.171	4.5 5 10 4.5 2	97
g.171—g.681	5 22 17·5 8·5	53
9.68I—9.18I	10 22.75 19 12.75 4.5	02
9-LEI-9-9EI	12.5 29.75 31.5 14.75 5.5	95
9.98I—9.88I	14 44 43.5 24 6.5	133
9.881—9.181	23 60 62 34.5 10	193.5
g.181—g.681	31 87.5 449 117 3.5	275
9-621—9-231	43.5 80.5 100.5 31 9.5 6	271
g.121—g.g21	35 94.25 91.75 35 19 4.5	279.5
g.gz1—g.gz1	33.25 76 79.25 40.5 19	254
9.881-9.181	20.75 59.25 75.5 11.5	198.5
9-181-9-611	18.5 55 45.25 21.25 12.5	153.5
9-611—9-211	10.5 39.75 43 19.75 7	121
9-211-9-911	4.5 25.25 28.75 11 6	78.5
2.911—2.811	01 20 20 20 20 20 20 20 20 20 20 20 20 20	31.5
9-811—9-111	24 4 0 2 1 1 2 2 2 2	15.5
g-111—g-601	1 to 4 to 1 to 2 to 2 to 2 to 2 to 2 to 2 to 2	14.5
G-60I-G-20I	1 .5	. 9
9-201-9-901	2.5	3.5
9-901-9-801	ie	÷
	Quick Intelligent Intelligent Slow Intelligent Slow Slow USION Slow USION Slow Dull Very Dull	Totals

Intellectual Grade.

TABLE XXII.

Girls' Auricular Height in cms.

Totals	308·5 768 668·5 277 107 37	2166
9.941-9.841	12821	6
9.841-9.141	02 to 4 to	12
9.171-9.681	8 4 1	21
9.68I-9.28I	2 111.5 111.5 3 -	67
9-281-9-981	10 10 20 20 20 20 20 20 20 20 20 20 20 20 20	39
g.gg1—g.gg1	13 27 37·5 9 2	89.5
9.881—9.181	17 39·5 25 19 3	106.5
9-18I9-67I	21 60 40.5 17.5 5	145
9.681—9.18I	33 74 61.5 32.5 9	212
9.281—9.981	28 90 84 26 16	249
9.981—9.881	47.5 91 82.5 29 13	264
g.881—g.181	31 105·5 89·5 36 11 5	278
9.181—9.611	33.5 91 58.5 40 11 8	242
9-611—9-211	20 65 56 14 10	166
9.211—9.911	14 26.5 36.5 15 10 2	104
g.g11—g.g11	16 29·5 32·5 10 5	95
9.811—9.111	10 12 11 11 6 8	43
g.111—g.601	3 8 8 1	29
G-60I—G-20I	1.5 6.5 8 1	21
G-201—G-901	67 69 69 79	10
9-901-9-801		67
	Auck Intelligent Intelligent Slow Intelligent Slow Intelligent Slow Intelligent Slow Intelligent Slow Intelligent Slow Intelligent Slow Intelligent Intelligent	Totals

Intellectual Grade.

TABLE XXIII.

Boys' Cephalic Index.

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	<u>x</u>	್ಲಿ ಎ	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Total	285° 764 762 353 137° 43	2345
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	16-06		63
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	06-68		ಣ
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	68—88	1 2 2 1 2 5 5	9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	88-78	1:5	9.5
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	28-98	3.5 7 10 4 1	25.5
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	98—98	3 111.5 111.5 5	33
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	28-48	4.5 27.5 16.5 7 2	61.5
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<i>†8–88</i>	15.5 23 31.75 16.25 10	2.16
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	£8—č8	25 50 37·25 16·75 13	146
ntelligent — 1.5 3.5 2 3.5 2 8 11 18.5 37 29 36 31.5 celligent — 1.5 3.5 3.5 29.5 16 8.5 112 86.5 112 80.25 celligent — 1.5 3.5 3.5 8.5 16 80.25 81.7 8.5 10 80.25 and 11 18.5 81.5 10 81.5 112 80.25 and 11 11 18.5 81.5 10 81.5 112 80.25 and 11 11 18.5 81.5 10 81.5 112 80.25 and 11 11 18.5 81.5 81.5 81.5 81.5 81.5 81.	28—I8	30.5 64 56 34 6 3.5	194
ntelligent ————————————————————————————————————	18-08	22.5 80.25 78.25 28.5 14.5 5	529
ntelligent — 1.5 3.5 3.5 8.5 16 20.5 24 52.5 87.7 86.5 14.5 18.25 31.75 86.5 103 11 — 1 — 2 3 3 14.5 18.25 31.75 36.5 36.5 36.5 36.1 11 — 1 — 1 — 1 1 4.5 6 8.5 11. 18.5 31.75 36.5 38.5 11 — 1 — — 1 1 1 4.5 6 8.5 11. 5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5	08-62	31.5 80.25 92.75 51 13 4	272.5
ntelligent — 1.5 3.5 2 3.5 2 8 11 18.5 37 7.5 — 7.6 8 11 18.5 31 11 18.5 31 11 18.5 31 11 18.5 31 11 18.5 31 11 18.5 31 11 11 11 11 11 11 11 11 11 11 11 11	62-82	36 112 126 45·5 24 7·5	351
ntelligent	84-14	29 86·5 103 36 13	272.5
ntelligent — 68—69 ent — 1 — 2 3.5 2 8 11 cfelligent — 7.5 3.5 2 8 11 cfelligent — 7.5 3.5 3.5 28 28 25 ull — 1 — 2 3 3 14.5 18.25 ull — 1 — 1 1 4.5 6 ull — 1 — 1 1 1 4.5 6 ull — 1 — 1 1 1 4.5 6 ull — 1 — 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	22-92	37 81 59·5 36·5 14	230
ntelligent	92-92	18.5 52.5 60.25 31.75 8.5	176.5
ntelligent	S2-72	$11 \\ 24 \\ 28.25 \\ 18.25 \\ 6 \\ 1$	2.88
Intelligent charge and	72-82	8 20.5 28 14.5 4.5	2.92
ntelligent ent c7—68 ent 1	&7—97	2 16 7.5 3	
O7-68	82IL	3.5 7.5 1	23.5
1.5 08 08 08 08 08 08 08 0	T2-02	23.5	8.5
1 1 1 1 1 1 1 1 1 1	02-69	1	5
ntelligent ent itelligent ull ull	69-89	1.5	ಬಾ
ntellige ent telligeu iii ulli	89-29	1 - 1 - 1	1
ntell ull ull als		ent	:
QHZZZZZ>		ntel ent itell ull	Totals

Intellectual Grade.

TABLE XXIV.

Girls' Cephalic Index*.

		1 1
Totals	329 783·5 682·5 284 106 41	2226
9.86-9.06		1
9.06-9.88	1 3 - 2 - 1	11
g.88—g.98	2 2 2 1	16.5
g.98g.48	10 26.5 30 8 8 2.5	62
g.48—g.78	23.5 66 58.5 18 2	169
G.78—G.08	56 130 104.5 37.5 15.5 6	349.5
G-08—G-81	84.5 165.25 164.75 83 24.5	525
G-82—G-92	67.5 170.25 150.25 67.5 28 11	494.5
9.92-9.42	37 112 81 5 33 5 16	285
9.72-9.82	24.5 57 44.5 13.5 6	149.5
9.82-9.02	13 21.5 22.5 9 5.5 4	75.2
9.02—9.89	7.007.49.8 5.00.60	33.5
g.89—g.99	1 3.5	133
g.99—g.†9	1 2 2 2 1 1 2 2 1	10.5
9.49—9.79	12221	111
G.79—9.09	1.5	2.2
	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	Totals

Intellectual Grade.

* By an oversight of the computator the units of cephalic index were here taken not the same as in Table XXIII.

TABLE XXV.

Boys' Health.

Grade.		Very Robust	Robust	Normally Healthy	Rather Delicate	Very Delicate	Totals
Intellectual Gra	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	28 46·5 36 19 6 3	77 272·5 266·5 102 42·25 3·25	120 336·5 313·5 138 56·25 17·75	40·5 92 111 76 29·5 14	5 6 8 2 2 3	270·5 753·5 735 337 136 41
In	Totals	138.5	763.5	982	363	26	2273

TABLE XXVI.

Girls' Health.

Grade.		Very Robust	Robust	Normally Healthy	Rather Delicate	Very Delicate	Totals
Intellectual Gra	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	31 39·5 39·5 15 5	135·5 256·5 189 74·5 26 9	106·25 355·25 284 97 39·5 13	58·25 142·25 166·5 89·5 37·5 15	4 19·5 16 11 4 3	335 813 695 287 112 43
Iı	Totals	133	690.5	895	509	57.5	2285

TABLE XXVII.

Boys' Hair Colour.

Grade.		Red	Fair	Brown	Dark	Jet Black	Totals
Intellectual Gra	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	7 26 35.5 11.5 2 4	104 263·25 243·25 123·25 40·75	83 221·5 254 120·75 45·75 18	64 214·75 200·25 73·5 30·5 12	5 - 10 - 15·5 - 6 - 2 - 1	263 735·5 748·5 335 121 47
Ï	Totals	86	786.5	743	595	39.5	2250

TABLE XXVIII.

Girls' Hair Colour.

de.		Red	Fair	Brown	Dark	Jet Black	Totals
Intellectual Grade.	Quick Intelligent Intelligent Slow Intelligent Slow Slow Dull Very Dull	20·25 32·5 23·25 6 4 2	128·75 279·5 263·75 97·25 40·5 17·25	123 321·5 244·75 117·25 39·75 15·75	57 172·5 153·75 55 23·25	1 8.5 7 4 1	330 814·5 692·5 279·5 108·5 42
I	Totals	88	827	862	468.5	21.5	2267

TABLE XXIX.

Boys' Hair Set.

Intellectual Grade.

pe.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Hair Tyl	Smooth Wavy Curly	212 34·5 9	613·25 95·75 25·5	588·25 76·25 25·5	263 46 10:5	113·5 17 4	33 5 1	1823 274·5 75·5
	Totals	255.5	734.5	690	319.5	134.5	39	2173

TABLE XXX.

Girls' Hair Set.

Intellectual Grade.

r Type.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Hair Tyl	Smooth Wavy Curly	198.5 90 30	460 180 76	$415 \\ 144.5 \\ 62$	174.5 52.5 37	72 20 19	25 6 7	1345 493 231
_	Totals	318.5	716	621.5	264	111	38	2069

TABLE XXXI.

Boys' Eye Colour *.

Intellectual Grade.

our.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
e Col	Light Medium Dark	108·5 105·5 48	295·25 273·25 164·5	263·5 308·5 160	127·75 147·75 76	59 38·5 31·5	13 20 6.5	867 893·5 486·5
Ey	Totals	262	733	732	351.5	129	39.5	2247

^{*} In this investigation, "Light" covered blue of all shades, light grey, very light green, "Medium" included dark grey, green, light chestnut, orange and grey combined, and "Dark" was taken to embrace dark chestnut, light and dark brown, "black."

TABLE XXXII.

Girls' Eye Colour.

Intellectual Grade.

lour.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Eye Colour.	Light Medium Dark	$128 \\ 162 \\ 62.5$	284 345·5 186	215 302·5 153·5	97 124 70	$\frac{41}{49}$	14 16·5 11·5	779 999·5 506·5
Ħ.	Totals	352.5	815.5	671	291	113	42	2285

TABLE XXXIII.

Boys' Athletic Power.

Intellectual Grade.

Power.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
thletic P	Athletic Non-Athletic	159·5 46	421·75 163·25	355·5 187·5	158·75 99·75	40·5 48·5	12 15	1148 560
Athl	Totals	205.5	585	543	258.5	89	27	1708

TABLE XXXIV.

Girls' Athletic Power.

Intellectual Grade.

ower.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Athletic P	Athletic Non-Athletic	167·5 74·5	369·5 225·5	259·5 220·5	98·5 122·5	32 55	11 18	938 716
Ath	Totals	242	595	480	221	87	29	1654

TABLE XXXV.

Boys' Temper.

Intellectual Grade.

er.		$egin{array}{c} ext{Quick} \ ext{Intelligent} \end{array}$	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Tempe	Quick Good Natured Sullen	51 180 11	136·25 476·25 50	136·25 478·25 90·5	43 238 66	17.5 65.5 34.5	6 17·5 15·5	390 1455·5 267·5
	Totals	242	662.5	705	347	117:5	39	2113

Totals

364

1371.5

2034

298.5

TABLE XXXVI.

Girls' Temper.

Intellectual Grade.

Slow

Dull

12

63

36

111

Slow

 $\begin{array}{c} 37.75 \\ 171.25 \end{array}$

58

267

Very Dull

5·25 22·75 13·5

41.5

ľ.		Quick Intelligent	Intelligent	Slow Intelliger
Temper.	Quick Good Natured Sullen	72·5 206 23·5	136·75 464·25 74	99·75 444·25 93·5
	Totals	302	675	637:5

TABLE XXXVII.

Boys' Handwriting.

Intellectual Grade.

Grade.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Handwriting Gr	Very Good Good Moderate Poor Bad Very Bad	35 103 67·5 11 2	57·5 237 240·75 67·25 7	32·5 196·5 280·25 91 27·25 5	14·5 71 120·75 63·5 13·75	$\begin{array}{c} 6 \\ 20 \\ 51.25 \\ 25.25 \\ 2 \\ 2 \end{array}$	4·5 19·5 9·5 3	145.5 632 780 267.5 55 13
H	Totals	218.5	609.5	632.5	287.5	106.5	38.5	1893

TABLE XXXVIII.

Girls' Handwriting.

Intellectual Grade.

Grade.		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
Handwriting Gr	Very Good Good Moderate Poor Bad Very Bad	38 115 67 26·5 7	47 277 231·5 62 11 2	30 185 244·5 75·5 9	6 55.5 112.5 48 10 1	4 19 43 21 7 4	$egin{array}{c} 1 \\ 6 \\ 14 \\ 11 \\ 1 \\ 3 \\ \end{array}$	126 657·5 712·5 244 45 16
H	Totals	255.5	630.5	548	233	98	36	1801

Biometrika v

19

TABLE XXXIX. Alternative Psychical Characters in Boys.
Intellectual Grade.

		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
	(a) Keen Conscientiousness Dull	231·5 26	520·25 132·75	451 252	148·75 171·75	48.75 80.25	11·75 25·25	1412 688
	Totals	257.5	653	703	320.5	129	37	2100
Characters.	(b) Shy Self-Assertive	142·5 101	385 265°5	415·5 295	190·25 133·75	74·75 52·25	22·5 14	1230·5 861·5
	Totals	243.5	650.5	710.5	324	127	36.5	2092
	(c) Self-Conscious Unself-Conscious	135·5 113·5	312 325	337·75 331·75	147.5 180	44.75 90.75	14 21·5	991·5 1062·5
Psychical	Totals	249	637	669.5	327.5	135.5	35.5	2054
Ps	(d) Noisy Quiet	92 206·5	265·5 465·5	265 498·5	131·75 218·75	56·25 86·75	15·5 26	826 1502
	Totals	298.5	731	763.5	350.5	143	41.5	2328
	(e) Popular Unpopular	216·5 25	548·5 101·5	513·75 132·75	222·25 72·25	69 44	18·5 9	1588·5 384·5
	Totals	241.5	650	646.5	294.5	113	27.5	1973

				Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals
	(a)	Keen Conscier Dull	ntiousness	252 40·5	579·5 113·5	390·5 178	132·5 107·5	35 54	11.5 28.5	1401 522
		Totals	•••	292.5	693	568.5	240	89	40	1923
al Characters.	(b)	Shy Self-Assertive		130·75 138·75	419·75 252·75	411 176	183·5 70·5	64 37	22·5 17·5	1231·5 692·5
		Totals		269.5	672.5	587	254	101	40	1924
	(c)	Self-Conscious Unself-Conscio		133·5 144·5	337·5 354·5	282 298	129·5 116·5	52·5 43·5	20·5 17·5	955·5 974·5
TOO TOO		Totals		278	692	580	246	96	3 8	1930
- 22 ·	(d)	Noisy Quiet	•••	124·25 197·75	255·5 536·5	186·75 477·75	82·5 202·5	34 78	15·5 27	698·5 1519·5
		Totals	•••	322	792	664.5	285	112	42.5	2218
	(e)	Popular Unpopular	•••	253·5 26·5	496.75 89.75	443·25 113·75	150·5 74	53 36	12·5 21·5	1409·5 361·5
		Totals	***	280	586.5	557	224.5	89	34	1771

Psychical Characters.

ON THE RELATION BETWEEN THE SYMMETRY OF THE EGG AND THE SYMMETRY OF THE EMBRYO IN THE FROG (RANA TEMPORARIA).

By J. W. JENKINSON, M.A., D.Sc., Oxford.

PART I.

As every embryologist will be aware, the relation between the first segmentation furrow of the frog's egg and the sagittal plane of the frog embryo has been both the source of a famous theory and the central point of an equally celebrated controversy. For while the supposed coincidence of the two planes led Roux directly to the experiment in which one of the first two blastomeres being killed a half embryo was produced from the survivor and so to the definite formulation of the preformationist doctrine of "Selbstdifferenzirung" and "Mosaikarbeit," the criticism which this theory called forth was soon directed to a re-examination, and eventually resulted in a denial of the facts on which the hypothesis was based.

Roux's own statement as to the relations between the planes in question, made in 1883, is sufficiently explicit. After describing the difficulties he had to encounter in obtaining an accurate measurement of the angle between the two, and giving the magnitudes of such measurements, unfortunately only a small number, as he was able to get, he concludes as follows: "So ist es wohl berechtigt wenn ich das hervorspringende Bestreben beider Ebenen zusammenfallen zu lassen, als das Gesetzmässige auffasse, und die gefundenen kleineren und grösseren Abweichungen nicht auf Abweichungen von dem Gesetz sondern auf die noch restirenden Fehlerquellen zurückfuhre und so das Gesetz aufstelle.—Mit der Ebene der ersten Furchung wird beim Froschei zugleich auch die künftige Medianebene des Individuums bestimmt und zwar fallen beide zusammen" (Roux, 1883, p. 109). Nor is the relation thus established one of mere coincidence, it is a causal relation, as we read in the *Mosaikarbeit*, published in 1893 (p. 850): "Das Prinzip der organbildende Keimbezirke beginnt somit erst mit der Furchung eine 'feste' Bedeutung zu erhalten; dieselbe ist nicht blos eine topographische, sondern auch eine causale," a conception which is of course a necessary

part of the hypothesis of nuclear predetermination elaborated by Weismann out of Roux's *Mosaiktheorie*. Like many other of the facts upon which this theory is built, the universality at least of the coincidence of these two planes has been denied. Oscar Hertwig has stated—on the strength of observations made on eggs compressed between horizontal glass plates—that they may make any angle with one another. Schulze and Kopsch think it probable that they coincide in the majority of cases.

Not one of these authors has, however, thought it worth while to examine a large—a statistically intelligible—number of cases, though it would appear that the magnitude in question is obviously a variable one and preeminently amenable to such treatment. It is by this method therefore that I have sought for a solution of the problem.

In the meantime the centre of interest has shifted. The very numerous experiments that have been made on the behaviour of eggs segmenting under pressure and on the development of isolated blastomeres, have distinctly negatived the idea of the preexistence in the fertilized egg-cell of definite nuclear units for the determination of the inheritable characters of the organism, an idea which has now been abandoned by Roux himself, and less importance has come to be attached to segmentation as a mechanism for separating such units; more attention is now paid to the initial structure of the ovum, and the presence in it—demonstrated by recent research in some cases—of definite cytoplasmic organ-forming substances as a cause of differentiation.

In the frog's egg itself (R. fusca) Schulze has shown that though the symmetry of the unfertilized ovum is radial about the axis, a bilateral symmetry is acquired during fertilization by the formation of a crescentic band—at first grey, but afterwards white and added to the white area on the vegetative side of the egg—along the border of the pigmented area on one side. The grey crescent arises, according to Roux, by immigration of the pigment into the interior of the egg. Both Roux (1903) and Schulze agree that the point of entry of the sperm is in the plane of this bilateral symmetry, and on the side opposite to that on which the grey crescent appears; and Roux, following out his earlier idea of the causal connection between the sperm path and the first furrow, believes that it is the entry of the sperm that is responsible for the change of symmetry. It is further stated by both authors that the side of the grey crescent is postero-dorsal, since the dorsal lip of the blastopore is formed here. The plane of symmetry and the sagittal plane therefore tend to coincide.

Normally, according to Schulze, the first furrow also lies in this plane, but considerable deviations are possible, their frequency increasing with the length of time that the eggs have remained in the uterus before being laid.

Morgan has investigated the relation between these three planes in R. temporaria and R. palustris; the first furrow lies in the plane of symmetry in 24 °/ $_{\circ}$ of the cases in the first species, in 50 °/ $_{\circ}$ in the second, and when this occurs the

sagittal plane coincides with both. But the first furrow may be at right angles to the plane of symmetry, and in that case the sagittal plane may coincide with either or be in between.

A complete treatment of the whole question demands therefore the determination of the position in each of a large number of eggs of the sperm-path, the plane of symmetry, the first furrow and the sagittal plane. This is, however, unfortunately impossible, since the sperm path disappears long before the appearance of the sagittal plane. It is possible, however, to determine either the first three or the last three in one and the same egg; and this I have attempted to do. In the first part of this paper I can only give the results of the measurement of the angles between the plane of symmetry, the first furrow and the sagittal plane in a fairly large number of cases. The relation between the sperm path and the first furrow involves the cutting of a large number of eggs into series of sections, and must be left till later.

The angle between the first furrow and the sagittal plane may be measured in various ways. The eggs may be fastened by the jelly to glass plates coated with paraffin and the direction of the planes marked, with the aid of a lens, by a needle on the wax. Or the eggs may be fastened direct to the underside of a glass plate and the directions marked with a paint-brush. These methods are, however, very inaccurate, and I have discarded all the measurements made in this and previous years in this way. They are inaccurate for two reasons. In the first place it is very difficult to place the marks accurately, and in the second, the sagittal plane has to be determined by the direction of the medullary folds or plate, a direction which is probably in many cases not the original direction of the median plane, for during the closure of the blastopore the eggs rotate not only about a horizontal axis but about a vertical axis as well, though of course to a less, and to an irregular extent.

It became necessary therefore to determine the sagittal plane by the position of the dorsal lip of the blastopore in an early stage before rotation has begun. To do this the egg must be viewed from the lower side. I made use of the following apparatus. The microscope was placed with the tube horizontal, and to the stage was attached a holder which carried a slide on which the eggs were placed, and below this a mirror at 45°. The eggs were illuminated from below. The slide was ruled with a diamond with parallel lines, and by means of the micrometer and goniometer with which the ocular was provided it was a simple matter to read off the angle between the first furrow and a line on the slide, and later on to determine the position of the sagittal plane in the same fashion.

The same method was used for the plane of symmetry.

One possible objection to this means of measurement is, I have satisfied myself, groundless. Between the first and the second measurements the eggs must be kept in a damp chamber, and it might be thought that in moving them

to and fro, however carefully, some slight shifting might occur. I measured the first furrow in a set of eggs, then violently shook the slide and jogged it on the table, and then measured again. The difference in many cases, nearly half, was less than 3° and in no case very great*; and the eggs of course were never ordinarily subjected to such violent treatment. The eggs were always taken straight from the uterus, placed in rows on the slide, moistened with water, artificially fertilized, and allowed to remain in water until the jelly had become well swollen. They were then removed from the water and kept in a damp chamber till required.

The following are the results of the measurements.

The angle between the first furrow and the sagittal plane was determined in 889 cases, and in 397 of these the position of the plane of symmetry was also observed. In 14 other cases the angle between the plane of symmetry and the first furrow was found, in 112 other cases that between the plane of symmetry and the sagittal plane. There are thus 509 observations of the angle between the plane of symmetry and the sagittal plane, 411 observations of that between the plane of symmetry and the first furrow.

I. First Furrow and Sagittal Plane.

Table I. gives the frequencies for groups of 10°.

TABLE I.

First Furrow and Sagittal Plane.

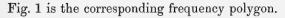
Groups of 10°.

Class	Frequency		Class	Frequency
-90-81	27		+ 0-10	111
8071	26		11-20	86
70—61	24		21—30	84
6051	32		3140	43
50 - 41	30		41—50	45
4031	42		51—60	34
30-21	53	-	6170	31
20-11	69		71-80	29
10-0	104		81—90	19
				889

 $M = 2.12^{\circ} \pm .914$ $\sigma = 40.39^{\circ} \pm .646$.

Angle: 0° 1° 2° 3° 4° 5° 6° 7° 8° 9° 10° 11° 12°...18° Frequency: 6 10 8 5 9 5 2 1 1 4 1 1 2 ... 1

^{*} The actual frequencies of these differences were:



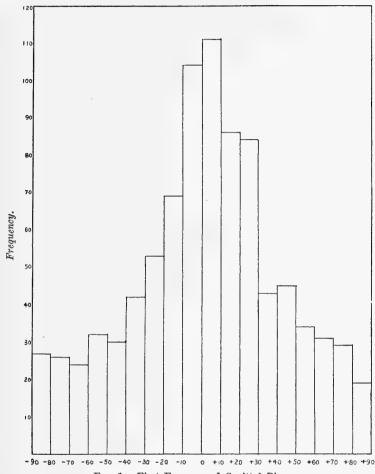


Fig. 1. First Furrow and Sagittal Plane.

It will be seen that there is a very decided tendency for the two planes to coincide. Still all deviations are possible and all occur, and occur pretty equally in either direction, for the polygon is fairly symmetrical.

This tendency towards coincidence might not unnaturally lead to the supposition that there is a causal connection between the two. The correlation table (Table II.) quite negatives this idea.

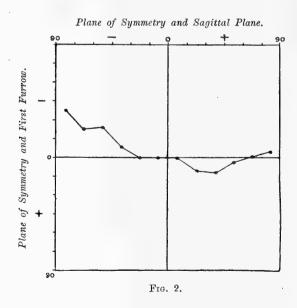
The table, which was constructed by taking in each egg the angle between the plane of symmetry and the first furrow and that between the plane of symmetry and the sagittal plane, shows clearly how small the correlation is; it works out at $\rho = 138 \pm 031$. Figs. 2 and 3, regression schemes constructed from the correlation table, emphasize the point. It will be noticed, however, that in Fig. 2 the regression line is rather sharply bent away from the horizontal on the

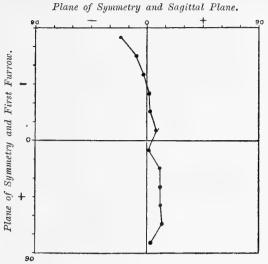
TABLE II.

Correlation between First Furrow and Sagittal Plane.

Plane of Symmetry and Sagittal Plane.

. 9	90		_				0	;		+		90	Total	s Means
and First Furrow.	1 	1 3 - 1	4 1 - 1	5 3 2 1 3	1 3 4 2 7 8	8 6 6 4 4 24	9 5 3 6 5 21	1 1 1 3 14	$\frac{1}{2}$ $\frac{3}{7}$	1 1 3 4	1 1 1 -	$\frac{1}{2}$	32 20 23 17 27 85	-1·4 - ·6 - ·11 + ·14 + ·2 + ·5
Plane of Symmetry	1 - - - -	1 - 1 - 1 - 1 - 1 - 1	$\begin{array}{c c} 2 \\ \hline - \\ \hline 1 \\ \hline 1 \end{array}$	$\frac{3}{3}$ $\frac{1}{4}$	8 3 5 1 1 5	15 6 5 8 4	15 6 2 3 5 12	11 4 3 5 - 5	3 4 1 3 3 2	1 - - 3	1 2 2 2 2 2	2 1 1 -	63 24 22 23 16 45	+ ·1 + ·7 + ·7 + ·7 + ·8 + ·21
							0					90		
Totals Means	$\frac{2}{8-2.5}$	7	10	25	48 +·08	99 + 04	92 + 05	49 +·7	+ .8	13 + .26	12	- 32	397	
						ρ	=:138 ±	<u>⊦</u> .031.						





Figs. 2 and 3. Schemes of Regression constructed from Table II.

In Fig. 2 the dots indicate the mean value of the angle between Plane of Symmetry and First Furrow for each class of angle between Plane of Symmetry and Sagittal Plane, in Fig. 3 the converse.

left-hand side. As we shall see presently, and as indeed may be gathered from Table II., this is due to the tendency of the first furrow to lie either in or at right angles to the plane of symmetry, and Professor Pearson has suggested to me that if the upper and lower arrays of the table were omitted the value of ρ would be still further reduced. This is, as a matter of fact, the case.

Table III. is the correlation table constructed from the six middle arrays of Table II.; Fig. 4 the corresponding regression scheme. The line of regression is now practically horizontal, and the value of ρ —less than the probable error—practically nil.

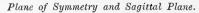
TABLE III.

Correlation table constructed from the Middle Strip of Arrays of Table II.

Plane of Symmetry and Sacrittal Plane

				riane	or Sy	mmetr	y and	Sagn	Can T I	апе.				
90 90 45 [0			+		9	0	Totals
of Symmetry and First Furrow.	=	<u> </u>	$\frac{-}{1}$	2 1 3	2 7 8	$\begin{array}{c} 4\\4\\24\end{array}$	6 5 21	$\begin{array}{c}1\\3\\14\end{array}$	$\frac{}{3}$	1 3 4	1 _	$\frac{}{3}$	45	17 27 85
Plane of Syr First F	<u>1</u>	1 - -	2	3 3	8 3 5	15 6 5	15 6 2	11 4 3	3 4 1	1 _	$\frac{1}{2}$	2 1 1	45	$63 \\ 24 \\ 22$
90						c)					9	5	
Totals	1	2	3	12	33	58	55	36	18	9	4	7		238
Means	+ .2	2	+ 1	+ .08	+ .04	+ .01	21	+.13	+ 11	9	+ .7	+ .2		
						$\rho = 0$	09 + ·04	4.						

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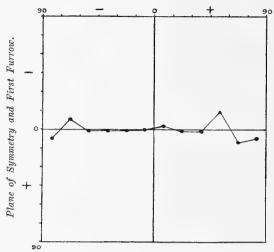


Fig. 4. Regression Scheme constructed from Table III. The dots mark mean values of the angle between Plane of Symmetry and First Furrow.

In short, between the first furrow and the sagittal plane in the frog's egg there is no correlation, or—if the correlation table is an expression of that canon of induction known as the method of concomitant variations—no causal connection.

The two planes coincide in so many cases merely because each, as we shall see, and particularly the sagittal plane, tends to lie in the plane of symmetry. Beyond that there is no connection between them. The symmetry of segmentation and the symmetry of the embryo are independent, and in this case at least the truth of Driesch's famous aphorism is vindicated—"Furchungsmosaik braucht kein Mosaik der Potenzen zu sein."

II. Plane of Symmetry and Sagittal Plane.

The number of observations is here not so great, but still great enough to produce a symmetrical result (Table IV., Fig. 5). It will be seen that the tendency of these two planes to coincide is more considerable, the standard deviation being smaller than in the case of the first furrow and the sagittal plane.

TABLE IV. Plane of Symmetry and Sagittal Plane.

Groups of 10°.

		*	
Class	Frequency	Class	Frequency
- 9081	4	+ 0-10	91
80—71	6	1120	52
70—61	3	2130	42
60 - 51	8	3140	27
50 - 41	14	4150	15
40 - 31	23	5160	7
30-21	29	61—70	11
20 - 11	60	71—80	6
10-0	103	81—90	8
			500
	16	2 22 1 222	509

 $M = 2.23^{\circ} \pm .889$ $\sigma = 29.75^{\circ} \pm .629$.

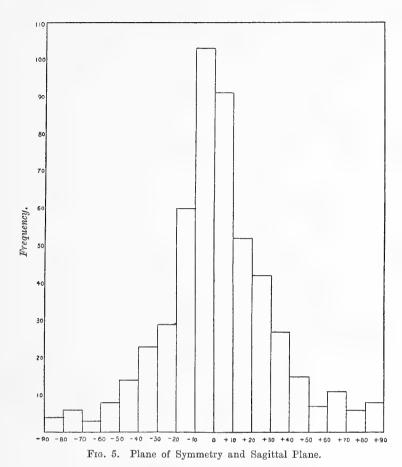


TABLE V. Correlation between Plane of Symmetry and Sagittal Plane.

First Furrow and Sagittal Plane. TotalsFirst Furrow and Plane of Symmetry. $\frac{32}{20}$ $\begin{array}{c} 1 \\ 1 \\ 2 \end{array}$ $\frac{2}{2}$ $\frac{4}{2}$ $\frac{2}{5}$ $\frac{5}{2}$ $\frac{2}{9}$ 2 4 $23 \\ 17 \\ 27 \\ 85$ 1 3 $\begin{array}{c} \tilde{5} \\ 7 \\ 14 \end{array}$ 20 $\frac{4}{25}$ $\begin{array}{c} 15 \\ 7 \\ 2 \end{array}$ $\begin{matrix}1\\3\\7\\3\\3\end{matrix}$ $\frac{4}{1}$ $\frac{4}{6}$ $\frac{5}{4}$ $\begin{array}{c} 22 \\ 23 \end{array}$ 2 2 Ī Totals Means -3.8-1.9 -1.7-.18 | -.03 | +.72 | +2.2 | +1.6 | +1.6 | +.16

 $\rho = .372 \pm .025$.

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The correlation table (Table V.), constructed by taking the first furrow as a fixed line and correlating the angles made with it by the sagittal plane and the plane of symmetry, and the regression scheme (Fig. 6) bring out the result in another way.

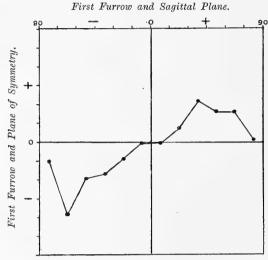


Fig. 6. Regression Scheme of the mean values of angles between First Furrow and Plane of Symmetry for each class of angle between First Furrow and Sagittal Plane. Constructed from Table V.

The correlation is obviously spoilt by those cases in which the first furrow is at right angles to the plane of symmetry; but by taking the 36 central squares of the table only (Table VI. and Fig. 7), the value of ρ may be increased to $\cdot 439 \pm \cdot 032$. By taking the six middle arrays only, it may be increased still further to $\cdot 477 \pm \cdot 028$.

TABLE VI.

Constructed from the 36 Central Squares of Table V.

Q 45	First	t Furi	ow an		ittal l		45	Totals
netry.	 1 3		1 5 20	2 4 25	5 7 14	5 2 9	0	13 19 75
rst Furrow of Sym	5 4 6	9 6 1	15 7 2	11 4 1	13 1 2	$\frac{1}{1}$		54 22 13
Æ 45			c				45	
Totals	19	20	50	47	42	18		196
Means	-1.0	- · 7	06	+ .21	+ .41	+.9		
			$\rho = \dot{\gamma}$	439 ± ·0	32.			



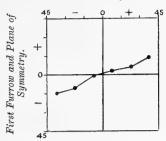


Fig. 7. Regression Scheme constructed from Table VI. The dots have the same significance as in Fig. 6.

III. Plane of Symmetry and First Furrow.

As Table VII. shows, the first furrow tends to lie either in or at right angles to the plane of symmetry, though the former predominates. In Fig. 8 I have accordingly divided the frequency polygon into two parts, one distributed about

TABLE VII.

Plane of Symmetry and First Furrow.

Groups of 10°.

Variation ab	out 0°.	Variation about	90°.
Class	Frequency	Class Freque	ency
-45 36	8	+46— 55 17	
35— 26	17	56— 65 14	
25— 16	21	66— 75 13	
15— 6	26	76— 85 17	
5—+ 5	98	86	
+ 6— 15	26	- 85 - 76 23	
16— 25	16	75— 66 9	
26— 35	18	65— 56 15	
3 6— 45	13	55— 46 16	
	$\overline{243}$	168	3
Variation abo	out 0°	Variation about 90	0
<i>M</i> = '53° ±	·853	$M = 90.17^{\circ} \pm 1.212$	
$\sigma = 18.70^{\circ} \pm$.603	$\sigma = 23.29^{\circ} \pm .857$	•

0°, the other about 90°. This alternative of two "predilection" directions, to borrow a phrase of Roux's, for the first furrow to choose from, completely throws out the correlation (Table VIII. and Fig. 10); but if the range from -45° to $+45^{\circ}$ only be considered (Table IX.) the value of ρ rises to 271 ± 038 . In the "scatter" diagram (Fig. 9), in which each instance is separately recorded, the coincidence of the two planes is very well shown by the crowding of the dots along the diagonal.

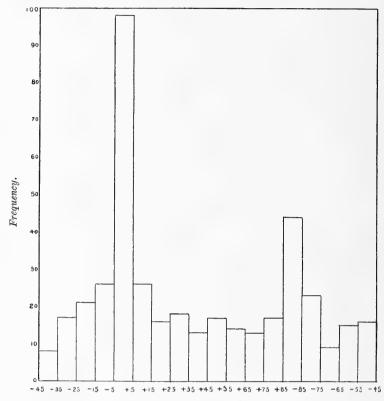


Fig. 8. Plane of Symmetry and First Furrow.

TABLE VIII.

 ${\it Correlation \ between \ Plane \ of \ Symmetry \ and \ First \ Furrow.}$

	Fi	rst Furrow	and Sag	gittal Pla	ane.			
o 6	_		0	+	-		90	Totals
and Sagrittal Plant 1	$egin{array}{c c} - & - & - \ \hline 2 & - \ 2 & 4 \ 3 & 6 \ 6 & 5 \ \end{array}$	$ \begin{array}{c cccc} & 1 & 2 & 2 \\ \hline & 2 & - & - \\ \hline & 8 & 8 & 8 \\ 9 & 26 & & & \\ \end{array} $	- 1 1 4 10	2 2	$\begin{bmatrix} - & - & - \\ 2 & 1 \\ 3 & 6 \\ 4 & 3 \\ 3 & 5 \end{bmatrix}$	1 1 4 9		2 7 10 25 48 99
Plane of Symmetry and Sagittal Plane.	$\begin{array}{c cccc} 5 & 4 \\ 2 & 2 \\ 2 & 2 \\ 1 & 2 \\ 1 & -1 \\ 1 & 1 \end{array}$	2 9 4 5 3 1 2	26 2 5 — 3 —	20 4 -	5 2 5 3 5 4 1 2 - 1	6 -1 5 1	4 2 1 — 3	92 49 29 13 12
<u>P</u> %			0				90	
Totals 29 20	25 27	30 58	52	48 29	27	29	23	397
Means + '4 - '6	+ 18 - 13	- 1 - 14	+ 4	+ .6 + .	32 + .09	+.5	+ .6	
		$\rho = 0$	087 ± ·032	2.				

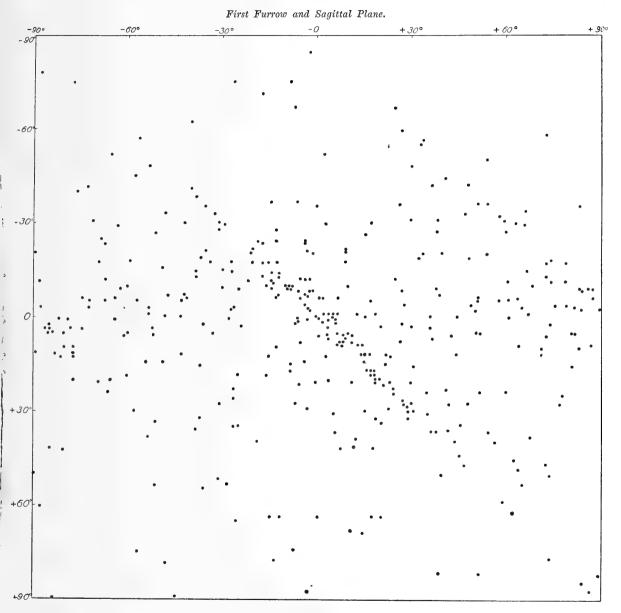


Fig. 9. 'Scatter' Diagram of the Correlation between the Plane of Symmetry and the First Furrow.

First Furrow and Sagittal Plane.

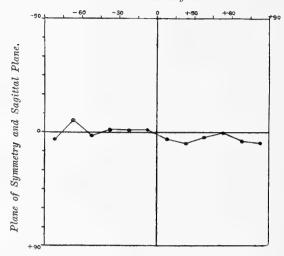


Fig. 10. Regression Scheme constructed from Table VIII. The dots are the means of the angles between Plane of Symmetry and Sagittal Plane for each class of angle between First Furrow and Sagittal Plane.

TABLE IX.

Constructed from the Central Squares of Table VIII.

First Furrow and Sagittal Plane.

pu 45		_	(+		45	Totals
nmetry al Plane.	4 6 5	.— 8 9	2 8 26	$\begin{array}{c} 1\\4\\10\end{array}$	2 2 6	3 4 3		12 32 59
Plane of Symmetry and Sagittal Plane.	$\begin{array}{c} 4 \\ 2 \\ 2 \end{array}$	2 4 3	9 5 —	26 2 5	9 20 4	5 5 5		55 38 19
A5			c)			45	
Totals	23	26	50	48	43	25		215
			$\rho = 27$	± .038				

The examination, therefore, of a fairly large number of instances

- (1) supports the statement that the first furrow and the sagittal plane tend to coincide, though deviations of any magnitude are possible;
- (2) but contradicts the supposition that there is any causal nexus between the two;
- (3) shows that the symmetry of the egg has a marked effect upon the symmetry of the embryo and upon the symmetry of segmentation. The effect, however, is not the same in the two cases.

A question that of course will obviously occur is, to what are the deviations from coincidence due? They may be the result of internal or external factors, and of the latter heat and light and gravity at once suggest themselves as possible. Many years ago Pflüger showed that, by preventing the jelly from absorbing water, the egg of the frog could be prevented from rotating inside it and compelled to remain in any arbitrarily selected position. The first and second furrows were, however, shown to be vertical, the third horizontal as in the normal egg. The median plane of the embryo was determined by the plane which included the original, now tilted, egg-axis and the present vertical axis, a plane afterwards termed by Born, who examined the internal structure of eggs so placed in "Zwangslage," the "streaming meridian," since there occurred equally on each side of it an upward streaming of cytoplasm and pigment, a downward sinking of the heavy yolk granules. The first furrow, according to Pflüger, in such inverted eggs may make any angle with this plane; according to Born, it is generally either in or at right angles to it, and Roux corroborates this.

It is evident that under the influence of gravity a very marked bilateral arrangement is conferred upon the constituents of the egg and that this symmetry impresses itself on segmentation and embryonic development, and it does not seem impossible that, before the fertilized egg, which is laid with its axis in any position, is able to rotate inside its jelly membranes, a slight bilateral symmetry may be conferred upon it under the influence of gravity, and that this may interfere with the other bilaterality produced by the entrance of the sperm.

I attempted to measure the angle between the original position of the egg (before rotation), the plane of symmetry and the first furrow; but the measurements are, I am afraid, too few and too inconclusive. I give here, however (Fig. 11), a curve of the angles made by the first furrow with the streaming

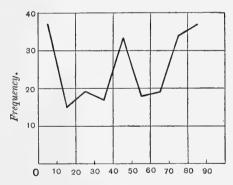


Fig. 11. The First Furrow and the 'Gravitation Symmetry Plane.'

meridian (gravitation symmetry plane) of a number of eggs kept in "Zwangslage." If the measurements are not too few (215) to be trusted, the curve brings out the very interesting point that the first furrow tends to lie either in, or at right angles

to, or at 45° to the plane of symmetry, as though equally strong attractions were exerted by the two "predilection" planes, to use Roux's expression, upon the nuclear spindles.

I have also made a few experiments (447 eggs) on the influence of heat and light upon the direction of the sagittal plane. The eggs were placed, as before, on slides ruled with parallel lines, in a damp chamber lined and covered with black cloth. They were then exposed continuously to the light and heat of an incandescent burner placed 15 inches away. As the curve (Fig. 12) shows, there

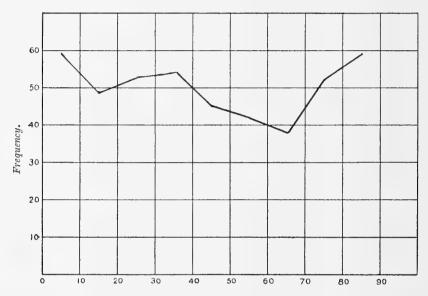


Fig. 12. Angle between direction of Light and the Sagittal Plane.

seems to be a slight tendency for the sagittal plane to be diverted into either the direction of the incidence of light or a direction at right angles to it. The observations are so few, and the tendency so slight, that I cannot lay especial stress upon the result, and publish it with all reserve. Further experiments with heat only, or light only, and light of various colours will perhaps make a more positive conclusion possible.

The curves of Figs. 1, 5 and 8 are not and cannot be reduced to normal curves. I have drawn the appropriate normal curves on the top of these polygons and there is a complete absence of fit. The apex of the polygon in each case projects a good way above the apex of the probability curve, while the ends of the latter lie outside the ends of the polygon.

The latter is very probably due to the fact that the limitation of the range of variability to 90° on each side is an artificial one. It is extremely likely that deviations slightly greater than 90° occur in small numbers, but that these have

been—in actual observation—included as large deviations on the opposite side of the curve*.

In the case of the angle between the first furrow and either the sagittal plane or the plane of symmetry, this is unavoidable, since the two ends of the furrow are, externally, alike; but it would be possible—I am sorry to say I neglected to do this—to distinguish between deviations which are 180° apart and of opposite sign in the case of the plane of symmetry and the sagittal plane, since each of these is polarized, there being a larger extent of unpigmented yolk at one end of the plane of symmetry than at the other, and the sagittal plane being marked, at one end only, by the dorsal lip of the blastopore.

Indirectly, it is true, the two ends of the first furrow might be distinguished from one another by the position of the furrow on the bilaterally symmetrical unpigmented yolk area; but at the large deviations in question—about 90°—this would hardly be practicable.

With regard to the first point of difference between the frequency polygons and the normal curves, Professor Pearson suggested to me that the discrepancy might possibly be due

- (1) to a tendency of the planes not only to coincide, but to lie at 180° with one another, the two positions being indistinguishable in observation;
- (2) to the existence of two kinds of eggs, one in which the planes practically always coincide, another in which they deviate one from another at random.

The first supposition is untenable.

As Schulze and Roux have pointed out, the dorsal lip always appears on one side of the egg, at one end of the plane of symmetry, namely on the side of the grey crescent, where the unpigmented area extends most nearly to the equator. With regard to the first furrow there is, externally, no difference between its ends; the only internal difference is in the position in it of the male and female pronuclei, which lie a little away from, but on opposite sides of, the axis. One end of the plane of the first furrow might therefore be termed male, the other female. The male pronucleus must lie on that side of the egg on which the spermatozoon has entered, and this is always (Schulze and Roux) on the side opposite to the grey crescent. This plane could not, therefore, under any circumstances, deviate by both 0° and as much as 180° from either the plane of symmetry or the sagittal plane.

With regard to the second proposed explanation.

In Table X. will be found the parentage of the eggs used in the several experiments, with the date of each.

^{*} Professor Pearson obtained general formulae for fitting normal curves to the observations, by supposing the extremities of such normal curves beyond 90° cut off, reversed and added to the frequency on the opposite side; but even so the observations failed to fit the normal curve modified in this manner.

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TABLE X.

Table showing the dates of the Several Experiments and the Parentages of the eggs used in each.

Experiment	Date	Parentage
A	30 iii. 06	one done 9
$_{ m C}^{ m B}$	31 iii. 06 }	one 3
D),),	one \mathcal{S} one \mathcal{S} one \mathcal{S}
$_{ m F}^{ m E}$	1"iv. 06 }	one 3)
G	7	one 3 one 9
$_{ m H'}$	2"iv. 06 }	one 3 one 9
K	3"iv. 06"	one 3)
J I	" " {	one of one one
N O	" "	one 3
	?? ? ?)	,

In Tables XI.—XIII. the frequencies in the individual experiments of each class of angle are set forth.

(a) With regard to the First Furrow and the Sagittal Plane (Table XI.).

It is evident that in some experiments (A, F, G, H, I, N, O) the two planes tend to coincide, while in the remainder the distribution is almost at random.

This difference is, however, clearly not due to the length of time the eggs remained in the uterus, for A and O, for example, are respectively at the beginning

TABLE XI.

First Furrow and Sagittal Plane.

Frequencies in the Individual Experiments.

Experi- ment								F	reque	ncies								
A	2	3	2	1	2	4	5	8	6	15	6	8	3	4	1	1	1	
В	1	2	1	3	3	4	3	5	4	4	5	4	5	2	2	3	2	1
C	3	4	5	8	3	3	2	2	1	5	2	3	5	2	8	1	4	
D	5	2	2		1	1		2	_	1	1	'		3	_	1	2	3
\mathbf{E}	1	4	5	5	4	3	2	4	5	2	2	4	4	5	5	9	6	3
\mathbf{F}	2	1	1		1	1	3	7	7	16	6	7	1	1	1		_	<u> </u>
G	1	1	_	_		1		3	4	6	5	4	3	2	_	1	—	2
H	1	4		1		3	2	9	6	15	12	3	4	2	2	1	3	1
K	7	4	2	3	5	2	5	1	6	5	3	3	2	5	5	4	3	7
J			2	4	1	8	4	5	3	3	5	8	2	9	1	3	_	_
I	_	1	1	1	_		6	3	13	3	8	2	1			3	1	I —
N	2		1	2	5	4	7	9	13	10	8	5	4	4	2	2	3	
0	1	<u> </u>	1	1	-	2	8	3	7	7	7	13	4	1	3	_	2	2

and end of the series. Nor is it due to any peculiarity of the ova or spermatozoa. B, C, D and E, it is true, were all obtained from the same female, though not all fertilized by the same male; F and G were also produced by the same parents, and so were N and O, but in J the distribution is a random one: in I it is very strongly gathered about 0° , though in these two cases ova from one female were fertilized by spermatozoa from one male.

(β) The Plane of Symmetry and the First Furrow (Table XII.).

In B, C, G, H, I and J the frequency is greatest about 0° ; in D and K the frequency about 90° rather exceeds that about 0° ; in E the variation is a random one.

TABLE XII.

Plane of Symmetry and First Furrow.

Frequencies in the Individual Experiments.

Experi- ment									Frequ	encie	3							
В	4		2	4	2	4	1	3	6	12	3	3	3		1	_		5
C	3	1	_	4	2	2	3	3	5	12	2	1		2	1	3		3
D	6	1	_			1			1	4	_	_	1		2	1	<u> </u>	6
E	3	2	6	4	2	2	3	4	5	5	2	3	3	7	4	4	3	3
G	1		1		2	1		1	8	4	1	1	_	_	3		_	3
H	2	3	1	_	1	3	5	3	17	14	2	5	2		_	2	_	3
K	5	6	2	3	2	2	2	5	3	8	5	3	3	3	4	1	3	11
J	2	2	3	_	_		1	3	10	5	1	3	3	1	2	2	3	2
I	1		1				_	3	4	3	ī	1		1	_	_		ī
)												
g	0 8	0 7	0 6	0 5	0 4	0 3	0 2	o 1	0) I	0 2	20	30 4	to i	so (50 1	70 8	Bo g
				_	_ ′									+		,		

It is clearly impossible to suppose that these differences are due to any peculiarity in the eggs, or spermatozoa produced by individual parents.

(γ) In the case of the Plane of Symmetry and the Sagittal Plane the tendency towards coincidence is shown in every experiment (Table XIII.).

TABLE XIII.

Plane of Symmetry and Sagittal Plane.

Frequencies in the Individual Experiments.

Experi- ment								F	reque	encies								
В	_	1		1	1	5	4	8	7	4	2	2	3	5	4	2	1	3
C		2		3	_	3	1	7	9	9	4	8	1	1	_		2	
D	1	_	_		3	1	2	10	10	15	12	2	2			1		
E	_	1		1	3	4	4	5	17	12	4	3	3	2		2		3
G	1	-		1	2	1	2	3	11	13	4	10	4	1		2		_
\mathbf{H}				1	1	2	5	11	10	21	7	6	5	2		1	1	
\mathbf{H}'		1		_	1	3		6	8	7	3	1		_				
K	1	1	2	1	1	3	5	5	15	9	11	ĩ	3	3	2	2	1	1
J						1	3	4	6	4	2	6	3	i	1	_	_	1
1	1	1			_		1	î	4	3	ī	ĭ	2	_	_	_		_
9	0 8		0 6		0 4		30 2	0 I	0 0		0 2			lo 5		io 7	0 8	80 (

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Although, therefore, the differences in distribution observed in the different experiments may, in the case of the first furrow and sagittal plane, and the plane of symmetry and the first furrow, be possibly applied, as Professor Pearson has suggested, to the explanation of the discrepancy between the observed polygon and the corresponding normal curve, such an explanation will hardly hold good in the case of the plane of symmetry and the sagittal plane.

I may add here that my results do not seem to lend support to Morgan's statement that, when the first furrow lies in the plane of symmetry, the sagittal plane coincides with both.

This position of the first furrow occurs in my experiments B, C, G, H, I and J; but in G, H and I the distribution of the angle between the first furrow and the sagittal plane is markedly crowded about 0° , in B, C and J it is random.

Further, in the "scatter" diagram (Fig. 9) of the correlation between the plane of symmetry and the first furrow, the dots which signify coincidence of the two are of course those which lie pretty thickly ranged along the diagonal. On Morgan's view all these dots should lie in the centre of the table: it is plain that they do not*.

In conclusion, I have to express my thanks to Mr E. H. J. Schuster for the generous loan of his calculator, and to Professor Pearson for the suggestions he has been good enough to make.

* It should be pointed out however that the tendency of the sagittal plane to lie in the plane of symmetry does increase slightly as the angle between the first furrow and the plane of symmetry diminishes.

Thus the value of the standard deviation for the angle between plane of symmetry and sagittal plane for all the cases (Table IV.) is

$$\sigma = 29.75^{\circ} \pm .63$$
 (n=509, M=2.23° ±.89).

For the 397 cases where the first furrow is also known (Table II.)

$$\sigma = 30.16^{\circ} \pm .72 \ (n = 397, \ M = 3.41^{\circ} \pm 1.02).$$

But if those cases only are considered in which the angle between first furrow and plane of symmetry is not greater than 45° (as in Table III.), then

$$\sigma = 28.41^{\circ} \pm .87 \ (n = 238, M = 5.10^{\circ} \pm 1.24).$$

By taking the two middle arrays only of Table III.—those cases in which the said angle is not greater than 15° —

$$\sigma = 27.94^{\circ} \pm 1.09 \ (n = 148, \ M = 5.16^{\circ} \pm 1.55);$$

while when the range of the difference between first furrow and plane of symmetry is restricted to 5° (by taking the diagonal strip of Fig. 9),

$$\sigma = 27.46^{\circ} \pm 1.32$$
 (n = 98, $M = 4.84^{\circ} \pm 1.87$).

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MISCELLANEA.

I. A Rejoinder to Professor Kapteyn.

By KARL PEARSON, F.R.S.

In the Recueil des Travaux botaniques Néerlandais, No. 3, 1905, will be found a reply to my recent criticism of Professor Kapteyn's theory of skew curves*.

Professor Kapteyn's reply consists, as far as I am able to follow it, of two statements accompanied by a complete ignoration of the criticisms I have made on his treatment of skew variation.

His statements are

(a) That he has arrived at a more general proof of the equation

$$y = \frac{h}{\sqrt{\pi}} F'(x) e^{-h^2 [F(x) - M]^2}$$
 (i)

than Professor Edgeworth had previously done and that I have misrepresented his method of obtaining this equation.

(b) That I have largely profited by his theory and in fact adopted it as the basis of my own treatment.

I wish to consider briefly these two points.

(a) ydx is an elementary frequency and Kapteyn's equation can be written at once:

$$y \, \delta x = \frac{h}{\sqrt{\pi}} e^{-h^2 (F(x) - M)^2} d(F(x) - M)$$
$$= \frac{h}{\sqrt{\pi}} e^{-h^2 z^2} dz$$

if z be put for F(x) - M.

Thus whatever Kapteyn's process of deduction may be, its final result is absolutely no more than asserting that some quantity z obeys the normal law and x the observed variable is a function of this "shadow" variable z. The process is completely the same in result as stretching a normal curve with varying degrees of stretch parallel to its base.

It is perfectly true that Professor Kapteyn only reaches this result after fifteen pages of preliminary talk, but the mathematical demonstration of (i) occupies something less than a page, and it involves nothing more than the assumptions made by Professor Edgeworth (see Kapteyn, p. 16). The normal curve is actually assumed on p. 16, and the validity of the

^{*} Biometrika, Vol. iv. pp. 199-203.

assumption is just as large or small as the weight we choose to give to the three Gaussian conditions by which the normal curve is usually supported.

Further, when the assumptions have been made what is the result? Why, we are not really a bit forwarder than on the simple assumption that the general frequency-curve is:

$$y = \phi(x)$$
....(ii),

where $\phi(x)$ is perfectly arbitrary. Both (i) and (ii) involve an arbitrary function and therefore can be made to give the most general frequency distribution which is conceivable! I pointed this out years ago in criticising Professor Edgeworth's solution*.

Mathematically Kapteyn and Edgeworth seem to me to follow entirely the same path. But biologically there is a very serious flaw in Kapteyn's preliminary reasoning. He asserts that "the frequency-curve is generated under the influence of causes the effect of which is proportional to $\frac{1}{F''(x)}$ " (p. 16). No causes that we are aware of in biological or indeed sociological investigations lead to a mathematical relationship of this kind. The relationships, which actually arise between the characters and between characters and environments, are not causative, but *correlational*, and this is a fundamental distinction which Kapteyn entirely overlooks.

Accordingly I personally am unable to see any real distinction between Kapteyn and Edgeworth. They both obtain a form of equation which is no more nor less general than $y=\phi(x)$, but it is put into a form which enables them to prostrate themselves before the Gaussian fetish.

(b) Professor Kapteyn asserts that in propounding as a general form of frequency-curve the equation

$$\frac{1}{y}\frac{dy}{dx} = \frac{x+a}{f(x)}$$
(iii)

I am simply adopting the general differential equation of his curve (i). I am afraid I should look upon it as nothing more than stating in a convenient form the general result $y=\phi(x)$, for it contains the perfectly arbitrary function f(x). There is nothing more in it than this, and I should not value in the least the discovery that (iii) was the general form of frequency-curve! But if (iii) really embraces Professor Kapteyn's curve and he wishes to claim priority for this find, I have only to say that I can give him, if he desires it, conclusive evidence that (iii) has been habitually discussed in my lectures on statistics for at least five or six years, if not longer!

My custom has been to follow exactly the lines indicated in my memoir on Skew Correlation+. Namely, to give (iii) and then assume that f(x) could be expanded in the form $f(x)=S(c_nx^n)$. I then determine the values of the constants c_n by a finite difference-equation between the moments.

The Drapers' Memoir referred to above was only published in 1905, but if Professor Kapteyn looks at *Biometrika*, Vol. II. p. 281, issued in June, 1903, he will see the general formula(e) for c_n in terms of the moments given, and this was at a time anterior to my knowledge of Professor Kapteyn's paper.

In the question of an important discovery, priority by the usual scientific courtesy turns on priority of publication.

Professor Kapteyn's memoir is dated October, 1903. My formula was published in June, 1903, showing that I was then using the expression:

^{*} Phil. Mag., Jan. 1901, p. 111.

[†] Drapers' Research Memoirs, Biometric Series II. Dulau and Co.

In my opinion, however, there is absolutely no important discovery here, Kapteyn's or rather Edgeworth's (i) and my (iii) are in my opinion only convenient analytical ways of expressing the general relation (ii). My sole object in referring to the matter is to meet Professor Kapteyn's charge, that I have largely profited by his paper and the suggestion that I had invented (iii) as a differential equation to frequency distributions after the appearance of that paper.

We now, having cleared off Professor Kapteyn's first two statements, come I think to the kernel of the matter. Neither (i) nor (iii) is more general than (ii), the whole problem turns on the proper and suitable choice of F(x) in (i) or f(x) in (iii) just as it turns on a proper choice of $\phi(x)$ in (ii). Up to this point neither party has made any real progress.

Kapteyn selects $F(x) = (x + \kappa)^q$, and I selected $f(x) = S(c_n x^n)$.

The test of the merits of the two selections must depend upon certain points which I will shortly consider. But first I would meet another remark of Kapteyn's. He says I stop at c_2 , but he does not note why, although the reasons have been stated, i.e.

- (i) I have given the expressions to deduce any c_n whatever, but the higher c's depend upon the high moments, which I have shown are subject to large percentage probable errors.
- (ii) The c series converges in practice rapidly, the reducing factor being of the order of the skewness and the kurtosis, both of which are usually much smaller than unity. This is indicated by the general rough approach of most statistics as a first approximation to a Gaussian curve, and as a second approximation to a point binomial, and as a third approximation to the hypergeometrical series.
 - (iii) The sufficiency with which $f(x) = c_0 + c_1 x + c_2 x^2$ gives actual frequency distributions. These are the justifications for my own choice of f(x).

To not one of my criticisms of Professor Kapteyn's choice of F(x) does he make any reply whatever. I pointed out:

- (i) That a good frequency-curve must be a graduation formula, and that Kapteyn by making his result depend on certain total areas had shown that he failed to realise this essential condition*.
- (ii) That we ought in every frequency distribution to be able to realise the effect of the unit of grouping, but that Kapteyn's method wholly ignores this important point.
- (iii) That the probable error of every constant involved ought to be ascertainable, and this is not the case with Kapteyn's constants; he finds for one case that his constant q=0 or $q=\infty$ give both a "pretty close" representation. As the whole range of q must lie between these arithmetical values, it is clear that it cannot be an important constant which will enable us to effectively discriminate between two allied distributions†.
- * Further: constants deduced from class frequencies are never as accurate as those deduced from moments. In fact they often are very bad indeed. Thus suppose it necessary to find the standard deviations (1) by moments, (2) by areas, say from the quartiles. Sheppard (*Phil. Trans.* Vol. 192 A, p. 134) has shown that if the total frequencies are n and n', the probable errors are $.74728\sigma\sqrt{n}$ and $.91908\sigma/\sqrt{n'}$ respectively. Or, if n were 1000, n' would have to be 1513 or 50 p.c. larger to obtain as good a result. The errors resulting from this source are as serious as the failure of 'class' fitting (when only the same number of classes are taken as constants to be determined) to graduate the observations.
- † Professor Kapteyn's reply to this criticism is given above and it is, I venture to think, no reply at all. He says that it only shows "how widely different forms may be made to represent with tolerable precision the same frequency-curves." This gives the whole theory away. Any frequency distribution of n classes is absolutely determined by its moment-coefficients μ_2 , μ_3 , μ_4 ... μ_n . The class frequencies can be expressed in terms of the μ 's (Thiele) if enough are taken. Any constant therefore of the frequency distribution ought to be uniquely expressible in terms of these constants. After

- (iv) That the fundamental physical constants are not ascertainable from Kapteyn's constants, and this alone seems to me sufficient to deprive his method of all practical significance.
- (v) That his assumptions would involve the existence of a number of organic variables, the distribution of which followed a *truncated* normal curve; no such variables have been observed in the very wide biometrical experience we have had.
- (vi) Further that if they did exist, we ought to discover a number of perfectly correlated organic characters. Hundreds of correlations between organic characters have now been investigated, but no case of perfect correlation has yet been discovered.

Professor Kapteyn instead of replying to my criticisms (i) to (vi) states that he has reached a result more general than Edgeworth's. This I fail entirely to agree with and I believe no mathematical logician would agree with it either. He next asserts that I have in some way purloined his result (i) under a form (iii). My reply is that (i) or (iii) are of no importance at all until we come to select forms for the arbitrary functions involved, and that if they were of importance, I am not indebted to Professor Kapteyn for form (iii), for I used it for years and published it some months before his paper appeared.

I am quite ready to leave the result even of testing the practical value of the two series of curves as *empirical* descriptions of frequency to the computator; and this for the simple reason that Kapteyn's curves have been tested by a trained computator and fail to fit at all in certain cases where mine do fit. The source of this failure is shown in my paper; Kapteyn has not got general skewness and general kurtosis with his formula. But of this more on another occasion. Kapteyn promises us a general method of determining the analytical form of his F(x). I shall look forward to his paper with the greatest interest, for it involves indirectly no less than a revolution in physics. It amounts to the determination of the arbitrary analytical function which expresses the relation between two physical quantities, from a graph of their observed relationship. Clearly if we can find F(x) in (i), it is identical with the discovery of $\phi(x)$, the functional form of the relation between two physical characters

x and y. The solution will be of the greater value because every observed class $z = \int_{x_1}^{x_2} y dx$ is subject to the probable error $67449 \sqrt{z(1-z/N)}$ where N is the total frequency, so that the form of F(x) has to be determined analytically, not from exact knowledge, but from a knowledge that y lies with a definite amount of probability within a certain belt of varying breadth. The gain in power to the poor physicist who is too apt to select $y = S(c_n x^n)$ to describe his observation curves will be enormous.

this is done the question to be answered is: What is its probable error? Every constant used in my frequency theory is uniquely and absolutely given as soon as the moment coefficients have been ascertained and its probable error can then be found. It is accordingly an absolutely significant constant for the frequency distribution quite apart from its relation to any special form of curve. And it may be compared from one distribution to a second, without any assumption as to the goodness of fit of curves. For example, just as we can test whether μ_2 differs significantly for two distributions, so we can also test whether any function,

$$f(\mu_2, \mu_3, \dots \mu_n),$$

differs significantly, and this will be one test of true differentiation in the distributions. Thus we may test if

$$\gamma = 2\mu_2/\mu_3$$
 and $p = 4\mu_2{}^3/\mu_3{}^2 - 1$

are significantly different for two distributions. This is perfectly legitimate whether we take γ and p constants of my curve (Type III) or not; they are unique functions of the μ 's. But when Professor Kapteyn expresses his frequency in terms of a constant which may have values in the same case from 0 to ∞ , it must be obvious that he has at once destroyed the fundamental purpose of frequency investigations, which lies in testing by the theory of probable errors the difference of random samples of two populations.

II. On the Curves which are most suitable for describing the frequency of Random Samples of a Population.

BY KARL PEARSON, F.R.S.

(1) In determining the variability of random samples, or in other words in forming the probable error of a class frequency, an argument of the following kind is usually adopted: Let the chance of occurrence of an individual with a character of the given class be p, and q=1-p be the chance of an individual not of this class occurring, then if a random sample of n individuals be taken the distribution of M such random samples will have frequencies given by the terms of the binomial $M(p+q)^n$.

The first four moment coefficients of this distribution about its mean* are:

Now if n be indefinitely large,—and neither p nor q be indefinitely small,—there results $\beta_1=0$ and $\beta_3=3$, i.e. no skewness and mesokurtosis+. Accordingly, as is well known, the binomial passes over into the symmetrical (or Gaussian) normal curve of errors, with a standard deviation $c\sqrt{npq}$. The great bulk of investigators,—at least of the wiser class who know the importance of basing inferences on probable errors—are thus accustomed to content themselves with calculating the probable error of a class frequency from the formula

P.E. =
$$67449 \sqrt{npq}$$
(vi),

c, the group base, being taken as unity. The odds against the correspondence between an observed class frequency and its theoretical value are then calculated from tables of the probability integral. In other words the distribution of random samples of a class frequency is assumed to follow the normal curve

$$y=y_0e^{-\frac{1}{2}x^2/\sigma^2}$$
(vii),
 $\sigma=\sqrt{npq}$.

where

These lead to

The validity of this process for practical statistics remains unquestioned, provided n is fairly large and neither p nor q approximate to zero \ddagger . Historically this is the very problem, for the solution of which the probability integral and the normal curve were introduced.

But if any frequency distribution be examined, we find class frequencies, which are themselves small, for example often small classes towards the extreme values of the character, and it is not legitimate to put $\beta_1=0$ and $\beta_2-3=0$ and adopt the normal curve in considering the probable error of such class frequencies; for, although n be fairly large p will be very small and np, the frequency of the class in the sample, be possibly only a few units. Thus the value of 1/(npq) may easily range from unity downwards. For example, if n=1000 and np=2 or 3 we cannot possibly consider the skewness represented by $\beta_1=3$ to 5 or the kurtosis $\beta_2-3=3$ to 5 as passably corresponding to a symmetrical, mesokurtic Gaussian curve of errors.

- * Pearson: Phil. Trans. Vol. 186 A, p. 347.
- + Biometrika, Vol. iv. p. 173.
- ‡ Thus Mendelian halves and quarters with 100 to several hundred individuals in the series may be quite effectively tested in this manner.

A similar difficulty arises whatever values we take for p and q (between 0 and 1) if n itself be small, i.e. if we are dealing with random samples of small size.

To surmount this difficulty we are compelled to return to the original binomial $M(p+q)^n$.

Now the calculation of any number of the terms of this binomial is very troublesome, especially when n is large, but np small. Accordingly we need an integral which will stand as closely to the sum of the first s terms of this binomial for any values of n and p, as the normal probability integral does to the same sum when n is large and p moderate. This expression is directly and effectively provided by the curve *

$$y=y_0e^{-\gamma x}\left(1+\frac{\gamma x}{m}\right)^m \qquad \qquad \text{(viii)},$$
 where
$$m=4\left(\frac{1}{npq}-\frac{4}{n}\right)-1 \qquad \qquad \text{(ix)},$$

$$\gamma=\frac{2}{c}\,\frac{1}{p-q} \qquad \qquad \text{(x)},$$
 and
$$y_0=M/a\cdot m^{m+1}e^{-m}/\Gamma\left(m+1\right) \qquad \qquad \text{(xi)}.$$

c of course will usually be taken unity and the origin is the mode or maximum frequency. The areas of this curve give as completely as the probability integral does the odds against any observed deviation from the modal value.

It will be obvious that to find the odds against any given deviation we require the ratio of an incomplete to a complete Γ -function. Numerical tables to assist the calculation of incomplete Γ - and incomplete β -functions are nearly finished and will be shortly published.

Thus within these limits a solution is reached for the problem of the probable error of random sampling when n, p, q are anything whatever.

(2) The whole of the preceding investigation is, however, subject to a limitation which often escapes notice. We have supposed the chance of any individual arising with the character of a given class to be p, and that this chance remains constant throughout the collection of the sample. This statement of the problem is however incorrect, when the size of the sample is in any manner commensurable with the total population from which it is drawn. Such cases are by no means uncommon in the treatment of vital statistics for the case of man. Further in the consideration of determinant theories of inheritance, when the character of the individual depends on the random sampling of a finite number of determinants, the size of the sample not being small as compared with the number of selectable determinants, we are again excluded from using either the probability integral or the incomplete Γ -function for the determination of the distribution.

For example, if a cell-division leads to the exclusion of n' determinants out of N=n+n' available determinants, where n and n' are commensurable, it is not possible to approach the matter as we have done above; for in the cases treated n' is supposed large as compared with n. We accordingly reach the following more general problem:

A population consists of N individuals, Np of which possess a given character and Nq do not, what will be the distribution of frequency in this character for M random samples of magnitude n which is commensurable with N?

The solution is of course the hypergeometrical series

$$\begin{split} M \cdot \frac{pN(pN-1)\dots(pN-n+1)}{N(N-1)\dots(N-n+1)} \left\{ 1 + n \, \frac{qN}{pN-n+1} + \frac{n\,(n-1)}{1\cdot 2} \frac{qN(qN-1)}{(pN-n+1)\,(pN-n+2)} \right. \\ \left. + \frac{n\,(n-1)\,(n-2)}{1\cdot 2\cdot 3} \, \frac{qN(qN-1)\,(qN-2)}{(pN-n+1)\,(pN-n+2)\,(pN-n+3)} + \ldots \right\} \; \dots \text{(xii)}. \end{split}$$

^{*} Skew-Curve of Type III: see Phil. Trans. Vol. 186 A, p. 373.

Thus the hypergeometrical series, and not the point binomials (or their limits either the normal curve or Type III skew curve), form the general solution to the problem of random sampling.

If we wish to consider the odds against any observed deviation from the most probable result for a class frequency, we must accordingly endeavour to determine the value of the first s terms of the above hypergeometrical series. But the labour of such an investigation is great and we are naturally thrown back, as Laplace was, on the discovery of an integral which will replace the finite difference series.

I have shown* in an earlier paper what are the values of the moments of the hypergeometrical series. In the notation of the present memoir, we have

$$\begin{split} \mu_2 &= c^2 npq \left(1 - \frac{n-1}{N-1}\right)(\text{xiii}), \\ \mu_3 &= c^3 npq \left(p-q\right) \left(1 - \frac{n-1}{N-1}\right) \left(1 - \frac{2\left(n-1\right)}{N-2}\right)(\text{xiv}), \\ \mu_4 &= c^4 npq \left(1 - \frac{n-1}{N-1}\right) \left\{1 - \frac{6\left(n-1\right)}{N-2} \left(1 - \frac{n-2}{N-3}\right) \\ &+ 3pq \left(n-2\right) \left(1 - \frac{n-1}{N-2} \left[\frac{n-10}{n-2} + \frac{9}{N-3}\right]\right)\right\}(\text{xv}). \end{split}$$

The mean value is at a distance c(1+nq) from the left-hand zero start of the series, i.e. cnq from the value when the sample consists wholly of individuals with the character, and this is identical with the mean value calculated on the basis of the binomial $(p+q)^n$.

If n and N are both large, but still commensurable, the above results reduce to the simpler forms:

$$\begin{split} &\mu_2\!=\!c^2npq\left(1-\frac{n}{N}\right) & \dots & (\text{xvi}), \\ &\mu_3\!=\!c^3npq\left(p-q\right)\!\left(1-\frac{n}{N}\right)\!\left(1-\frac{2n}{N}\right) & \dots & (\text{xvii}), \\ &\mu_4\!=\!c^4npq\left(1-\frac{n}{N}\right)\!\left\{1+3npq\left(1-\frac{n}{N}\right)\!-\!6\,\frac{n}{N}\!\left(1-\frac{n}{N}\right)\!\right\} & \dots & (\text{xviii}). \end{split}$$

It will thus be clear that when the sample is commensurable with the population from which it is drawn, the standard deviation of the class frequency must no longer be taken \sqrt{npq} , but $\sqrt{npq(N-n)/(N-1)}$, a result which even if we now use tables of the probability integral will give us a very different value for the probable error in the class frequency. But it is clear that we ought not to use such probability integral tables, we ought to replace the sum of the first s terms of the hypergeometrical by an integral which gives the value of this sum with a degree of accuracy similar to that with which the probability integral in like case gives the symmetrical binomial. But such integrals representing the areas of certain curves fitting closely to the hypergeometrical series were provided by my memoir of 1895 †.

It is there shown that if

$$p$$
 lie between $\frac{1}{2} \pm \sqrt{\frac{1}{N} \left(1 + \frac{1}{N}\right)}$,

the sums of the series are closely given by the areas of the curve

$$y = \frac{y_0}{\left(1 + \frac{x^2}{a^2}\right)^m} e^{-\nu \tan^{-1} x/a} \qquad (xix),$$

* Phil. Mag. Feb. 1899, p. 239.

† Phil. Trans. loc. cit. p. 361 and seq.

$$a = \frac{1}{4} c \sqrt{4 (1 + pN) (1 + qN) - (N - 2n)^2}$$

$$\nu = \frac{N (N - 2n) (p - q)}{\sqrt{4 (1 + pN) (1 + qN) - (N - 2n)^2}}$$

$$m = \frac{1}{2} (N + 2)$$

$$(xx).$$

If on the other hand p lies outside the above limits, then the sum of the series is given by the areas of the curve

$$y = y_0 \left(1 - \frac{x}{a_1}\right)^{-\nu a_1} \left(1 - \frac{x}{a_2}\right)^{\nu a_2}$$
(xxi),

where a_1 and a_2 are the roots of the quadratic equation

$$\frac{c^{2}(n+1)(N-n+1)(1+qN)(1+pN)}{(N+2)^{2}} + \frac{cN(N-2n)(p-q)}{2(N+2)}x + x^{2} = 0$$

$$v = (N+2)/(a_{1}-a_{2})$$
.....(xxii).

and

Thus, (xix) which falls under my skew curve Type IV, and (xxii) which is included in my skew curves of Type I, complete the full solution of the problem of the random sample.

The partial integrals of (xix) and (xxi), which can be fairly easily found graphically, fall under the incomplete G-function*, and the incomplete G-function.

The incomplete Γ - and β -functions can be determined by aid of tables which have just been calculated and will shortly be published.

Thus we see that the skew curves (vi), (xix) and (xxii) directly arise in the course of our investigations when we come to deal in full generality with the problem of random sampling. But what we know so far of cell-division and determinantal theories of inheritance suggests forcibly that the character of any sub-class of a population is fixed by a random sample of a number of determinants, the size of the sample being commensurable with the number of determinants. In all such cases the distribution of frequency will approximate to the curves we have here discussed. They thus cease to be approximations in any other sense than the Gaussian or normal curve is an approximation when the probability integral is used to determine the probable error of a random sample.

It is true, indeed, that they contain a good deal more than the general theory of random samples. Thus the general frequency curve must be of the form

$$\frac{1}{y}\frac{dy}{dx}=\frac{x+a}{f(x)}.$$
 If we take
$$f(x)\!=\!c_0\!+\!c_1\frac{x}{\sigma}\!+\!c_2\left(\!\frac{x}{\sigma}\!\right)^2\!+\!\ldots\!+\!c_s\left(\!\frac{x}{\sigma}\!\right)^s\!+\!\ldots,$$

then I have given the finite difference equation which determines the successive c's in terms of the moments and shown that the convergency ratio of the successive constants is a factor (less than unity like in general the skewness and kurtosis) which vanishes for the normal curve. It will, I think, be obvious that to give the general rule for finding as many terms as we please, give their degree of convergency, and then retain three because they are found to fulfil all practical requirements is a process more legitimate than to assume every function must be of the form

$$F(x) = (x + \kappa)^q$$

and give no measure at all of the deviation from this form, and no statistical illustration (such as that of random sampling) in which such a function habitually and necessarily arises. Yet such is the course recently adopted by Professor Kapteyn and considered by him "rational" as compared with mine.

* I term the complete G-function, $G(r, \nu) = \int_0^\pi \sin^r \theta e^{+\nu\theta} d\theta$. This has been tabled by Dr A. Lee, B_*A . Report, Dover, 1899. The incomplete G-function is $G(r, \nu, \theta) = \int_0^\theta \sin^r \theta e^{\nu\theta} d\theta$, and has not yet been dealt with.

On certain Points connected with scale Order in the Case of the Correlation of two characters which for some arrangement give a Linear Regression Line.

By KARL PEARSON, F.R.S.

In a recent memoir on contingency*, I have considered the problem of what alterations can be made in scale order without sensibly modifying the value of the correlation. The problem as I there state it is as follows: To find under what other condition than normal correlation small changes in the order of grouping will not affect the value of the correlation (p. 19). The wording requires some explanation. If for any arrangement of the scales of the two variables there be normal correlation, then my memoir shows that the method of contingency gives the value of the correlation, even if the order of the scales be any whatever, in fact if the normal correlation order be absolutely unknown. Of course, if we proceed in any such case by the usual product method of determining the correlation we shall reach absolutely different results when the scale order of grouping is largely changed. My object in stating the above problem was to determine, if possible, whether any and if so what changes in the scale orders would not sensibly modify the correlation, when we still endeavoured to determine it, not by contingency, but by the method of products. The conclusion I came to was as follows—that with any distribution with linear regression "small changes (i.e. such that the sum of their squares may be neglected as compared with the square of mean or standard deviation) may be made in the order of grouping without affecting the correlation coefficient" (p. 35). I think this conclusion is quite sound, and deserves further consideration. Although in the statement of the proposition I have used the word "small changes" in scale order (p. 19) and in the summary of my memoir (p. 35) stated what is to be understood by small, in this case, I think, as Mr G. U. Yule points out to me, that the wording on p. 20 is too unguarded, if the reader has not been sufficiently impressed with the wording on p. 19, or reached the summary on p. 35. It will not be without value possibly to give the actual algebraical result on which the statement on p. 35 is based, for it has some importance for the general philosophical idea of correlation.

Let x and y represent the two variable characters and let $u\delta x$ be the frequency of the character between x and $x + \delta x$; $v \delta y$ that of the character between y and $y + \delta y$; u and v being functions of x and y respectively and the distribution of the frequencies being of any nature. Now suppose the array $v_s \delta y_s$ of frequency between y_s and $y_s + \delta y_s$ to be bodily interchanged in position with the array $v_{s'}\delta y_{s'}$ between $y_{s'}$ and $y_{s'}+\delta y_{s'}$. Let N be the total frequency, and suppose the mean \overline{y} to become $\overline{y} + \delta \overline{y}$, the standard deviation σ_y of the y character to become $\sigma_{\nu} + \delta \sigma_{\nu}$. Then we have:

or

^{* &}quot;Mathematical Contributions to the Theory of Evolution, III. On the Theory of Contingency and its Relation to Association and Normal Correlation." Drapers' Research Memoirs (Dulau and Co. London).

Hence we see that $\delta \sigma_y$ is small, if the frequencies of interchanged subgroups are small as compared with N and accordingly:

$$\delta\sigma_y/\sigma_y = \frac{v_{s'}\delta y_{s'} - v_s\delta y_s}{V} \frac{(y_s - y_{s'})}{\sigma_y} \frac{y_s - \overline{y} + y_{s'} - \overline{y}}{2\sigma_y} \dots (ii).$$

We now turn to the change in the product-moment.

Thus

$$P + \delta P = S\left(mxy\delta x\delta y\right) - v_{s'}\delta y_{s'}\overline{x}_{s'}\left(y_{s'} - y_{s}\right) - v_{s}\delta y_{s}\overline{x}_{s}\left(y_{s} - y_{s'}\right) - N\overline{x}\left(\overline{y} + \delta y\right),$$

where $w\delta x\delta y$ is the total frequency of individuals, with characters between x and $x + \delta x$ and y and $y + \delta y$ and \overline{x}_s and $\overline{x}_{s'}$ are the means of the arrays corresponding to y_s and $y_{s'}$. But $P = S(wxy\delta x\delta y) - N\overline{xy}$, hence:

$$\begin{split} &\delta P = (y_s - y_{s'}) \, \langle (\overline{x}_{s'} - \overline{x}) \, v_{s'} \delta y_{s'} - \langle \overline{x}_s - \overline{x} \rangle \, v_s \delta y_s \rangle, \\ &\delta P / P = \frac{y_s - y_{s'}}{\sigma_y} \left(\frac{\overline{x}_{s'} - \overline{x}}{r\sigma_x} \, \frac{v_{s'} \delta y_{s'}}{N} - \frac{(\overline{x}_s - \overline{x})}{r\sigma_x} \, \frac{v_s \delta y_s}{N} \right) . \end{split} \tag{iii}.$$

Now if r be the correlation before and $r+\delta r$ after a change is made, we have, since $r=P/(N\sigma_x\sigma_y)$,

$$\frac{\delta r}{r} = \frac{\delta P}{P} - \frac{\delta \sigma_x}{\sigma_x} - \frac{\delta \sigma_y}{\sigma_y} \dots (iv).$$

Now we have supposed at present no change to be made in the x's; thus we may treat $\delta \sigma_x$ as zero, and using (ii) and (iii) we have, rearranging:

$$\begin{split} \frac{\delta r}{r} &= \frac{y_s - y_{s'}}{r\sigma_y\sigma_x} \left[\frac{v_{s'}\delta y_{s'}}{N} \left\{ \overline{x}_{s'} - \overline{x} - \frac{r\sigma_x}{\sigma_y} (y_{s'} - \overline{y}) \right\} - \frac{v_s\delta y_s}{N} \left\{ \overline{x}_s - \overline{x} - \frac{r\sigma_x}{\sigma_y} (y_s - \overline{y}) \right\} \right] \\ &\quad - \frac{(y_s - y_{s'})^2}{2\sigma_y^2} \frac{v_{s'}\delta y_{s'} + v_s\delta y_s}{N} \quad \dots \dots (v). \end{split}$$

Now suppose the regression to be originally linear, then we have $\bar{x}_s - \bar{x} = \frac{r\sigma_x}{\sigma_y}(y_s - \bar{y})$ not only for s and s' but for all values of s whatever. In other words the whole series of terms in square brackets vanishes and summing for all pairs of interchanges:

$$\frac{\delta r}{r} = -\frac{S\left(y_s - y_{s'}\right)^2 \left(v_{s'} \delta y_{s'} + v_s \delta y_s\right)}{2 N \sigma_y^2} \qquad (vi).$$

If we make similar interchanges of x_p and $x_{p'}$ we can show that*:

$$\begin{split} \frac{\delta r}{r} &= -\frac{S\left(y_{s} - y_{s'}\right)^{2}\left(v_{s'}\delta y_{s'} + v_{s}\delta y_{s}\right)}{2N\sigma_{y}^{2}} - \frac{S'\left(x_{p} - x_{p'}\right)^{2}\left(u_{p'}\delta x_{p'} + u_{p}\delta x_{p}\right)}{2N\sigma_{x}^{2}} \\ &+ \frac{S'''\left(y_{s} - y_{s'}\right)\left(x_{p} - x_{p'}\right)\left(w_{1}\delta x_{p}\delta y_{s} - w_{2}\delta x_{p'}\delta y_{s} - w_{3}\delta x_{p}\delta y_{s'} + w_{4}\delta x_{p'}\delta y_{s'}\right)}{Nr\sigma_{x}\sigma_{y}} \ \dots (\text{vi}) \ \text{bis.} \end{split}$$

Here S denotes a summation or integration for all possible interchanges of the y arrays, i.e. say, columns of the correlation table; and S' denotes a like summation for all possible interchanges of the x-arrays, say the rows of the table. S''' is a summation involving the frequency at all points where interchanged rows and columns cross. Of course this result assumes that the units of grouping of both characters are so "fine" that the squares of the ratios of the array frequencies to the total frequency are negligible.

We may now draw some interesting conclusions from (vi). Suppose the material to be such that the correlation is linear under some arrangement. Then for slight interchanges the squares and products of the interchanges are negligible and δr will be zero. Thus, r being positive, we

* The reader will find a verification of this formula arising from writing (i) the correlation table with its columns inverted, then $\delta r/r=-2$, and (ii) again in addition with its rows written backwards, in this case $\delta r/r=0$. In (i) the first term only remains and its numerator $=4N\sigma_y^2$. In the second case the numerators of the three terms are respectively $4N\sigma_y^2$, $4N\sigma_x^2$ and $4Nr\sigma_x\sigma_y$.

see from (vi) that r is an absolute maximum. Clearly $\delta r/r$ is always negative even for interchanges between arrays at considerable distances. Or, we conclude that if there be one arrangement of the material for which the regression line is linear, then any interchanges, however extensive; will reduce the value of the correlation as calculated by the product moment method. This conception of the linear regression line as giving the arrangement with the maximum degree of correlation appears of considerable philosophical interest. It amounts practically to much the same thing as saying that if we have a fine classification, we shall get the maximum of correlation by arranging the arrays so that the means of the arrays fall as closely as possible on a line.

Further, if the mean square of the interchanges, i.e. the expression

$$\frac{S\left(y_{s}-y_{s'}\right)^{2}\left(v_{s'}\delta y_{s'}+v_{s}\delta y_{s}\right)}{2N},$$

be small as compared with the standard deviation squared, i.e. σ_y^2 , then the change δr will not be sensible. In other words *small* changes in the scale ordering, not confined to adjacent or even to two arrays, will not sensibly modify the correlation as found by the product moment method.

Lastly, considering the proof of (vi) we see that no portion of the investigation is dependent on the whole of the one y-array being interchanged with the whole of another. We may consider $v_s\delta y_s$ and $v_{s'}\delta y_{s'}$ as only portions of the total array—to be taken, however, proportionately from all its constituents. Now let $V_s\delta y_s$ and $V_{s'}\delta y_{s'}$ denote the whole of the frequency of the two arrays, and write the first array $V_s\delta y_s+\frac{1}{2}m-\frac{1}{2}m$ and the second array $V_{s'}\delta y_{s'}-\frac{1}{2}m+\frac{1}{2}m$. Now transfer the $-\frac{1}{2}m$ of the first array to the position of the second and the $+\frac{1}{2}m$ of the second to the position of the first, i.e. take $v_s\delta y_s=-\frac{1}{2}m$ and $v_{s'}\delta y_{s'}=+\frac{1}{2}m$; it follows that $v_s\delta y_s+v_{s'}\delta y_{s'}=0$ and the two arrays are

$$V_s \delta y_s + m$$
 and $V_{s'} \delta y_{s'} - m$,

i.e. exactly the values they would have had if a portion of the second array drawn at random from all its sub-groups had been inscribed in the same sub-groups of the first array. But in this case we see since $v_s \delta y_s + v_{s'} \delta y_{s'} = 0$, that (vi) will give us absolutely $\delta r = 0$, or there will be no change in the correlation. This result seems of considerable value. Suppose the regression linear, and one character, x say, easily measured or known; then if a number m of individuals which ought to fall into a given class of y, be shifted by oversight or error of judgment into a second erroneous class of y, this will not sensibly affect the correlation, if N being the total frequency, the square of the ratio m/N is negligible, as compared with its first power. Thus suppose in correlating age with hair tint, the first character being accurately known, an observer were to place his series of contributory observations of hair tint in the wrong group, say in one of the brown reds instead of pure browns, this would not sensibly modify the resulting correlation. The fact that the error would not produce a modification is not in the first place due to the possible smallness of the misplaced group. The product moment is changed and the standard deviation is also modified, but the modification of the correlation depends on such manner on the changes of these two, that they act in opposite senses and cancel the modification, provided the original regression was strictly linear.

While not desiring to encourage carelessness in observing or tabling or in the formation of scale orders without due consideration, still the results of this note seem to indicate that in many cases absolute unanimity of judgment in classifying or great stress on small details of scale grouping are not needful in order to reach sensibly identical values of the correlation. This view coincides with my actual and not unique experience, when having been in grave doubt as to where 30 or 40 individuals were to be placed, I put them first in one category and then in a second, only to find out that the correlation worked out with the group first in one and then in the other category was sensibly identical. The theorems developed in this note seem to explain this stability—when we use not contingency but product moment methods, and suppose the regression ultimately linear.

IV. On the Classification of Frequency-ratios †.

By D. M. Y. SOMMERVILLE, D.Sc.

In statistical work which deals with integral variates, the data frequently appear in the form of ratios, or unreduced proper fractions; and to facilitate comparison these are arranged in classes according to magnitude, all the ratios falling within the same class being considered as equivalent. The problem then arises to find the best distribution of the fractions so that there may be approximately the same number in each class; or, if the fractions with various denominators do not all occur with the same frequency so that it is necessary to assign to them certain weights, to find the distribution which will make the total weight of each class approximately the same.

I. Let */p denote any proper fraction with the denominator p, and */p the assemblage of all the proper fractions whose denominators do not exceed n. The following theorem is then established:

If the fractions $*/\overline{\geqslant n}$ are distributed into n classes, $\frac{0}{n}$ to $\frac{1}{n}$, $\frac{1}{n}$ to $\frac{2}{n}$, ..., $\frac{n-1}{n}$ to $\frac{n}{n}$, and any fraction which falls between two classes is counted $\frac{1}{2}$ in each of these two classes, each of the others being counted 1 in the class in which it occurs, then in each class there will fall $\frac{1}{2}(n+1)$ fractions, except in the extremes which contain $n+\frac{1}{2}$.

[If the fractions at the extremes, $\frac{0}{1}$, $\frac{0}{2}$, ..., $\frac{0}{n}$; $\frac{1}{1}$, $\frac{2}{2}$, ..., $\frac{n}{n}$, are also counted $\frac{1}{2}$ there will be $\frac{1}{2}(n+1)$ fractions in the extreme classes also.]

This is the normal distribution (N.D.).

There are three other "even" distributions:

- (1) n-1 classes, $\frac{1}{2}(n+2)$ in each, extremes $n+\frac{3}{2}$.
- (2) n+1 classes, $\frac{1}{2}n$ in each, extremes n.
- (3) n+2 classes, $\frac{1}{2}(n-1)$ in each, extremes n.

These are obtained from the N.D. for n-1, n+1, n+2 respectively.

Then by making pairs of classes coalesce, from the second onwards, we get the following evenest distributions:

- (1) n even: $\frac{1}{2}n+1$ classes, 0 to $\frac{1}{n}$, $\frac{1}{n}$ to $\frac{3}{n}$, ..., n+1 in each, extremes $n+\frac{1}{2}$.
- (2) $n \cdot \text{odd}$: $\frac{1}{2}(n+3)$ classes, 0 to $\frac{1}{n+1}$, $\frac{1}{n+1}$ to $\frac{3}{n+1}$, ..., n in each.

The N.D. can be easily written down. To find the classes in which */p occurs, divide $n, 2n, 3n, \ldots$ by p; let q_1, q_2, q_3, \ldots be the quotients and f_1, f_2, f_3, \ldots the remainders. Then if $f_s \neq 0, \frac{s}{p}$ lies in the $(q_s + 1)$ th class, but if $f_s = 0, \frac{s}{p} = \frac{q_s}{n}$ and $\frac{s}{p}$ lies $\frac{1}{2}$ in the q_s th and $\frac{1}{2}$ in the $(q_s + 1)$ th class. Each class must contain either */p or */n - p, and if any class contains both,

† Abstract by the Author of a paper "On the Distribution of the Proper Fractions," by D. M. Y. Sommerville, D.Sc., Proc. Roy. Soc. Edin. Vol. xxxvi. (1906), pp. 116—129.

each of them is counted $\frac{1}{2}$. Writing the classes horizontally with the fractions $*/\overline{p}$ in columns under their respective denominators, the N.D. for n=12 is represented as follows:

1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	0	0	0	0	0	0_1
					ī	1	1	1	1	1	ī_2
-			ī	1	ī		$\overline{2}$	2	2	2	$\overline{2}_{\overline{3}}$
		ī	ī		$\overline{2}$	2	$\overline{2}$	$\overline{3}$	3	3	34
		ī		2	$\overline{2}$		3	$\bar{3}$	4	4	$\overline{4}_{\overline{5}}$
	Ī.		$\overline{2}$		3	3	$\overline{4}$	4	$\overline{5}$	5	<u>5</u> 6
	ī		$\overline{2}$		3	4	$\overline{4}$	5	5	6	<u>6</u> 7
		$\overline{2}$	-	3	$\frac{3}{4}$	-	5	$\overline{6}$	6	7	$\frac{7}{7_8}$
		$\overline{2}$	$\ddot{3}$		$\overline{4}$	5	$\overline{6}$	$\overline{6}$	7	8	89
			$\ddot{3}$	4	5		$\overline{6}$	7	8	9	$\overline{9}_{\overline{10}}$
					$\overline{5}$	6	7	8	9	10	$\overline{10}_{\overline{1}\overline{1}}$
1	2	3	4	5	6	7	8	9	10	11	11112

A bar denotes that the fraction is counted $\frac{1}{2}$.

II. Giving weights μ_p to the various denominators and expressing that the normal distribution is even, we get a series of equations,

$$\mu_p = \mu_{n-p}$$

i.e. the frequency-curve for the denominators must be symmetrical.

If we divide the fractions $*/ \nearrow n$ into n+m classes, then we have to divide the fractions $*/ \nearrow (n+m)$ normally and consider $\mu_p=0$ if p>n and therefore also if p< m. Also if $p \ge m$, $\mu_p=\mu_{n+m-p}$. Hence if the frequency-curve is symmetrical from m to n (n+m being even), and if the denominators < m may be neglected, we may divide the fractions $*/ \nearrow n$ into n+m classes, and then make pairs of classes from the second onwards coalesce. We have then the distribution

into
$$\frac{1}{2}(n+m+2)$$
 classes, 0 to $\frac{1}{n+m}$, $\frac{1}{n+m}$ to $\frac{3}{n+m}$, ..., each of weight $\sum_{p=m}^{p=n} \mu_p$.

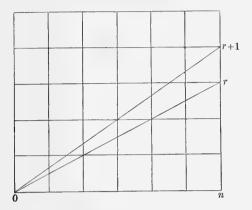
The general case where the frequency-curve is skew is not solved, but by considering it as symmetrical about the mode, e.g., and neglecting the lower denominators, as above, it may be possible to obtain an approximate solution, provided the mode lies among the higher denominators.

For other results which are only true when the extreme fractions are counted $\frac{1}{2}$ we may refer to the complete paper.

The following graphical method of obtaining the first theorem was communicated to me by Professor Steggall.

Any positive fraction can be represented uniquely in the positive region of the plane by a point whose coordinates x, y are respectively the numerator and denominator. The lines y=0, x=y, x=n will then confine all the proper fractions $*/\!\!\!>\!\!\!> n$. These are divided into the classes described above by the lines rx=ny (r=0, 1, ..., n). The number of fractions in the class

r/n to (r+1)/n is then the number of representative points confined between the lines rx=ny, (r+1)x=ny, i.e. $\frac{1}{2}(r+2)(n+1)-\frac{1}{2}(r+1)(n+1)=\frac{1}{2}(n+1)$, counting 0/0 as $\frac{1}{2}$. This fraction, which occurs in each class, disappears when we make the subtraction, and we have the result stated above.



V. Note on the Significant or Non-significant character of a Sub-sample drawn from a Sample.

By KARL PEARSON, F.R.S.

If two independent samples be drawn from an indefinitely large group or population, and their means be m and M' and their sizes n and N', and their standard deviations σ and Σ' , then the usual test of significant and non-significant difference in type is made by comparing the difference of mean m-M' with the probable error of this difference '67449 $\sqrt{\sigma^2/n + \Sigma'^2/N'}$. This process may be considered as legitimate, if the samples are absolutely independent and drawn from an indefinitely large population.

It has become not unusual to apply this test to cases of the following kind, where its application has yet to be justified: a population is described by a sample, say N in size, M in type and Σ in variability. This sample is obtained from p localities, or if in one locality by p methods or instances, or generally there is a p-fold heterogeneity in its collection. One of the p sub-groups of the sample is defined by n, m and σ . It is frequently assumed that the proper test for significant or non-significant difference between the sub-sample and the general sample

is the relative magnitude of
$$m-M$$
 and $\cdot 67449 \sqrt{\frac{\sigma^2}{n} + \frac{\Sigma^2}{N}}$. This treatment is, I think, erroneous.

To begin with it must be observed that as the sub-sample is made larger and larger, the value of its mean must approach closer and closer to that of the general sample, and thus the probable error of the difference ought to be less and less and ultimately vanish. Instead of this it approaches the finite value $\cdot 67449 \sqrt{2\Sigma^2/N}$. Clearly the above expression for the probable error of the difference of types in sub-sample and sample is not correct. We have yet to ascertain how far it is approximate, when N is large as compared with n.

The sort of problem to which the above doubtful process is applied is of the following kind, for example: a general sample of the population is found to have q per cent. of its members

affected by a certain disease or associated with a certain characteristic. A sub-sample marking a class or locality is found to have q' of its members thus differentiated. Does the group marked by the sub-sample differ significantly from the general sample out of which it is drawn? Or, again, do children of a particular parentage differ in physique from those of the general population, the test being made on a sample and a sub-sample of the school population?

I would suggest the following method of approaching the problem. Consider the general sample (N, M, Σ) to consist of two component samples, the sub-sample (n, m, σ) and all the remainder (N', M', Σ') . Then if the whole sample be homogeneous and random, and the two components also homogeneous and random, their difference of types m-M' will have for its probable error:

$$E_{(m-M')} = 67449 \sqrt{\frac{\sigma^2}{n} + \frac{\Sigma'^2}{N'}}.$$

The test therefore of the difference being due to random sampling is the relative magnitude of

$$m-M'$$
 and $E_{(m-M')}$.

But if we consider the general sample we have at once:

$$\begin{split} N &= N' + n, & \text{or}: \quad N' &= N - n, \\ M &= (N'M' + nm)/N, & \text{or}: \quad M' &= M + \frac{n}{N - n} (M - m), \\ N \Sigma^2 &= n \left\{ \sigma^2 + (m - M)^2 \right\} + N' \left\{ \Sigma'^2 + (M - M')^2 \right\}, \\ \Sigma'^2 &= \frac{N \Sigma^2 - n \sigma^2}{N - n} - \frac{n N}{(N - n)^2} (M - m)^2. \\ m &- M' &= \frac{N}{N - n} (m - M), \\ \frac{\Sigma'^2}{N'} + \frac{\sigma^2}{n} &= \left(\frac{N}{N - n} \right)^2 \left(\frac{\Sigma^2}{N} + \frac{\sigma^2}{n} \left(1 - \frac{2n}{N} \right) - \frac{n (M - m)^2}{N (N - n)} \right). \end{split}$$

or:

Accordingly:

Or we must compare the relative magnitude of:

$$\frac{N}{N-n}(m-M) \quad \text{and} \quad 67449 \frac{N}{N-n} \sqrt{\frac{\Sigma^2}{N} + \frac{\sigma^2}{n} \left(1 - \frac{2n}{N}\right) - \frac{n(M-m)^2}{N(N-n)}}.$$

In other words, the probable error of the difference in type of the general sample and the sub-sample, or of m-M, is:

$$\cdot 67449 \sqrt{\frac{\Sigma^2}{N} + \frac{\sigma^2}{n} \left(1 - \frac{2n}{N}\right) - \frac{n(M-m)^2}{N(N-n)}}.$$

This expression satisfies the requisite condition of becoming zero as the sub-sample increases in magnitude up to the value of the general sample.

Now if N be large as compared with n, clearly the important term in this expression is σ^2/n and M-m will be of the order $v\sqrt{\sigma^2/n}$, where v is a small integer, 1, 2 or 3, say. Hence the order of the last term in the root is:

$$v^2\sigma^2/N^2$$

or, since σ will not differ very widely from Σ , we may say $v^2 \Sigma^2 / N^2$. Now the probable error of Σ is $67449 \frac{\Sigma}{\sqrt{2N}}$ and accordingly if we put $\Sigma \left(1 \pm \frac{67449}{\sqrt{2N}}\right)$ for Σ we should not alter significantly the first term under the radical; thus Σ^2 / N may be read:

$$\frac{\Sigma^2}{N} \left(1 \pm \frac{\cdot 67449}{\sqrt{2N}} \right)^2 \text{ or } \frac{\Sigma^2}{N} \left\{ 1 \pm \frac{w}{\sqrt{N}} \right\},$$

where w is a small number. But n being small the first and last terms give:

$$\frac{\Sigma^2}{N} \left(1 - \frac{v^2}{N} \right) = \frac{\Sigma^2}{N} \left\{ 1 - \frac{w}{\sqrt{N}} \times \frac{u}{\sqrt{N}} \right\},\,$$

u being a small number. But u/\sqrt{N} will then be very small. Accordingly if n be small, the last term in the radical is sensibly smaller than the probable error of the first and we may read for the probable error of m-M the expression:

$$\cdot 67449 \sqrt{\frac{\Sigma^2 - 2\sigma^2}{N} + \frac{\sigma^2}{n}}.$$

Further the probable error of the difference or sum of Σ^2 and σ^2 is of the order of $\frac{2\sigma^2}{\sqrt{2n}}$ and thus to a first approximation we might put in the smaller term or first term $\sigma^2 = \Sigma^2$. There results:

$$\cdot 67449 \sqrt{\frac{\sigma^2}{n} - \frac{\Sigma^2}{N}}.$$

In other words, when the number of a sub-sample is very small, the probable error of m-M approaches $\cdot 67449 \sqrt{\frac{\sigma^2}{n} - \frac{\Sigma^2}{N}}$ and not $\cdot 67449 \sqrt{\frac{\sigma^2}{n} + \frac{\Sigma^2}{N}}$. Our only excuse for using the latter form would be the negligibility altogether of the term Σ^2/N . In which case it would be better à priori to adopt the value $\cdot 67449 \sqrt{\sigma^2/n}$. It will be clear therefore that the value frequently adopted is not justified when a sub-sample is tested against a general sample. The proper method seems to be to compare: m-M with $\cdot 67449 \sqrt{\frac{\sigma^2}{n} - \frac{2\sigma - \Sigma^2}{N} - \frac{n(M-m)^2}{N(N-n)}}$.

Now let it be reasonable to suppose a quantity significant when it is β times its standard deviation, or $\beta/67449$ times its probable error, then we have for significance test:

$$m - M > \beta \sqrt{\frac{\sigma^2}{n} - \frac{2\sigma^2 - \Sigma^2}{N} - \frac{n(M - m)^2}{N(N - n)}}.$$
Or:
$$m - M > \beta \sqrt{\frac{\sigma^2}{n} - \frac{2\sigma^2 - \Sigma^2}{N}} / \sqrt{1 + \frac{\beta^2 n}{N(N - n)}};$$

and this is true whatever be the magnitudes of N and n. If it be said that the right-hand side is always less than $\beta \sqrt{\frac{\sigma^2}{n} + \frac{\Sigma^2}{N}}$, and that accordingly significance cannot have been asserted to exist, where it is not existent, this is perfectly true. But there is another side to this fact, too often forgotten. No samples suffice to demonstrate the absolute absence of differentiation; the statistician can only say: Relatively to the size of my samples, I find no significant differentiation. It may after all be there and would be demonstrated if the samples were tenfold as large. The absence of significance relatively to the size of the samples is too often interpreted by the casual reader as a denial of all differentiation, and this may be disastrous. Hence if the statistician using too large a value of the probable error errs on the side of safety, when he asserts significant differentiation for certain cases A, B, C, \ldots , but that he has not found it for E, F, G, \ldots , this may strengthen his demonstration in the first cases, but it weakens any influence as to non-significance in the latter cases.

Using the above formula it may be that a considerable number of cases, for which no proof of significant differentiation has been given,—and which have been taken accordingly as having no differentiation,—can now be demonstrated to have significant differentiation. And this appears of some importance.

Several other cases of probable error tests of significance deserve reconsideration, and I hope to find time to publish my notes on them shortly.

VI. Professor Ziegler and Galton's Law of Ancestral Inheritance.

In the published account (Jena, 1905) of the lecture on "Die Vererbungslehre in der Biologie" delivered by Professor Ziegler before the "XXII Congress für innere Medizin" the following footnote occurs:

"Da die grosselterlichen Anteile bei den einzelnen Enkeln nicht gleichmässig sind, so kann auch das von Galton formulierte Vererbungsgesetz nicht richtig sein. Es lautet so: Die Veranlagung eines Kindes setzt sich in folgende Weise aus den Vererbungsanlagen seiner Vorfahren zusammen; von den Eltern 50 prozent, von den Grosseltern 25 prozent, von den Urgrosseltern 25 prozent u.s.w.

F. Galton, Natural Inheritance, London, Macmillan, 1889.

Ders., The average Contribution of each several Ancestor to the total Heritage of the Offspring. *Proceedings of the Royal Society of London*, Vol. LXI. pp. 401—413, 1897."

If Professor Ziegler had read with understanding even the title of the second of the two works that he mentions, he would have seen that the Law of Ancestral Inheritance formulated by Galton makes no statement whatsoever concerning the relative shares of each several ancestor in any single case. Thus the question as to whether all the grandchildren of one particular grandparent receive the same or different contributions from him towards their total heritage has no bearing whatsoever on this law.

It is unnecessary in the pages of *Biometrika* to dwell further on this point, but perhaps one may be permitted to express some surprise that a man of Professor Ziegler's standing, in a lecture on heredity, in which space is found to enlarge on unproved and unproveable theories concerning chromasomes, should relegate to a footnote, and there completely misrepresent, such an important contribution to the subject as Galton's Law of Ancestral Inheritance.

EDGAR SCHUSTER.

VII. Variazione ed Omotiposi nelle inflorescenze di Cichorium Intybus L.

DAL DR FERNANDO DE HELGUERO, Roma.

Nella presente nota si studia la *Variazione* del numero dei fiori nelle infiorescenze di Cichorium Intybus L. e la *Omotiposi*, cioè la correlazione esistente fra le infiorescenze della stessa pianta.

Il materiale consta di 1000 infiorescenze raccolte durante il mese di Agosto 1905 a S. Leucio (Provincia di Caserta, Italia), appartenenti a 624 piante diverse. Questo materiale forma oggetto di due studi distinti, il primo riguardante la Variazione del carattere in esame, il secondo la Omotiposi.

1. Variazione.

Le 1000 infiorescenze sono state divise in tre gruppi a seconda che la pianta che le portava presentava o no altre infiorescenze. Il primo gruppo riguarda piante con una sola infiorescenza,

il secondo comprende le infiorescenze portate da piante con 2 infiorescenze, il terzo le infiorescenze portate da piante che ne avevano 3 od un numero maggiore :

Nº dei fiori		Totale		
	1º Gruppo	2º Gruppo	3º Gruppo	Totale
8 9 10 11 12 13 14 15 16 17	2 7 28 107 126 84 27 7 1	1 5 13 80 98 76 16 7 3	1 9 14 72 86 73 47 8 1	4 21 55 259 310 233 90 22 5
Totale	389	300	311	1000

Questi gruppi danno i seguenti parametri:

	M	σ	$100\sigma/M$
1° Gruppo 2° Gruppo 3° Gruppo	11.931 12.070 12.206	1·2262 1·2484 1·3409	10·28 10·34 10·98
Totale	12.056	1.2716	10.54

Si vede dalla tabella che le infiorescenze appartenenti a piante più vicine al massimo di fioritura (con più fiori) hanno una media più elevata.

Questo è confermato dalle medie parziali dei varî lotti corrispondenti alle diverse raccolte delle infiorescenze. Le piante furono raccolte in 5 diverse volte durante il mese di Agosto e perciò nel periodo decrescente della fioritura: Ecco le medie parziali:

	\mathbf{Medie}
1º Lotto	12.235
2º Lotto	12:321
3° Lotto	11.945
4º Lotto	11.905
5° Lotto	11.810.

Studiamo il poligono empirico di frequenza per l'intiero gruppo delle 1000 infiorescenze.

Si trova
$$\mu_2 = 1.6169, \qquad \beta_1 = .01252,$$

$$\mu_3 = .2300, \qquad \beta_2 = 3.44728,$$

$$\mu_4 = 9.012, \qquad \sigma + 3\beta_1 - 2\beta_2 = -.857.$$

E la curva normale sarebbe:

$$y = 313.74e^{-\frac{(x-12.056)^2}{3.23372}}$$
.

Ecco la tabella dei valori calcolati y confrontati cogli empirici y':

x	y'	y	<i>y'</i> – <i>y</i>
7 8 9 10 11 12 13 14 15 16 17		11-9 17-5 84-9 222-3 313-4 238-2 97-6 21-5 2-6	$ \begin{array}{rrrrr} & - & \cdot 1 \\ & + & 2 \cdot 1 \\ & + & 3 \cdot 5 \\ & - & 29 \cdot 9 \\ & + & 36 \cdot 7 \\ & - & 3 \cdot 4 \\ & - & 5 \cdot 2 \\ & - & 7 \cdot 6 \\ & + & 2 \cdot 4 \\ & + & 1 \end{array} $

L'area racchiusa fra i due poligoni calcolata col metodo di Duncker è del 3·45 °/. La rappresentazione è perciò soddisfaciente*. La curva è tracciata nella figura 1°.

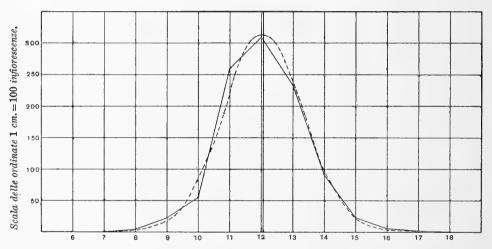


Fig. 1. Variazione del Cichorium Intybus L. (1000 inflorescenze.)

Poligono empirico.

---- Curva normale.

Equazione $y = 313.74e^{-\frac{(x-12.065)^2}{3.23372}}$.

Riguardo alla Variazione noi poniamo le seguenti conclusioni:

- 1°. La moda nella Variazione del numero dei fiori nelle infiorescenze di Cichorium Intybus L. è 12 : perciò non un numero della serie del Fibonacci.
 - 2º. La Variazione è normale coi parametri

$$M = 12.056$$
, $\sigma = 1.2716$, $\frac{100\sigma}{M} = 10.54$.

[* $\sqrt{\beta_1}$ is $2\cdot 1$ and $\beta_2 - 3$ is $4\cdot 3$ times the probable error, the distribution therefore probably differs significantly from the normal curve. Further, $\chi^2 = 20$ about, and $P = \cdot 02$, or the odds are about 50 to 1 against such divergence from normality. Eds.]

3°. Nelle piante più vicine al massimo di fioritura la media è più elevata che nelle altre : riguardo alla variabilità non possiamo asserir nulla per quanto le cifre esposte nelle tabelle lascino dei sospetti che anche essa sia maggiore.

2. Omotiposi.

Per lo studio della Omotiposi non si deve che seguire le norme date dal Prof. Pearson nella memoria: "On the principle of Homotyposis etc., Part I, Homotyposis in the vegetable Kingdom," *Phil. Trans. of the R. Soc.* A, Vol. 197, pp. 285–379, memoria del più grande valore biologico e fondamentale in queste ricerche.

Il modo di trattare i dati è del tutto identico a quello della "fraternal inheritance."

Le nostre 624 piante appaiono così distinte a seconda del numero di infiorescenze che portavano al momento della raccolta :

piante	con 1	sola infiorescenza	389
,,	2	infiorescenze	150
,,	3	77	50
"	4	,,	20
"	5	"	11
"	6	,,	2
22	7	"	_2
		Totale	624

Le coppie di infiorescenze delle piante aventi 2 sole infiorescenze danno la seguente tavola di correlazione, resa simmetrica :

Tavola di correlazione per le piante aventi 2 inflorescenze.

	8	9	10	11	12	13	14	15	16	17	Totale	
8 9 10 11 12 13 14 15 16 17	1 - - - - -	2 - 2 - 1 -	1 -6 2 3 1 -	2 6 34 33 4 1 —	33 34 29 —	3 4 29 34 6 —	$ \begin{array}{c c} & 1 \\ & 1 \\ & 1 \\ & 6 \\ & 4 \\ & 3 \\ & - \end{array} $	3 4		- -	1 5 13 80 98 76 16 7 3	Media 12.07; $\sigma = 1.2484$.
Totale	1	5	13	80	98	76	16	7	3	1	300	

Si trova

$$\rho = .5915.$$

Si sono poi utilizzate le piante aventi più di due infiorescenze, considerando ogni pianta tante volte quante sono le coppie che si posson formare colle sue infiorescenze prese due a due. Per esempio, una pianta con 7 infiorescenze figura per $\frac{7\times 6}{2}$ =21 piante distinte.

In tal modo con tutte le piante aventi più di una infiorescenza si è fatta la tavola :

Tavola di correlazione per tutte le piante aventi più di una infiorescenza.

	8	9	10	11	12	13	14	15	16	17	Totale	
8 9 10 11 12 13 14 15 16 17	1 1 1 2 	1 2 2 15 10 1 2 —	1 2 8 19 11 4 1 —	1 15 19 134 90 18 1	2 10 11 90 114 97 9 4	1 18 97 122 53 2 —	2 1 1 9 53 96 10	- - 4 2 10 10 3		 - - - - - -	5 33 46 278 337 297 172 29 6	$M = 12.2226$; $\sigma = 1.3536$.
Totale	5	33	46	278	337	297	172	29	6	1	1204	

Si trova

$$\rho = 6130.$$

I risultati concordanti delle due tavole ci permettono di enunciare la conclusione evitando le obbiezioni che ad esse singolarmente potrebbero farsi: alla prima, di basarsi sopra un numero troppo scarso di coppie, alla seconda, di dare un' eccessiva importanza alle piante con molte infiorescenze.

Dobbiamo ora confrontare la variabilità delle singole piante colla variabilità generale : ma ciò non ci è possibile direttamente per il numero troppo scarso di infiorescenze portate da ciascuna pianta.

Perciò ho seguito invece il metodo del Prof. Pearson calcolando la deviazione normale di ciò che egli chiama un "array," un gruppo, limitandomi alle piante portanti 2 sole infiorescenze.

Ho perciò raggruppato tutte le piante di cui una infiorescenza ha un numero fisso m di fiori ed ho calcolato la deviazione normale delle altre infiorescenze di questo gruppo di piante. Ho calcolato così σ per $m=10,\ 11,\ 12,\ 13$ e 14 ed ho fatto la media ponderale di questi valori : ho ottenuto così come variazione normale di un gruppo $\sigma=9258$.

Il rapporto percentuale di questo valore alla deviazione normale dell' intiera popolazione mi dà la variazione percentuale: essa è uguale a 72:81.

Enunciamo allora le conclusioni:

- 1°. L'indice di correlazione per le infiorescenze di *Cichorium Intybus L.* prodotte dalla stessa pianta è circa '6.
- 2º. La correlazione è un po' maggiore per gli individui aventi più infiorescenze, cioè più vicini al massimo di fioritura, che per gli altri.
 - 3°. La variazione percentuale di un gruppo rispetto a tutte le infiorescenze è 72.81.

Si presenterebbe ora il problema della legge di variazione (se normale o no) delle infiorescenze prodotte dalla stessa pianta. Io non ho potuto fare ricerche sul Cichorium Intybus per la scarsità delle infiorescenze che si trovano sopra ogni singola pianta: ho potuto invece studiare per questo riguardo l' Aster chinensis L. e per l' analogia dell' argomento credo opportuno dare qui la statistica di 1326 infiorescenze raccolte sopra un' unica pianta colossale verso la metà del Maggio 1904 a Ferentino (Roma).



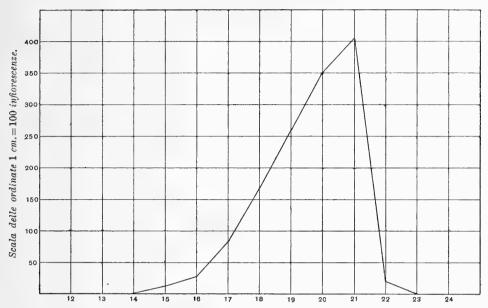


Fig. 2. Variazione dell' Aster chinensis L. (1326 inflorescenze.)

Nº di fiori ligular	ri. Inflorescenze.
15	13
16	26
17	83
18	167
19	257
20	350
21	404
22	21
	Totale 1326

La media è a 19:57164. È notevole il massimo a 21 numero della serie del Fibonacci.

La curva è decisamente abnormale, asimmetrica; in fatti i parametri

$$\mu_2 = + 2.00807,$$

 $\mu_3 = - 2.28508,$
 $\mu_4 = +12.82515,$

da cui $\sigma = 1.41706$,

 $\beta_1 = + .64487,$

 $\beta_2 = +3.18057,$

 $\sigma + 3\beta_1 - 2\beta_2 = +1.57347,$

conducono ad una curva del Tipo I colla asimmetria

A = .81803.

VIII. The Calculation of the Probable Errors of Certain Constants of the Normal Curve.

By RAYMOND PEARL.

Anything which serves to lighten the labour of computation incident to biometric investigations is very welcome. On this account I venture to call attention to a point in which the "Tables for Facilitating the Computation of Probable Errors," recently published by Miss Winifred Gibson* will be found very useful.

It has been shown by Pearson+ that in order to determine whether a given frequency distribution deviates sensibly from the normal or Gaussian law, it is necessary to know the probable errors for the normal curve of the following constants: the skewness, $\sqrt{\beta_1}$, $\beta_2 - 3$ the kurtosis and the "modal divergence." The formula for the probable error of the skewness, when n is the total number of individuals, is

$$P.E._{Sk} = 6744898 \sqrt{\frac{3}{2n}}$$
.

In a recently published note † I pointed out the fact that, after having calculated the value of this expression for any given n, in order to obtain the probable errors of $\sqrt{\beta_1}$, β_2-3 and the "modal divergence" for the same distribution it was merely necessary to multiply the calculated value successively by 2, by 4 and by σ (i.e. the standard deviation of the distribution). We have then only to find an easy way of getting the value of the expression

$$\cdot 6744898 \sqrt{\frac{3}{2n}}$$

in order to make the whole process of testing any distribution for normality very simple indeed.

It is clear that we may write

$$\frac{.6744898}{\sqrt{\frac{3}{2n}}} = .6744898K \sqrt{\frac{1}{n}} = \frac{.6744898}{\sqrt{n}} K = \chi_1 K,$$

$$K = \sqrt{\frac{3}{2}} = 1.2247449 \, \S,$$

where

and χ_1 is the χ_1 of Miss Gibson's Table I.

Therefore to test the approach to normality of any distribution we have merely to perform the following operations:

- (i) Look out χ_1 for the given n from Miss Gibson's tables and multiply it by the factor 1·2247449, using as many places of decimals as necessary. This gives the probable error of the skewness for the normal curve.
- (ii) Multiply the result by 2, which gives the probable error of $\sqrt{\beta_1}$ for the normal curve; multiply this result again by 2, and so obtain the probable error of β_2-3 ; finally multiply the probable error of the skewness by the σ of the distribution and obtain in this way the probable error of the modal divergence.

The relative divergence from zero of the skewness, $\sqrt{\beta_1}$, $\beta_2 - 3$ and the distance from mean to mode in comparison with their probable errors, measures the probability that the given distribution does not follow the normal or Gaussian law.

^{*} Biometrika, Vol. 1v. pp. 385—393.

[†] Biometrika, Vol. IV. pp. 169-212, and elsewhere.

[‡] Science, N. S. Vol. xxII. p. 802.

[§] From Barlow's Tables.

On the Probable Error of Mean-Square Contingency. IX.

BY JOHN BLAKEMAN AND KARL PEARSON.

Let there be any contingency table and n_p be the total frequency in the pth row, n_q in the qth column, n_{pq} the frequency of the constituent common to the pth row and qth column, N the total frequency dealt with in the table. Then it is known* that the total mean square contingency ϕ^2 of the table is given by:

$$\phi^{2} = \frac{1}{N} S_{pq} \left\{ \frac{\left(n_{pq} - \frac{n_{p} n_{q}}{N}\right)^{2}}{\frac{n_{p} n_{q}}{N}} \right\}, \quad (i)$$

the sum being for all values of p and q.

Let ϕ_{pq}^2 be the contribution to ϕ^2 of the p, q constituent frequency, i.e.

$$\phi_{pq}^2 = \frac{1}{N} \frac{\left(n_{pq} - \frac{n_p n_q}{N}\right)^2}{\frac{n_p n_q}{N}} = \frac{n_{pq}^2}{n_p n_q} - \frac{2n_{pq}}{N} + \frac{n_p n_q}{N^2}. \tag{ii}$$

Let ϕ_p^2 be the contribution to ϕ^2 from a single row, and ϕ_q^2 from a single column, i.e.

$$\begin{aligned} \phi_{p}^{2} &= S_{q} \phi^{2}_{pq} = S_{q} \left(\frac{n^{2}_{pq}}{n_{p} n_{q}} \right) - \frac{2S_{q} (n_{pq})}{N} + \frac{n_{p}}{N^{2}} S_{q} (n_{q}) \\ &= S_{q} \left(\frac{n^{2}_{pq}}{n_{p} n_{q}} \right) - 2 \frac{n_{p}}{N} + \frac{n_{p}}{N} \\ S_{q} (n_{pq}) &= n_{p} \text{ and } S_{q} (n_{q}) = N. \end{aligned}$$

Thus:

and similarly:

since

$$\phi_{p}^{2} = S_{q} \left(\frac{n_{pq}^{2}}{n_{p} n_{q}} \right) - \frac{n_{p}}{N},$$

$$\phi_{q}^{2} = S_{p} \left(\frac{n_{pq}^{2}}{n_{p} n_{q}} \right) - \frac{n_{q}}{N}.$$
(iii)

It follows that:

$$\phi^2 = S_p(\phi_p^2) = S_q(\phi_q^2) = S_{pq}\left(\frac{n^2_{pq}}{n_p n_q}\right) - 1.$$
 (iv)

Let us write

$$u_{pq} = \frac{n^2_{pq}}{n_p n_q}.$$
 (v)

Then:

We shall now proceed to find the probable error of $u_{\rho q}$. We state the following preliminary propositions[†], where σ denotes the standard deviation of random sampling:

$$\sigma^2_{n_{pq}} = n_{pq} \left(1 - \frac{n_{pq}}{N} \right), \dots (vii)$$

$$\sigma^2_{\ n_q} = n_q \, \left(1 - \frac{n_q}{N} \right), \ \dots \ (\mathrm{ix})$$

$$\sigma_{n_p} \, \sigma_{n_q} \, R_{n_p n_q} \! = \! n_{pq} \! - \! \frac{n_p n_q}{N} \, , \ldots \ldots (\mathbf{x})$$

^{*} Drapers' Research Memoirs, Biometric Series, 1. On the Theory of Contingency, etc., p. 6.

⁺ Drapers' Research Memoirs, Biometric Series, II. On the Theory of Skew Correlation, etc., pp. 11-17. Dulau & Co.

where throughout p and p' and q' and q' denote different columns and rows, and R is a correlation coefficient between subscript frequencies. Taking logarithmic differentials of (v), i.e. treating the deviations of random sampling as of differential order as is usually done,

$$\frac{\delta u_{pq}}{u_{pq}} = \frac{2\delta n_{pq}}{n_{pq}} - \frac{\delta n_p}{n_p} - \frac{\delta n_q}{n_q}.$$
 (xx)

Then squaring, summing and dividing by the number of random samples:

$$\frac{\sigma^2 u_{pq}}{u^2_{pq}} = 4 \frac{\sigma^2_{n_{pq}}}{n_{pq}^2} + \frac{\sigma^2_{n_p}}{n_p^2} + \frac{\sigma^2_{n_q}}{n_q^2} + 2 \frac{\sigma_{n_p} \sigma_{n_q} R_{n_p n_q}}{n_p n_q} - 4 \frac{\sigma_{n_{pq}} \sigma_{n_p} R_{n_{pq} n_p}}{n_{pq} n_p} - 4 \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} \cdot \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_q} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_q} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}} R_{n_{pq} n_q}}{n_{pq} n_{pq}} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}}}{n_{pq} n_{pq}} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}}}{n_{pq} n_{pq}} - \frac{\sigma_{n_{pq}} \sigma_{n_{pq}}}{n_{pq}} $

Whence using (vii), (viii), (ix), (x), (xviii) and (xix) we find

$$\sigma^2_{u_{pq}} = u^2_{pq} \left(\frac{4}{n_{pq}} - \frac{3}{n_p} - \frac{3}{n_q} + \frac{2n_{pq}}{n_p n_q} \right)$$
.(xxi)

We have next to find the correlation of deviations in u_{pq} and $u_{p'q'}$ due to random sampling. Three cases can occur according as p and q are equal or unequal to p' and q' respectively. We have by multiplying (xx) by a similar form:

$$\begin{split} \frac{\sigma_{n_{pq}}\sigma_{n_{p'q'}}R_{n_{pq}n_{p'q'}}}{u_{pq}u_{p'q'}} &= 4 \frac{\sigma_{n_{pq}}\sigma_{n_{p'q'}}R_{n_{pq}n_{p'q'}}}{n_{pq}n_{p'q'}} - 2 \frac{\sigma_{n_{pq}}\sigma_{n_{p'}}R_{n_{pq}n_{p'}}}{n_{pq}n_{p'}} \\ &- 2 \frac{\sigma_{n_{pq}}\sigma_{n_{q'}}R_{n_{pq}n_{q'}}}{n_{pq}n_{q'}} - 2 \frac{\sigma_{n_{p}}\sigma_{n_{p'q'}}R_{n_{p}n_{p'q'}}}{n_{p}n_{p'q'}} \\ &+ \frac{\sigma_{n_{p}}\sigma_{n_{p'}}R_{n_{p}n_{p'}}}{n_{p}n_{p'}} + \frac{\sigma_{n_{p}}\sigma_{n_{q'}}R_{n_{p}n_{q'}}}{n_{p}n_{q'}} \\ &- 2 \frac{\sigma_{n_{q}}\sigma_{n_{p'q'}}R_{n_{q}n_{p'q'}}}{n_{q}n_{p'q'}} + \frac{\sigma_{n_{q}}\sigma_{n_{p'}}R_{n_{q}n_{p'}}}{n_{q}n_{p'}} \\ &+ \frac{\sigma_{n_{q}}\sigma_{n_{q'}}R_{n_{q}n_{q'}}}{n_{q}n_{q'}}. & (xxii) \end{split}$$

Whence using (xiii), (xvi), (xix), (xi), (x) and (xvii) we have:

$$\sigma_{u_{pq}} \, \sigma_{u_{p'q'}} R_{u_{pq} u_{p'q'}} \! = \! u_{pq} \, u_{p'q'} \left(\! \frac{n_{pq'}}{n_p n_{q'}} \! + \! \frac{n_{p'q}}{n_{p'} n_q} \right) \! . \quad \dots \dots \dots (\text{xxiii})$$

Taking p = p' in (xxii) and using (xiv), (xviii), (xvii), (xi), (x) and (xii) we find:

$$\sigma_{u_{pq}}\,\sigma_{u_{pq'}}\,R_{u_{pq'}u_{pq'}} = u_{pq}\,u_{pq'}\bigg(\frac{n_{pq}}{n_p\,n_q} + \frac{n_{pq'}}{n_p\,n_{q'}} - \frac{3}{n_p}\bigg). \quad \dots \dots ({\bf xxiv})$$

Similarly:

$$\sigma_{u_{pq}}\sigma_{u_{p'q}}R_{u_{pq}u_{p'q}} = u_{pq}u_{p'q}\left(\frac{n_{pq}}{n_pn_q} + \frac{n_{p'q}}{n_{p'}n_q} - \frac{3}{n_q}\right).$$
 (xxv)

Turning back to (vi) and taking differentials, we have:

$$2\phi\delta\phi = S_{pq}(\delta u_{pq}).$$

Square, sum and divide by the number of random samples, and we find:

$$\begin{split} 4\phi^{2}\sigma_{\phi}^{2} &= S_{pq}\left(\sigma^{2}_{u_{pq}}\right) + 2\,\Sigma_{1}\left(\sigma_{u_{pq}}\,\sigma_{u_{p'q'}}\,R_{u_{pq}u_{p'q'}}\right) \\ &\quad + 2\,\Sigma_{2}\left\langle\sigma_{u_{pq}}\,\sigma_{u_{p'q}}\,R_{u_{pq}u_{p'q}}\right\rangle \\ &\quad + 2\,\Sigma_{3}\left\langle\sigma_{u_{pq}}\,\sigma_{u_{pq'}}\,R_{u_{pq}u_{pq'}}\right\rangle, \end{split}$$

where Σ_1 denotes a summation for all unlike values of p, p', q and q'; Σ_2 for all like values of q and unlike of p and p'; Σ_3 for all like values of p, unlike of q and q'.

Substituting from (xxi), (xxiii), (xxiv) and (xxv) we have

We will consider the parts of this in order. Let ψ_{pq} be $taken = \frac{1}{N} \left(n_{pq} - \frac{n_p n_q}{N} \right) = contribution$ from any constituent to the mean contingency. Then

$$\phi^2_{pq} \!=\! N^2 \! \psi^2_{pq} \! / \! n_p n_q. \qquad \dots \dots \dots \dots (\text{xxvii})$$

Hence

Again

$$S_{pq}\left(\frac{u_{pq}^{2}}{n_{pq}}\right) = S_{pq}\left(\frac{n_{pq}^{3}}{n_{p}^{2}n_{q}^{2}}\right) = S_{pq}\left\{\frac{\left(N\psi_{pq} + \frac{n_{p}n_{q}}{N}\right)^{3}}{n_{p}^{2}n_{q}^{2}}\right\}$$

$$= N^{3}S_{pq}\left(\frac{\psi_{pq}^{3}}{n_{p}^{2}n_{q}^{2}}\right) + 3NS_{pq}\left(\frac{\psi_{pq}^{2}}{n_{p}n_{q}}\right) + \frac{1}{N}, \quad \dots \dots (xxix)$$

remembering that $S_{pq}(\psi_{pq})=0$ and $S_{pq}(n_p n_q)=N^2$. Next consider

$$\begin{split} S_{pq}\left(\frac{u^2_{pq}}{n_q}\right) + 2\Sigma_2\left(\frac{u_{pq}u_{p'q}}{n_q}\right) &= S_q\left\{\frac{S_p\left(u_{pq}\right) \times S_p\left(u_{pq}\right)}{n_q}\right\} \\ &= S_q\left\{\left(\phi_q^2 + \frac{n_q}{N}\right)^2 \middle/ n_q\right\} \\ &= S_q\left(\frac{\phi_q^4}{n_q}\right) + \frac{2\phi^2}{N} + \frac{1}{N}. \end{split} \tag{XXX}$$

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Similarly:
$$S_{pq}\left(\frac{u^{2}_{pq}}{n_{p}}\right) + 2\Sigma_{3}\left(\frac{u_{pq}u_{pq'}}{n_{p}}\right) = S_{p}\left(\frac{\phi_{p}^{4}}{n_{p}}\right) + \frac{2\phi^{2}}{N} + \frac{1}{N}. \qquad (xxxi)$$
Lastly:
$$2S_{pq}\left(\frac{u^{2}_{pq}n_{pq}}{n_{p}n_{q}}\right) + 2\Sigma_{1}\left(u_{pq}u_{p'q'}\right)\left(\frac{n_{pq'}}{n_{p}n_{q'}} + \frac{n_{p'q}}{n_{p'}n_{q}}\right) \\ + 2\Sigma_{2}\left(u_{pq}u_{p'q}\right)\left(\frac{n_{pq}}{n_{p}n_{q}} + \frac{n_{p'q}}{n_{p'}n_{q}}\right) + 2\Sigma_{3}\left(u_{pq}u_{pq'}\right)\left(\frac{n_{pq}}{n_{p}n_{q}} + \frac{n_{pq'}}{n_{p}n_{q'}}\right) \\ = 2S_{pq}\left\{S_{q'}\left(u_{pq'}\right)S_{p'}\left(u_{p'q}\right)n_{pq}/n_{p}n_{q}\right\} \\ = 2S_{pq}\left\{\left(\phi_{p}^{2} + \frac{n_{p}}{N}\right)\left(\phi_{q}^{2} + \frac{n_{q}}{N}\right)\frac{n_{pq}}{n_{p}n_{q}}\right\} \\ = 2S_{pq}\left(\phi_{p}^{2}\phi_{q}^{2}\frac{n_{pq}}{n_{p}n_{q}}\right) + \frac{4\phi^{2}}{N} + \frac{2}{N}. \qquad (xxxii)$$

Then substituting from (xxix), (xxx), (xxxi) and (xxxii) in (xxvi) we have:

$$\begin{split} 4\phi^2\sigma_{\phi}^{\ 2} &= 4N^3S_{pq}\left(\psi^3_{\ pq}/n_p^{\ 2}n_q^{\ 2}\right) + 12\phi^2/N + 4/N \\ &- 3S_q\left(\frac{\phi_q^4}{n_q}\right) - 3S_p\left(\frac{\phi_p^4}{n_p}\right) - 12\phi^2/N - 6/N \\ &+ 2S_{pq}\left(\phi_p^2\phi_q^2\frac{n_{pq}}{n_pn_q}\right) + 4\phi^2/N + 2/N \\ &= 4\phi^2/N + 4N^3S_{pq}\left\{\psi^3_{pq}/n_p^2n_q^2\right\} \\ &+ 2S_{pq}\frac{(\phi_p^2\phi_q^2)}{N} - 3S_q\left(\frac{\phi_q^4}{n_q}\right) - 3S_p\left(\frac{\phi_p^4}{n_p}\right) \\ &+ 2NS_{pq}\left(\phi_p^2\phi_q^2\frac{\psi_{pq}}{n_pn_q}\right). \end{split} \tag{xxxiii}$$

When the contingencies, mean and mean squared, approach zero, the terms of the third, fourth and fifth orders may be neglected as compared with that of the second order and we find

$$\sigma_{\phi}^{\,2} {=} \frac{1}{N}, \ \, \text{or} \ \, \sigma_{\phi} {=} \frac{1}{\sqrt{N}}. \qquad \qquad \qquad (\text{xxxiv})$$

But if C be the coefficient of mean squared contingency:

$$C = \sqrt{\frac{\phi^2}{1+\phi^2}},$$
 $\sigma_C = \frac{\sigma_{\phi}}{(1+\phi^2)^{\frac{3}{2}}} = (1-C^2)^{\frac{3}{2}} \sigma_{\phi}.$ (xxxv)

and accordingly

Hence the probable error of $\,C\,$

 $= \cdot 67449 \, (1 - C^2)^{\frac{3}{2}} \, \sigma_{\phi} \,,$

and in the particular case of no contingency

$$=\frac{.67449}{\sqrt{N}}$$
 by (xxxiv).

Hence unless a coefficient of mean squared contingency be two or three times this value, we have no evidence that the quantities under discussion can be considered as contingent on each other.

The general expression for σ_{ϕ} in (xxxiii) can be dealt with in several ways. It might be thought that ψ_{pq} being of changing sign, the cubic terms as well as those of the fifth order in ψ_{pq} would be small; but this is not our experience in actual application. Terms will occur in which n_{pq} is very large as compared with $n_p n_q / N$ owing to the existence of a few isolated units in outlying compartments, and it by no means follows that the second term is less than the first, or the sixth term less than the third. We have not succeeded in getting any

appreciation of "negligible terms" when the contingency is not very small. The whole formula may be written:

$$\phi^2 \sigma_{\phi}^2 = S_{pq} \left(\phi^2_{pq} \frac{n_{pq}}{n_p n_q} \right) + \frac{1}{2} S_{pq} \left(\phi_p^2 \phi_q^2 \frac{n_{pq}}{n_p n_q} \right) - \frac{3}{4} S_p \left(\frac{\phi_p^4}{n_p} \right) - \frac{3}{4} S_q \left(\frac{\phi_q^4}{n_q} \right). \quad \dots (\text{xxxvi})$$

If we endeavour to get some idea of the general magnitude of this expression, by evaluating it for a normal correlation surface we find, for infinitesimal groupings, that the last two terms become infinite if r does not lie between $-1/\sqrt{3}$ to $+1/\sqrt{3}$ and the first term becomes infinite when r does not lie between -1/2 to +1/2. In fact in such cases we seem to reach indefinitely large probable errors. We doubt, however, the justice of this view and believe it merely signifies that with indefinitely fine grouping beyond a certain range of values of r, the assumption that the errors of random sampling may be treated as differentials is incorrect, and thus our process of reaching (xxxvi) is no longer legitimate when applied to such normal distributions. The whole matter, however, deserves careful investigation from the theoretical standpoint. Even from the practical side the error in any constituent due to random sampling must be at least unity, and accordingly if the theoretical value of the constituent be only a few units or a fraction even of a unit $\delta n_{pq}/n_{pq}$ is not necessarily a small quantity. We ought accordingly to provide in practice for a contingency grouping which leaves no constituent to consist of but a few units, if we wish to justify our fundamental assumption in determining the probable error.

In actual practice with fairly coarse grouping and not replacing the summations by integrations, the value for σ_{ϕ} will always be finite, for we make no summation where either n_p or n_q are zero, i.e. we do not as in using the normal surface extend our distribution all over space. For the cases in which we have tried it (xxxvi) then gives reasonable results, and we will now indicate how the calculations can be made fairly briefly.

In the accompanying table we have the contingency between Intelligence and Handwriting in schoolgirls. The columns correspond to grades of intelligence, the rows to grades of handwriting. The first number of each constituent group is the actual frequency in the total of 1801 girls with the characteristics of that group. The reciprocal of 1801 is $555,247/10^9$. This is put on the calculator and the column of row totals multiplied by it, with the result n_q/N put under each row total; each one of these is now put on the machine in succession and multiplied by the series of column totals n_p ; we thus obtain $n_p n_q/N$, which is registered as the second number in each constituent. The difference of the first and second number of each constituent with due regard to sign is $N\psi_{pq}$ the constituent contingency. This is registered as the third number in the constituent. The square of this—taken from Barlow's tables—and divided by the second number is $N\phi_{pq}^2$, or N times the mean square contingency contribution of each constituent. This is the fourth number registered in the constituents. The sum of these fourth numbers for each row gives $N\phi_q^2$, and for each column $N\phi_p^2$. These are registered in the column and row beyond "totals." Adding up this column or row, we have

$$S_q(N\phi_q^2) = S_p(N\phi_p^2) = 172.52 = N\phi^2$$
, hence $\phi^2 = .09580$ and $C = \sqrt{\phi^2/(1+\phi^2)} = .2957$.

This is the coefficient of mean squared contingency between handwriting and intelligence, and is our standard method of finding C. So far all the work is usual and necessary. Now square from Barlow the column of $N\phi_q^2$ and the row of $N\phi_p^2$; we obtain the column and row of $N^2\phi_q^4$ and $N^2\phi_p^4$. Divide these by their respective column and row total frequencies and we have the numbers given underneath $N^2\phi_q^4$ and $N^2\phi_p^4$, or $N^2\phi_q^4/n_q$ and $N^2\phi_p^4/n_p$ respectively. Adding up these column numbers and row numbers we find on division by N

$$\frac{1}{N}S\left(\frac{N^{2}\phi_{q}^{\ 4}}{n_{q}}\right) = \cdot 05758, \quad \frac{1}{N}S\left(\frac{N^{2}\phi_{p}^{\ 4}}{n_{p}}\right) = \cdot 03199,$$

values registered on the table. These are two of the sums needed for (xxxvi). If the distribution were normal and the group ranges infinitesimal these should be equal. They clearly differ widely. Next divide $N\phi_q^2$ by 1801, i.e. multiply these quantities by the reciprocal, placed

on the machine. The results are tabled beneath the values of $N\phi_q^2$, or these are ϕ_q^2 . Put each ϕ_{q^2} on the calculator and multiply it by the row $N\phi_{p^2}$. These products are given as the fifth figure in each constituent. The sixth figure is $Nn_{pq}/(n_p n_q)$ or is the result of dividing the first figure by the second. The seventh figure is the sixth multiplied by the fourth or

$$= \! N \phi^2_{pq} \times N n_{pq} \! / \! (n_p \, n_q) \! = \! N^2 \phi^2_{pq} \, n_{pq} \! / \! (n_p \, n_q),$$

and the eighth is the sixth figure multiplied by the fifth

$$= \phi_{p}^{2} N \phi_{q}^{2} \times N \frac{n_{pq}}{n_{p} n_{q}} = N^{2} \phi_{p}^{2} \phi_{q}^{2} n_{pq} / (n_{p} n_{q}).$$

These are added up for each row and placed as the third and fourth figures in the $N^2\phi_a^4$ column: added up for the column and divided by N, they give

$$S_{pq} \{N\phi_{pq}^2 n_{pq}/(n_p n_q)\} = 2444,586,$$

$$S_{pq} \{N\phi_p^2 \phi_q^2 n_{pq}/(n_p n_q)\} = 014,0827,$$

which determine the first and second sums in the value of $\phi^2 \sigma_{\star}^2$. But

$$\begin{split} S_{pq} \left\{ N \phi^2_{\ pq} n_{pq} / (n_p n_q) \right\} &= S_{pq} \left(\phi^2_{\ pq} \right) + S_{pq} \left(N^2 \phi^2_{\ pq} \frac{\psi_{pq}}{n_p n_q} \right) \\ &= (\cdot 09580) + N^4 S_{pq} \left\{ \psi^3_{\ pq} / (n_p^2 n_q^2) \right\} : \\ N^3 S_{pq} \left\{ \psi^3_{\ pq} / (n_p^2 n_q^2) \right\} &= \cdot 14865 / N, \end{split}$$

whence it follows that while

$$N^3 S_{pq} \{ \psi^3_{pq} / (n_p^2 n_q^2) \} = 14865 / N,$$

 $\phi^2 / N = S_{pq} (\phi^2_{pq}) / N = 09580 / N$

is less in value. Thus the cubic terms in the contingency are more important than the square, and cannot in this case be neglected compared to them in the present case.

Again
$$S_{pq} \{N\phi_p^2\phi_q^2n_{pq}/(n_pn_q)\} = \phi^4 + N^2S_{pq}\left(\frac{\phi_p^2\phi_q^2\psi_{pq}}{n_pn_q}\right):$$
 whence
$$NS_{pq} \{\phi_p^2\phi_q^2\psi_{pq}/(n_pn_q)\} = \frac{\cdot 0140827 - (\cdot 09580)^2}{N}$$

$$= \cdot 00490/N,$$
 while
$$S_{pq} \langle \phi_p^2\phi_q^2 \rangle / N = \phi^4/N = \cdot 00918/N.$$

while

Thus the fifth order term is only one-half roughly of the fourth order term and is not in this case negligible with regard to it. It is clearly the very dull, very bad handwriters whose excess so emphasises these terms. In this, as in other cases, we cannot accordingly neglect any of the terms contributory to the probable error and we have by (xxxiii):

$$\begin{split} \phi^2 \sigma_\phi^{\ 2} = & \frac{1}{N} \{ \cdot 24446 + \cdot 00704 - \cdot 06718 \} = \frac{\cdot 18432}{N} \ , \\ \text{or,} \qquad \qquad \sigma_\phi^{\ 2} = & 1 \cdot 9240 / N = \cdot 001068, \ \text{and} \ \ \sigma_\phi = \cdot 0327 \ *. \\ \text{But} \qquad \qquad \sigma_C = & \sigma_\phi / (1 + \phi^2)^{\frac{3}{2}}, \ \text{by (xxxv)} \\ & = & \left\{ \frac{\cdot 001068}{1 \cdot 315813} \right\}^{\frac{1}{2}} = \cdot 0285. \end{split}$$

Hence the probable error of C = 0192

The probable error of C, if it were found from the coefficient of correlation, would be $.67449 (1-r^2)/\sqrt{N} = .0139$. Thus the coefficient as found by mean squared contingency is rather more subject to error than the coefficient of correlation, say in the ratio of 4 to 3. The rule given in Pearson's memoir+ appears, to judge by this case, to err on the side of asserting no significance, where after all it may exist.

The actual arithmetic of determining the probable error is not so laborious as might have been anticipated.

The coefficient of mean contingency obtained from the diagram in the memoir just cited is ·31, so that it differs from C= ·30 by less than the probable error.

- * Probable Error of $\phi^2 = 67449 \times 2\phi \sigma_{\phi} = 0042$.
- † Drapers' Research Memoirs: Biometric Series, I., p. 18. Dulau & Co.

Contingency between Handwriting and Intelligence in Girls.

Writing	Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	Totals n_q	$N\phi_q{}^2~\&~\phi_q{}^2$	$N^2 \phi_q^{~4}, \& N^2 \phi_q^{~4}/n_q$
Very Good	38 17·88 +20·12 22·64 ·761 2·125 48·11 1·617	47 44·11 +2·89 ·19 ·392 1·066 ·20 ·418	30 38·34 -8·34 1·81 ·153 ·782 1·42 ·120	6 16·30 -10·30 6·51 ·616 ·368 2·40 ·227	4 6·86 -2·86 1·19 ·619 ·583 ·69 ·361	1 2·52 -1·52 ·92 ·645 ·397 ·37 ·256	$\begin{array}{c} 126 \\ \cdot 069961 = n_q/N \\ = N \psi_{pq} \\ = N \phi_{pq}^2 \\ = N \phi_p^2 \phi_q^2 \\ = N n_{pq} n_p n_q \\ = N^2 \phi_{pq}^2 n_{pq} n_p n_q \\ = N^2 \phi_{pq}^2 n_{pq} n_p n_q \end{array}$	33·26 ·018468	1106·23 8·780 53·19=* 2·999=†
Good	115 93·28 +21·72 5·06 ·864 1·233 6·24 1·065	277 230·18 +46·82 9·52 ·445 1·203 11·45	185 200·06 -15·06 1·13 ·174 ·925 1·05 ·161	55·5 85·06 -29·56 10·27 ·700 ·652 6·70 ·456	19 35·78 - 16·78 7·87 ·703 ·531 4·18 ·373	6 13·14 -7·14 3·88 ·732 ·457 1·77 ·335	657·5 ·365075 — — — — —	37·73 ·020966	1423·55 2·165 31·39 2·925
Moderate	67 101·08 - 34·08 11·49 ·486 ·663 7·62 ·322	231·5 249·43 -17·93 1·29 ·251 ·928 1·20 ·233	244·5 216·80 +27·70 3·54 ·098 1·128 3·99 ·111	112·5 92·18 +20·32 4·48 ·394 1·220 5·47 ·481	43 38·77 +4·23 ·46 ·396 1·109 ·51 ·439	14 14·24 - ·24 ·00 ·412 ·983 ·00 ·405	712·5 ·395614 ————————————————————————————————————	21·26 ·011805	451:99 -634 18:79 1:991
Poor	26·5 34·62 -8·12 1·90 ·665 ·765 1·45 ·509	62 85 42 - 23 42 6 42 342 726 4 66 248	75·5 74·24 +1·26 ·02 ·134 1·017 ·02 ·136	48 31·57 +16·43 8·55 •539* 1·520 13·00 •819	21 13·28 +7·72 4·49 ·541 1·581 7·10 ·855	11 4·88 +6·12 7·68 ·564 2·254 17·31 1·271	244 ·135480 ————————————————————————————————————	29·06 ·016135	844·48 3·461 43·54 3·838
Bad	7 6·38 +·62 ·06 ·333 1·097 ·07 ·365	11 15·75 -4·75 1·43 ·172 ·698 1·00 ·120	9 13·69 -4·69 1·61 ·067 ·657 1·06 ·044	10 5·82 +4·18 3·00 ·270 1·718 5·15 ·885	7 2·45 +4·55 8·45 ·271 2·857 24·14 ·774	1 0 90 + 10 01 282 1 111 01 313	45 ·024986 ————————————————————————————————————	14·56 ·008084	211·99 4·711 31·43 2·501
Very Bad	2 2·30 - ·30 ·04 ·838 ·870 ·03 ·729	2 5·66 -3·66 2·37 -432 -353 -84 -152	4 4·92 - ·92 ·17 ·168 ·813 ·14 ·137	1 2·09 -1·09 ·57 ·679 ·478 ·27 ·325	4 0.88 +3.12 11.06 .682 4.545 50.27 3.100	3 0·32 +2·68 22·44 ·711 9·375 210·38 6·666	16 ·008984 ———————————————————————————————————	36·65 ·020350	1343·22 83·951 261·93=‡ 11·109=§
Totals n_p	255.5	630.5	548	233	98	36	1801 •555247/10 ³	=	$\frac{1}{N}S_q\left(\frac{N^2\phi_q^4}{n_q}\right)$ = '05758
$N\phi_{p}^{\ 2} \ N^{2}\phi_{p}^{\ 4} \ N^{2}\phi_{p}^{\ 4}/n_{p}$	41·19 1696·62 6·640	21·22 450·29 ·714	8·28 68·56 ·125	33·38 1114·22 4·782	33·52 1123·59 11·465	34·93 1220·10 33·892	$\frac{1}{N} S_p \left(\frac{N^2 \phi_p^4}{n_p} \right) = 03199$	$ \begin{array}{r} \hline 172.52 \\ = N\phi^2 \\ \phi^2 = .09580 \\ \pm .0042 \end{array} $	<i>C</i> = ·2957 ± ·0192

The first four numbers in each constituent are those required in the usual calculation of mean square contingency; the second set of four are those required to determine its probable error. The actual arithmetical work if we need the coefficient of mean square and its probable error is thus just doubled.

* $S_p \{N^2 \phi_{pq}^2 n_{pq}/(n_p n_q)\}$.

† $S_p \{N^2 \phi_{pq}^2 n_{pq}/(n_p n_q)\}$.

† $S_{pq} \{\phi_{pq}^2 n_{pq}/(n_p n_q)\} = \frac{1}{N} (\cdot 2444586)$.

§ $S_{pq} \{\phi_{pq}^2 \phi_{qq}^2 n_{pq}/(n_p n_q)\} = \frac{1}{N} (\cdot 014083)$.

$$\{S_{pq} \{\phi_p^2 \phi_q^2 n_{pq} | (n_p n_q)\} = \frac{1}{N} (.014083).$$

On a Coefficient of Class Heterogeneity or Divergence.

By KARL PEARSON, F.R.S.

(1) In considering the sub-groups of a population—especially in dealing with local races in man, animals or plants—a problem of the following character has not infrequently arisen: It is found that a sub-class, for example a local sample, differs considerably from the general population. This divergence may have any magnitude upwards from the probable limits of random sampling. We require some coefficient which will express by a single number the relative divergence from the general population of each sub-class or local group. For example, we take the frequency of alternative characteristics of the local population and find these are represented by certain percentages in the general population; we know also the percentages in the sub-group. We can, of course, take the difference of each individual percentage and of the general population percentage and find the probable error of this difference, but this gives us a series of numbers, and not a single measure of the general heterogeneity of the group. These numbers may also belong to correlated characters, and when one number marks a great excess in percentage we may expect a great defect in a second percentage for this very reason. But this makes the weight to be given to such a complex system of numbers extremely difficult to estimate.

The necessity for some general coefficient of class heterogeneity was impressed upon me, while discussing with Mr J. F. Tocher his reduction of the Anthropometrical Surveys recently made of the inmates of Scottish Asylums and of the children in Scottish Schools. It was needful to find a single number, which would measure local heterogeneity, or the divergence from a random sample of the general population in a series of characters of the local population. The number chosen must be such (i) that allowance is made for the size of the sample, (ii) that the numbers for different sub-groups or localities are strictly comparable, and (iii) that we have some idea as to the size of its probable error. Following up a suggestion of Mr Tocher I have reached what I think is a workable coefficient of divergence, which may be useful in dealing with local race problems.

Suppose a contingency table formed in which the columns are marked by the alternative characters under consideration and each row is peculiar to a sub-group or district. Thus let the characters be $a, \beta, \gamma, \delta \dots$ and the sub-groups $a, b, c, d, e \dots$ We have the table:

Totals β δ η γ $n_{\alpha\omega}$ $n_{\alpha\beta}$ $n_{a\gamma}$ $n_{a\delta}$ $n_{a\epsilon}$ $n_{\alpha\eta}$ α n_a $n_{b\epsilon}$ b $n_{b\omega}$ n_{ba} $n_{b\beta}$ $n_{b\eta}$ n_b $n_{b\delta}$ $n_{c\eta}$ c $n_{c\beta}$ $n_{c\omega}$ $n_{c\delta}$ $n_{d\epsilon}$ d $n_{d\beta}$ $n_{d\delta}$ $n_{d\eta}$ n_{da} n_d n_e n_{ea} $n_{e\epsilon}$ $n_{e\eta}$ $n_{e\beta}$ $n_{e\gamma}$ $n_{e\delta}$ $n_{e\omega}$ n_z $n_{z\epsilon}$ $n_{z\eta}$ $n_{z\omega}$ n_{γ} n_{η} n_{ω} N

TABLE I.

Here the first column gives all the districts or sub-groups which form the total population The distribution of the alternative characters in the total population is given in the last row, while the last column gives the total frequency of each sub-group. Any number such as $n_{i\gamma}$

 n_{ϵ}

 n_{δ}

Totals

 n_{β}

is the frequency of the alternative character γ in the sub-group or district *i*. For example $a, \beta, \gamma \dots$ may be the alternative hair colours in a country of which the different districts are $a, b, c, d \dots z$. Such tables arise over and over again in anthropometric surveys. If now each sub-group or district were a random sample of the general population, then the coefficient of contingency of this table—say the coefficient of mean square contingency—should within the limits of probable error be zero. We have thus a table of the contingency between geographical sub-districts and the alternative characteristics. And the greater this contingency the more markedly are the sub-groups divergent from random samples of the general population. In other words the population is geographically* heterogeneous. Accordingly if we take the same or nearly the same set of characters for two populations and about the same number of sub-groups or districts, such tables as the above give by their coefficients of contingency a reasonable measure of inter-racial comparison. The population or race with the highest coefficient of contingency is clearly the most heterogeneous. The relative heterogeneity of Prussians, Swedes, Italians, Scottish and, perhaps, English could, I think, be now determined in this manner from published data for at least hair and eye colour.

But we require not only an inter-racial coefficient of heterogeneity, but an intra-racial coefficient, which will measure the relative heterogeneity of the various groups. To reach this, pick out any district or sub-class b and oppose it to the rest of the population in a table of the following kind:

\mathbf{T}	A	RI	\mathbf{E}	II.

	а	β	γ	δ	€	η	<u> </u>	ω	Totals
b Rest	n_{ba} $n_a - n_{ba}$	$\begin{vmatrix} n_{b\beta} \\ n_{\beta} - n_{b\beta} \end{vmatrix}$	$n_{b\gamma} \\ n_{\gamma} - n_{c\gamma}$	$n_{b\delta} \\ n_{\delta} - n_{b\delta}$	$n_{b\epsilon} \\ n_{\epsilon} - n_{c\epsilon}$	$n_{b\eta} \\ n_{\eta} - n_{b\eta}$	_	$n_{b\omega} \\ n_{\omega} - n_{b\omega}$	$n_b \\ N-n_b$
Totals	. n _a	n_{β}	n_{γ}	n_{δ}	n_{ϵ}	n_{η}		n_{ω}	N

This is also a contingency table, of a very contracted character it is true, but none the less absolutely valid, if it be only used for relative purposes. Let the coefficient of mean square contingency of this table be found and be C_b , then the relative values of C_a , C_b , C_d , etc. will be measures of the class and local differences, or what we may call intra-racial differences. I suggest these C's as the coefficients we are seeking. We will now investigate the nature of C_b -Let χ_b^2 be the mean square contingency, then:

$$\begin{split} \chi_b^2 &= \frac{1}{N} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} + \frac{\left(n_a - n_{ba} - \frac{n_a \left(N - n_b \right)}{N} \right)^2}{\frac{n_a \left(N - n_b \right)}{N}} \right\} \\ &= \frac{1}{N} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \left(1 + \frac{n_b}{N - n_b} \right) \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_a - \frac{n_a n_b}{N} \right)^2}{\frac{n_a n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_{a}^{\omega} \left\{ \frac{\left(n_b n_b - \frac{n_b}{N} \right)^2}{\frac{n_b n_b}{N}} \right\} \\ &= \frac{1}{N - n_b} \sum_$$

^{*} The sub-groups need not of course be 'geographical'; they might be economically, socially, or otherwise differentiated.

Now if ϕ^2 be the mean square contingency of Table I. and if ϕ_b^2 be the contribution to it of the b row we have:

$$\phi^2 = \phi_a^2 + \phi_b^2 + \phi_c^2 + \dots + \phi_z^2$$

where

$$\phi_b^2 = \frac{1}{N} \stackrel{\omega}{S} \left\{ \frac{\left(n_{ba} - \frac{n_a n_b}{N}\right)^2}{\frac{n_a n_b}{N}} \right\} \dots (ii).$$

Or, we have:

$$\chi_b^2 = \frac{N}{N - n_b} \phi_b^2.$$

But:

$$C_b = \sqrt{\frac{\chi_b^2}{1 + \phi_b^2}} = \sqrt{\frac{\phi_b^2}{1 - \frac{n_b}{N} + \phi_b^2}}$$
.(iii).

Thus we have the following rule:

Start with Table I. and determine the contributions ϕ_a^2 , ϕ_b^2 , ϕ_c^2 ... ϕ_z^2 of each sub-group or locality to the total mean square contingency of this table. Then C_a , C_b , ... C_z determined as above are the "coefficients of divergence" of the respective sub-groups or classes or localities from the general population, and their relative magnitudes measure the relative divergency of such groups or localities.

(2) If the Class b were, for example, merely a random sample of the general population, we should have $\phi_b{}^2=0$ and $C_b=0$. It becomes accordingly of importance to determine the probable error of C_b on the assumption that Class b is a random sample. If C_b differs from zero by several times its probable error, the divergence of the Class is almost certainly significant. The general expression for the probable error of a coefficient of mean square contingency has been dealt with in another paper*. In the notation of that paper

$$\phi^2 \sigma_{\phi^2} = S_{pq} \left(\phi^2_{pq} \frac{n_{pq}}{n_p n_q} \right) + \frac{1}{2} S_{pq} \left(\phi_{p^2} \phi_{q^2} \frac{n_{pq}}{n_p n_q} \right) - \frac{3}{4} S_p \left(\frac{\phi_{p^4}}{n_p} \right) - \frac{3}{4} S_q \left(\frac{\phi_{q^4}}{n_q} \right) \dots \dots (iv).$$

 ϕ^2 will now be χ_b^2 and we have to perform the summations for the two rowed table, Table II, above. The q summation will be from a to ω and the p summation for the two rows of our table. I take the terms in order.

(i)
$$S_{pq}\left(\phi^2_{pq} \frac{n_{pq}}{n_p n_q}\right)$$
. This in our present notation stands for
$$\overset{\omega}{S}\left(\phi^2_{ba} \frac{n_{ba}}{n_b n_a}\right) + \frac{n_b}{N-n_b} \overset{\omega}{S}\left(\phi^2_{ba} \frac{n_a-n_{ba}}{n_a \left(N-n_b\right)}\right),$$

since ϕ_{pq}^2 for any constituent of the second row is by the line above Equation (i) = $\frac{n_b}{N-n_b}\phi_{ba}^2$, where ϕ_{ba}^2 is the contribution to the mean square contingency from the first row constituent immediately above. Let us write $\nu_b = n_b/(N-n_b)$. Then we have, if we write

$$\tau_b^2 = \int_a^\omega \left\{ \phi^2_{ba} \, n_{ba} / (n_b n_a) \right\} \quad \dots (v),$$

$$S_{pq}\left(\phi^{2}_{pq}\frac{n_{pq}}{n_{p}n_{q}}\right) = \tau_{b}^{2}\left(1-\nu_{b}^{2}\right) + \nu_{b}^{2}\phi_{b}^{2}/n_{b}$$
(vi).

(ii) $\frac{1}{2}S_{pq}\left(\phi_p^2\phi_q^2\frac{n_{pq}}{n_pn_q}\right)$. For the first line $\phi_q^2=\phi_b^2$ and for the second line $=\nu_b\phi_b^2$. Hence

* "On the Probable Error of Mean Square Contingency," see Equation (xxxvi), Biometrika, Vol. v. p. 195.

the value of this, if we remember that $\phi_p^2 = \phi^2_{ba} + \nu_b \phi^2_{ba}$ for the a column, is given by

$$\frac{1}{2}\phi_{b}^{2} \overset{\omega}{S} \left\{ (1 + \nu_{b}) \phi^{2}_{ba} \frac{n_{ba}}{n_{b}n_{a}} + \nu_{b} (1 + \nu_{b}) \phi^{2}_{ba} \frac{n_{a} - n_{ba}}{n_{a} (N - n_{b})} \right\}$$

$$= \frac{1}{2} (1 + \nu_{b}) (1 - \nu_{b}^{2}) \phi_{b}^{2} \overline{r_{b}^{2}} + \frac{1}{2} (1 + \nu_{b}) \nu_{b}^{2} \phi_{b}^{2} / n_{b} \dots \dots (vii).$$
(iii)
$$\overset{3}{4} S_{p} \left(\frac{\phi_{p}^{4}}{n_{p}} \right) = \frac{3}{4} (1 + \nu_{b})^{2} \overset{\omega}{S} \left(\frac{\phi^{4}_{ba}}{n_{a}} \right) = \frac{3}{4} (1 + \nu_{b})^{2} \omega_{b}^{4} \dots (viii).$$

$$\omega_{b}^{4} = \overset{\omega}{S} \left(\frac{\phi^{4}_{ba}}{n_{a}} \right) \dots (ix).$$

(iv) $\frac{3}{4}S_q\left(\frac{\phi_q^4}{n_q}\right)$. This since the summation is for only two rows is given by

$$\frac{3}{4} \left(\frac{\phi_b^4}{n_b} + \nu_b^2 \frac{\phi_b^4}{N - n_b} \right)$$

or

if

$$\frac{3}{4} S_q \left(\frac{\phi_q^4}{n_q} \right) = \frac{3}{4} (1 + \nu_b^3) \phi_b^4 / n_b \dots (x).$$

Writing (vi), (vii), (viii) and (x) in (iv) we find:

$$\chi_b{}^2\sigma^2\chi_b = \left\{\tau_b{}^2\left(1-\nu_b{}^2\right) + \nu_b{}^2\;\phi_b{}^2/n_b\right\} \left\{1 + \tfrac{1}{2}\left(1+\nu_b\right)\,\phi_b{}^2\right\} - \tfrac{3}{4}\left\{\widehat{(1+\nu_b{}^3)}\,\frac{\phi_b{}^4}{n_b} + (1+\nu_b)^2\;\omega_b{}^4\right\}.$$

But by the line above equation (iii) $\chi_b^2 = (1 + \nu_b) \phi_b^2$. Hence:

$$\begin{split} \sigma^2 \chi_b &= \frac{1}{n_b} \left\{ \frac{\nu_b^2}{1 + \nu_b} + \frac{n_b \tau_b^2}{\phi_b^2} (1 - \nu_b) \right\} \left\{ 1 + \frac{1}{2} (1 + \nu_b) \phi_b^2 \right\} \\ &- \frac{3}{4n_b} \left\{ (1 - \nu_b + \nu_b^2) \phi_b^2 + (1 + \nu_b) \frac{n_b \omega_b^4}{\phi_b^2} \right\} \quad \dots \dots (xi). \end{split}$$

This involves a knowledge of ϕ_b^2 , τ_b^2 and ω_b^4 . The first will have been found in determining the contingency coefficient of the entire table; the second in determining its probable error, and the third only has to be specially calculated.

Finally we have*

$$\sigma_{C_b} = \{1 - C_b^2\}^{\frac{3}{2}} \sigma_{\chi_b} \dots (xii).$$

Or the

Probable Error of
$$C_b = 67449 (1 - C_b^2)^{\frac{3}{2}} \sigma_{\chi_b}$$
.

(3) I propose to illustrate this numerically on a table already largely worked out in the paper referred to above. It has been shown that handwriting is contingent in a certain degree on grade of intelligence. I propose to investigate which group of handwriters has a distribution of intelligence most markedly different from that of the general population, i.e. which is intellectually most heterogeneous. This is not in itself a problem of any importance but it will serve to illustrate the application of the above formulæ, and the numerical work needful for their evaluation. Turning to the table, p. 197, I extracted the results given in Table III. The only new quantities to be calculated are the values of

$$\omega_b^4 = \mathop{S}\limits_a^\omega \left(\frac{\phi^4{}_{ba}}{n_a}\right) = \frac{1}{N^2} \mathop{S}\limits_a^\omega \left(\frac{(N\phi^2{}_{ba})^2}{n_a}\right).$$

Now $N\phi^2_{ba}$ is the fourth number in each constituent of the table on p. 197. The squares of these from Barlow's Tables are the first number in each constituent of Table IV.; n_a is given under the total at the foot and immediately above n_a , its reciprocal. These reciprocals placed successively on the calculator and multiplied by the first number in each column

TABLE III.

Handwriting	n_b	ν_b	$1 + \nu_b^3$	$\phi_{b}{}^{2}$	$N\phi_{b}^{2}$	$N^2 au_b{}^2$	$N^2\omega_b^4$	$\sigma_{\chi_{ar{b}}}$	C_b	P.E. of C_b
Very Good	126	·0752	1·0004	·0185	32·26	53·19	2·232	·0321	·1395	·0210
Good	657·5	·5750	1·1901	·0210	37·73	31·39	1·749	·0239	·1787	·0154
Moderate	712·5	·6546	1·2805	·0118	21·26	18·79	·631	·0238	·1384	·0156
Poor	244	·1567	1·0038	·0161	29·06	43·54	2·237	·0296	·1354	·0194
Bad	45	·0256	1·0000	·0081	14·56	31·43	·776	·0367	·0907	·0244
Very Bad	16	·0090	1·0000	·0204	36·65	261·93	15·246	·0714	·1418	·0467

TABLE IV.
Intelligence.

				Intemge				
		Quick Intelligent	Intelligent	Slow Intelligent	Slow	Slow Dull	Very Dull	$N^2\omega_b^{-4}$
	Very Good	512·57 2·006	*04 *000	3.28	42·38 ·182	1·42 ·014	*85 *024	2.232
	Good	25·60 ·100	90.63	1:28	105·47 ·453	61:94 :632	15:05 ·418	1.749
riting.	Moderate	132.02	1:66	12·53 ·023	20·07 ·086	·21 ·002	.000	·631
Handwriting.	Poor	3·61 ·014	41.22	.000	73·10 ·314	20.16	58·98 1·638	2.237
	Bad	.000	2:04	2·59 ·005	9.00	71·40 ·729	.000	·776
	Very Bad	.000	5.62 .009	.000	·32 ·001	122·32 1·248	503·55 13·988	15.246
	Reciprocals Totals	·003914 255·5	·001586 630·5	·001825 548	·004292 233	·010204 98	·027778 36	-555247/10 ³ 1801

constituent give $(N\phi^2_{ba})^2/n_a$ which is recorded as the second number in each constituent. The sum of these for each row gives $N^2\omega_b^4$ recorded to the right and also in Table III., $\sigma^2\chi_b$ can now be found from the form

$$\sigma^{2}_{\chi_{b}} = \frac{1}{N} \left[\left(\nu_{b} + \frac{N^{2} \tau_{b}^{2}}{N \phi_{b}^{2}} (1 - \nu_{b}) \right) (1 + \frac{1}{2} (1 + \nu_{b}) \phi_{b}^{2}) - \frac{3}{4} \left(\frac{1 + \nu_{b}^{3}}{\nu_{b}} \phi_{b}^{2} + (1 + \nu_{b}) \frac{N^{2} \omega_{b}^{4}}{N \phi_{b}^{2}} \right) \right].$$
And again
$$C_{b} = \sqrt{\frac{\phi_{b}^{2}}{1 - \frac{n_{b}}{N} + \phi_{b}^{2}}} = \sqrt{\frac{\phi_{b}^{2}}{1/(1 + \nu_{b}) + \phi_{b}^{2}}} \text{ from (iii)}.$$

These values are also recorded in Table III. Then σ_{C_b} was found from (xii) and so the probable error of C_b .

The values of C_b show us that the class of "Good" handwriters is most and that of "Bad" handwriters least divergent from the general population. The other four classes have values of C_b sensibly equal and equal to '14. The "Good" handwriters have '18 and the "Bad" '09, and the question is whether these are significantly different from '14, or from each other. The probable error of the difference is about '03. It would therefore be reasonable to assume that "Good" and "Bad" handwriters do differ from each other, though it is less easy to assert marked difference from the community at large. On the whole it seems reasonable to suggest that in distribution of intelligence the "Good" handwriters are less like a random sample of the general girl population than "Bad" handwriters. In other words heterogeneity of intelligence is more marked in the class "Good" than in the class "Bad."

As I have said, the illustration is one of numerical method only and not of interest in itself. The special purpose of the present note is the suggestion of a coefficient which may be of value in the many cases in which we wish to compare the deviation of local samples of a population from the proportions exhibited by a general population.

XI. Inheritance in the Female Line of Size of Litter in Poland China Sows.

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From the data of the American Poland China Record, the authors determined the inheritance of the size of litters from mother to daughter, using 6145 litters farrowed in 1902. The methods were those commonly employed in statistical studies of heredity.

The tabulation of the sizes of litters from mothers and daughters and the determination of the coefficient of correlation (r) shows that there is an actual correlation between the size of litters of two successive generations, and the authors feel justified in concluding that size of litter is a character transmitted from mother to daughter. The coefficient of correlation for the five years is small (06) but it is appreciable and consequently it would appear proved that by judicious selection of sows from large litters, the average for the breed may be increased.

Correlation in size of Litter of Poland China Sows between Mother (M) and Daughter (D). American Poland China Record.

Age of Daughters	Number of Cases	$rac{ ext{Mean}}{ ext{\textit{M}}}$	Mean D	σ_M	σ_D	r	P. E. of <i>r</i>
1 Year 2 Years 3 Years 4 Years 5 Years	2010 2047 1157 606 325	7·908 7·6927 7·5809 7·6304 7·6738	6:6451 7:5598 7:8799 8:2821 8:4031	2:0764 1:9818 1:9615 1:9856 2:1001	1·7582 1·9415 2·0693 2·0661 2·1571	·1088 ·0885 ·0883 ·0379 ·0032	± '0149 ± '0148 ± '0197 ± '0274 ± '0375
1—5 Years	6145	7.7349	7.4391	2.0202	2.0312	.0601	± ·0086

The decrease from 1088 to practically zero (10032) from the first to the fifth year does not necessarily mean that the inheritance of fecundity is lost as a sow grows older, but probably indicates that inheritance from the dam gradually plays relatively less and less of a part in the determination, while other factors, notably nutrition, play more. The correlation tables are given over page. This work is being followed with an investigation of the inheritance of size of litter through the male line and from the ancestors in the female line.

Size of Litters in which Dams

CORRELATION TABLES OF SIZE OF LITTERS OF SOWS WITH SIZE OF LITTERS IN WHICH DAMS WERE FARROWED. AMERICAN POLAND CHINA RECORD.—LITTERS OF 1902.

TABLE I. Yearling Sows. Size of Litters of Yearling Sows.

wed.		1	2	3	4	5	6	7	8	9	10	11	12	13	Totals
Size of Litters in which Dams were Farrowed.	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17				2 1 5 15 21 27 31 21 14 8 4 2 —	-2 2 2 22 26 34 47 65 53 16 20 7 4 1	1 3 20 28 65 89 67 76 38 21 15 6 2					- - 1 2 2 3 10 6 4 2 - -			7 21 70 125 275 368 368 371 193 121 56 23 10 1
Size	Totals	3	16	41	152	299	431	463	327	172	70	30	3	3	2010

TABLE II. Two-Year-Old Sows. Size of Litters of Two-Year-Old Sows.

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Totals
were rarrowed.	1 2 3 4 5 6 7 8 9 10 11 12 13				$\begin{array}{c} -1 \\ 2 \\ 4 \\ 6 \\ 15 \\ 10 \\ 15 \\ 8 \\ 5 \\ 2 \\ 1 \\ - \\ - \end{array}$			1 2 14 34 70 86 95 61 33 21 9 2	-2 4 10 36 68 84 78 65 45 21 9 3 1		1 2 2 6 27 32 32 33 14 13 4 1	$ \begin{array}{c} -\\ -\\ 3\\6\\8\\12\\11\\20\\15\\7\\3\\1\\1 \end{array} $		- 1 1 2 4 1 1 - -	- - 1 1 1 1 - -		5 23 64 164 317 391 408 324 187 96 45 15
	Totals	2	15	28	69	150	306	431	426	319	168	87	28	12	4	2	2047

TABLE III. Three-Year-Old Sows. Size of Litters of Three-Year-Old Sows.

wed		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	Totals
of Litters in which Dams were Farrowed	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	- - 1 1 1 - - - -	1 1 1 1 1 	1 3 2 5 - 1 1	1 5 5 9 3 3 - 4 - -		1 1 3 17 27 25 31 17 11 5 2 1	1 2 6 15 37 50 40 33 16 14 3 ——————————————————————————————————			 6 4 14 34 22 24 17 6 4 		1 3 3 4 2 2 - 3 - -		21	1 1	1 	1	
Size	Totals	4	4	15	30	80	141	217	230	200	131	68	18	12	3	2	1	1	1157

TABLE IV. Four-Year-Old Sows.

Size of Litters of Four-Year-Old Sows.

S		i	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Totals
Size of Litters in which Dams were Farrowed.	1 2 3 4 5 6 7 8 9 10 11 12 13 14		1 1	1 1 1 1	1 2 2 2 3 3 1 2		2 5 7 13 10 9 5 5 2 1	$ \begin{array}{c c} & 1 \\ & 5 \\ & 6 \\ & 13 \\ & 22 \\ & 15 \\ & 18 \\ & 5 \\ & 1 \\ & - \\ &$	$ \begin{array}{c} 1 \\ -2 \\ 5 \\ 11 \\ 18 \\ 24 \\ 23 \\ 18 \\ 10 \\ 5 \\ 1 \\ - \end{array} $		$ \begin{array}{c} -1 \\ 3 \\ 3 \\ 7 \\ 17 \\ 16 \\ 24 \\ 20 \\ 11 \\ 1 \\ 3 \\ -1 \\ 1 \end{array} $		1 - 2 2 2 6 1 - 2		- - 1 1 1 1 3 1 - -	1	2 9 24 45 78 123 122 109 48 30 10 2
30	Totals	-	2	3	16	36	60	87	118	111	107	36	16	5	8	1	606

TABLE V. Five-Year-Old Sows.

Size of Litters of Five-Year-Old Sows.

were		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Totals
of Litters in which Dams Farrowed.	1 2 3 4 5 6 7 8 9 10 11 12 13 14		1	1	1 1 2 2 1	1 1 4 1 3 4 - - 1	2 3 8 8 3 4 1	$egin{array}{c c} - & - & - & - \\ 1 & 3 & 4 & 12 & 11 & 8 & 3 & 3 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	$ \begin{array}{c c} & 1 \\ & 2 \\ & 6 \\ & 10 \\ & 10 \\ & 14 \\ & 11 \\ & 5 \\ & 2 \\ & 1 \\ & - \end{array} $	$ \begin{array}{c} - \\ 2 \\ 3 \\ 6 \\ 6 \\ 13 \\ 10 \\ 12 \\ 4 \\ 2 \\ 1 \\ 1 \end{array} $	2 4 8 11 4 6 3 4 —	- - 2 7 6 3 4 3 1 - 2	1 - 2 1 1 3 2 2 - -	- - 1 3 - 1 1	2 - 1	1 	
Size	Totals	_	3	1	7	15	32	48	64	61	43	28	12	7	3	1	325

TABLE VI. All Litters, 1902.

Size of Litters of Sows One to Five Years Old.

wed.		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	Totals
of Litters in which Dams were Farrowed	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17		5 1 2 5 7 8 6 1 4 1 —		$\begin{array}{c c} - & 3 & 4 & \\ 10 & 28 & \\ 44 & 49 & \\ 54 & 37 & \\ 21 & 16 & \\ 5 & 2 & \\ - & \\ - & \\ 1 & \end{array}$	-2 10 27 51 84 98 122 93 40 34 12 6	2 6 37 86 159 206 166 141 88 36 29 11 3	3 9 36 82 205 259 242 207 105 61 25 7	1 3 30 90 168 228 223 191 121 63 21 9 3 —		-3 6 13 27 73 105 94 97 51 12 3 1 -		1 1 1 3 7 10 9 18 10 8 7 2 —		1 1 3 2 6 3 		1	1	2 19 75 206 460 905 1185 1173 1019 565 327 134 49 23 1
Size	Totals	9	40	88	274	580	970	1246	1165	863	519	249	77	39	18	6	1	1	6145

NOTICES AND BIBLIOGRAPHY.

NOTICES.

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- Researches into the Theory of Probability. Meddelanden från Lunds Astronomiska Observatorium, Serie II. No. 4. Lund, 1906.
- In (1) Professor Edgeworth, starting from various conditions, some of which he afterwards shows can be relaxed, gives four methods by which one can reach an "approximate expression of the frequency with which in the long run different values are assumed by a quantity which is dependent on a number of variable items or elements." These conditions are that the elements assume different values in random fashion and in the long run recur with a proportionate frequency capable of being represented by a single definite frequency curve; that the variations are independent of each other*; that the method of aggregation by which the elements are compounded is summation, etc. etc.

Professor Edgeworth first gives a method which consists of equating the $t^{\rm th}$ moment of the frequency with the same moment of the given locus. He then shows that the same curve can be reached by working on the lines followed by Professor Morgan Crofton and by the method originated by Laplace and developed by Poisson. He then gives confirmatory evidence by using Laplace's analysis with some of the conditions used by Crofton and inserts the fresh condition that if there be two or more magnitudes each fluctuating according to the law of error, then the sum of each must also fluctuate according to that law.

* [The assumptions that the elementary cause-groups are independent and that the aggregate is obtained by summation have yet to be justified. In particular the first assumption is opposed to the basis of every determinantal theory of heredity, and accordingly the frequency distributions of characters, which result from the fusion and throwing out of chromasomes, i.e. characters in living organisms, are extremely unlikely to comply closely with Professor Edgeworth's form of frequency. I have repeatedly urged the necessity for considering contributions to the aggregate as correlated, i.e. the hypergeometrical as distinguished from the binomial form of series, as the basis of frequency distributions. The skew curves I have introduced proceed from the basis that the "contributory cause-groups" give contributions to the aggregate which are correlated. See Biometrika, Vol. IV. pp. 196, 203 et seq. K. P.]

The general form reached is written

$$e^{-\kappa_1} \frac{1}{3!} \left(\frac{d}{dx}\right)^3 + \kappa_2 \frac{1}{4!} \left(\frac{d}{dx}\right)^4 - \dots + (-1)^t \frac{1}{(t+2)!} \left(\frac{d}{dx}\right)^{t+2} \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2}{2\sigma}}$$

$$\kappa_1^2 = \frac{\mu_3^2}{8\mu_3^3}; \qquad \kappa_2 = \frac{\mu_4 - 3\mu_2^2}{4\mu_2^2}; \text{ etc.}$$

where

If this form be rewritten as

$$F(x) = A_0 \phi(x) + A_3 \phi^{\text{iii}}(x) + A_4 \phi^{\text{iv}}(x) + \dots$$

$$\phi(x) = \frac{1}{\sqrt{2a-a}} e^{-(x-b)^2/2\sigma}$$

where

it becomes the same as that called Type A by Dr Charlier in (3), (5) and (6) and it is also the same as that given by Dr Thiele in "Theory of Observations" (London, C. and E. Layton, 1903) p. 35. Charlier's method of reaching his form is by following Hagen's development of Laplace. The same writer also gives in (4), and considers more minutely in (5) and (6), the form (Type B) which he writes

$$F(x) = B_0 \psi(x) + B_1 \Delta \psi(x) + B_2 \Delta^2 \psi(x) + \dots$$

where

$$\psi(x) = \frac{e^{-\lambda} \sin \pi x}{\pi} \left[\frac{1}{x} - \frac{\lambda}{1!(x-1)} + \frac{\lambda^2}{2!(x-2)} \dots \right].$$

This curve with a range limited in one direction is, we believe, new though Thiele has given a form very closely allied to it (loc. cit. p. 21).

Charlier uses the method of moments for fitting his curves, but though both Edgeworth and he do this, and their series finally take the same form, different graduation results will be reached owing to the index form being used in the one case and not in the other; the difference may, in some cases, be negligible but in others it becomes of more importance and we shall therefore refer to it later.

It will be noticed that in all cases it is proposed to use a series to describe the frequency distribution and there seem to us so many objections to this course in practice that it is well to take this opportunity of examining it. The objections to it are as follows:

- (i) If one of the later coefficients has a large value the neglect of later terms of the series may involve a considerable error, while their inclusion demands the use of the higher moments which are untrustworthy owing to their large probable errors.
- (ii) In some cases the series lead to negative frequencies, which is objectionable. This can often occur with Type A and is noticeable with Thiele's example (*loc. cit.* p. 50).
- (iii) It is necessary to make successive graduations using an increasing number of terms in order to find how many terms of the series are required to give a satisfactory graduation.
- (iv) As we cannot tell at the first how many terms to use, it is necessary to base the solution of the equations for finding the constants on integrations over the whole series from $-\infty$ to $+\infty$ and then neglect terms which may or may not be significant, or else to make successive trials with an increasing number of terms from equations formed from the actual number of terms used. The latter method would be better if the position of negative terms could be decided at the outset and if integration could be effected between any limits that might be indicated. This would however seem to be impossible and Charlier uses the former method; the objection does not apply to Edgeworth's series.

The effect of these objections in the case of Charlier's work is interesting as it is quite impossible to reproduce one of his frequency curves (the bi-modal curve, fig. 5 of (6)) statistically because the negative frequencies play so important a part in the series that if positive frequency only be taken (which is what would happen in practice) an entirely different curve is obtained. We are by no means satisfied that in such cases the integration for moments from $-\infty$ to $+\infty$ is

sound because of the terms which must be omitted in practice, and we think the point deserves more consideration in the mathematical treatment of (5) than it receives. It will perhaps be advisable to give the details of the curve given by Charlier to which our objections refer, and show our failure to reproduce it. The equation to the curve of fig. 5 is

$$F(x) = N[\phi_0(x) - 1 \phi_4(x)],$$

 $\phi_n(x) = \sigma^{n+1} \phi^n(x),$

where

and the ordinates corresponding are given in the first row of the following statement in which, as the curves are symmetrical, the last few terms are omitted.

From Charlier's fig. 5 of (6) Above graduated	- ·0021 - ·0060 - ·0089	+·0095 +·0810 +·1999	+ ·2904 + ·2971 + ·2792 + ·297	1
	- ·0012 - ·0016 + ·0035	+·0269 +·0832 +·1695	+ ·2572 + ·3155 + ·3333 + ·315	5

The moments were calculated about the mean from the figures given but the negative frequencies which Charlier does not give in his diagram and which are meaningless in practical work, were neglected. The values were as follows:

Second moment=4.7089

Third ,, =zero
Fourth ,, =
$$46.987$$

 $\sigma = 2.1700$

and the equation is

$$F(x) = N' [\phi_0(x) - 03671\phi_4(x)].$$

The resulting ordinates are given and will be seen to be very far from the original figures. While of course we know we can reproduce the curve in Charlier's figure by using the negative frequencies we cannot help thinking that there are strong practical objections to the use of the curve in the form in which he writes it so long as such results as that just given can be obtained. If integration had been effected only over the positive area of the curve instead of from $-\infty$ to $+\infty$, the difficulty would not have arisen—but how is such integration to be effected?

The objections here raised to negative frequencies have been surmounted (as is, we think, theoretically necessary) in Edgeworth's work by leaving the equation in the form already given from which it can be seen that negative frequencies are impossible. There are however other difficulties that may arise and one of them can be seen in the example given by Edgeworth on pp. 522 and 523 of (2). This example deals with statistics of fecundity and the total frequency in the series of observations is 1000 while the totals in the first, second and third approximations in Table III, p. 523, are 947, 977 and 960 respectively. These differences between the calculated and observed frequencies are due to the area of part of the curve being neglected in reading off the graduation figures; in other words the frequency curve (Third Approximation) gives 40 cases out of 1000 as having less than no members in a family and the effect of this is that the frequency is on the average understated for the remainder of the curve. The application of Charlier's Type A would have given the graduation shown in the following table and a comparison of this graduation and Edgeworth's brings out the difference between the two methods to which reference has already been made.

For families of from 2 to 9 members, Edgeworth's graduation is close but both tails in his graduation and the start in Charlier's are quite unsatisfactory, while Charlier's curve gives a distorted graduation prior to 7 members, from which point however it agrees admirably. It seems probable however that Charlier would use his Type B for such a distribution and we have added a graduation by the third of his methods of fitting; the agreement is poor in comparison with that shown by Pearson's Type I. An attempt with Charlier's first method of fitting led to

an unsatisfactory result. In all the graduations we could doubtless improve the agreement by using a greater number of terms in the series, but we think a considerable increase in the number would be required to give what we should consider a satisfactory graduation.

Size of family	Observations	Edgeworth's third Approximation	Charlier Type A † $\sigma = 2.928$; $\beta_3 =1214$ $\beta_4 = .0104$	Charlier Type B	Pearson Type I‡
- 3		1*	-2		
-2		9*	4	_	
-1	_	30*	15	12	2
	64	64	38	64	67
1	116	102	71	104	116
2	140	130	108	129	138
3	145	135	137	134	139
4	134	130	148	128	128
5	106	111	135	116	110
6	82	92	108	93	89
7	72	73	78	73	69
8	49	53	54	53	51
9	37	36	37	36	35
10	25	20	27	25	24
11	13	10	18	14	15
12	10	4	12	10	9
13	5	_	7	5	5
14	2	_	4	2	2
15	•4	MARKALINE A	2	1	1
Totals	1000	1000	1001	1000	1000

* Approximation by help of diagram in Edgeworth (2).

+ Notation of Charlier (6), mid-ordinates, found by Charlier's tables, being used.

"Chances of Death," Vol. 1, p. 74.

To the actuary, influenced perhaps by professional bias, the justification of a formula for graduating frequency distributions is its width of application; to some extent we feel that such is also the justification of any theoretical conditions from which a curve is evolved. Edgeworth's series and Charlier's Type A will be found to give good graduations provided the distributions are not markedly skew but they become less satisfactory as the range of the observations takes a definite limit. Charlier's Type B on the other hand is certainly capable of graduating some distributions having a range limited in one direction but, though it can hardly be criticised fully at present, as the author states in (6) that his work on it is not yet complete, it may be well to point out that the solutions he gives are approximate and the choice of solution in any particular case seems somewhat arbitrary. The comparatively poor agreement reached above may be due to this approximate fitting and not to the failure of the curve itself. A statistical criterion to show whether Type A or Type B should be used in any particular case is certainly needed before these types can be used extensively in practice, but even then it would seem impossible to graduate the U-shaped distributions or those that rise abruptly from the axis of x at both ends.

One or two examples, besides that already mentioned, are given in (2), while there is a plentiful supply of statistical examples in (6) and most of them show a close agreement between the theoretical and actual frequencies; some are less satisfactory and fig. 9 of (6) gives so poor a fit that the odds against the graduation are more than 50 to one. There are many other points of interest in (6) beside the main subject, such as a proof, on the basis of Type A, of the relative positions of the mode, mean and median, a method of checking the numerical calculation of

moments, tables of the areas, ordinates and third and fourth differential coefficients of the normal curve, a table of $\psi(x)$ for Type B and a discussion of the dissection of a frequency distribution into components in which some approximate results are given and the suggestion of shortening the solution of the fundamental nonic by means of graphical work is made.

We have put forward the above criticisms to show the practical difficulties we have met in using the suggested methods; though these difficulties seem very important to us they do not

blind us to the energy and ingenuity expended on the papers.

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As this is hardly the type of statistical work that will appeal to our readers it is unnecessary to criticise it.

W. P. E.

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R. P.

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A BIOMETRICAL STUDY OF CONJUGATION IN PARAMECIUM.

By RAYMOND PEARL, Ph.D., University of Pennsylvania, Philadelphia, Pa. U.S.A.

"**** Isolation takes rank with Heredity and Variability as one of the most fundamental principles of organic evolution. For, if these other two principles be granted, the whole theory of descent resolves itself into an inquiry touching the causes, forms and degrees of Homogamy."

ROMANES, 1897.

I. Introduction.

Some time ago it occurred to the writer that it would be of considerable interest to determine whether there was any tendency towards "assortative mating" in the conjugation of Protozoa, especially in the case of the Infusoria. The nuclear phenomena of the process of conjugation in the Infusoria are now fairly well known, as a result of the fundamental researches in this field of Bütschli and Balbiani, and in more recent times of those of Richard Hertwig, Maupas, and Calkins. Briefly the essential facts regarding the process of conjugation are as follows: at intervals in the cultural history (and in nature) pairs of individuals firmly unite with one another and remain together for a certain, usually relatively short, period of time. During this time an exchange of nuclear material takes place. The nuclear and cytoplasmic changes preceding, accompanying and following this exchange are very characteristic, and suggest a certain parallelism to the phenomena connected with the maturation and fertilization of the ovum in sexually reproducing forms. After this exchange of nuclear material has occurred the individuals of the conjugating pair separate and begin anew a cycle of reproduction by fission. Without going at all into the much disputed questions of the homologies of the protozoan nucleus or the different phases of the conjugation process, it is clear that conjugation presents some interesting analogies, at least, to sexual processes in higher forms.

The point which I particularly wished to investigate was whether the original pairing in the conjugation process is entirely at random, or whether there is a tendency for individuals like one another in certain characters to pair together. Pearson and his associates have demonstrated that there exists in man a significant and measurable degree of assortative mating. This assortative mating is of two kinds, (a) preferential mating, and (b) homogamy. In homogamy there is a tendency for a class of males having a given character to unite with a class of females of a generally like character. This results in a positive correlation between

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the members of mated pairs with reference to the character under consideration. From his family measurement data Pearson* has found the following values for the coefficients of correlation measuring homogamy in man. These values measure the degree of correlation between husband and wife with respect to the characters enumerated.

With reference to the character "duration of life" cooperative work + has shown that the mean correlation between husband and wife is 2233. In general, the intensity of homogamy in man, so far as it has been investigated, may be considered to be fairly represented by a coefficient of correlation of from 22 to 23. This tendency of like to mate with like may be due either to "real conscious or unconscious assortative mating in man" or to individuals mating within local sub-races where, on account of the similarity of the environmental effects upon all individuals, there is little differentiation. If it be due to this latter cause, random mating would, of course, give a coefficient of correlation of approximately the same magnitude as that actually observed. That there is real assortative mating with reference to the character "duration of life" was demonstrated by observing that when male and female records were paired together at random the resulting coefficient of correlation differed from zero by less than half its probable error. Since, then, the observed positive correlation between husband and wife is not a mere chance result, the assortative mating thus demonstrated must be due either to conscious choice or to some unknown nonconscious factor.

Now it is quite clear that in the pairing of two infusorians in conjugation conscious choice is not likely to play any important part. Do we find assortative mating in such a case?

At the beginning of the fall semester of the academic year 1903—1904 Miss Mary J. Burr, a student in the University of Michigan, started work on this problem under my direction. As material she used the series of mounted slides of conjugating Paramecia which have for some years been used for teaching purposes in the Zoological Laboratory of that institution. These slides were prepared in 1895—1896 by the Honourable D. C. Worcester, Commissioner of the Interior of the Philippine Islands, who at that time was a member of the zoological staff of the University of Michigan, for the special purpose of serving as material for a study of the nuclear phenomena of conjugation. In this preliminary work 200 pairs of conjugants were measured by Miss Burr. These records form the series designated as AA in the present paper. A preliminary paper‡ was published on this work, but it was thought best not to publish the complete report until it could be checked with additional material.

^{*} Biometrika, Vol. 1. p. 373. † Biometrika, Vol. 11. pp. 481—498. ‡ Sixth Annual Report, Michigan Academy of Science, pp. 184, 185.

After repeated failures I finally succeeded during the past summer (1905) in getting sufficiently abundant material of conjugating Paramecia in the Zoologisches Institut at Leipzig. This additional material made it possible to extend considerably the scope of the work beyond what had been planned when the investigation was begun. As will appear later the Leipzig material fully confirmed the results gained from the earlier AA series.

The main problems with which the present paper specifically deals may be stated as follows:

- 1. Is the portion of the Paramecium population which is in a state of conjugation at a given time differentiated in respect of type or variability or both, from the non-conjugating portion of the population living in the same culture at the same time?
- 2. Is there any tendency for like to pair with like ("assortative mating") in the conjugation of Paramecium, and if so, how strong is this tendency?

At this point I wish to acknowledge gratefully my indebtedness to those who have in various ways aided me in this work. To the officials of the Carnegie Institution I am indebted for a grant in aid of this and other biometric work now in progress. It is a pleasure to express my heartiest thanks for this aid. To Professors Carl Chun, and Otto Zur Strassen I am indebted for the numerous facilities of the Zoologisches Institut at Leipzig, which were so freely and kindly placed at my disposal during my stay there. The work was brought to completion in the Biometric Laboratory of University College, London, and it is a pleasure to acknowledge my great debt to Professor Karl Pearson for helpful advice and kindly criticism.

II. Material and Methods.

The material on which this paper is based is comprised in eight* series of measurements including altogether 1894 individual Paramecia. The cultural history of the different series is as follows:

Series AA, F_E and F_L . The individuals in these series were contained in the mounted slides in the Zoological Laboratory of the University of Michigan

* Note added Nov. 10. In his before-publication criticism of this paper Mr J. J. Lister (Nature, Vol. 74, p. 584) suggests that I have mixed and lumped together these different series and that in consequence all my results are invalid. The reader of my paper will be able to judge of the correctness of Mr Lister's suggestion. I shall be very glad to have a specific instance where I have combined two or more series pointed out. I have always supposed it to be a fundamental axiom regarding the worth of scientific evidence, that the greater the number of pieces of independent evidence there are leading to the same conclusion by so much the more certain does that conclusion become. Acting on this principle I spent a great deal of time getting data from as many independent conditions as possible, and when, as appears in the paper, they all led to the same result, I began to feel that that result was the correct one. According to Mr Lister's new epistemological doctrine this conclusion was wrong and it would have been far better to have measured only one series of individuals. As a working biologist I cannot but feel that Mr Lister ought in justice to his colleagues to issue a definite statement as to whether in his own investigations he follows the principle that the evidence of one witness is more trustworthy than that of several independent witnesses. R. P.

prepared by Professor D. C. Worcester as mentioned above. In series AA pairs of conjugants were chosen for measurement quite at random. In the F series the pairs were chosen on the basis of the nuclear condition for a special purpose, and in a manner which will be fully described later in the paper. Regarding the cultural history of this material information on some particulars is unfortunately lacking. The reason for this is that shortly after the material was collected by Professor Worcester he left the University on an exploring expedition to the Philippine Islands, and, having been afterwards called to public service there, the work on Paramecium was never completed. His notes made at the time the material was collected were misplaced and cannot now be found. The most essential points regarding the material he was, however, able to furnish me from memory. For his kindness in this matter I am very grateful. His statement is as follows:

The material "was obtained originally by collecting decayed cow-lily leaves from one of the Three Sister Lakes*. The material collected was put into stender dishes in the laboratory and covered in the usual way......A little later an epidemic of conjugation started in one of the dishes. It had not progressed far when I discovered it, and from that time for three or four days killings were made at regular intervals, as is usually done with developing embryological material. I cannot state at this time just what the intervals were, but if the bottles in which the material was preserved still exist they ought to showt. The killings were kept up as long as there seemed to be any use in continuing them in order to get a complete series of specimens. The killing fluid was four per cent. solution of formaldehyde saturated with bichloride of mercury. The method pursued was to nearly fill a four-dram homoeopathic vial with the killing fluid and then squirt violently into it a considerable amount of water containing as many Paramecia as possible. As soon as the Paramecia had settled to the bottom of the vial the killing fluid was drawn off and the specimens were shaken up two or three times in distilled water, which was drawn off in each instance as soon as settling had taken place. They were then stained for twelve hours in a one per cent. solution of picrocarmine, rinsed in distilled water, carefully dehydrated[‡], and left in cedar oil, where they seemed to retain their colour perfectly. Mountings were ultimately made in xylol damar, covering glasses being supported by capillary glass rods to prevent crushing of the specimens. I have neglected to state that when the epidemic of conjugation began in this dish I drew off all available material and placed it in clear water in a smaller dish, for convenience in killing. In making the above statements I am, of necessity, trusting entirely to memory, but am very confident that they are correct."

^{*} Small glacial lakes in the vicinity of Ann Arbor. R. P.

[†] This they unfortunately do not. R. P.

[‡] By a highly ingenious process which made the change to the higher grades of alcohol perfectly gradual and so avoided distortion from diffusion currents. To the apparatus which he devised for this purpose Professor Worcester's success in producing such perfect preparations as these are, was, I believe, largely due. R. P.

From the above account it will be seen that the conjugation was between individuals from the same culture. Regarding the general character of this material, I can only say that the preparations are by far the finest I have ever seen of fixed and mounted infusoria, in point of giving a true representation of the condition of the living organisms in respect of shape and size of body. This I may say has been the comment of all who have seen the slides. Unfortunately the stain has now faded somewhat, so that the nuclear conditions are not shown as clearly as was formerly the case.

Series A. C. D and E. The individuals included in these series all came from a single culture in the Zoologisches Institut at Leipzig. This culture was set with dry hay and pond water in an aquarium jar holding about three litres. July 25th. 1905. In about a week there was an abundance of infusorian forms in the culture, the dominant species in point of numbers being Chilomonas paramecium, Paramecium caudatum, and an unidentified species of the common hypotrichan genus Oxytricha, together with immense numbers of a large form of the bacterium Spirillum. Very soon the Oxytrichae began to diminish in numbers, while at the same time the Paramecia rapidly increased until finally there was a very flourishing culture of this form. At this time I was measuring for another purpose specimens of Chilomonas from this culture, and on Tuesday, August 15th, I noticed on a slide which had been mounted during the afternoon of the Saturday before a single pair of conjugating Paramecia. A careful search through samples taken from the culture was at once instituted, with the result that during the remainder of that day I succeeded in finding eight pairs of conjugants. The next day in seven hours of continuous searching I found 22 pairs, the next day 54 pairs, and from that time on the numbers continued to increase until the height of the epidemic was passed. From these facts it will be evident that the epidemic was only just at its beginning on August 15th. It should be stated that from the time all of the cultures were started regular routine examinations were made to see whether conjugation was occurring in any of them. No conjugating individuals were found before this first pair on August 15th.

The plan which it seemed wisest to follow in handling this material was to take samples at somewhat widely separated intervals during the course of the conjugation epidemic. It was deemed best to follow this plan because I had strong reasons to expect, from an experimental study* on variation in Paramecium which has been going on for some two years, that there would be a marked cyclic change in the variation constants during the course of the epidemic, due to environmental influences. It seemed desirable to detect and measure such a progressive change if it should occur. Now it is evident that the simplest way to attain this end would be to make bulk killings of large samples of the culture at suitable intervals, and then measure the preserved individuals at leisure. This method, however, I did not dare to adopt for the reason that the conjugants

^{*} For a preliminary report see Pearl, R., and Dunbar, F. J., "Some Results of a Statistical Study of Variation in Paramecium." Seventh Report, Michigan Academy of Science, pp. 77—86.

were, throughout the epidemic, present in relatively small numbers. It was feared that if large enough samples were taken to ensure statistically adequate numbers of conjugating pairs the culture would either be exhausted, or its balance so disturbed that the Paramecia would rapidly disappear from it. Accordingly the plan adopted was to take a single drop of culture fluid on the slide at a time, search carefully through it, and if a pair of conjugants were found, kill and measure them in the manner presently to be described. By working in this way as rapidly as was consistent with accuracy, it was possible to measure a reasonable sample in two or three working days.

Between each of the different samplings made in this way roughly a week elapsed. It would, of course, have been possible to have measured, even on this plan, somewhat larger samples than those actually taken, but it was hardly practical. After searching and measuring under high pressure for three days of about eight working hours each, one's eyes were so fatigued by the strain that further work without an intervening period of rest was almost an impossibility. The samples taken are, moreover, quite adequate, I think, to show the prevailing condition in the culture at the time.

The measurements taken, then, fall into time groups, as shown in the following table.

Series	Dates of Measurement	Number of Conjugants measured	Number of Non-Conjugants measured
A C D E	August 15th P.M.—August 18th noon, inclusive " 24th A.M.—" " 26th P.M. " 30th " " " " September 6th " " " "	105 pairs 101 ,, 16 ,,	210 202 32 132

A word of explanation is needed regarding Series D and E. These series would have been as large as the others but for the fact that there were but few individuals in the culture to be measured. By August 30th the epidemic of conjugation was practically over. The 16 pairs of Series D were all that could be found after a painstaking search lasting all day, and with two persons working separately. I was compelled then to do with this very short series. No reason for the ending of the epidemic was evident, so far as the observable cultural conditions were concerned.

By September 6th, however, the case was somewhat different. During the week from August 30th to September 6th blue-green algae had begun to grow very rapidly in the culture, until at the latter date they had formed a more or less dense mat over nearly the whole surface of the culture. Concurrently with this increase in the algae the numbers of Paramecia had steadily and rapidly diminished, so that there were comparatively few survivors, and it was only with some difficulty that I got the 132 which were measured. These survivors were

obviously different from what had been the prevailing type of non-conjugants in Series C and D, the most noticeable fact being that the individuals in Series E were unusually broad in proportion to their length. All conjugants, of course, had disappeared long before Series E was taken. After September 6th the growth of algae rapidly increased, and by September 8th Paramecia had completely disappeared from the culture so far as I could determine.

We have then, from this single culture, 1020 individuals included in four samples taken at intervals covering practically the whole course of a conjugation epidemic.

Series B. This is a very short series, comprising only 12 pairs of conjugants and 24 non-conjugants. These came from another of my cultures at Leipzig, set like the one described above, with hay and pond-water and at the same date, July 25th. It, however, had developed in a somewhat different direction, probably largely as a result of having been placed in slightly different conditions with respect to light. The dominant organisms in this culture were algae, various species of Euglena, hypotrichous infusoria, both large and small, and Paramecium. Conjugating Paramecia were first found in this culture on the morning of August 22nd, and measurements on them were begun at once, on the same plan as that adopted in Series A, C, D, and E. During that day only 10 pairs of conjugants were found. From this it was concluded that an epidemic of conjugation was just starting; but this was not the fact, for on the next day, with the most thorough searching, only two pairs of conjugants were found. After that none were found. It seems likely that in this instance there was no true conjugation epidemic at all, but that instead the fact was that in a restricted portion of the culture a limited number of individuals reached the physiological condition for conjugation at the same time.

We may now discuss the methods used in killing and measuring the material, and in the calculation of the constants. The method used in killing and mounting the individuals of Series AA and F has already been described (p. 216). The measuring on these series was done with an ordinary ocular micrometer at a relatively low magnification, such that in Series AA one division of the micrometer was equal to 13 microns, and in the F series to 8.6 microns. At the time these measurements were made no filar micrometer ocular was available. The units of measurement were really a half of 13 microns and 8.6 microns respectively, because at the low magnification it was possible to estimate accurately with the eye whether the points to be measured fell within the upper or lower half of a scale division. It was neither practicable nor, considering the objects in view, worth while to make any closer measurements on these series.

The other series discussed in this paper, viz., A, B, C, D and E, were killed and measured in a somewhat different way. First as to the killing; whenever, in examining a drop of culture fluid on a slide a pair of conjugants was seen, all the individuals on that slide were killed by dropping on it from a pipette eight to ten times as much killing fluid as there was water. The killing fluid used was

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Worcester's formol-sublimate mixture*, consisting of a saturated solution of corrosive sublimate in 10 per cent. formalin. This fluid, when properly used, kills Paramecium without visible distortion or shrinkage⁺. It is the fluid which has been used in collecting the extensive series of Paramecium material mentioned above (p. 216). Some time has been spent in an attempt to measure the same individuals before and after killing, but it has not been possible to find a means which would keep them quiet enough to measure during life with anything approaching accuracy, which did not obviously distort them at the same time. This statement is made after considerable experience with the various substances which have been suggested for this purpose, such as, for example, thin gelatine solutions, etc. That whatever of shrinkage and distortion is produced by the use of the killing fluid is less than the errors of measuring I am certain, though at present I cannot give figures to prove this. Of course it is not to be understood that absolutely all the individuals so killed will not be distorted. Naturally, there will always be specimens which the killing fluid reaches only in a diluted state, but such specimens will be obviously recognizable as distorted, and of course will not be included in the records.

The individuals were at once measured while still in the killing fluid. By this procedure any distortion which might arise from the action of diffusion currents was avoided. The search for conjugant pairs was greatly facilitated by the use of a mechanical stage. The microscope used was by Bausch and Lomb, and the actual magnification was that given by a 2 inch objective and a 1 inch ocular, with a tube length of 160 millimetres. The method of measuring followed was the same as had been previously used in a study of variation in Arcella[†]. By means of a camera lucida the points to be measured were projected on cards, marked with a fine-pointed pencil, and subsequently measured with a sliding-arm caliper with a vernier reading to tenths of a millimetre. By multiplying the

* Cf. Pearl, R., Journal of Applied Microscopy, Vol. vi. p. 2451.

⁺ Note added Nov. 10. In his criticism of this paper, Mr Lister (loc. cit.) says: "In the first place, the specimens have been preserved and fixed, a process which every practical biologist knows to be attended with distortion." By this statement Mr Lister can only intend to spread abroad as widely as possible an ex cathedra pronouncement that I am not a "practical biologist." During the last six years a large part of my time has been spent in the study of living and fixed Paramecia. From statements made in Mr Lister's note I am convinced that he has never made any careful or thorough study of Paramecium (cf. infra, p. 221). Yet, so far as I can see, for no other reason than that I happen to be in a very modest way a worker in biometry, Mr Lister says that I am not a "practical biologist," and with all the weight of his authority implies that my statement that my material was undistorted is

I know of no way to answer a criticism which simply denies the existence of a scientific conscience. Fortunately the innate courtesy of men of science generally makes such criticisms rare. I can only repeat what is stated in the paper above that the distortion produced by the method of killing I have used on Paramecium is well within the limits of instrumental error in the measuring, or in other words that the specimens were not visibly distorted. The truth of this statement I stand ready to demonstrate directly to anyone interested, by exhibition of living and killed specimens side by side. In the present state of development of micro-photographic technique it is unfortunately not a thing which can be demonstrated on paper. R. P.

[‡] Pearl, R., and Dunbar, F. J.: Biometrika, Vol. II. pp. 321-357.

measurements in millimetres so obtained by the proper reduction factor found by calibrating with a stage micrometer divided to hundredths of a millimetre, they were reduced to microns, and so recorded. The arrangement of microscope, camera and paper, was of course kept the same throughout the measuring.

With reference to the selection of individuals to measure, it may be said that in Series A, B, C, D and E specimens were taken entirely at random. Every pair of conjugants, not obviously distorted, which were found on a slide were measured. When the dimensions of the conjugant pair had been marked off. the two undistorted non-conjugants which were nearest to the conjugant pair in the field of view were measured. By taking the non-conjugants in this way any sub-conscious tendency to choose with reference to size characters was avoided. No selection of conjugant pairs on the basis of size was exercised, or was even possible, because all conjugant pairs seen were measured with the exception of a very few-less than 15 pairs out of all measured-which were obviously distorted. In Series AA no non-conjugants were measured. The conjugant pairs were taken as in the other series, i.e., all undistorted conjugants on a slide were measured. In Series F the conjugants were chosen with reference to nuclear condition and separated into two groups on this basis. One group—"Series F. Early"—consisted of specimens in very early stages of the conjugation process and included only individuals in which the micronucleus had not yet divided, and either had not moved out of its notch in the macronucleus, or if it had, was still lying near and anterior to it. The other group—"Series F, Late"—included only pairs in which separation was soon to ensue, where namely the exchange of nuclear material was in process or had already taken place. For two reasons it was very difficult to get even as many specimens as were obtained in these two sharply separated stages. In the first place, in the very early and very late stages of the conjugation process the nuclear changes go on rather rapidly, and as they are perfectly continuous it is obvious that of any single restricted stage there will not be a large number of representatives. Furthermore, some were rejected which should undoubtedly have been included, but in which, on account of the stain having faded, it was impossible to be certain of the stage. No non-conjugants were measured in Series F.

The characters measured were the length and greatest breadth of the body, in all the series except F, where only the length was measured. In taking these measurements the length offered no difficulty, nor did the breadth in the case of the non-conjugants*. In the case of the conjugants, however, the breadth

^{*} Note added Nov. 10. Mr Lister (loc. cit.) says: "Paramecium, as is well known, is not a symmetrical animal. It has been described as 'slipper-shaped'—not a very good comparison, but it will serve to bring out the fact that the proportion of length and breadth presented to the observer will vary according to the aspect from which the individual is viewed." With all due respect to Mr Lister's authority I wish to point out the fact that this statement is entirely erroneous so far as the maximum breadth dimension of a normal Paramecium is concerned. The maximum breadth falls at a transverse plane of the body posterior to the oral groove. At the level of the maximum breadth the outline of a cross-section of the body of Paramecium is circular, and the maximum breadth

is a difficult character to measure, principally for the reason that the line of union between the two individuals is in many cases somewhat indistinct, and it thus becomes difficult to decide at just what point the body of one individual ends and that of the other begins. Furthermore, the close application of the oral surfaces of the bodies of the conjugants to each other in all but the earliest stages of the conjugation process changes somewhat the shape of a cross section of the body. This change is in the direction of a flattening of the oral (ventral) side of the body. Since for obvious reasons in the case of the conjugants the longest dorso-ventral diameter in the sagittal plane had to be taken as the breadth dimension, it is clear that any tendency towards flattening of the oral contour will appear directly in the measurements. The result of such a tendency will be to make the mean breadth lower, relatively to the length, in the conjugants as compared with the non-conjugants. As will be seen later, this is exactly what the measurements show. The conjugants are, in proportion to their length, narrower than the non-conjugants. For the reasons just stated, no special weight must in the opinion of the writer be laid on the breadth dimensions of the The difficulties in the case were perfectly apparent while the measurements were being made, and the breadth dimensions for the conjugants were only included as a matter of routine, and because there was some curiosity to see how the constants would turn out. As a matter of fact the results are much better, i.e., more regular and consistent from series to series, than was expected after the appreciation of the difficulties in the case which one gets from seeing and measuring the actual specimens. It should be kept distinctly in mind, however, that much weight cannot be laid on the results from the breadth measurements of conjugants.

In both the conjugant and non-conjugant individuals the point on the long axis of the body where the line of greatest breadth crossed it had, of necessity, to be estimated by the eye, but, owing to the shape of the body, this usually gives no difficulty in practice. In a normal Paramecium the outline of the body slopes off rather sharply from the region of the greatest breadth to the posterior end. The region of greatest breadth varies somewhat in relative position in different individuals and in different samples. It usually falls slightly behind the

dimension is in consequence the same whatever side of the animal happens to be uppermost. This I take to be a fact known to everyone who has more than the most superficial objective acquaintance with Paramecium. There are very many ways in which it can be demonstrated. One very simple way is to bring a living Paramecium which is rotating on its long axis into such position that its maximum breadth dimension falls between two cross hairs of an ocular micrometer. Another way is to observe with a Braus-Drüner microscope a living Paramecium standing on end, so that one gets a direct view of the posterior end. It will then be seen that the outline at the plane of greatest breadth is a circle. Finally if Mr Lister will look at an actual cross-section (1 to 5 microns thick) of the body of a Paramecium he will see that in the region of the greatest breadth the sections are circular in outline. With his notions of the limitations of technique Mr Lister may doubt the possibility of making these sections, but I have studied a long series of such sections of Paramecium. It seems a very trivial thing to say in a technical paper, but apparently it needs to be pointed out to Mr Lister at least that the asymmetry of Paramecium is the result of the asymmetrical course of the oral groove. Posterior to the oral groove the animal is entirely symmetrical. R. P.

mouth, but may be at the level of the mouth. In cases of doubt as to where the greatest breadth was, a series of transverse diameters were marked off and the longest diameter by actual measurement on the card taken as the breadth. It was necessary to do this in but few cases, however.

To prevent any possibility of misunderstanding as to the measurements taken, the outline drawings in Fig. 1 are introduced.

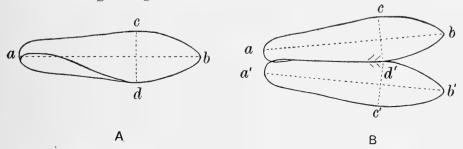


Fig. 1. Diagram to show measurements taken. A, Non-conjugant. B, Pair of conjugants. ab and a'b' = lengths. cd and c'd' = breadths.

Besides the characters length (L) and breadth (B), the length-breadth index = $100\,B/L$, and the difference (in microns) between the lengths of the two individuals of the conjugant pair $(=L_{A\,\text{or}\,B}-L_{B\,\text{or}\,A})$ or of the two individuals of a random pair of conjugants or non-conjugants were studied. The "difference" was taken as always positive, or in other words, without reference to whether A or B was the shorter member of the pair.

The species of Paramecium was the same in all the series, namely P. caudatum. I was in some doubt at the outstart as to whether the Leipzig form might not be P. aurelia, but a careful examination of stained specimens left no doubt that this form had but one micronucleus, thus agreeing in this, as in all the other specific characters, with the form studied at Ann Arbor, namely, P. caudatum.

Finally, as to the calculation of the biometric constants tabulated, it may be said that the ordinary methods, now well known, were followed. In all cases, unless a specific statement to the contrary is made, it will be understood that Sheppard's correction of the second moment was used in getting the standard deviation. In determining the constants for the short series B and D, the material was not grouped at all. For the units of grouping in the other series the reader is referred to the tables in the Appendix to this paper. The constants are tabled to three places of decimals in the case of the means, standard deviations and coefficients of variation, and four places in the case of the coefficients of correlation. It will be understood that in the computing decimals were kept to a larger number of places.

There is one point which needs mentioning regarding the method of recording the data in the case of the conjugants. In every instance the first individual

of a pair of conjugants to be measured was recorded as A, and the second measured as B. Since the order of measurement was entirely random, it is clear that with reference to size, both A and B groups are random samples out of the whole conjugant population A+B. Their constants then should be sensibly equal.

III. Fundamental Constants.

For the sake of convenience in reference, the constants for variation in the various series are collected and shown together in Table I. In the first column of the table is given the letter designating the series; in the second column the class, i.e. conjugant or non-conjugant; in the third column the character, i.e. length, breadth, index or difference; in the fourth column the number of the correlation table in the Appendix, from which the values of the constants on the same horizontal line were deduced; in the fifth, sixth and seventh columns respectively the means, standard deviations and coefficients of variation, and their probable errors; and finally, in the eighth column, the number of individuals included in the frequency distributions from which the constants were calculated. The means and standard deviations for length, breadth and difference are given in microns; for the index in per cent.

IV. Variation in Paramecium.

Before considering especially the specific problems of the paper it will be of interest to compare our results as to variability in this form with those obtained from other series. To this end Tables II. and III. have been formed. Table II. gives the means, standard deviations, and coefficients of variation for the character length in the total series of the present paper in bold faced type, together with the same values for (a) Simpson's* series of 100 individuals; (b) a series of 250 individuals taken from a culture at Ann Arbor†; (c) three "control" series of 500 individuals each, all descended from a common ancestor, and kept in a small volume of culture fluid for 100, 200 and 300 hours respectively‡; (d) three series of 500 individuals each, all descendants from the same ancestor as gave rise to the control series enumerated under (c), but reared for 100, 200 and 300 hours respectively in a very weak solution of cane sugar‡.

This table brings out a number of points of interest. In view of the rather large total number of individuals we may safely conclude I think that it gives a fairly trustworthy representation of the degree of variability of Paramecium in respect to the character length of body. It is obvious that generally with an increase in the mean there is associated an increase in the standard deviation

^{*} Biometrika, Vol. 1. p. 405.

[†] Pearl, R., and Dunbar, F. J.: Seventh Report, Michigan Academy of Science, pp. 77-86, 1905.

 $[\]ddagger$ Ibid. An account of the experiments on which these series are based will be found in the paper referred to.

TABLE I.

Constants of Variation in Paramecium.

22 22 22 23 24 25 27 27 27 27 27 27 27 27 27 27 27 27 27	Class Conjugant A , A , B , B , B All Conjugants , B Non-Conjugants	Length Breadth Index Length Breadth Index Length Breadth Index Length	Table A 3 A 5 A 7 A 3 A 5 A 7 A 1	Mean 167.976 ± .695 43.358 ± .253 25.814 ± .173 168.310 ± .779 45.386 ± .279	Standard Deviation 10.559 ± .491 3.840 ± .179 2.626 ± .122 11.827 ± .550	Coefficient of Variation 6.286 ± .294 8.856 ± .415	No.
22 22 22 23 24 25 27 27 27 27 27 27 27 27 27 27 27 27 27	", A ", A ", B ", B ", B All Conjugants ", ",	Breadth Index Length Breadth Index Length Breadth	A 5 A 7 A 3 A 5 A 7	$43 \cdot 358 \pm 253$ $25 \cdot 814 \pm 173$ $168 \cdot 310 \pm 779$ $45 \cdot 386 \pm 279$	$3.840 \pm .179$ $2.626 \pm .122$	8·856 ± ·415	
22 22 22 23 24 25 27 27 27 27 27 27 27 27 27 27 27 27 27	", A ", A ", B ", B ", B All Conjugants ", ",	Breadth Index Length Breadth Index Length Breadth	A 7 A 3 A 5 A 7	$43 \cdot 358 \pm 253$ $25 \cdot 814 \pm 173$ $168 \cdot 310 \pm 779$ $45 \cdot 386 \pm 279$	$3.840 \pm .179$ $2.626 \pm .122$	8·856 ± ·415	105
))))))))))))))))))))	$\begin{array}{ccccc} & & & A & & \dots \\ & & & B & & \dots \\ & & & B & & \dots \\ & & & B & & \dots \\ & & & B & & \dots \\ & & & & & & & \dots \\ & & & & & & &$	Length Breadth Index Length Breadth	A 3 A 5 A 7	$168 \cdot 310 \pm .779$ $45 \cdot 386 \pm .279$	_		
27 27 27 27 27 27 27 27 27 27 27 27 27 2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Breadth Index Length Breadth	$egin{array}{c} A \ 5 \ A \ 7 \end{array}$	45·386 ± ·279	11.827 + .550		105
77 77 77 77 77 77 77 77	All Conjugants \dots \dots \dots \dots \dots \dots \dots \dots	Index Length Breadth	A7			$7.027 \pm .329$	105
))))))))))))	All Conjugants	Length Breadth			4·240 ± ·197	9·343 ± ·439	105
22 27 22 22 27 22 22 22))	Breadth		$26.862 \pm .175$	$2.665 \pm .124$	0.000 / .000	105
))))))))	" "	1		168·143 ± ·522	11.212 ± .369	6.668 ± .220	210
27 27 27 29	**	Index	$\begin{array}{c}A~1\\A~8\end{array}$	$44.371 \pm .194$ $26.338 \pm .126$	$4.170 \pm .137$ $2.697 \pm .089$	9·398 ± ·312	$\begin{vmatrix} 210 \\ 210 \end{vmatrix}$
27 22 22	Non-Conjugants	Difference	18	8·943 ± ·435	$2.697 \pm .089$ $6.610 \pm .308$	73·914 ± 4·978	105
?? 9?		Length	A2	$189.976 \pm .724$	$15.549 \pm .512$	8·185 ± ·271	210
99		Breadth	A 2	$52.827 \pm .273$	5·870 ± ·193	11·112 ± ·370	210
1 1))))))))	Index		27·848 ± ·116	2·502 + ·082		210
22))))))	Difference	18	17.619 ± .785	11·924 ± ·555	67.676 ± 4.359	105
C	Conjugant A	Length	C3	176.064 ± .887	13·222 ± ·627	7·510 ± ·358	101
>>	" A	Breadth	C5	42·906 ± ·226	3·372 ± ·160	7·860 ± ·375	101
>>	" A	Index	C7	24·342 ± ··161	2·399 ± ·114		101
27	$,, B \dots$	Length	C3	175.965 ± .870	$12.965 \pm .615$	7·368 ± ·351	101
22	,, B	Breadth	C5	43 411 ± ·231	3·436 ± ·163	7.915 ± .378	101
22	$B \dots$	Index	C7	24·649 ± ·159	2·372 ± ·113	F 400 . 057	101
"	All Conjugants	Length	C1	176:015 ± :621	13:094 ± :439	7:439 ± :251	202
>>	" "	Breadth Index	C1	43·158 ± ·162	3·414 ± ·115	7.910 ± .267	$\begin{vmatrix} 202 \\ 202 \end{vmatrix}$
27	27 27	Difference	18	$24.495 \pm .113$ $7.931 \pm .448$	$2.390 \pm .080$ $6.681 \pm .317$	84·245 ± 6·219	101
22	", Non-Conjugants	Length	C_2	209·356 ± ·906	19·099 ± ·641	9.123 ± 0.219	202
77	" Non-Conjugants	Breadth	C2	54·208 ± ·280	5·905 ± ·198	10.894 ± .370	202
"))))	Index		25.911 ± .106	2·238 + ·075	10 001 _ 0.0	202
22	" "	Difference	18	21.010 ± 1.003	$14.939 \pm .709$	71·105 ± 4·785	101
D	Conjugant A	Length	D1	181.250 ± 2.288	13.571 ± 1.618	7·487 ± ·898	16
,,	$B \dots$,,,	D1	182.563 ± 2.099	12.445 ± 1.484	6.817 ± .817	16
,,	All Conjugants	"	D1	181.906 ± 1.554	13.037 ± 1.099	7·167 ± ·607	32
59	"Non-Conjugants	"	D1	217.656 ± 2.319	19.453 ± 1.640	8.937 ± .759	32
E	All Mon Conjuganta	Longth	<i>E</i> 7.1	014.470 1 1.074	70.001	0.700 077	100
	All Non-Conjugants	Length Breadth	E1 $E1$	214·470 ± 1·074	18·291 ± ·759	8.529 ± .357	132
"	"	Index	E_2	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5.786± .240	9·149 ± ·384	$\begin{vmatrix} 132 \\ 132 \end{vmatrix}$
"	"	Thues	122	20 000 <u>r</u> 120	2·132 ± ·089		102
В	Conjugant A	Length	<i>B</i> 1	169·667 ± 3·813	10.501 + 0.606	11.541 + 1.610	10
	Conjugant $A \dots B$	1	B_1	166.667 ± 2.324	19.581 ± 2.696 11.938 + 1.644	11.541 ± 1.610 $7.163 \pm .991$	12 12
"	All Conjugants	77	B1	$168 \cdot 167 + 2 \cdot 242$	16.285 ± 1.585	9·684 ± ·953	24
"	" Non-Conjugants		\tilde{B} 1	199·708 ± 1·890	13.727 ± 1.336	6.874 ± .672	24
	" " "						
AA	Conjugant A	Length	AA1	218.150 + 1.110	18·901 ± ·637	8:664 ± :294	200
,,	" A	D 1/1	$\overline{AA1}$	56.880 ± .476	8·114 ± ·274	14·265 ± ·491	200
"	$B \dots$	Length	AA2	$217 \cdot 200 \pm 1 \cdot 134$	19·309 ± ·651	8.890 ± .302	200
"	$B \dots$	Breadth	AA2	56·445 ± ·523	8.901 ± .300	15·769 ± ·545	200
,,	All Conjugants		AA3	217.675 ± .645	19·112 ± ·456	8.783 ± .211	400
"	"	Breadth	AA4	56.663 ± .287	8.519 ± .203	15.035 ± .367	400
E!	Comingration	Т (2	E*-	200 100			
$F_{\scriptscriptstyle E}$	Conjugant A	Length	F_1	$209 \cdot 103 \pm 1 \cdot 432$	17.767 ± 1.013	8·497 ± ·488	70
"	All Conjugants		F_{0}	207·874 ± 1·345	$16.689 \pm .951$	8.028 ± .461	70
"	All Conjugants	"	F_2	208·489 ± ·983	17·247 ± ·695	8·272 ± ·336	140
$F_{\scriptscriptstyle L}$	Conjugant A	Longth	E'o	014407 1 1 050	15.005 · 05 ·	0.055	
1	, n	1	F_3	214.497 ± 1.378	17:927 ± .974	8·357 ± ·458	77
>>	All Conjugants	1 "	F_4	213.604 ± 1.353 $214.051 \pm .966$	$17.609 \pm .957$ $17.774 \pm .683$	8·244 ± ·451	77
25	An Conjugants	"	1. 4	214 UUIT 900	11 114 T 1083	8·304 ± ·321	154

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TABLE II. Variation in the Length of Paramecium.

Series and Class	Mean	Standard Deviation	Coefficient of Variation	No.
Series A , All Conjugants	$\begin{array}{c} 168 \cdot 143 \pm \cdot 522 \\ 176 \cdot 015 \pm \cdot 621 \\ 182 \cdot 200 \pm \cdot 480 \\ 189 \cdot 976 \pm \cdot 724 \\ 207 \cdot 080 \pm \cdot 518 \\ 208 \cdot 489 \pm \cdot 983 \\ 209 \cdot 356 \pm \cdot 906 \\ 213 \cdot 340 \pm \cdot 601 \\ 214 \cdot 051 \pm \cdot 966 \\ 214 \cdot 470 \pm 1074 \\ 217 \cdot 380 \pm \cdot 592 \\ 2217 \cdot 675 \pm \cdot 645 \\ 221 \cdot 800 \pm \cdot 587 \\ 224 \cdot 980 \pm \cdot 533 \\ 229 \cdot 050 \pm \cdot 246 \cdot 080 \pm \cdot 983 \\ \end{array}$	$\begin{array}{c} 11 \cdot 212 \pm \cdot 369 \\ 13 \cdot 094 \pm \cdot 439 \\ 15 \cdot 917 \pm \cdot 340 \\ 15 \cdot 549 \pm \cdot 512 \\ 17 \cdot 171 \pm \cdot 366 \\ 17 \cdot 247 \pm \cdot 695 \\ 19 \cdot 099 \pm \cdot 641 \\ 19 \cdot 936 \pm \cdot 425 \\ 17 \cdot 774 \pm \cdot 683 \\ 18 \cdot 291 \pm \cdot 759 \\ 19 \cdot 630 \pm \cdot 419 \\ 19 \cdot 112 \pm \cdot 456 \\ 19 \cdot 457 \pm \cdot 415 \\ 17 \cdot 680 \pm \cdot 377 \\ 19 \cdot 152 \pm \\ 23 \cdot 041 \pm \cdot 695 \end{array}$	$\begin{array}{c} 6\cdot 668 \pm \cdot 220 \\ 7\cdot 439 \pm \cdot 251 \\ 8\cdot 736 \pm \cdot 188 \\ 8\cdot 185 \pm \cdot 271 \\ 8\cdot 292 \pm \cdot 178 \\ 8\cdot 272 \pm \cdot 336 \\ 9\cdot 123 \pm \cdot 309 \\ 9\cdot 345 \pm \cdot 201 \\ 8\cdot 529 \pm \cdot 357 \\ 9\cdot 030 \pm \cdot 194 \\ 8\cdot 783 \pm \cdot 211 \\ 8\cdot 772 \pm \cdot 189 \\ 7\cdot 859 \pm \cdot 169 \\ 8\cdot 361 \pm \\ 9\cdot 363 \pm \cdot 285 \\ \end{array}$	210 202 500 210 500 140 202 500 154 132 500 400 500 500 100 250
Total				5000

so that, as a result, the coefficients of variation, measuring the amount of variation relative to size, cluster well together in value. It may be concluded, I think, until equally extensive series showing a different result are forthcoming, that the usual or "normal" value for the coefficient measuring variation in the length of Paramecium caudatum is 8-9 %. The good agreement in the values of the coefficients of variation for the different series is very satisfactory, and is something which probably no biologist would have predicted before measurements were made. One has been accustomed to think that Paramecium because it is a soft-bodied creature is likely to show great and altogether irregular fluctuations. As a matter of fact Paramecium is distinctly less variable in size than is, for example, Arcella \(\) (coefficient of variation = 10.2676°/,) or the crab, Eupagurus prideauxi§ (coefficient of variation for carapace length = from 12 to $19^{\circ}/_{\circ}$), or the ophiuroid, Ophiocoma nigra|| (coefficient of variation > 20 for both disc-breadth and arm-length), all which organisms have a more or less firm exo-skeleton. Furthermore it is perhaps of some interest to note that the degree of variation in length of Paramecium is of the same general order of magnitude as that in the capacity of the human skull.

There can be no doubt I think of the substantial homogeneity of each of the Especially does this impress itself when we compare the variability of

^{*} Biometrika, Vol. 1. p. 405.

[†] Pearl, R., and Dunbar, F. J.: Seventh Report, Michigan Academy of Science, pp. 77-86, 1905.

[‡] Pearl, R., and Dunbar, F. J.: Biometrika, Vol. 11. p. 327.

[§] Schuster, E. H. J.: Biometrika, Vol. 11. p. 195, Table VIII. bis.

^{||} McIntosh, D. C.: Biometrika, Vol. II. pp. 463-473.

the various "Selected Ancestry" series with random series, whether conjugant or non-conjugant. The individuals in these "Selected Ancestry" series all came from the same original single ancestor, and each sample was reared throughout its history under as uniform environmental conditions as it was possible to obtain.

It is apparent that when the table is viewed as a whole the individuals in the conjugant series tend to be both smaller and less variable than those in the non-conjugant series. In the early history of the Leipzig culture all the individuals in it were small, but, as will be shown later in a more direct way, throughout the period during which it was under observation the mean size of the individuals increased. At the same time the variability in proportion to size tended to increase somewhat.

Turning now to the character breadth we unfortunately have at present only one other series for comparison with those reduced in this paper. For the present the longer non-conjugant series alone will be considered with reference to this character. The results are shown in Table III.

TABLE III.

Variation in Breadth of Paramecium.

Series and Class	Mean	Standard Deviation	Coefficient of Variation	No.
Series A , All Non-Conjugants , C , , , , Simpson's Series	52·827 ± ·273	5·870 ± ·193	11·112±·370	210
	54·208 ± ·280	5·905 ± ·198	10·894±·370	202
	63·250 ± ·340	5·786 ± ·240	9·149±·383	132
	68·125	9·155	13·439	100

From this table it is at once evident that in proportion to the magnitude of the dimension the breadth is somewhat more variable than the length in Paramecium, but the difference is not great. The values of the means are, for all three of the present series, lower than that for Simpson's, but this is only what would be expected from the fact that the mean lengths are lower for these particular series also. It would appear that, as the breadth increases in magnitude, it becomes proportionally less variable, but the series of data available at present are too few to decide whether such a relationship is usual.

If we consider the variation analytically we have the results shown in Table IV. This table gives the values of mean, mode, μ_2 , μ_3 , μ_4 , β_1 , $\sqrt{\beta_1}$, β_2 , $3-\beta_2$, κ_2 , and the skewness* for the length and breadth of all conjugants and all non-conjugants of Series A. I have not thought it worth while to determine the analytical constants for any other of the present series for the reason that they are statistically so short, and because I hope to be able to publish eventually the reductions of much more extensive material on variation in Paramecium.

^{*} The analysis of these curves is carried out by the methods given in Pearson's memoir on Skew Variation (*Phil. Trans.* Vol. 186 A, pp. 343—414), and its Supplement (*Ibid.* Vol. 197 A, pp. 443—459).

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In order to test the approach of the distributions to the normal law the probable errors have been determined for the four constants chiefly concerned in such a test, viz. $\sqrt{\beta_1}$, β_2 , d (= difference between mean and mode) and the skewness, on the assumption that the distributions follow the normal or Gaussian law. These probable errors will then define the amount by which the constants will fluctuate, on account of the errors of random sampling from their true values for the normal

TABLE IV.

Analytical Constants for Variation in Paramecium.

				Series A					
Const	ant		Conju	igants	Non-Conjugants				
			Length	Breadth	Length	Breadth			
Number of Ind	lividua	ls	210	210	210	210			
Unit	•••	•••	5 microns	3 microns	5 microns	3 microns			
μ_2		***	5.0287	1.9323	9.6714	3.8286			
μ_3			9882	1.1952	6.2239	1.9867			
μ_4	•••	•••	72.6598	13.5622	270.7506	42.6096			
eta_1	•••	•••	.0077	-1980	.0428	.0703			
$\sqrt{\overline{oldsymbol{eta}_1}}$	• • •		.0876	.4450	•2069	.2652			
eta_2			2.8733	3.6323	2.8946	2.9069			
$3 - \beta_2$	•••		.1267	6323	1054	.0931			
κ_2	***	***	0209	.2330	0958	- 1353			
Mean	***	***	168 • 1429 *	44:3714*	189.9762*	52.8269			
Mode	•••		168.6853*	43.5997*	188.1581 *	51.9275			
d			.5424	.7717	1.8181	.8994			
Skewne	ess		0484	.1851	·1169	.1532			

curve. If the observed values of the constants differ from their theoretically true values by more than two or three times their probable errors, we shall conclude that the distribution does not follow the normal law in one or more particulars. The values for the probable errors of the four constants mentioned, on the assumption that the distributions are normal are as follows: Probable error of $\sqrt{\beta_1} = \pm .1140$ for each distribution; probable error of $\beta_2 = \pm .2280$ for each distribution; probable error of the skewness = $\pm .0570$ for each distribution; finally the probable errors of d are a0 for length of conjugants, a0. a0 for breadth of

^{*} It will be understood that the absolute values of mean and mode are given, and not, as in the case of the moment-coefficients, the values in terms of the unit at the head of each column.

conjugants, \pm ·2377, (c) for length of non-conjugants, \pm ·8863, and (d) for breadth of non-conjugants, \pm ·3346.

It will at once be noted that the skewness is positive in three out of the four cases, or in other words, that the mean falls at a higher value than the mode in these distributions. Having regard to the probable errors, however, the skewness and difference can be regarded as certainly significant in only one distribution—that for the breadth of conjugants. For the length of the conjugants both these constants have values sensibly equal to zero. For both of the non-conjugant distributions it is somewhat doubtful whether the skewness and difference are to be considered to have significant values, but probably they are. It should be said, however, that so far as symmetry is concerned all the curves are not far from the normal type.

If we examine the degree of kurtosis*, measured by the deviation of β_2 from 3 in comparison with the probable error of β_2 , it is evident that all the distributions except that for the breadth of the conjugants are mesokurtic within the limits of error from random sampling. The value of $3 - \beta_2$ in the case of the breadth of the conjugants is almost certainly significant and indicates that the distribution is platykurtic, or in other words, is more "flat-topped" than the normal curve.

The value for $\sqrt{\beta_1}$ differs from zero by an amount which is certainly significant in the breadth distribution of conjugants, and probably significant for the breadth of non-conjugants. For the length distributions the values are insignificant. It should be noted that though in several cases the constants are insignificant in comparison with their probable errors when considered singly, yet the skewness, difference, and $\sqrt{\beta_1}$ for all but one the distributions show a deviation in the same sense. When we have a number of constants all pointing towards skewness rather than symmetry in the distributions we cannot safely say that as a whole the distributions are normal, even though each observed constant taken singly differs by something less than its probable error from its theoretical value. There is a cumulative effect of a number of like results, though each may be insignificant by itself

We conclude then that while all these distributions deviate from the normal law the length distributions do not diverge greatly. The breadth distributions clearly demand skew curves for graduation. The breadth distribution of the conjugants belongs to Pearson's (*loc. cit.*) Type IV., while the same distribution for non-conjugants is of Type I.

It will be understood that these conclusions are not intended to be general but to apply only to the four cases discussed. As has been mentioned above, I hope later to discuss the whole question of variation in Paramecium with much more extensive material.

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^{*} For the introduction of this term to express, in connexion with the prefixes lepto-, meso-, and platy-, the conditions as to the shape of a frequency curve in the region of the mode, cf. Pearson, K., *Biometrika*, Vol. IV. pp. 169—212.

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V. Differentiation of the Conjugant Population.

When the measurements at Leipzig were begun the first point which attracted attention was the fact that, even to the eye the conjugant individuals were distinctly smaller than the non-conjugants living in the culture at the same time. When the measurements were reduced this fact of differentiation within the population was still more clearly shown. We may proceed now to examine its amount and nature. What evidently is required is a comparison of conjugants and non-conjugants with respect to means, variabilities and organic correlations, for each of the characters discussed, namely length, breadth and index. In order not to make too complex a table I shall treat each character separately, taking the length first in Table V. In this table there is given for each series the mean, standard deviation, and coefficient of variation for length in (a) non-conjugants and (b) conjugants; the absolute difference between the constants which is expressed as positive when the non-conjugant constant is larger, and negative when the conjugant is larger; the probable error of the absolute difference; and the relative difference defined as the percentage which the absolute difference is of the nonconjugant constant.

TABLE V.

Differentiation of Conjugants from Non-Conjugants in Length.

Series	Group	Means	Standard Deviations	Coefficients of Variation
A	Non-Conjugants	189·976 ± ·724	15·549 ± ·512	8·185 ± ·271
,,	Conjugants	168·143 ± ·522	11·212 ± ·369	6·668 ± ·220
>>	Absolute Difference	21·833± ·893	4·337 ± ·631	1·517± ·349
>>	Relative "	11·5°/。	27·9°/。	18·5°/。
C ,,	Non-Conjugants	209·356± ·906	19·099 ± ·641	9·123 ± ·309
	Conjugants	176·015± ·621	13·094 ± ·439	7·439 ± ·251
??	Absolute Difference	33·341±1·098	6·005 ± ·777	1·684 ± ·398
??	Relative ,,	15·9°/。	31·4°/。	18·5 °/。
D	Non-Conjugants Conjugants	217.656±2.319 181.906±1.554	19·453±1·640 13·037+1·099	8·937 ± ·759 7·167 ± ·607
>> >> >>	Absolute Difference Relative ,,	35·750±2·792 16·4°/ _o	6·416±1·974 32·98°/。	1·770 ± ·972 19·8°/。
B	Non-Conjugants	199.708±1.890	13·727±1·336	6·874± ·672
	Conjugants	168.167±2.242	16·285+1·585	9·684+ ·953
"	Absolute Difference	31.541 ± 2.932	-2.558 ± 2.073	-2.810±1.166
	Relative ,,	15.8°/。	$18.6^{\circ}/_{\circ}$	40.9°/。

We first notice the large differences between the means. Averaging for the four series the conjugants are 14.9 per cent. shorter than the non-conjugants living in the same culture at the same time. The absolute variability, measured by the standard deviation, averages in Series A, C and D (all from the same culture. it will be remembered) 30.8 per cent, lower in conjugants than in non-conjugants, Of course we should expect the standard deviations for conjugants to give lower values than for non-conjugants, because the conjugants have the lower mean values. Not all the difference, however, is due to this factor, as a glance at the coefficients of variation at once shows. From these it is seen that (averaging Series A. C and D) in proportion to size the conjugants are 18.9 per cent, less variable than the non-conjugants. Series B is in apparent contradiction to this conclusion regarding variability, since it gives a negative difference in both variability columns; that is, in this series, the conjugants are the more variable both absolutely and relatively. The probable errors show, however, that neither for standard deviations nor coefficients of variation are the differences significant. This Series B, for reasons stated above (p. 219), is a very short series, comprising only 12 pairs of conjugants, and a corresponding number of non-conjugants. As a matter of fact, within the large errors incident to such small random samples conjugants and non-conjugants are equally variable in Series B. The means for this series are in good accord with the others, showing as they do a difference of 15.8 per cent. in favour of the non-conjugants.

I think then, that there can be but one conclusion from the facts set forth in Table V., viz. that the Paramecia which are conjugating at a given time are markedly differentiated from the non-conjugant individuals living in the same culture at the same time in both type and variability. For the character length of body this differentiation is in the direction of lowered mean and variability for conjugants as compared with non-conjugants*.

^{*} Note added Nov. 10. Mr Lister (loc. cit.) in criticism of this conclusion says: "Now the non-conjugant population of the latter species [Paramecium caudatum] measured by Dr Pearl to ascertain the range (sic) of their variability would include, not only ordinary individuals, but all stages of individuals in process of differentiation as gametes. The non-conjugants are a heterogeneous population; the conjugants are, on the other hand, approximately homogeneous. This appears to me another and grave source of error in his results on the degree of differentiation and variability of the conjugants." My conclusions from the data presented in this paper are that conjugants are smaller in mean dimensions and less variable than non-conjugants. The first of these conclusions Mr Lister agrees to, because by searching the literature he has found that Maupas observed the same thing. If he had searched the literature a little more diligently he would have found that practically every one who has ever worked on conjugation in Paramecium has noted this fact. Finally if Mr Lister had himself ever carefully observed a culture of Paramecium in which conjugation was going on he would not have needed to go to the literature to learn that conjugant Paramecia are smaller than non-conjugant. To the second of my conclusions, viz., that conjugants exhibit lower variability than do individuals in fission generations Mr Lister objects that the non-conjugant populations measured were heterogeneous. In his opinion then the difference between the variation constants for conjugants and non-conjugants arises because the non-conjugant populations exhibit a spuriously high variability resulting from heterogeneity. Or in other words his contention is that a random sample of non-conjugant individuals from a culture in which conjugation is occurring will show higher variability than a random sample of

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The facts regarding variation in length for the four series A, C, D and E are shown graphically in Diagram I. (pp. 234, 235). This will perhaps bring out more forcibly the facts of Table V. In the diagram we have the frequency distributions plotted to such scales that the areas of all are equal. The units of abscissae are microns of body length, and the ordinates give percentage frequencies. Beginning at the top the polygons are arranged in order of collection. Polygons for conjugants are drawn with continuous lines, those for non-conjugants with dotted lines.

The differences between conjugants and non-conjugants are made very evident by these diagrams. They also bring out clearly another point, namely the progressive change in the means as we pass from the beginning of the epidemic (Series A) to the end (Series E). The mean length of the conjugants increased, during the period from August 15 to August 30, 13:637 microns or 8:2 per cent. of the original mean. In the same way, during the period from August 15 to September 6 the mean length of the non-conjugants increased 24:494 microns, or

"ordinary" Paramecia from a culture in which conjugation is not occurring. Now the worth of this contention can best be judged by an examination of the following table, which has been formed by rearranging the values given in Table II. (p. 226).

Coefficients of Variation for Paramecium.

A Conjugants	B Non-conjugants in cultures where conjugation was occurring	C "Ordinary" Paramecia of selected ancestry from cultures in which con- jugation never occurred
6·668 (210) 7·439 (202) ———————————————————————————————————	8·185 (210) 9·123 (202) 8·529 (132) ————————————————————————————————————	8·736 (500) 8·292 (500) 8·772 (500) 9·345 (500) 9·030 (500) 7·359 (500)
Av. = 7.053	Av. = 8.612	Av. = 8.672

Now the "ordinary" Paramecia of this table (column C) were all of selected ancestry, i.e., were the resultants of the continued division of one single individual. Therefore we should expect them to show if anything reduced variability as compared with Paramecia of mixed ancestry. Further their entire cultural history, beginning with the original single individual, was known and in it conjugation did not occur. But our non-conjugants (column B) are not, as Mr Lister presumes that they are, more variable than are these "ordinary" individuals. They are on the whole about equally variable, as we should expect them to be. Finally it is clear from column A and other data given in the body of the paper that the variability of conjugants is of a totally different order from that of non-conjugants or "ordinary" Paramecia in fission generations. In the light of these figures based on the careful and painstaking measurements of large numbers of individuals I leave it to the reader to judge of the significance of Mr Lister's "grave source of error" in my results. R. P.

12.9 per cent. of the original mean*. These values give some idea of the great changes which are produced in Paramecium as a result of environmental influences. That this increase in mean length in the present case is due to environmental influences and is in no way connected with the conjugation epidemic is evidenced by the fact that the conjugants show an increase as well as the non-conjugants though not by so great an amount. Furthermore the same sort of change has been found in other cases†. Further discussion of this interesting and important matter of environmental influence on variation in Paramecium may be deferred for the present, as I hope to return to it in a special paper based on data collected ad hoc.

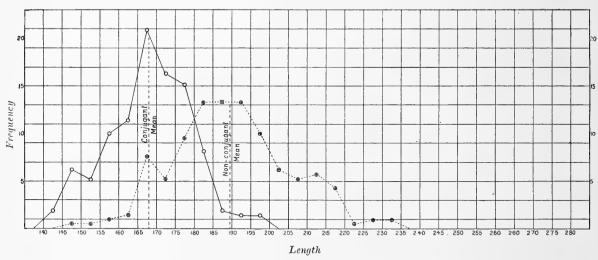
In connection with this increase of mean length during the period of examination, it will be noted that both the absolute and relative differences between conjugants and non-conjugants increase, being lowest for Series A and highest for Series D. In other words, the conjugants and non-conjugants are more differentiated from one another at the end of the conjugation epidemic than they were at the beginning. This is due to the fact that the environmental influences produce a greater effect on the non-conjugants than on conjugants. The significance of this fact on the theoretical side will be discussed later.

Examining the coefficients of variation in Table V., we see that the differences -both absolute and relative—are practically constant for all three series, A, C, and D. In other words, though the means of both conjugants and non-conjugants increase, the amount of variation in proportion to the size does not sensibly change. This seems to be a rather important result, when it is remembered that Series C and D must have included among the non-conjugants measured a larger proportion of recent ex-conjugants than did Series A. It points distinctly to the conclusion that the biological significance or purpose of the conjugation process is not to bring about increased variability. Because clearly if conjugation were followed by greater variation in the ex-conjugants, we should expect the non-conjugant distributions of series C and D (containing more ex-conjugants) to differ sensibly more from the conjugant distributions in variability than does that of series A. Furthermore, if we compare the coefficient of variation for length of series $E = (8.529 \pm .357)$ with the values of the same constant for the non-conjugants of series A, C and D (= $8.185 \pm .271$, $9.123 \pm .309$ and 8.937 ± .759 respectively), it clearly is not significantly greater. But the individuals of series E must have been, in considerable proportion, ex-conjugants, Putting all the results together, there seems no doubt that the primary significance of conjugation is not to produce variability, whatever else it may be.

^{*} The increase, is of course, apparently somewhat greater in the case of the non-conjugants if we take only the period to August 30th, thus making D the last series, since Series D shows a slightly higher mean than Series E. Since, however, D is such a short series it seems likely that we shall come nearer the actual facts by taking the mean of Series E to represent the maximum for the period and culture under discussion. In any event the difference between the means of series D and E for length is not significant in comparison with its probable error.

⁺ Cf. Pearl, R., and Dunbar, F. J., loc. cit.

Series A. August 15th-18th.



Series C. August 24th-26th.

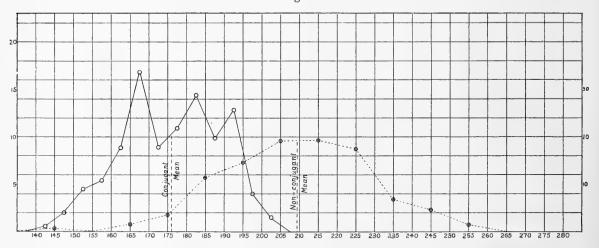
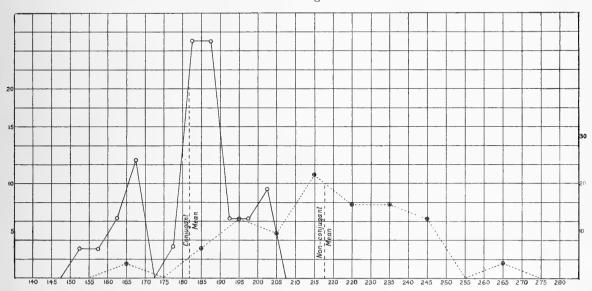
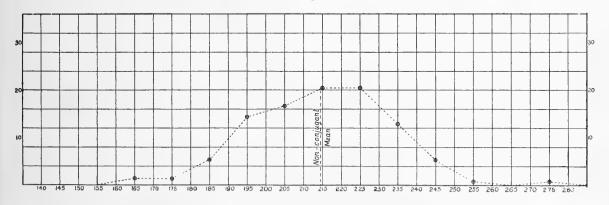


Diagram I. Frequency polygons for variation in length in Series A, C, D and E. Continuous lines=conjugants. Dotted lines=non-conjugants. On the left margin are given the scales of frequency for the continuous line polygons, and on the right margin those for the dotted line polygons.

Series D. August 30.



Series E. September 6.



We may turn now to the character breadth, for which Table VI, has been formed on exactly the same plan as Table V, for length, except that the short series B and D are not included. They show essentially the same relations as A and C and, in view of the small number of individuals, it seems hardly worth while to publish the results from them in detail.

TABLE VI. Differentiation of Conjugants from Non-Conjugants in Breadth.

Series	Group	Group Mean		Coefficient of Variation
A ,,	Non-Conjugants	52·827 ± ·273	5·870 ±·193	11·112±·370
	Conjugants	44·371 ± ·194	4·170 ±·147	9·398±·312
"	Absolute Difference Relative ,,	8·456 ± ·335 16·0 °/。	1·700 ± ·237 28·96 °/。	1·714 ± ·484 15·4°/。
	Non-Conjugants	54·208 ± ·280	5·905 ± ·198	10·894 ± ·370
	Conjugants	43·158 ± ·162	3·414 ± ·115	7·910 ± ·267
??	Absolute Difference	11·050 ± ·324	2·491 ± ·229	2·984 ± ·456
??	Relative ,,	20·4 °/。	42·2 °/。	27·4°/。

From this table it is seen that in breadth the same kind of differences occur between conjugants and non-conjugants as have already been found for length. The conjugants are markedly narrower, and less variable in this character than the non-conjugants. In no case is there any doubt about the difference between conjugants and non-conjugants being significant. The differences are proportionately somewhat larger for breadth than for length, but it should be kept in mind that a part of this excess in relative breadth differences, has the simple explanation that the conjugants have their oral surfaces somewhat flattened, as a result of the union (see above, p. 222). This results in an artificial lowering of the mean and variability in the breadth distributions for conjugants.

Some information regarding the extent of this decrease in breadth due to the conjugation process itself may be gained if we look at the matter in another way. Assume, for the moment, that the selection of conjugants is a selection based on length alone, and that breadth is only different in conjugants from what it is in non-conjugants because it is organically correlated with length. Then clearly the mean breadth of conjugants would be the same as the mean breadth of a group of non-conjugants having the same mean length as the conjugants. Now, for series A and C, the characteristic equations* relating breadth to length in the non-conjugants are as follows:

Series A, Non-conjugants.
$$B = .2224L + 10.576$$
, p.e. = 3.199 , C , $B = .1897L + 14.493$, p.e. = 3.145 ,

^{*} These are calculated by well-known methods given by Pearson, Phil. Trans. Vol. 187 A, pp. 253-318, and also in convenient form by Yule, Jour. Roy. Stat. Soc. Vol. 60, pp. 1-44.

where B signifies breadth in microns and L signifies length in microns. The probable errors of determinations made by these equations are given in microns.

If now, we substitute, for L in these equations the mean length of the conjugants in series A and C respectively and solve for B, we shall get the probable mean breadth of a group of non-conjugants selected to the same mean length as the conjugants. This has been done with the following results:

Series A, Mean Breadth predicted = 47.971 microns, " " observed = 44.371 ", Difference = 3.600 ", Series C, Mean Breadth predicted = 47.883 microns, " " observed = 43.158 ", Difference = 4.725 ".

Now these differences, which in view of the probable errors of the determinations are barely sensible, must represent the sum total of decrease in mean breadth due to (a) direct selection of breadth, provided it occurs, and (b) shrinkage of the breadth dimension measured due to the conjugation process itself. We know from direct observation that (b) occurs and, as will be brought out as we go on, there is no evidence that (a) occurs at all. Hence it seems to me not unlikely that these differences represent practically solely the changes in the oral-aboral breadth dimension due to the conjugation process itself as explained above.

Another interesting point which comes out of Table VI. is that, as we pass from Series A to Series C, there is no increase in the mean breadth corresponding to the increase in length due to environmental influences. The non-conjugants, it is true, show a slight increase (= 1.381 microns), but this is hardly significant in view of the probable error. The conjugants show a decrease of about the same amount. In other words, it is seen that the environmental change which occurred in the culture during the time between the taking of Series A and Series C caused an increase in mean length but not in mean breadth, so consequently the shape was changed, the individuals becoming more slender. This point will be discussed further in connection with the indices.

We may now turn to a consideration of the length-breadth index for conjugants and non-conjugants. Table VII. has been prepared for this character in the same way that Table VI. was for breadths. For the same reasons as before, only Series A and C are included.

This table brings out more clearly several results which have been reached by examination of the lengths and breadths alone. In the first place it is seen that the non-conjugants have a higher mean index in both cases than do the conjugants, but the difference is not great. In other words, as was concluded above, the conjugants are narrower in proportion to their length than the non-conjugants, due to the flattening of the conjugants as a result of the union.

TABLE VII. Differentiation of Conjugants from Non-Conjugants. Index.

Series	Group	Mean	Standard Deviation
$A_{,,}$	Non-Conjugants	$27.848 \pm .116$	2·502 ± ·082
	Conjugants	$26.338 \pm .126$	2·697 ± ·089
"	Absolute Difference Relative ,,	1·510 ± ·171 5·4 °/。	-:195±:121 7:8°/。
C ,,	Non-Conjugants	25·911 ± ·106	$2.238 \pm .075$
	Conjugants	24·495 ± ·113	$2.390 \pm .080$
"	Absolute Difference	1·416 ± ·155	- ·152 ± ·110
	Relative ,,	5·5 °/。	6·8 °/。

We also note that, in passing from Series A to Series C, the index is lowered for both conjugants and non-conjugants about two points (actually the difference for non-conjugants is 1.937 and for conjugants 1.843). The individuals in the culture at the time Series C was taken have become narrower in proportion to length than they were when Series A was taken.

After Series C was taken from the culture the environmental conditions changed rapidly, and with this change, as has been mentioned, a vigorous growth of algae began. At the same time the shape of the Paramecia changed markedly in the reverse direction to the change which had occurred in the interval between Series A and C. Thus in Series E the index (for non-conjugants, of course,) had risen to a mean value of $29.508 \pm .125$, and the variability of the index had decreased to 2.132.

The variabilities of the indices show a relation which at first sight appears paradoxical. In both series the index is more variable in the conjugants than in the non-conjugants, in spite of the fact that both length and breadth, on which the indices are based, are more variable in the non-conjugants. This greater variability of the index in the conjugants, however, really arises from the fact that, as we shall see, the coefficient of correlation between length and breadth is much lower in the conjugants than in the non-conjugants. This point will be much clearer if we consider the general formula for the standard deviation of an index. It has been shown by Pearson* that if x_1 and x_3 be the absolute sizes of two correlated characters, v_1 and v_3 their coefficients of variation

 $\frac{\sigma_1}{m_1}$, $\frac{\sigma_2}{m_2}$, r_{13} the coefficient of correlation between x_1 and x_3 , and i_{13} be the mean

value of the index $\frac{x_1}{x_3}$, and Σ_{13} its standard deviation, then

$$\Sigma_{13} = i_{13} \sqrt{(v_1^2 + v_3^2 - 2r_{13}v_1v_3)}$$
(i).

^{*} Roy. Soc. Proc. Vol. 60, p. 492.

Now it is quite clear that for any given values of v_1 and v_3 the value of the expression under the radical will decrease as r_{13} increases. In our present case the excess of the non-conjugant coefficients of variability over those for the conjugants is not great enough to overbalance the tendency of the high non-conjugant r_{13} to lower the value of Σ_{13} . This is quite clear if we arrange for a single case (Series A) the value of each term in equation (i) in parallel columns for conjugants and non-conjugants. Doing this, we have the following results:

Term	Conjugant	Non-Conjugant
$\begin{matrix} i_{13} & & & \\ v_1{}^2 & & & \\ v_3{}^2 & & & \\ 2v_{13} & & & \\ 2r_{13}v_1v_3 & & \\ v_1{}^2+v_3{}^2 & & \\ v_1{}^2+v_3{}^2-2r_{13}v_1v_3 \end{matrix}$	26·338 88·303609 44·462224 ·5566 34·879840 132·765833 97·885993	27.848 123.476544 66.994225 1.1780 107.141126 190.470769 83.329643

So then we have for the conjugants

$$\Sigma_{13} = \frac{26.338 \times 9.8937}{100} = 2.6058,$$

and for the non-conjugants

$$\Sigma_{_{13}} = \frac{27.848 \times 9.1285}{100} = 2.5421.$$

The values obtained by direct calculation from the index distributions are 2.697 and 2.502 respectively. The values from the formula are thus in very fair agreement with those from the frequency distributions directly, considering that the constants were taken only to three places of decimals.

It is quite clear, then, that it is the higher value of r_{13} for the non-conjugants which brings down the value of Σ_{13} for that group. Series C shows the same relation,

We may now turn to the organic correlations. Besides the correlation of length with breadth, the correlation of the index with length and with breadth will be considered. In Table VIII. are collected all the determinations so far made of the correlation between length and breadth of body in Paramecium. The upper portion of the table is arranged on the same plan as Tables V., VI. and VII. to bring out the differences between conjugants and non-conjugants in respect to degree of correlation between length and breadth. The constant tabulated is the well-known coefficient of correlation, r. In the column headed "Table" is given the number of the table in the Appendix, from which each value of r was calculated.

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TABLE VIII.

Correlation between Length and Breadth of Body in Paramecium.

Series	Group	r	Number	Table
A ,,	Non-Conjugants Conjugants	·5890 ± ·0304 ·2783 ± ·0429	210 210	A 2 A 1
22	Absolute Difference Relative ,,	·3107 ± ·0526 52·7°/。	_	=
C ,,	Non-Conjugants Conjugants	·6135 ± ·0296 ·2063 ± ·0454	202 202	C 2 C 1
"	Absolute Difference Relative ,,	·4072 ± ·0542 66·4 °/。	_	_
E	Non-Conjugants	·6787 ± ·0317	132	<i>E</i> 1
AA "	Conjugants A B	·3952 ± ·0402 ·3728 ± ·0411	200 200	$AA\ 1$ $AA\ 2$
Simpson's	Non-Conjugants	·421 ± ·055	100	

The table shows that the organic correlation between length and breadth of body in Paramecium is rather high and in all cases positive, or in other words, with an increase in length is associated an increase in breadth. If we consider for a moment only the non-conjugants, the coefficient is in every case greater than '5. This emphasizes the fact, which has been mentioned before, that the shape of the body in this infusorian is relatively constant and definite. the coefficients are not, however, unduly high for such an organism is indicated by the fact that in material on variation in the flagellate infusorian Chilomonas paramecium*, the coefficient of correlation of length with breadth is in two fairly extensive series almost exactly equal to that found for the non-conjugant Paramecia of Series C. In this connection, I think we must conclude that Simpson's value for the length-breadth correlation is probably not to be considered as typical for normal Paramecia. It is too low, probably due to the fact that his individuals were measured shortly after fission had occurred. We have what is perhaps a parallel instance in the present series in the very marked lowering of the conjugant correlations. I am inclined to think that the typical or normal value for the correlation between length and breadth of body in Paramecium is not far from '6.

In order to help to an understanding of the degree of relationship implied by correlation coefficients of the magnitude we have found for the length and

^{*} Cf. Biometrika, Vol. v. pp. 64 et seq.

breadth of non-conjugant Paramecia, I have formed Table IX., which gives for purposes of comparison a series of coefficients for different organs and characters.

TABLE IX.

Comparison of Values of the Correlation Coefficient for Various Characters.

Organism			Correlated Characters							r
Actinospheriu	ım*		Number o	f cysts aı	nd size	of body				.7692
"			22 22	nuclei	22	22				*8540
22			11 11	cysts	27	cysts				- 16689
Arcella †			Diameter	of shell a	nd dia	meter of	openin	g		·8 3 6
Paramecium			Length an	d breadt	h, mea	n of all n	on-con	jugants		627
Daphnia ‡			Body leng	th and ce	ell leng	th (Hatcl	hing to	3rd me	oult)	·5505
,,	• • •		,,	22	"		$_{ m 0.4th}$ n			*3930
22			27	22	"		4th m			247

The regressions for the length-breadth correlations are sensibly linear in the present samples. To show the nature of the regression, Diagrams II. and III. have been prepared \S . Diagram II. gives the regression for breadth on length in the case of the conjugants, and Diagram III. the same for the non-conjugants, of Series A.

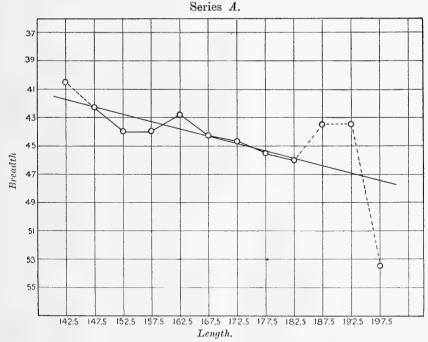


DIAGRAM II. Regression of breadth on length for the conjugants of Series A.

^{*} Smith, G. Biometrika, Vol. II. pp. 243, 246.

⁺ Pearl, R., and Dunbar, F. J. Ibid. Vol. II. p. 330.

‡ Warren, E. Ibid. Vol. II. p. 258.

[§] In the regression diagrams of this memoir, a broken line links points depending on too few observations to be reliable. The absence of any line between two points marks a total failure of intervening observations.



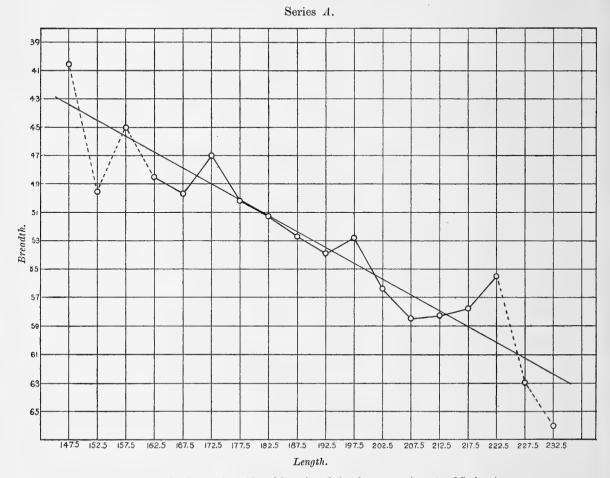


DIAGRAM III. Regression of breadth on length for the non-conjugants of Series A.

Considering the relative smallness of our total numbers, a straight line gives a very good fit to the means of the arrays.

Returning to Table VIII., we see that in both Series A and C the conjugants have length and breadth much less highly correlated than have the non-conjugants. The lowering of the correlation I believe to be due principally to the change in shape which results from the union of the individuals in the conjugation process. Also, the element of difficulty in measuring the breadth of conjugants (cf. supra, p. 222) would operate to lower the length-breadth correlations.

The increase in the value of the length-breadth correlations for the non-conjugants as we pass from Series A to Series E is also to be noted. This again marks the change in the variation constants accompanying the change in environmental conditions in the culture.

We may turn now to the index correlations. For Series A, C and E there have been determined the correlation of the length-breadth index with length

and with breadth for both conjugants and non-conjugants. These index correlations were all calculated by formula, and not from tables directly. That the formula gives very close results for such correlations has been pointed out by several workers, notably C. D. Fawcett* and Macdonnell†. Pearson‡ has shown that in terms of the organic correlations $r_{12} \dots r_{34}$, and the coefficients of variation $v_1 \dots v_4$ of four variable characters, $x_1 \dots x_4$, the coefficients of correlation ρ between

the two indices $\frac{x_1}{x_3}$, and $\frac{x_2}{x_4}$ has the value

$$\rho = \frac{r_{12}v_1v_2 - r_{14}v_1v_4 - r_{23}v_2v_3 + r_{34}v_3v_4}{\sqrt{v_1^2 + v_3^2 - 2r_{13}v_1v_3\sqrt{v_2^2 + v_4^2 - 2r_{24}v_2v_4}}} \qquad (i).$$

In the present instance it is desired to correlate the length-breadth index x_1/x_3 with first length x_3 , and then breadth x_1 . For the index-length correlation substituting the proper value in (i) we get

$$\rho = \frac{r_{13}v_1 - v_3}{\sqrt{v_1^2 + v_3^2 - 2r_{12}v_1v_3}}$$
 (ii).

In the same way for the index-breadth correlation we have

$$\rho = \frac{v_3 - r_{13}v_3}{\sqrt{v_1^2 + v_3^2 - 2r_{13}v_1v_3}}...$$
(iii).

In the values of ρ in each instance there are clearly two factors, (a) the true organic correlation arising from the existence of an organic correlation r_{13} , and (b) the spurious correlation between the index and the characters concerned. The expression for the spurious correlation in the case of the index-length correlation is

$$\rho_0 = \frac{-v_3}{\sqrt{v_1^2 + v_3^2}}$$
(iv),

and that for the index-breadth correlation is

$$ho_0 = rac{v_3}{\sqrt{{v_1}^2 + {v_3}^2}} \dots (v).$$

The latter differs from (iv) only in being positive where that is negative. In the following Table X. there are given in the column headed "Gross" the values calculated from formulae (ii) and (iii), i.e. the values for ρ . In the column headed "Spurious" are given the values of ρ_0 calculated from (iv) and (v), and finally in the column headed "Net" we have the portion of the gross correlation due to true organic correlation between the index and the character, or in other words, the value tabulated in this column is $\rho - \rho_0$.

The results from the index correlations are rather remarkable. In spite of the fact that the index is formed by taking 100 times the breadth divided by the length, the net organic correlation of index with length is in every case positive,

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TABLE X.

Index Correlation in Paramecium.

Series	Group	Characters	Gross	Spurious	Net	No.
A ,,	Conjugants Non-Conjugants	Index and Length "Breadth "Length "Breadth	- ·4096 ± ·0387 ·4864 ± ·0355 - ·1797 ± ·0450 ·3685 ± ·0402	- ·5804 ± ·0309* ·5804 ± ·0309 - ·5931 ± ·0302 ·5931 ± ·0302	·1708 ± ·0452* - ·0940 ± ·0461 ·4134 ± ·0386 - ·2246 ± ·0442	210 210 210 210 210
C ,,	Conjugants Non-Conjugants	Index and Length ,, Breadth ,, Length ,, Breadth	- '6002 ± '0304 '6102 ± '0298 - '2728 ± '0439 '3943 ± '0401	- ·6851 ± ·0252 ·6851 ± ·0252 - ·6420 ± ·0279 ·6420 ± ·0279	·0849 ± ·0471 - ·0749 ± ·0472 ·3692 ± ·0410 - ·2477 ± ·0445	202 202 202 202 202
E ,,	Non-Conjugants	Index and Length ,, Breadth	- ·3263 ± ·0525 ·3855 ± ·04998	- ·6819 ± ·0314 ·6819 ± ·0314	·3556±·0513 -·2964±·0535	132 132

while that for index and breadth is in every case negative. In the case of the conjugants for both series the net index-breadth values are probably not significant. The spurious values are very high and of roughly the same order of magnitude in all cases. Just as where the characters length and breadth are considered separately, the correlations are here always higher for non-conjugants than for conjugants. It is also quite clear, considering the net organic relationship, that the index is throughout more highly correlated with length than with breadth. There would appear to have been no significant change in the index correlations during the history of the culture.

As there seems to be some doubt in the minds of many biologists as to whether the expression $\rho - \rho_0$, measuring the portion of a gross index correlation due to the organic correlation of the characters entering into the index, has any real significance, or if it has, what this significance is, I have prepared the two diagrams which follow with the hope that they may make the matter somewhat clearer. It seems to me that the difficulty regarding the expression $\rho - \rho_0$ comes largely from the fact that biologists usually think of correlation in terms of regression, and the effect of spurious correlation has not hitherto, so far as I know, been expressed in those terms. Diagrams IV. and V. bring out this relation quite clearly. The plan on which these diagrams have been constructed is as follows; in the first place the characteristic equation showing the actually observed relation of index to length

* It should be stated that the probable errors tabled in the "spurious," and "net" columns were calculated from the formula P.E. of $r=67449\,\frac{1-r^2}{\sqrt{N}}$. This procedure assumes that the coefficients are actual coefficients of correlation obtained from tables by the formula $r=\frac{Sxy}{N\sigma_1\sigma_2}$, which, of course, is not the case. In all probability the probable errors as given in the table are not widely divergent from the true values.

was calculated for a particular group (the conjugants of Series A). This characteristic equation is the equation to the regression line which one would actually observe if one made a correlation table of index and length. In calculating it from

the usual expression $b_{xy} = r_{xy} \frac{\sigma_x}{\sigma_y}$, r_{xy} was put equal to the observed ρ , or gross

index correlation; σ_x was the observed standard deviation of index and σ_y the observed standard deviation of length. Then by the usual method a characteristic equation in terms of the units of measurement was formed. In the case of the conjugants of Series A this characteristic equation took the form

$$I = 42.9018 - 0.0985L$$

in which I denotes the probable mean index of an array of type L in length. This line was then plotted on decimal paper. The next step was to calculate for the same group what may be called the spurious regression of index on length, on the assumption that there is no correlation between length and breadth. The equation

for this spurious regression coefficient we may write as $b_{xy_0} = r_{xy_0} \frac{\sigma_{x_0}}{\sigma_y}$, in which

 $r_{xy_0} = \rho_0$, the "spurious" coefficient, and σ_{x_0} is the standard deviation of the "spurious" index distribution. This standard deviation is calculated from the usual formula for the standard deviation of an index*

$$\Sigma_{13} = i_{13} \sqrt{(v_1^2 + v_3^2 - 2r_{13}v_1v_3)},$$

by putting the organic correlation between length and breadth equal to 0. For the case in hand $r_{xy_0} = -.1571$. Forming the regression equation and remembering that it will pass through a mean of its own given by the equation

$$i_{xy_0} = \frac{m_1}{m_3} (1 + v_3^2),$$

in which m_1 and m_3 are the observed mean breadth and length respectively and v_3 is the coefficient of variation for length we get

$$I_0 = 52.9236 - .1571L$$
.

This is the equation of the regression line for index on length when there is no organic correlation of length with breadth. This was plotted to the same scale as the gross regression line, and the two lines are exhibited in Diagram IV. We see at once that, on account of the organic correlation between index and length, apart from the correlation between length and breadth, the regression line AB is pulled around through the shaded area to the position A'B' in the direction of the arrows. The amount and direction of this change is always given by the expression $b_{xy} - b_{xy_0}$, so that we may say that the shaded area in the diagram is in each case the graph of what has taken place owing to $\rho - \rho_0$ differing from zero.

Diagram V. was prepared in exactly the same way and plotted to the same scale but represents the facts for the index-length correlation in the non-conjugants of Series A. Comparing the two diagrams we see that the effect of organic relationship between index and length is much greater in amount in the non-conjugants than in the conjugants.

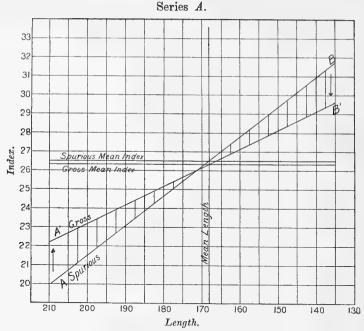


Diagram IV. Showing the relation of the index-length correlations for conjugants of series A. AB is the regression line of index on length when all correlation between length and breadth in the individual is destroyed. It is the regression line for the spurious correlation between index and length A'B' is the "gross" or observed line of regression of index on length. The shaded portion shows the area through which the "spurious" line is moved (in the direction of the arrows) as a result of the existence of an organic correlation between length and breadth in the individual.

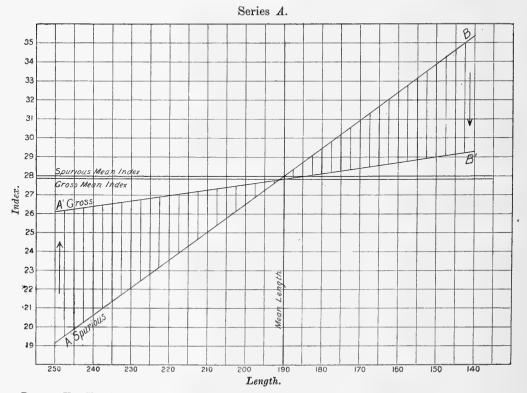


DIAGRAM V. Showing the relation of the index-length correlations in the non-conjugants of Series A.

The significance of the letters is the same as in Diagram IV.

In order to bring out in another way the two facts of (a) environmental change during the history of the culture, and (b) the differentiation of conjugants from non-conjugants I have prepared the following regression tables showing the relation between the three characters length, breadth and index. In order to avoid too many decimals I have multiplied all the regression coefficients by 10. Apart from this the tables are self-explanatory.

TABLE XI.

Regression Table. Series A.

Conjugants.

Non-Conjugants.

Corresponds	Unit change of			
to a probable change in	10 microns in length	10 microns in breadth	10°/° in index	
Length Breadth Index	10μ 1·035μ - ·985 °/ _°	7.483μ 10μ $3.145 ^{\circ}/_{\circ}$	-17.031μ 7.522μ $10 ^{\circ}/_{\circ}$	

Corresponds	Unit change of			
to a probable	10 microns	10 microns	10 °/°	
change in	in length	in breadth	in index	
Length	10μ 2.224μ $289^{\circ}/_{\circ}$	15·602μ	- 11·170μ	
Breadth		10μ	8·647μ	
Index		1·570°/ _°	10 °/。	

TABLE XII.

Regression Table. Series C.

Conjugants.

Non-Conjugants.

Corresponds		Unit change of	of	
to a probable change in	10 microns in length	10 microns in breadth	10°/o in index	
Length Breadth Index	10μ $\cdot 537\mu$ $-1.096 ^{\circ}/_{\circ}$	7.913μ 10μ 4.273 °/ $_{\circ}$	$\begin{array}{c} -32.879 \mu \\ 8.715 \mu \\ 10 \ ^{\circ}/_{o} \end{array}$	

Corresponds	Ι	Unit change o	of
to a probable change in	10 microns in length	10 microns in breadth	10 °/₀ in index
Length Breadth Index	10μ 1.897μ $320 ^{\circ}/_{\circ}$	19·842μ 10μ 1·495°/ _°	$\begin{array}{c} -23\cdot276\mu \\ 10\cdot402\mu \\ 10^\circ/_\circ\end{array}$

TABLE XIII.

Regression Table. Series E.

Non-Conjugants.

Corresponds	Unit change of		
to a probable change in	10 microns in length	10 microns in breadth	10°/° in index
Length Breadth Index	10μ 2·147μ - ·380°/。	21·454 μ 10 μ 1·420°/ $_{\circ}$	$\begin{array}{c} -27.994 \mu \\ 10.463 \mu \\ 10 ^{\circ}/_{\circ} \end{array}$

These tables show very clearly the relation of the different characters in the different series. It will be noted that with a given change in either length or breadth roughly about twice as great a probable change in the associated character (breadth or length) occurs in the non-conjugants as in the conjugants. primarily the result of the higher correlation between length and breadth in the non-conjugants. On the other hand the index changes less with a given change in length or breadth in the non-conjugants than in the conjugants. This means that the shape as measured by the index is more constant with changing lengths and breadths in non-conjugants than in conjugants. In all cases, as we should expect, a unit change in breadth makes a larger change in the index than a unit change in length.

We may now summarize the results of this section as follows. It has been found that in several samples taken at different times from two different cultures there is a pronounced differentiation between conjugant and non-conjugant Paramecia living in the same culture at the same time, in respect to type, variability and organic correlation. The conjugant individuals when compared with the non-conjugant are found to be shorter and narrower, and less variable in both length and breadth. The conjugants have a lower mean index, or in other words are relatively more slender, and are more variable in shape of body as indicated both by the length-breadth index and by the organic correlation between length and breadth. The conjugants have the length and breadth less highly correlated than the non-conjugants. I would especially emphasize the fact that the differences here enumerated are by no means small and of doubtful character, but are, on the contrary, of large and significant amount. The difference in size between conjugants and non-conjugants is perfectly obvious to the eye without any measuring, if one's attention is only called to the matter. The differences here are quite as great or even greater than those which distinguish the most divergent races of men, for example, in the character stature. This point is dwelt upon lest someone might hastily conclude that the differentiation found between conjugants and non-conjugants was something dependent on the proper kind of figure-juggling. The discussion of the biological significance of this differentiation will be left to a later section of the paper, where all the results may be taken as a whole.

During a period in the history of a single culture, occupying about four weeks in time, definite and significant changes occurred in the type of the non-conjugant Paramecia. Similar changes occurred in the conjugants but were smaller in amount. Up to within a week of the dying out of the Paramecia the individuals became, as time went on longer, without a corresponding increase in breadth. As a consequence the body became relatively slenderer in shape. The relative variability of the characters remained constant throughout this period. During the last week of the cultural history the individuals became broader again.

VI. Assortative Mating in Conjugation.

We come now to the consideration of the problem which originally led to the taking up of this work. This problem was: Is there any definite tendency for individuals relatively alike in size to conjugate with one another? It seemed to me at the outstart that though conscious choice, or any selection factor depending on a sexual differentiation, were obviously out of court, yet theoretically it was by no means impossible that a sensible degree of correlation between conjugants might exist. Thus the nature of the conjugation process itself made it seem possible if not probable that the two individuals in a conjugant pair must reasonably well "fit" one another if the conjugation were to be successful. Also it was not at all difficult to conceive that this sorting out of "fitted" pairs might be accomplished in a perfectly mechanical way when Jennings'* work on the reaction of the organism was considered. The difficulty of course came in conceiving that the "fit" of the two individuals would have to be any better, to ensure successful conjugation than we should in the long run get by pairing altogether at random individuals in the same culture. It seemed to me altogether likely that this condition was what actually existed, and I fully expected when the work was begun to find that putting together at random pairs of individuals would lead to just as high a coefficient of correlation between the members of the pairs as we should find from actual conjugants. How far from the facts this expectation was, the results which follow will show. The plan which was adopted to reach a solution of this question of assortative pairing was to determine by actual measurement the degree of correlation between the same and different characters in conjugated pairs and then to determine by experimentally pairing at random the records for these same individuals what degree of correlation we have between the individuals of a pair when there is no assortative mating whatever. Also it seemed desirable to find out what would be the result of putting together at random pairs of non-conjugants and pairs in which one individual was a conjugant and the other a non-conjugant.

A word should be said regarding the practical methods followed in this portion of the work. The first point which needs attention is one regarding the order of entry of individuals into the correlation tables. Suppose we call the individual of each conjugating pair which was the first to be measured A, and the individual of the pair last measured B. Then if, as was actually the case, there is no selection of the first individual to be measured on the basis of size characters, but instead the choice of A is quite accidental, then clearly the biometric constants for the A individuals ought not to differ significantly from those for the B individuals. As a matter of fact they did not differ significantly. Consequently it is a matter of indifference, so long as we are dealing with the same character in both members of the pair, whether A or B is entered into the correlation table as the first variable.

^{*} Various papers in Amer. Jour. Physiol., Amer. Naturalist, Amer. Jour. Psychol., etc. Specially for the reactions preceding conjugation, cf. Jour. Comp. Neurol. and Psychol. Vol. xiv. pp. 441—510.

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Obviously then the proper thing to do is to enter each pair twice, once with A as the first variable and once with B as the first. This will result in making the table symmetrical* with the totals for the rows and columns equal. In each case in the present paper I have first formed correlation tables with A as the first variable, and deduced from each such table its correlation coefficient r. those cases where we were dealing with the same character in both individuals of the pair the tables were made symmetrical and the coefficients of correlation again calculated. In the case of the symmetrical tables the coefficient was not calculated directly from the table but by a formula which is derived from a more general theorem given by Pearson+ for determining the effect on the frequency constants of adding together different samples of material. He shows that if we let x and x' be measures of two organs, and there be N pairs of organs formed by i heterogeneous groups containing n_1 , n_2 , n_3 , ... etc., pairs with means m_1 , m_1' , m_2 , m_2' , m_3 , m_3' , ... etc., standard deviations σ_1 , σ_1' , σ_2 , σ_2' , σ_3 , σ_3' , ... etc., and correlations r_1 , r_2 , r_3 , ... etc., and M, M' be the means of the whole community, Σ, Σ' the standard deviations and R the correlation, then

$$R\Sigma\Sigma'N = S(n\sigma\sigma'r) + S\{n(m-M)(m'-M')\}\dots(i)$$

where S denotes summation with regard to all i groups.

In the case of the symmetrical table clearly the following relations will hold.

$$N = 2n,$$

 $M = M',$
 $\Sigma = \Sigma',$
 $i = 2.$

Equation (i) will then become

$$R\Sigma^{2}N = 2n\sigma\sigma'r + 2n(m-M)(m'-M),$$

whence, dividing by 2n we get

 $R\Sigma^{2} = \sigma\sigma' r + (m - M)(m' - M).$ $M = \frac{m + m'}{2}$ $R\Sigma^{2} = \sigma\sigma' r - \frac{(m - m')^{2}}{4}....(ii).$

But since

we have

On p. 278 of Pearson's memoir above referred to the values of Σ^2 and Σ'^2 are given as follows:

$$egin{aligned} \Sigma^2 = & rac{S\left(n\sigma^2
ight)}{N} + rac{S\left\{n_p n_q \left(m_p - m_q
ight)^2
ight\}}{N^2}, \ & \\ \Sigma'^2 = & rac{S\left(n\sigma'^2
ight)}{N} + rac{S\left\{n_p n_q \left(m_p' - m_q'
ight)^2
ight\}}{N^2}. \end{aligned}$$

^{*} The reason for using such symmetrical tables was first pointed out by Pearson, Phil. Trans. Vol. 197 A, p. 293.

[†] Phil. Trans. Vol. 192 A, p. 277.

In the present case we shall have

$$\Sigma^{\prime 2} = \frac{\sigma^2 + \sigma^{\prime 2}}{2} + \frac{1}{4} (m - m^{\prime})^2.$$

Whence substituting in (ii) we have finally

$$R = \frac{\sigma \sigma' r - \frac{1}{4} (m - m')^2}{\frac{1}{2} (\sigma^2 + \sigma'^2) + \frac{1}{4} (m - m')^2} \dots (iii),$$

which is the desired result.

In order to save space I have given in the Appendix, in those cases where we have both symmetrical and unsymmetrical tables for a given pair of characters, only the symmetrical tables in all but a few instances where the others are introduced for a special purpose.

We may now turn to the results. In Table XIV. are given the coefficients of correlation for what we may call "direct assortative pairing," namely for those cases in which the given character—either length, breadth, or index—in one individual is correlated with the same character in the other individual of the pair.

TABLE XIV.

Direct Assortative Pairing in the Conjugation of Paramecium.

Series	Characters		Coefficient of Correlation from symmetrical tables	Tables	Coefficient of Corre- lation from tables in which each pair is entered but once	No. of pairs
A " " " " " " " " " " " " " " " " " " "	Length of A Breadth of A Index of A Length of A Breadth of A Index of A Length of A Grade A Length of A Breadth of A Breadth of A	Length of B Breadth of B Index of B Length of B Breadth of B Index of B Length of B Ength of B Breadth of B	$\begin{array}{c} \cdot 5327 \pm \cdot 0333 \\ \cdot 2176 \pm \cdot 0443 \\ \cdot 2176 \pm \cdot 0449 \\ \cdot 249 \pm \cdot 0225 \\ \cdot 3417 \pm \cdot 0419 \\ \cdot 5095 \pm \cdot 0351 \\ \cdot 4302 \pm \cdot 0972 \\ \cdot 7941 \pm \cdot 0509 \\ \cdot 5882 \pm \cdot 0221 \\ \cdot 3490 \pm \cdot 0296 \\ \end{array}$	A 3 and 4 A 5 ,, 6 A 7 ,, 8 C 3 ,, 4 C 5 ,, 6 C 7 ,, 8 D 1 B 1 AA 3 AA 4	$\begin{array}{c} ^{\circ}5365 \pm ^{\circ}0469 \\ ^{\circ}2956 \pm ^{\circ}0601 \\ ^{\circ}4017 \pm ^{\circ}0552 \\ ^{\circ}7250 \pm ^{\circ}0318 \\ ^{\circ}3492 \pm ^{\circ}0589 \\ ^{\circ}5157 \pm ^{\circ}0493 \\ ^{\circ}4355 \pm ^{\circ}1366 \\ ^{\circ}9106 \pm ^{\circ}0333 \\ ^{\circ}5893 \pm ^{\circ}0311 \\ ^{\circ}3533 \pm ^{\circ}0417 \end{array}$	105 105 105 101 101 101 16 12 200 200

I think it will be granted by all that these results are remarkable. When we remember that the highest values which have been so far obtained for the coefficients measuring assortative mating in man do not exceed '3, these very high values for Paramecium seem at first sight astonishing or even incredible. In only one case out of five does the coefficient for the lengths give a value lower than '5, and this is in the case of a very small series in which the probable error of the determination is about \pm '1. It should perhaps be stated again that these coefficients represent the actual conditions found by making careful measurements on pairs of conjugants taken entirely at random from three different cultures at different times. There can be no doubt, I think, of the existence of a high degree of correlation between the same characters in the two members of pairs

of conjugating Paramecia as they occur under normal cultural conditions. But although these results demonstrate the existence of a high correlation, they thereby immediately direct attention to the very interesting and important question as to what its origin and meaning may be. The purpose of the further analysis is to throw light, if possible, on these problems.

The first point needing consideration is the character of the regression for these direct correlations. In order to show this, I have prepared diagrams giving the means of the arrays and the fitted regression lines, for the three direct correlations of Series A. Diagram VI. gives the regression of the length of B on the length of A; Diagram VII. the regression of breadth of B on breadth of A; and Diagram VIII. the regression of index of A on index of B.

There can be no doubt of the essential linearity of the regressions. The diagrams show very clearly the regularity with which an increase in the size of one member of the conjugant pair is accompanied by a proportional increase in the other member.

The cross correlations may now be examined. Neglecting the indices, which it hardly seems worth while to consider separately in the cross correlations we have for each group two possible cross correlations, viz., length of A with breadth of B, and length of B with breadth of A. Cross correlations for the short series

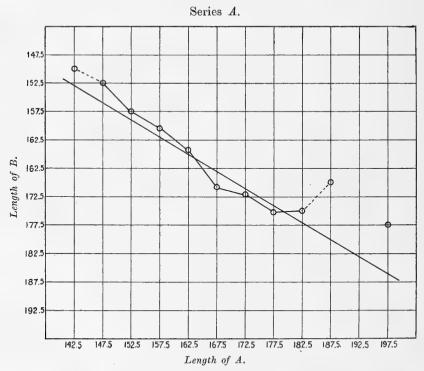


Diagram VI. Regression line for the homogamic correlation between the lengths of the individuals of conjugant pairs in Series A. (See footnote, p. 241.)

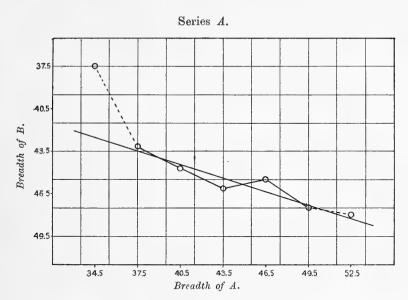


Diagram VII. Regression line for the homogamic correlation between the breadths of the individuals of conjugant pairs in Series A.

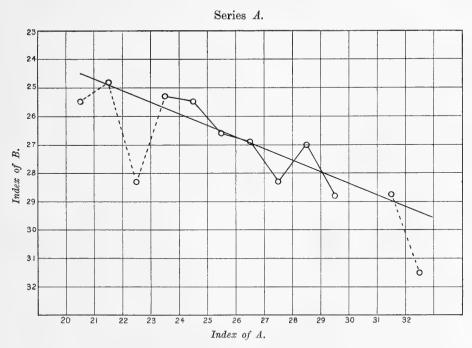


Diagram VIII. Regression line for the homogamic correlation between the indices of the individuals of conjugant pairs in Series A.

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B and D have not been determined. For the other series the coefficients are shown in Table XV.

TABLE XV.

Coefficients of Cross Assortative Pairing in the Conjugation of Paramecium.

Series	Char	acters	Coefficient of Correlation	No. of pairs	Table
A "C "AA "	Length of A ,, B ,, A ,, B ,, A ,, B	Breadth of <i>B</i> ,, <i>A</i> ,, <i>B</i> ,, <i>A</i> ,, <i>A</i>	$\begin{array}{c}0360 \pm .0657 \\ .0969 \pm .0652 \\ .0789 \pm .0667 \\ .1150 \pm .0665 \\ .1740 \pm .0463 \\ .1482 \pm .0466 \end{array}$	105 105 101 101 200 200	A9 $A10$ $C9$ $C10$ $AA5$ $AA6$
		Mean	•10)82*	

We see that these cross coefficients are, with a single exception, positive, but they are all very low. In Series AA alone are the values significant when compared with their probable errors. The higher values for the cross correlations in this series are due, without much doubt, to the higher direct correlation for the breadths, and the relatively high organic correlation between length and breadth which we have found in this series. The relation of the cross coefficients to the direct and organic correlation coefficients will be taken up later.

With the coefficients of assortative pairing, both direct and cross, for the actually occurring conjugant pairs in hand we may attack directly the problem of the origin of the high direct correlations. The first question which arises is as to whether these correlations represent any true assortative pairing or merely arise because conjugation goes on within a limited, differentiated portion of the population, which portion, as has been shown above, is much less variable than the nonconjugant population. If the latter is the true explanation then clearly any random pairing of conjugants ought to give rise to coefficients of correlation equally high within the limits of the probable errors concerned. What then must be done is to make from the records pairs of conjugants chosen entirely at random, and then determine the degree of correlation for such pairs. This "random pairing" has been carried out in the case of the conjugants in the following way. Each individual conjugant's measurements were copied on to a small card or ticket, then these cards were shuffled together in a convenient receptacle, and drawn out blindly, two cards at a time. The two cards so drawn formed a "random" pair of conjugants, and by entering each such pair twice (vide supra p. 249) the symmetrical random tables were formed. For each series and pair of characters a number of these random tables were made. The length-length random correlations are the only ones which it is necessary to discuss here. Others have been

^{*} This is the mean numerical value, without regard to the sign of the coefficients.

made but give the same results. Also, though usually more than one coefficient of correlation for random pairing will be given it has not been thought necessary to publish but one random correlation table for each series. We have then in Table XVI. the coefficients measuring the correlation between the lengths of the two members of random pairs of conjugants. It will be understood that when two values are given for a single series, these values represent different trials. No two random tables on the same material will, of course, give *identical* results. I have tried to give examples of the better and worse results which one gets.

TABLE XVI.

Length-Length Correlation in Random Pairs of Conjugant Paramecia.

Series	Char	acters	Coefficient of Correlation	Table
A A C AA ,,	Length of X ,,, X ,,, X ,,, X	Length of <i>Y</i> ,, <i>Y</i> ,, <i>Y</i> ,, <i>Y</i> ,, <i>Y</i>	- '0847 ± '0462 - '1075 ± '0460 '0449 ± '0474 '0345 ± '0337 - '0360 ± '0337	A 11 C 11 —

It is at once evident that actual conjugation and random pairing of conjugants are quite different things. No one of these random values can be regarded as significantly different from zero, whereas for the same characters and the same individuals paired together as they are in actual conjugation, the coefficients are > 5. The results given for Series A are the most divergent from zero of any of the lot, and in the second of these trials we have a result which may just possibly be significant in comparison with its probable error, but certainly the others are not. We do not even find agreement as to the sign of the random correlation. It would seem that some other factor besides mere random pairing among the conjugants is necessary to produce the high degree of correlation which we find in conjugation.

To test this matter still further I made random pairings in the same way for (a) non-conjugants and (b) pairs, one member of which was a conjugant and the other a non-conjugant, and also (c) I considered as a pair the two non-conjugants which happened to lie in the field of the microscope nearest to each pair of conjugants measured.

These pairings were made to meet special objections which might be raised against considering what we are dealing with here as real homogamy. First it might be said that the observed correlations were in some way due to the fact that conjugants are differentiated from non-conjugants, and that random pairs of non-conjugants might show a spurious homogamic correlation. Random pairings (a) and (b) should test any such hypothesis as this. Again it might be maintained that since at different points in the culture and at different times the environment no doubt differs slightly, there would be a corresponding local differentiation of

the Paramecia in each local culture unit. Then, even though the pairing were quite at random in each locality, yet if the records for several such localities were mixed a spurious homogamic correlation would arise. Now the samples used in this work were taken in just such a way as would make most pronounced any spurious correlation due to local differentiation resulting from place or time factors. Small samples—a drop or two of culture fluid—were taken from different parts of the culture at intervals of time. But it is clear that if the observed homogamic correlation were spurious and due to this "local differentiation" factor, we ought to get sensibly as high values if we consider as a pair the two individuals lying nearest in the field of view to each pair of conjugants measured. Such pairs will have come from the same environment and have been killed at the same instant as the actually conjugated pairs. If such random pairs show no homogamic correlation, then it seems to me that it will have been demonstrated that the observed homogamy is not a spurious correlation due to local differentiation in the culture.

The results of these experimental random pairings are shown in Table XVII.

TABLE XVII.

Length-Length Correlation in Random Pairs of Non-Conjugant Paramecia.

Series			Characte:	rs				r	No. of pairs
À ., ., ., ., ., ., ., ., ., ., ., ., .,	" (Non-Co	onjugants) individuals to onjugants) " individuals to onjugants)	***	nts)	?? ?? ?? ??	(Non-Conjuga "" (Conjugants (Non-Conjuga (Conjugants)	•••	- '0894 ± '0462 '1204 ± '0459 '0908 ± '0462 - '0167 ± '0465 '0407 ± '0464 - '0575 ± '0473 '1190 ± '0468 - '0256 ± '0474	105 105 105 210 210 101 101 202

Here again we reach the same result as before, that random pairings, however made, among the individuals living in the same culture at the time of a conjugation epidemic give rise to correlations between the members of the pair sensibly equal to zero. In Table XVII., four out of the eight coefficients are plus and four minus, and none is significant in comparison with its probable error. These are just the results to be expected if the true value of the coefficient of correlation for random pairing is zero and we take a number of random samples to determine it. We must conclude, I think, that the high coefficient of assortative pairing observed in the actually conjugated pairs cannot be accounted for by any general assumption that there is so little variation in the conjugant population that random pairing will produce high correlation. Random pairing in the identical populations in which we find high homogamic coefficients actually gives rise to zero coefficients. Nor can it be said that the observed homogamy is due to the fact that small samples were taken at different times from different parts of the culture, and

that consequently we are dealing with a spurious correlation which appears because of local differentiation within the culture. If the two individuals lying nearest in the field of view to each conjugant pair measured be taken as a pair and a correlation table formed for such pairs, the coefficient for the homogamic correlation is sensibly zero. Yet such pairs came at the same instant from the same environment that the conjugated pairs did. Therefore the observed correlations for conjugated pairs cannot be due to these factors.

We may now proceed to look at this fact of a high degree of homogamy in conjugant pairs in another way. To say that there is a high degree of homogamy

TABLE XVIII.

Frequency Distributions of the Difference in Length between the Members of (a) Observed Conjugant Pairs, and (b) Random Pairs of Non-Conjugants.

		Conjuga	nt Pairs			dom Pairs o Conjugants		
Difference		Freq	uency			Freq	uency	
in microns	Serie	s A	Serie	s C	Difference in		Series C	
	Conjugated	Random	Conjugated	Random	microns	Series A		
0 1.9	11	10	12	4	0— 3.9	9	12	
2- 3.9	19	4	22	8	4-7.9	16	12	
4- 5.9	14	11	17	12	8-11.9	15	13	
6-7.9	16	9 .	13	12	12-15.9	14	6	
8 9.9	6	6	11	4	16-19.9	11	11	
10—11:9	10	9	5	8	20-23.9	13	6	
1213:9	5	6	5	5	24-27.9	10	12	
1415:9		10	4 3	4	28-31.9	7	7	
1617:9		4 10 8		3	<i>32—35</i> · 9	2	3	
18—19·9	4	6	2	9	<i>36—39</i> ·9	3	4	
20—21.9	6	5	2	4	4043.9	0	8	
22—23·9	1	6	1	7	44-47.9	3	3	
2425.9	1	5	2	3	<i>48—51</i> · 9	0	1	
2627.9	0	0	1	2	$52 - 55 \cdot 9$	1	0	
28-29.9	0	2	0	3	<i>5659</i> · 9	0	2	
30-31.9	1	0	0	6	60-63.9	1	0	
32-33.9		1	0	1	64-67.9		1	
34-35.9	_	4	0	1	_	-	_	
36—37.9		1	1	0				
38—39.9		2	_	0	_	_		
40—41.9		_	-	1		_	_	
42-43.9	_		_	1	distress	_	-	
44—45·9 46—47·9		_	_	2				
40—47°9 48—49°9				0	_	_	_	
40—43 3 50—51·9		_		0			_	
Totals	105	105	101	101		105	101	

in conjugant pairs means that the differences between corresponding characters in the two members of such pairs must be relatively small. It will be of interest to examine the difference distributions for the character length in actually conjugated pairs, and in random pairs of non-conjugants and conjugants. The difference distributions which follow were made by finding the absolute difference (in microns) between the lengths of the two members of a pair, taking the differences as always positive, and forming distributions of their frequencies. The unit of grouping adopted was in the case of the conjugated pairs and random pairs of conjugants 2 microns, and in the case of the random pairs of non-conjugants, 4 microns. These difference distributions are shown in Table XVIII.

It is at once evident from these frequency distributions that the differences in length between the members of pairs are absolutely very much less in the case of the conjugated pairs than in random pairs of either conjugants or non-conjugants, and also they show less "scatter" about the mean. The great divergence between conjugated and random pairs will perhaps not at first sight be evident to one unaccustomed to working with frequency distributions, because of the difference of the units of grouping used. If we plot these distributions, however, as has been done for Series C in Diagram IX., in such a way that the areas and base units of conjugant and non-conjugant polygons are the same, the facts are at once obvious.

It is seen that in over 60 per cent. of the conjugated pairs the two members differ in length by less than 8 microns, while in more than 60 per cent. of the random pairs of conjugants, and in more than 75 per cent. of the random pairs of non-conjugants the difference is 8 microns or more. A more precise comparison of the groups may be made from the constants of the frequency distributions which are exhibited in Table XIX.

TABLE XIX.

Variation Constants for Difference Distributions.

	Series and Groups	Mean	Standard Deviation*	Coefficient of Variation
Series A. ,, A. ,, A. ,, C. ,, C. ,, C.	Conjugated Pairs Conjugants (Random) Non-Conjugants (Random) Conjugated Pairs Conjugants (Random) Non-Conjugants (Random)	$\begin{array}{c} 8.943 \pm .435 \\ 14.143 \pm .631 \\ 17.619 \pm .785 \\ 7.931 \pm .448 \\ 15.673 \pm .758 \\ 21.010 \pm 1.003 \end{array}$	$6.610 \pm .308$ $9.593 \pm .446$ $11.924 \pm .555$ $6.681 \pm .317$ $11.297 \pm .536$ $14.939 \pm .709$	73.914 ± 4.978 67.830 ± 4.376 67.676 ± 4.359 84.245 ± 6.219 72.079 ± 4.885 71.105 ± 4.785

We see that the mean difference in the case of the random pairs is very much greater than in the case of the conjugated pairs. Also the random pairs give a much higher absolute variability. The coefficients of variation are large because

^{*} In calculating the standard deviations for the distributions, Sheppard's correction was not used, because we have no approach to high contact at the lower end of the range.

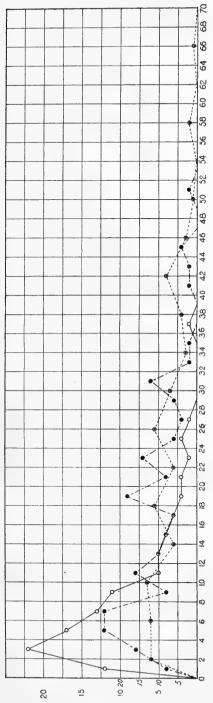


Diagram IX. Frequency polygons for variation in the difference between the lengths of the individuals of conjugated and random pairs in Series C. The unit of abscissa is 2 microns. The scale of ordinates is so taken as to make the areas equal. -o-, Conjugated pairs. ... \(\theta \cdot pairs of non-conjugants. Random pairs of conjugants.

the absolute values of the means are low. From these it would appear that, in proportion to its size, the difference is sensibly equally variable in the conjugant and in the random pairs. It is perhaps doubtful, however, whether any significance should be attached to the coefficient of variation in this case, considering the character we are dealing with. I think it is quite clear that in comparing the conjugated pairs and random pairs of conjugants with respect to the variability of the difference, we should use the standard deviation as the measure, since we are dealing with identically the same individuals in the two cases. The noteworthy thing in this case is that random pairings, whether of conjugants or non-conjugants, give higher mean differences between the members of the pair, and these differences more widely scattered about their mean value, than do normal actually conjugated pairs.

The results of this section may be summarized as follows: In a series of samples taken from different cultures and from the same culture at different times in the history of a conjugation epidemic, it has been found that there exists a high degree of correlation between the lengths of the two members of conjugating pairs. There is a sensible, though not a high, degree of correlation between the members of conjugant pairs with respect to the other characters studied, viz., breadth and index. These high homogamic correlations have been shown to be due to something other than random pairing in a homogeneous population of low variability. An examination of the distribution of the differences in length between the members of conjugant pairs has shown that, as would be expected, the mean difference is much lower and there is less "scatter" about the mean in the case of the conjugating pairs, as compared with random pairings of either conjugants or non-conjugants.

VII. Discussion and Interpretation of Results.

All discussion of results, either in the way of accounting for the phenomena or pointing out their significance, has been deferred to this point for the reason that with all the data in hand the relationship of the different sets of facts to each other comes out more clearly.

We may consider first the fact that the conjugant population is differentiated from the general non-conjugant population in the same culture at the same time. Maupas* maintained that there were several morphological stigmata by which Infusoria in the depressed condition preceding conjugation were marked. One of these morphological characteristics was reduced size. That pre-conjugants are smaller in size than ordinary individuals has been noted by a number of other workers. Thus, for example, Gruber† says that "meist kleinere durch rasch aufeinander folgende Theilungen enstandene Individuen sich conjugiren," though he proceeds in the next sentence to point out what is quite true, that it is "nicht

^{*} Arch. d. zool. exper. et gener. (2) t. vi. pp. 165-277 and Ibid. t. vii. pp. 149-517.

⁺ Bericht der Naturf. Ges., zu Freiburg. i/B. Bd. 11. p. 51.

immer die kleinsten Individuen welche conjugiren." Hertwig* found the same thing in his cultures, namely that conjugants were below average size†.

While there would appear then to be general agreement that the conjugating individuals are usually smaller in size than the average for the general population of non-conjugants, it has not hitherto been noted, so far as I know, that conjugants are also differentiated from the general population in variability and correlation. This is of course only natural since nothing but measurements of considerable numbers of individuals will give an appreciation of variation and correlation in size dimensions in so small an organism as Paramecium. The fact that conjugant individuals are markedly differentiated in variability from the general population if generally true is unquestionably of considerable importance in connection with the whole problem of reproduction and variation in the Infusoria, however the differentiation may be produced. The decrease in size preceding conjugation has usually been explained as due to a brief period at this time of unusually rapid division in which there is little time for growth between succeeding fissions. Calkins t has shown however that this period of rapid division does not always precede conjugation. Consequently the reduced size must, in some cases at least, be due to some other factor. In his most recent paper on the subject, this investigator has brought out some very interesting facts regarding the protoplasmic condition of Paramecium in periods of depression, showing that with the reduced size usually observed at such times there are associated characteristic changes in cytoplasmic and nuclear structures. His results, for the details of which the original paper must be consulted, certainly point to the conclusion that the reduction of size (and also probably the changes in variabilities and correlations) observed in conjugants depend upon fundamental and deep-seated changes in the physiological condition of the organism connected with reproduction. It seems to me that this conclusion is much more probable than that we have to do with any direct selection in the ordinary sense. It is quite clear that there is no immediate elimination of those members of the culture which do not conform to the conjugant type. The possibilities in the way of change of variability in Paramecium without selection, but instead as a result of a direct general bodily rearrangement, or "Umwandlung," are known to be great||, and it seems to me altogether likely that in the differentiation of conjugants from non-conjugants we are dealing with a case of this kind.

There is a point which might be raised in objection to the view that the differentiation of the conjugant population is to be thrown back on deep-seated physiological causes. It might conceivably be maintained that the reduced variability of conjugants which has been found is a result of the conjugation process

^{*} Abhandl, der k. bayer, Akad, der Wissensch, H. Cl. Bd. xvII, pp. 153—233.

[†] Note added Nov. 10. Mr Lister (loc. cit.) accuses me of being ignorant of the literature on this point. I leave it to the reader to judge what foundation exists for this accusation. R. P.

¹ Loc. cit. p. 158.

[§] Calkins, G. M.: Journ. of Exper. Zool. Vol. 1. pp. 423-461.

^{||} Cf. Pearl, R., and Dunbar, F. J.: Seventh Report, Michigan Academy of Science, pp. 77-86.

itself, and not a really significant thing at all. Our data for conjugants are obtained from conjugated pairs, and it might be maintained that the pro-conjugants were simply a random sample from the general population having equal variability with it. Then if we supposed that during the conjugation act itself there was a pronounced tendency towards equalization in size of the two members of a conjugant pair, we might get a reduction in the variability of conjugated individuals as a result of the act of conjugation while the pro-conjugants were not less variable than the general population. Now data were especially collected to determine whether any such process of equalization occurred during the act of conjugation, and anticipating results to be presented in detail farther on, it may be said that the most careful search has failed to find any evidence supporting this view. One has been compelled to conclude that such a process of equalization in size during conjugation does not occur to any appreciable degree. That there is absolutely no tendency to equalization cannot of course be said but, so far as the available data indicate, if any such tendency does exist it is far too slight in amount to account for the changes in variability and correlation observed. Furthermore, such a tendency to equalization would not help us at all in explaining the reduced mean size of conjugants, and it seems altogether probable that the same set of causes are responsible for the changes in means and variabilities.

The first problem with which this paper has to do was stated at the beginning (p. 215) to be "Is the portion of the Paramecium population which is in a state of conjugation at a given time differentiated in respect of type or variability, or both from the non-conjugating portion of the population living in the same culture at the same time?" So far as our present material goes the answer to this question is unequivocally that there is such a differentiation in both type and variability. The morphological differentiation of conjugants is held to be probably due to fundamental physiological changes which precede and lead to conjugation. The further question as to the cause of these physiological changes falls outside the scope of the present investigation. It is a subject on which there is urgent need for experimental work.

We may turn now to the question of homogamy in the conjugation of Paramecium. We have seen that when measurements are taken on the individuals of conjugated pairs, there is found to be a high degree of direct homogamic correlation. Our problem is to find, if possible, a reasonable explanation for the existence of this correlation. It is evident that there are at least two possibilities here which suggest themselves immediately. One is that there is no real pairing of like with like, but that after two individuals have become definitely united in a syzygy, an exchange of substance takes place until there is what we might call an equilibrium of internal pressures. In this process it might be conceived to result that the smaller individual of the pair becomes larger and the larger smaller, so that at the end both would be more nearly alike in size than they were at the beginning. If then we measured the coefficient of homogamic correlation after this had occurred, it might be found high without any real selection having

taken place in the pairing. The homogamy would be altogether physical instead of biological. The alternative hypothesis to that just outlined is that there is a real pairing of like with like, brought about in some way by non-conscious means.

In considering these two alternatives, it seemed to me that the first was rather improbable on general grounds. In the first place no biological evidence has been presented, so far as I know, to show that in the conjugation of Paramecium any such extensive interchange of endoplasm as would be demanded by this view occurs very early in the conjugation process. In this connection it should be pointed out that if we are to explain the degree of homogamy observed by any process of equalization, it will be necessary that the equalizing occur early in the conjugation, as otherwise it will not help us at all. The reason for this is clear. If random samples are taken from a conjugating population we shall get, on the average, just as many early as late stages of the conjugation process. Therefore if equalization between members of the pair does not occur till a late stage, obviously it will have affected but a small portion of the conjugant pairs in any random sample. So then we would not find a high degree of homogamic correlation in such a sample. But, as a matter of fact, we do; hence it is to be concluded, I think, that if any equalization occurs at all, it must occur very early in the process. But observation gives no indication that such an equalization takes place immediately after the union of the individuals. I have been unable to find the slightest evidence that any exchange of material between the two conjugants occurs prior to the exchange of the portions of the micronuclei which, of course, is relatively late in the conjugation process.

Again, on purely physical grounds, it seems to me by no means certain that the equalization hypothesis is adequate. Suppose we consider a Paramecium to be a bag of fluid (the endoplasm) surrounded by an elastic membrane (the ectoplasm and pellicle) in a state of tension. Then it would be expected, according to the laws of curved elastic membranes generally, that if two such bags were connected so that interchange of the contained fluid was possible, it would be pressed from the smaller into the larger, because the larger has the greater radius of curvature and hence less internal pressure assuming that the average state of surface tension is the same for large and small individuals. But this is of course the opposite of what the equalization hypothesis demands. It would seem likely that if an equalization between the two individuals of a conjugant pair occurred, it would have to be accounted for on biological, rather than purely physical grounds.

There is still another consideration which militates against the equalization hypothesis. If the apparent assortative mating arises through any such process, it is difficult to see why the direct homogamic correlation between breadths should not be of about the same degree as that between the lengths. In fact it would seem likely considering the form of the organism that any process of exchange of substance would more nearly equalize the breadths than the lengths of the two individuals of the pair. Thus the breadths would be correlated at least as

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closely as the lengths. But as a matter of fact, as we have seen, there is no approach to equality between the direct homogamic correlations for length and breadth. Those for breadth are always lower.

In order to make, so far as possible, a decisive test of whether the observed homogamic correlation is due to an equalization in size of the two members of the pair during the process of conjugation itself or is, on the other hand, a result of some process such that it exists at the moment of pairing, an investigation based on the following considerations was carried out.

If the observed homogamic correlation is due to any process of equalization in size during the act of conjugation itself, then clearly we should expect to find a higher degree of correlation between the members of pairs in late stages where the individuals would shortly separate than in early stages where the union had just been accomplished. To test this question, 70 pairs of conjugants in very early stages and 77 pairs in late stages were measured. The basis of the separation into "early" and "late" stages was the nuclear condition. The limits chosen as well as other data regarding these two series—designated respectively as "Series F, Early" and "Series F, Late"—have been given in detail earlier in the paper (p. 221) and need not be repeated here. The important thing to keep in mind is that, taken as a whole, the individuals of the F_E series were recently joined pairs, and those of the F_L series were on the whole nearly at the end of the process and would soon have separated. In Table XX, the constants of these two series are compared*. The differences are taken as positive when the "late" series is in excess of the "early," and negative when the opposite condition obtains.

We see at once that the "late" series does not significantly differ from the "early" in anything but the means, and there the difference is only barely significant. Both series are equally variable, and show equally high homogamic correlation. Instead of the "late" series giving the higher values for this correlation, as we should expect on the equalization hypothesis, the "early" series actually has slightly the higher coefficients! The differences are of course not significant in comparison with the probable errors. In fact no closer equality between two random samples of the same population could be desired. The results show that in these samples at least there was no significant change in the size relations of the body associated with the nuclear changes of the conjugation process during that portion of it studied. If any equalization in size between the two individuals occurred, it must have taken place very shortly after the union, and have been a very brief process. Both of these things seem improbable on biological grounds.

In order to get further evidence on the matter some direct observations on the living organism were made, though on account of lack of sufficiently abundant

^{*} It should be stated that the fundamental tables for the F series are grouped in units of the ocular micrometer. The constants deduced were multiplied by 8.6, the value of a micrometer unit in microns, to obtain the means and standard deviations tabled.

TABLE XX.

Variation and Homogamy in Early and Late Stages of the Conjugation Process.

	Charac	eter		Constant	Series .	F, Early	Series	F, Late	Diffe	erence	Tal	oles
Length	of All	Conj	igants	Mean S. D. C. V.	208·489 17·247 8·272	± ·983 ± ·695 ± ·336		± '966 ± '683 ± '321	+ 527	±1:379 ± :975 ± :465	F 2 &	% F 4
Length	of A	***		Mean S. D. C. V.	209·103 17·767 8·497	THE REAL PROPERTY.	17.927	±1:378 ± :974 ± :458	+ 160	±1.987 ±1.405 ± .669	F 1 8	% F 3
Length	of B	•••	•••	Mean S. D. C. V.	207·874 16·689 8·028	_	17:609	±1·353 ± ·957 ± ·451	+ '920	±1:908 ±1:349 ± :645	F18	% F 3
Different and B	nce bet			Mean	11.794		12.286		+ '482			
Correlat			$\{a, b\}$	r † r ‡		7 ± ·0307 2 ± ·0430		2± ·0334 3± ·0471		5 ± ·0454 9 ± ·0638		& F 4 & F 3
Numb	er of l	Pairs				70		77			_	

material it was not possible to do much in this direction. The results so far as they went were in entire accord with what was found from the statistics. I was unable to detect any change whatever in the relative lengths of the two members of the pair after conjugation had occurred.

Altogether, taking into account the results from the F series and from direct observations, together with the fact that we get closely accordant results for the homogamic correlations in all our series, though the Ann Arbor series were collected in a quite different manner from the Leipzig series, I think we must conclude that there is no evidence to support the view that these correlations arise because of any equalization in size during the conjugation itself. It is on the other hand quite clear, of course, that the evidence here presented does not demonstrate that equalization does not occur immediately after union is effected. I can think of but one way in which to get absolutely conclusive evidence on this point, and that is to isolate, kill and measure pairs immediately after definite union has occurred. If the homogamic correlation in a reasonably large sample of this kind is no different from that of conjugants in general, it will be demonstrated that homogamy is not due to equalization after union.

^{*} Without reference to whether A or B is the larger.

[†] Coefficient from symmetrical table in which each pair is entered twice. See p. 249.

[#] Coefficient from table in which each pair is entered but once.

We may now consider the second alternative, namely that the homogamic correlation is real and arises at the moment the definitive pairing occurs. The only difficulty with this alternative is that of understanding how any real assortative pairing can take place in such a low organism as Paramecium. This difficulty however is more apparent than real, I believe. Let us consider some of the known facts regarding the behaviour preceding conjugation*.

The points which are especially important for our present purpose are as follows. (1) It is well known that a modification of the body substance occurs, resulting in the organisms becoming adhesive on their oral surfaces (cf. Calkins, loc. cit., and Jennings†). They are then in what Calkins calls the miscible state. At such times, as has been noted by different observers, groups of several individuals may be formed and subsequently separated again. Single pairs by no means always remain united after they have once come together. Thus Jennings says: "Specimens.....become adherent in every possible way provided merely that some part of the oral surface of one of the individuals enters into the adhesion. Many such cases are clearly not early stages of any ordered conjugation, and they often separate after one individual has been dragged about for some time much against his struggles."

- (2) I have been able to observe in a few instances that the firm union of the two individuals in a definite ordered conjugation involves at the beginning only the extreme anterior ends. Next the mouth regions unite firmly, and somewhat later the portions of the body between the two points. I have not infrequently found pairs in which firm union had occurred at the anterior ends and the mouth regions, and in which there was no contact between the individuals in the intermediate region of the bodies. These observations confirm what has been found by Gruber§. He says, "Die Vereinigung geschieht zunächst vorne an der Spitze der beiden Infusorien und dann an den Mundöffnungen also näher den Hintergrunde. An diesen beiden Stellen bleiben die Thiere festvereinigt, während der übrige Theil des Körpers nur lose oder gar nicht mit dem des anderen Individuums vereinigt ist."
- (3) The coming together of a particular pair of individuals in the proper position for effective conjugation is without any doubt, I think, a matter of random chance. What is in all likelikood the true explanation of this has been given by Jennings in the following words: "A second important factor in bringing

^{*} It is a matter of deep regret to me that I have been able to make so few observations myself regarding the behaviour at the time of conjugation, but I have not yet been fortunate enough to obtain a culture in which a conjugation epidemic involving large numbers of the population was taking place. For observations of this kind on behaviour one must have large numbers of individuals. In what follows then I shall have to make use largely of the observations of other workers, though in no case is a statement made which has not been confirmed, either by my own observations, or by at least two independent investigators.

[†] Jennings, H. S.: Jour. Comp. Neurol. and Psychol. Vol. xiv. No. 6, pp. 480-482.

[‡] Cf. for example Jennings, loc. cit. p. 481, and Gruber, loc. cit. p. 45.

[§] Gruber, loc. cit. p. 46. || loc. cit. p. 482.

[¶] The first is the adhesiveness of the oral surfaces mentioned above. R. P.

about conjugation is found in the usual ciliary movements of the animals, and in the currents produced by these movements. As we have seen in the foregoing pages, there is a strong current passing backward along the oral side of Paramecium so that there is a tendency for all sorts of objects suspended in the water to be carried to the oral groove. This tendency is of course operative on other Paramecia in the neighbourhood, as well as upon lifeless objects. In the case of two Paramecia close together, this tendency is of course reciprocal; each tends to draw the other to its own oral groove. Thus if two Paramecia are swimming along close together, there is a strong tendency through their usual movements for them to come together with oral surfaces in contact. Under ordinary conditions this is often seen, but does not lead to conjugation because the oral surfaces are not adhesive. But when the oral surfaces are adhesive, as we know them to be at periods of conjugation, then the animals stick together."

Now, considering all these facts, we are able to understand I think how the observed homogamic correlation may arise. For the sake of clearness, a brief and somewhat categorical outline of the process as I conceive it to occur will be given first, and then the points which need further discussion will be taken up afterwards. (a) At the periods of conjugation, the individuals which are to conjugate are in a certain physiological state associated with the "miscible" condition in which the oral surfaces are adhesive. (b) As a result of the reciprocal action of the currents produced by the oral groove cilia, two individuals which by chance happen to be swimming parallel and close to one another are drawn together, and their oral surfaces adhere in whole or in part. (c) The extreme anterior ends of the oral grooves firmly adhere to one another first. (d) If the two individuals are so nearly the same size that the mouths approximately coincide when the anterior ends are together, firm union occurs at the mouth regions and definite conjugation follows. (e) If, on the other hand, the mouths do not approximately coincide the individuals separate again or die, and no conjugation results. (f) The homogamic correlations arise then as a result of the necessity for the mouths of the two individuals to come together (or "fit") when the extreme anterior ends are united. Individuals in which the distances from the anterior end to the mouth are approximately equal will not be greatly different in total length, and hence their lengths will be correlated.

We may now consider the evidence regarding the various points. The facts (a), (b), and (c) rest on direct observation. With reference to (d) it may be said that out of hundreds of pairs of conjugants examined none has been seen in which the mouths did not coincide. The extreme anterior ends of the individuals of conjugant pairs (points a, a' in Fig. 1) are in the great majority of pairs approximately equidistant from the mouths. In other words, if pairs of conjugants are examined with reference to the relative position of the extreme anterior ends it will be found that the end of one in most cases projects but relatively little in front of the anterior end of the other. Of course variation occurs in this as in everything else, but I think I am safe in saying that as a maximum

not more than 10 per cent. of the total difference in length between the individuals of conjugant pairs is due to difference at the anterior ends. I do not present measurements in support of this statement for the simple reason that the magnification used in the measuring was not sufficiently high for the accurate determination of this "anterior end difference," so small is it in the great majority of cases. I think, however, that the statement that in definitely conjugated pairs of Paramecium the mouths and anterior ends of the two individuals approximately coincide will not be questioned by anyone who has ever examined closely large numbers of such pairs. Finally if (d), and the comments which have just been made regarding it be true, then (c) must necessarily be true, because if we observe that all successful conjugants have the mouths and anterior ends approximately coinciding, then clearly all pairs which did not fulfil these conditions when the individuals came together by chance, must have either separated or died. The probability of separation being what actually happens is strongly indicated by the observations of Gruber and Jennings cited above. Similarly (f) necessarily follows from (d), if there be positive correlation between total length and distance from anterior end to mouth, the existence of which can hardly be

All things considered, I think that, at least till further evidence is forthcoming, the conclusion is justified that the observed homogamic correlation arises as a result of the factors set forth above, (a) to (e). On this view the real essence of the matter is the necessity for anterior ends and mouths to "fit" reasonably well if conjugation is to be successful. The mechanism by which individuals which do "fit" are brought together is readily to be accounted for by well-established factors in the "action system" of the organism, and involves no assumption of consciousness or any vitalistic hypothesis.

It is the belief of the writer that a considerable degree of homogamy will probably be found to exist in the conjugation of other Protozoa than Paramecium, though of course no other form has yet been investigated in connection with this matter. An observation recorded by Calkins*, concerning the infusorian *Lionotus fasciola*, is of interest in this connection. He says that "In conjugation a large form unites with a smaller one, the mouth parts being united." Such a conjugant pair is found in his Fig. 33. It would be very interesting to study this case biometrically, in the light of the results on Paramecium. There would seem to be two possibilities in the case of Lionotus; one that there is a dimorphic condition of pro-conjugants paralleling sexual differentiation in higher forms, either with or without positive assortative pairing: the other that there is a negative assortative pairing in the conjugation. In any event the case seems well worth investigating.

According to the explanation which has been given for the origin of the homogamic correlation in Paramecium, the assorting in the pairing is held to be concerned only with the lengths of the individuals. If this explanation be true the homogamic correlation between the breadths of the two individuals of a pair

^{*} Bulletin of the U.S. Fish Commission for 1901, pp. 413-468.

and the cross assortative correlations must arise from the existence of an organic correlation between length and breadth in the individual and the direct selection of lengths. It would seem that we had here the means of making a conclusive statistical test of whether all the assorting in the conjugation is on the basis of length alone, by making use of the theorems in selection which Pearson* has given. Thus it should be possible to determine what would be the values of the correlations between the breadths, and between length and breadth after a selection of the lengths alone. Unfortunately, however, these theorems cannot be applied in the present case because of a fact which has been discussed before in the paper, namely that the breadth dimensions of the conjugants are changed as a result of the union in conjugation itself. As we have no data on the pro-conjugant population it is impossible to make accurate allowance for the effect of this flattening of the conjugants upon the variations and correlations. The whole matter has been studied carefully from the statistical standpoint, with the general result which may be stated without the publication of all the equations and figures, that if we assume the assorting in the conjugation to be on the basis of length alone we get a system of values for the direct breadth with breadth correlations and the cross correlations which are not inconsistent with the observed values, allowing for the effect of the change in breadth which occurs during the union. It may be possible later to make an accurate allowance for this disturbing factor, and then the complete evidence can be presented.

Finally, in bringing the paper to a close, I wish to point out what seem to me to be some of the significant theoretical bearings of the results. These, I think, fall under two general heads; namely, first those considerations which arise from the fact that the conjugants are differentiated from the non-conjugants and secondly those considerations which are implied by the existence of a high degree of homogamy in the conjugation. These points will be discussed in the order mentioned.

The results of this work have given clear and indubitable evidence that in the different samples and different cultures the individuals which are conjugating at a given moment belong to a distinct type, clearly and markedly differentiated from the type of individuals which are not conjugating. The facts regarding the details of this differentiation have been shown in extenso earlier in the paper (Tables V., VI., VII., VIII., X., and XI., and Diagram 1), and I think there can be no doubt as to its existence in the mind of anyone who will take the pains to examine carefully these tables. Thus, unless the results are repudiated on the general ground that the material here used was in no way representative of Paramecia in general[†], these facts mean that there is in Paramecium what may be called

^{*} Phil. Trans. Vol. 200 A, pp. 1-66.

[†] That such a criticism cannot fairly be made is sufficiently evidenced by the fact, which every comparative table in the paper clearly shows, that there is a very good agreement between the results for different series taken from different cultures in different ways. Table II. by itself demonstrates that the material here used cannot be considered abnormal.

a conjugant type. Furthermore, this conjugant type is differentiated from the general population, not only in physiological but in morphological characteristics.

Now, it seems to me that the fundamentally important question is whether this differentiated conjugant type is relatively more constant as we pass from culture to culture or race to race than is the type of the general population. We know that under varying environmental influences the type of the general population in the case of Paramecia (and Protozoa generally) can be greatly modified, as a direct result of environmental action*. Is the conjugant type modified to as great a degree as is the type of the general population by such direct environmental influences? The question is clearly one of inter-rather than intra-racial variability, and as such requires a much larger amount of material than is now available for a conclusive answer. However, the results from the present material, as will be shown, point very definitely to the conclusion that the "conjugant type" is much less variable, that is, fluctuates less, as we pass from one environmental condition to another, than does the type of the general population. This fact will have been noticed, I think, from the tables given in Sections III., IV., and V. of the paper, but to make certain of the matter a direct consideration of the problem will be undertaken here.

In order to test the question as to whether the "conjugant" and "general population" types are equally changed with changing environmental conditions the biometrical procedure is to measure the amount of variation in the two types as we pass from one culture or sample to another. Now, in the present case, we have only four series of conjugants (A, C, D, and B) to put over against five series of non-conjugants (A, C, D, E, and B). The Ann Arbor series (AA and F) cannot fairly be included here because unfortunately no non-conjugants were measured from the cultures from which these came. With such small series as four in one case and five in another, it is quite clear that if any conclusions at all are to be drawn as to a difference between the series, the differences between the constants must be large. As a matter of fact the results of a comparison of conjugant and non-conjugant types in respect to length of body, are as follows \dagger :

Mean of conjugant means = 172 408. Mean of non-conjugant means = 203 177. Standard deviation of conjugant means = 4 459. Standard deviation of non-conjugant means = 10 513.

In other words we see that as we pass from one culture to another, and from one state of a culture to another, the non-conjugant type fluctuates more than twice as much as does the conjugant type. It might be objected that we should

^{*} Cf. for example, Yasuda, A.: Jour. Coll. Sci., Imp. Univ. Tōkyō, Vol. xm. pp. 101—140, and Pearl, R., and Dunbar, F. J., loc. cit.

[†] It should be stated that in calculating these inter-racial constants the different series were weighted roughly in proportion to the number of individuals included in each series. It seemed hardly fair to allow the same weight to the very short series B and D as to the longer A, C and E series. So then the series were assigned weights as follows: A = C = 8, B = D = 1, E = 4. As a matter of fact it makes very little difference in the final results if all the series are given equal weights.

expect that there would be absolutely more variation in the non-conjugant type than in the conjugant, because the non-conjugant individuals are larger, but if we take the variation in proportion to the mean size of the conjugant and non-conjugant groups we obtain the same result.

Thus:

Coefficient of variation of conjugant means = 2.586 °/ $_{\circ}$. Coefficient of variation of non-conjugant means = 5.174 °/ $_{\circ}$.

The general conclusion which we reach is that, so far as can be judged by the data at present available, the conjugant type is relatively much more constant as we pass from culture to culture than is the non-conjugant type. Of course our present data are much too meagre to demonstrate this conclusion. It is true for the material here studied: whether it is true generally can only be determined by further investigation; but the present results certainly give a fair degree of probability that it is generally true.

To recapitulate then the results of this investigation show that in the material studied (a) there is a differentiated "conjugant type" of Paramecium, and (b) this "conjugant type" is relatively fixed and constant under varying environmental conditions, as compared with the type of the general population in fission generations. Now I take it to be a well-established result of the work of Calkins and earlier investigators in this field that (c) at more or less regular intervals in the normal life history of a race of Paramecium the individuals which are to take part in the future propagation of the race not only do, but under normal conditions must pass through a period of conjugation. Otherwise the race will die out. Calkins' brilliant studies (loc. cit.) have shown that for a time the race may be kept going by various forms of artificial stimulation, but that in the end such stimulation fails in its purpose. But if these three conclusions, (a), (b), and (c), are true, then it clearly means that those individuals which take part in the perpetuation of the race conform at intervals to a definite and relatively fixed morphological type. This result I believe to be of considerable importance, for, if it be accepted, it seems to me to mean nothing less than that we must change somewhat radically our whole outlook on the relation of the Protozoa to evolution problems. It has been held as axiomatic in biology that acquired characters are inherited in the Protozoa because one cell is both soma and germ. But clearly it matters very little to the race whether acquired characters are inherited or not, if after every cycle of fission generations the organism must come back to the same type (barring any real evolutionary change which may have taken place) that it started from, or in the end die. The case then becomes not very much different from what obtains in higher organisms. In the Metazoa what is acquired by the soma in one generation is not usually, at least, passed on to the next. Real evolutionary progress depends on changes in the germ cells. But similarly, if what we have concluded for Paramecium be correct: All real evolutionary progress in such a protozoan form must consist in definite changes in the "conjugant type." So far as evolutionary progress is concerned the conjugant individuals in the Protozoa

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correspond to the germ cells of the Metazoa. Any modification which is to be of significance to the race or to the species must take place there, rather than during the cycle of divisions between conjugations.

It is somewhat remarkable that an entirely different line of evidence from that which has led to the above conclusions has led Calkins to conclude in his most recent paper on the subject* that the assumption seems to be warranted "that there is a fundamental difference in the protoplasmic elements which go to make up the body of a protozoan, one of which is to be compared with the somatic cells of metazoa, the other with the germ cells, the one connected with the vegetative functions of metabolism the other with reproduction; the one may give out and so lead to 'physiological death' (Hertwig), or it may be restimulated; the other may give out and so lead to 'germinal death' of the race."

It seems almost self-evident if Calkins' conclusion be accepted, that at the time of conjugation the protoplasmic elements which correspond to the germ cells of Metazoa and have to do with the reproductive functions are so to speak predominant. Then Calkins' conclusion becomes essentially identical with that which we have reached.

We have now to consider the significance of the fact that there exists a high degree of homogamy in the conjugation of Paramecium. One of the greatest difficulties against the acceptance of the theory of natural selection as the method of organic evolution has always been that of understanding how any incipient evolutionary change within a group of animals living together in the same environment is to be preserved if the individuals showing the divergent character can breed freely and successfully with those which do not have it. Thus Huxley+, in the chapter in the Life and Letters of Darwin on the "Reception of the Origin of Species," says: "In my earliest criticisms of the 'Origin' I ventured to point out that its logical foundation was insecure so long as experiments in selective breeding had not produced varieties which were more or less infertile; and that insecurity remains up to the present time." Romanes, in his paper on "Physiological Selection,"‡ states the difficulty very clearly in the following words: "...for in this particular case so formidable does the difficulty seem to me that I cannot believe that natural selection alone could produce any divergence of specific character, so long as all the individuals on an overcrowded area occupy that area together. Yet, if any of them quit that area, and so escape from the unifying influence of free intercrossing, these individuals also escape from the conditions which Mr Darwin names as those that are needed by natural selection in order to produce divergence. Therefore, it appears to me that, under the circumstances supposed, natural selection alone could not produce divergence; the most it could do would be to change the whole specific type in some one direction, and thus induce transmutation of species in a linear series, each succeeding member of

^{*} Jour. Exper. Zool. Vol. 1. p. 455.

⁺ Life and Letters, Vol. 1. p. 170.

[#] Jour. Linn. Soc. Zool. Vol. xix. pp. 337-411.

which might supplant its parent form. But in order to secure diversity, multiplication, or ramification of species, it appears to me obvious that the primary condition required is that of preventing intercrossing with parent forms at the origin of each branch, whether the prevention be from the first absolute or only partial."

Now it is evident that if we find in any species a tendency for individuals like one another in one or more characters to mate together, rather than with individuals unlike themselves, we have at once a vera causa for the "divergence of individuals into varieties" by preventing intercrossing with parent forms. We need not even suppose that unions of unlike individuals are infertile provided the unions themselves do not occur or occur only rarely. The importance of homogamy has been so forcibly stated by Romanes* that I cannot do better than quote what "To state the case in the most general terms we may say that if the other two basal principles are given in heredity and variability the whole theory of organic evolution becomes neither more nor less than a theory of homogamy—that is, a theory of the causes which lead to discriminate isolation, or the breeding of like with like to the exclusion of unlike. For the more we believe in heredity and variability as basal principles of organic evolution, the stronger must become our persuasion that discriminate breeding leads to divergence of type, while indiscriminate breeding leads to uniformity. This in fact is securely based on what we know from the experience supplied by artificial selection which consists in the intentional mating of like with like to the exclusion of unlike.... Only when assisted by some form of discriminate isolation which determines the exclusive breeding of like with like can heredity make in favour of change of type, or lead to what we understand by organic evolution."

Now, although the importance of homogamy as a factor in evolution has been recognized almost universally, yet so far as I know no one except Pearson in the work on assortative mating in man, which has already been referred to (p. 214), has hitherto attempted to find out exactly how great a tendency for like to mate with like actually exists in a given species. We have had general reasoning in the place of direct quantitative evidence. In the present case it has been shown that in what may be considered the simplest prototype of the mating of individuals, which becomes in higher forms associated with sexual differentiation, namely in the conjugation of the Protozoa, there is a relatively very high degree of homogamy. Like pairs with like to more than double as close a degree as in the case of man where conscious choice must be supposed to operate to the greatest extent. have then clearly all the necessary factors for divergent evolution. Let any variation appear among the pro-conjugant individuals (i.e. in the "conjugant type") of a race of Paramecium, and if any one of the characters in which the variation appears is correlated (to any degree) with any character directly selected in the homogamic pairing, we shall at once get the beginning of a divergent race or variety. If the explanation which has been given here (p. 267) of the method

^{*} Darwin and After Darwin, Vol. III. pp. 6, 7.

of assorting in conjugation is the correct one, then the relative position of the mouth is one directly selected character. But it by no means follows that it is the only one. There may be other characters selected to just as close a degree in the conjugating. For the present it is sufficient to have shown that in a species living under natural conditions, a high degree of homogamy is not only possible, but actually exists.

Finally it should be pointed out that the fact that we find such a high degree of homogamy in a protozoan form like Paramecium strongly suggests the possibility that in higher organisms there may be assortative mating of the gametes in the process of fertilization. Should such a homogamy of the gametes occur it would probably be of far greater importance than any assertative mating of somas.

VIII. Summary of Results.

The chief results of this study of variation and correlation in Paramecium caudatum in connection with the process of conjugation may be summarily stated as follows:

- 1. Biometrical analysis of the variation in a considerable number of individuals shows that Paramecium follows the same general laws which have been found to hold for continuous variation in higher forms. The coefficients for variation in length of Paramecium cluster very closely about a value of 8 per cent. Certain of the frequency distributions approach reasonably well to the normal or Gaussian curve, but this is by no means universally the case.
- 2. In following a single culture throughout the history of a conjugation epidemic, it was found that definite changes are produced in the population as a result of the action of the environment. These environmental effects, however, were more pronounced in the case of non-conjugants than in conjugants.
- There is no evidence that conjugation tends to produce increased variability in ex-conjugants. All the evidence indicates, on the contrary, that conjugation serves to restrict the variability induced by environmental influences or, in other words, to preserve relative stability of type.
- 4. Conjugant Paramecia are distinctly and markedly differentiated from the non-conjugant population living in the culture at the same time, in type, variability and organic correlation in respect to all characters studied. This differentiation includes not only the absolute dimensions of the body, but also the shape, as measured by the length-breadth index. This differentiation of conjugants from non-conjugants is in no sense insignificant in amount, nor is it confined merely to the means of the different characters. On the contrary, it is large in amount, and just as significant for the variabilities and correlations as for the means.
- There is a tendency for like to pair with like (homogamy) in respect to length of body in the conjugation of Paramecium of a closer degree than has hitherto been found for assortative mating in any organism. The homogamic

correlation between the lengths of the individuals of conjugant pairs has about the same value in all the series studied, and it may be concluded that the true value for the coefficient measuring assortative pairing in respect to length in Paramecium lies between '5 and '6.

- 6. A considerable degree of homogamic correlation between the breadths of the members of conjugant pairs was found. It is believed to be a result of direct assortative pairing with respect to length, and of the organic correlation between length and breadth in the individual. The same explanation is to be given for the cross assortative correlations which were observed.
- 7. The homogamic correlations are not due to any local environmental factor, tending to make all conjugants relatively alike, because if conjugants be paired together at random, all homogamic correlation disappears.
- 8. The homogamic correlations are not greater in late stages of conjugation than in early, hence it is not probable that they owe their existence to any process of equalization of size due to the act of conjugation itself.
- 9. Evidence is presented to show that the homogamic correlation arises through the necessity for the anterior ends and mouths of the two members of a pair to "fit" reasonably well in a successful conjugation. The method by which this is probably brought about is discussed.
- 10. One general result of the work is to indicate strongly that the relation of the Protozoa to evolution problems is not that usually assigned on the Weismannian hypothesis. With reference to the evolutionary history of the race, the conjugant individuals of the protozoan population appear to be in certain respects comparable to the germ cells of metazoan. In order that there should be any real evolutionary progress in the Protozoa, it seems to be necessary that there be definite changes in these differentiated conjugant individuals, or in what has been called in this paper the conjugant type. What Paramecium may acquire during a cycle of fission generations as a result of environmental action is of no consequence in the evolution of the race if at the end of the cycle the individuals must come back to a relatively fixed type (the conjugant) before starting on the next cycle.

Appendix of Measurements.

In this section are given the correlation tables from which the constants have been deduced. In order to facilitate reference to these tables those of a particular series are grouped together, and are designated with the letter of the series and the number of the table within the series. The order in which the tables are given for each series is as follows:

- 1. The organic correlation tables for conjugants and non-conjugants.
- 2. The direct homogamic tables.
- 3. The cross homogamic tables.
- 4. Random or other tables.

For series B and D the measurements are given in full, as no correlation tables were formed for these very short series.

TABLE A 1.

Series A. Correlation of Length and Breadth for All Conjugants.

Breadth in microns.

		33-35.9	6.88-98	89-41-9	6.44-24	6.24-24	48—50.9	51—53.9	6.99—79	57—59.9	6.29-09	Totals
Length in microns.	140—144 145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199	1 	1 1 7 5 1 2 —	2 3 7 4 10 7 3 2 1	1 7 4 7 5 8 9 12 3 2 1	$egin{array}{c c} -&2\\ -&3\\ 5\\ 14\\ 12\\ 7\\ 5\\ 1\\ 1\\ 1 \end{array}$	- 2 4 4 5 4 - -	1 1 3 1 1 2 -	2			4 13 11 21 24 44 34 32 17 4 3 3
	Totals	2	18	42	59	51	25	10	2	0	1	210

TABLE A 2.

Series A. Correlation of Length with Breadth for All Non-Conjugants.

Breadth in microns.

		6.88-98	6.17-68	6.44-24	6.24-24	48-50.9	51-53.9	6.95-45	6.65—29	6.29-09	6365.9	6.89-99	6.1169	Totals
Length in microns.	145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199 200—204 205—209 210—214 215—219 220—224 225—229 230—234	1	2	1 1 2 4 1 — 1 3 —	1 5 4 7 4 5 3 1 —	1 1 4 6 6 2 1 3 1	1 1 3 3 7 7 7 7 7 3 1 2 2	3 3 3 8 5 1 2 2 1	1 1 2 6 5 3 4 2 4 3 -	3 1 2 1 2 3 3 1			1	1 1 2 3 16 11 20 28 28 28 21 14 11 12 9 1
	Totals	1	3	13	30	29	44	34	32	17	3	2	2	210

TABLE A3.

Series A. Direct Homogamic Correlation. Length of A and Length of B. Each Pair entered Once.

Length of A in microns.

ons.		140-144	145-149	150—154	155—159	160—164	165—169	170-174	175-179	180—184	185—189	190—194	195—199	Totals
Length of B in microns.	140—144 145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199	1 1 - - - - - - -	2 1 — 1 1 — —	1 1 1 1 1	2 1 2 1 3 - 1 -	2 4 4 1 1 1 -	1 - 3 1 4 3 5 5 - -	 1 1 8 4 6 2					1	2 8 6 11 9 22 12 19 11 1 3 1
	Totals	2	5	5	10	15	22	22	13	6	3	0	2	105

TABLE A 4.

Series A. Direct Homogamic Correlation. Length of A and Length of B. Symmetrical Table.

Length of first conjugant in microns.

microns.		140144	145-149	150-154	155—159	160—164	165—169	170-174	175-179	180-184	185—189	190—194	195—199	Totals
th of second conjugant in	$\begin{array}{c} 140-144 \\ 145-149 \\ 150-154 \\ 155-159 \\ 160-164 \\ 165-169 \\ 170-174 \\ 175-179 \\ 180-184 \\ 185-189 \\ 190-194 \\ 195-199 \end{array}$	- 3 1 - - - - - - - -	3 2 1 2 3 2 - - -	1 1 2 2 1 1 1 2 —	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3 1 3 8 5 1 2 1 —		$ \begin{array}{c} -\\ 1\\ 1\\ 1\\ 1\\ 1\\ 8\\ 7\\ 2\\ -\\ 2\\ 1 \end{array} $			1 - - 3 - -		- - - 1 1 1 -	4 13 11 21 24 44 34 32 17 4 3 3
Length	Totals	4	13	11	21	24	44	34	32	17	4	3	3	210

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TABLE A 5.

Series A. Direct Homogamic Correlation. Breadth of A and Breadth of B. Each Pair entered Once.

T	1.1	0	- 4		•
Knor	odth.	α t	4	110	microns

rons.		83-35.9	6.8898	89-41.9	6.44-24	6.14-9	6.05—87	51—53.9	Totals
Breadth of B in microns.	$33 - 35 \cdot 9$ $36 - 38 \cdot 9$ $39 - 41 \cdot 9$ $42 - 44 \cdot 9$ $45 - 47 \cdot 9$ $48 - 50 \cdot 9$ $51 - 53 \cdot 9$ $54 - 56 \cdot 9$ $57 - 59 \cdot 9$ $60 - 62 \cdot 9$	1	1 4 6 1 — 1 —	$ \begin{array}{c c} & -1 \\ & 6 \\ & 11 \\ & 4 \\ & 3 \\ & 1 \\ & -1 \\ & 1 \end{array} $	1 -3 7 10 5 4 -		- 1 6 1 - 1	- 1 1 1 1 -	1 5 15 29 30 16 6 2 0
	Totals	1	13	27	30	21	9	4	105

TABLE A 6.

Series A. Direct Homogamic Correlation. Breadth of A and Breadth of B. Symmetrical Table.

Breadth of first conjugant in microns.

conjugant in		6.98-88	6.88-98	89-41.9	6.44-24	6.44-94	6.09—84	51-53.9	6.95-45	6.65—25	6.29-09	Totals
Breadth of second conjumierons.	33—35·9 36—38·9 39—41·9 42—44·9 45—47·9 48—50·9 51—53·9 54—56·9 57—59·9 60—62·9	1 1 - - -	1 5 6 3 - 1 -	$ \begin{array}{c c} & 5 \\ & 12 \\ & 14 \\ & 6 \\ & 3 \\ & 1 \\ & - \\ & 1 \end{array} $	1 6 14 14 13 6 5 —	3 6 13 16 12 1 —	3 6 12 2 1 1	- 1 5 1 1 2 -	1 - 1 - - -		1	2 18 42 59 51 25 10 2 0
Br	Totals	2	18	42	59	51	25	10	2	0	1	210

TABLE A 7.

Series A. Direct Homogamic Correlation, Index of A and Index of B. Each Pair entered Once.

Index of A in per cent.

		6.02-02	6.12-12	6.22-22	6.88-88	6.42-42	6.52-52	6.92-92	6.12-12	6.82-82	6-6~6~	30-30.9	811-31-9	32-32.0	Totals
Index of B in per cent.	19—19·9 20—20·9 21—21·9 22—22·9 23—23·9 24—24·9 25—25·9 26—26·9 27—27·9 28—28·9 29—29·9 30—30·9 31—31·9 32—32·9 33—33·9		1 2 2 1		1 5 1 2 3 1 2 —	1 1 2 1 4 2 3 1 		1 - 1 - 1 5 4 1 1 2 -	- - 1 1 1 1 2 - 4 1 - 1	1 1 1 3	1 1 2 1 3			1	1 0 4 11 7 16 18 13 11 7 10 3 2
	Totals	2	6	6	15	15	11	16	13	7	9	0	4	1	105

TABLE A8.

Series A. Direct Homogamic Correlation. Index of A and Index of B. Symmetrical Table.

Index of first conjugant in per cent.

per cent.		6.61-61	6.02-02	6.12-12	6.22-22.8	23-23.9	6.42-42	25-25.9	6.98-98	6.28-28	6.82-82	6.67-67	30-30.9	31-31.9	6.88-38	33-33.9	Totals
Index of second conjugant in p	$\begin{array}{c} 19 - 19 \cdot 9 \\ 20 - 20 \cdot 9 \\ 21 - 21 \cdot 9 \\ 22 - 22 \cdot 9 \\ 23 - 23 \cdot 9 \\ 24 - 24 \cdot 9 \\ 25 - 25 \cdot 9 \\ 26 - 26 \cdot 9 \\ 27 - 27 \cdot 9 \\ 28 - 28 \cdot 9 \\ 29 - 29 \cdot 9 \\ 30 - 30 \cdot 9 \\ 31 - 31 \cdot 9 \\ 32 - 32 \cdot 9 \\ 33 - 33 \cdot 9 \end{array}$		1 - 1 1 1 - - -	1 2 2 1 - -	- - 1 1 1 1 2 1 - - 1 1	$\begin{bmatrix} -1 \\ 1 \\ 10 \\ 3 \\ 4 \\ 4 \\ 1 \\ 2 \\ - \\ - \\ - \\ - \\ - \end{bmatrix}$	1 2 1 3 2 5 2 1 4 1 —	2 1 4 5 6 2 2 1 2 2	1 1 1 4 2 2 10 5 2 2 2 2	$\begin{bmatrix} 1 \\ 2 \\ 1 \\ 1 \\ 2 \\ 5 \\ 4 \\ 1 \\ 6 \\ 1 \\ - \\ 1 \\ 1 \end{bmatrix}$	1 2 4 1 2 1 6 1 —	 1 2 2 6 1 3 1	1 - 2 2 1 - 3 - 1		1 1 1	1	1 3 6 10 26 22 27 34 26 18 16 10 7
Ħ,	Totals	1	3	6	10	26	22	27	34	26	18	16	10	7	3	1	210

TABLE A9.

Series A. Cross Homogamic Correlation. Length of A and Breadth of B.

Breadth of B in microns.

ıs.		33-35.9	6.88—98	89-41	6.44-64	6.24-9	48—50.9	6.89-19	6.99-49	57—59.9	6.29-09	Totals
Length of A in microns.	$\begin{array}{c} 140 - 144 \\ 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ \end{array}$		1 1 1 - - - 1	1 - 3 4 2 2 1 2 -	$egin{array}{cccccccccccccccccccccccccccccccccccc$	1 -4 5 8 5 2 -	1 -2 -1 5 5 1 1 -	1 1 1 2 -			1	2 5 5 10 15 22 22 22 13 6 3 0
	Totals	1	5	15	29	30	16	6	2	0	1	105

TABLE A 10.

Series A. Cross Homogamic Correlation. Length of B and Breadth of A.

Breadth of A in microns.

ıs.		33—35.9	36—38.9	89-41.9	6.44-24	45-47.9	48-50.9	51—53.9	Totals
Length of B in microns.	140-144 $145-149$ $150-154$ $155-159$ $160-164$ $165-169$ $170-174$ $175-179$ $180-184$ $185-189$ $190-194$	1		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c c} & 2 \\ & 1 \\ & 1 \\ & 6 \\ & 6 \\ & 3 \\ & 1 \\ & - \\$	1 2 2 3 1	1 - 1 1 1 1 -	2 8 6 11 9 22 12 19 11 1 3
	Totals	1	13	27	30	21	9	4	105

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TABLE A 11.

Series A. Random Pairing. Length with Length for Conjugants.

Symmetrical Table.

Length of first individual in microns.

in microns.		140-144	145-149	150—154	155—159	160—164	165—169	170-174	175—179	180—184	185—189	190—194	195—199	Totals
of second individual	$\begin{array}{c} 140 - 144 \\ 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ \end{array}$		$ \begin{array}{c} -\\ 2\\ -\\ 1\\ 3\\ 3\\ 1\\ 2\\ -\\ 1\\ -\\ -\\ -\\ 1 \end{array} $	$ \begin{bmatrix} 2 \\ -1 \\ -1 \\ $	$ \begin{array}{c c} & - \\ & 1 \\ & 6 \\ & 1 \\ & 3 \\ & 3 \\ & 5 \\ & - \\ & 1 \\ & - \\ & 1 \end{array} $	3 1 - 1 6 3 4 4 2 - - - -	3 1 3 8 12 8 3 1 2	1 3 1 3 4 12 4 2 4 ————————————————————————————	1 3 5 4 8 2 6 3	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			1 1 - - 1 - -	4 13 11 21 24 44 32 17 4 3 3
Length	Totals	4	13	11	21	24	44	34	32	17	4	3	3	210

TABLE A 12.

Series A. Random Pairing. Length with Length for Non-Conjugants.

Symmetrical Table.

Length of first individual in microns.

		671-971	150—154	155—159	190-164	165—169	170-174	175-179	180—184	185—189	190—194	195—199	402-002	205-209	412-012	215-219	720-327	655-556	230—234	Totals
9	145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199 200—204 205—209 210—214 215—219 220—224 225—229 230—234	1	1				1 - 2 - 2 1 - 3 1 1		$\begin{bmatrix} - \\ 1 \\ 2 \\ 1 \\ 3 \\ 8 \\ 4 \\ - \\ 2 \\ 3 \\ 1 \\ 3 \\ - \\ - \\ - \end{bmatrix}$		1 2 2 3 2 - 2 - 4 3 3 4 2 - -		 1 3 1 3 2 1 3 	1 				1 1	1 - 1 - - -	1 1 2 3 16 11 20 28 28 28 21 14 11 12 9 1
	Totals	1	1	2	3	16	11	20	28	28	28	21	14	11	12	9	1	2	2	210

Length of second individual in microns.

TABLE **A** 13.

Series A. Random Pairing. Length of Conjugants with Length of Non-Conjugants.

Length of Conjugants in microns.

				gun		onju	8	U		CIUII				
microns.		140-144	641-941	150-154	155—159	160—164	165—169	170-174	175-179	180—184	185—189	461-061	195—199	Totals
Length of Non-Conjugants in mic	$\begin{array}{c} 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ 200 - 204 \\ 205 - 209 \\ 210 - 214 \\ 215 - 219 \\ 220 - 224 \\ 225 - 229 \\ 230 - 234 \\ \end{array}$	1 2 1	1 	1 1 1 1 1 2 1 2 - 2	3 1 4 2 4 2 3 1 —	3 1 3 6 4 3 2 - 1 1	1 1 5 1 2 7 5 5 - 4 5 3 5 -			1 -1 4 -2 2 2 2 2 1 -1 -1	1 - 2 - 1	1 1 1		1 1 2 3 16 11 20 28 28 28 21 14 11 12 9 1
	Totals	4	13	11	21	24	44	34	32	17	4	3	3	210

TABLE A 14.

Series A. Random Pairing. Length with Length for the two Non-Conjugant Individuals nearest to each Pair of Conjugants Measured. Symmetrical Table.

Length in microns.

		671—571	150—154	155—159	160-164	165—169	170-174	175-179	180—184	185—189	190—194	195—199	700-504	205-209	210-214	215-219	220-224	225-229	780-534	Totals
Length in microns.	145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 205—204 205—209 210—214 215—219 220—224 225—229 230—234	1			1 		1 1 1 1 2 1 1 1 2	1 - 2 1 - 3 2 4 2 1 1 1 - 1	1 1 2 1 3 - 5 3 2 2 2 2 1	1 4 1 2 5 4 1 3 2 3 —	3 2 4 5 1 4 3 1 1 2 2	1 1 2 3 3 4 1 —		-		1 - 2 - 2 2 2 1 1	1	1	1	1 1 2 3 16 11 20 28 28 28 21 14 11 12 9 1
	Totals	1	1	2	3	16	11	20	28	28	28	21	14	11	12	9	1	2	2	210

TABLE B1.

Series B. Measurements in microns of the Length and Breadth of Conjugants and Non-Conjugants.

	Conjug	gants	Non-Cor	njugants
Length A 159 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 158 B 168 A 178 B 168 A 178 B 165		Breadth	Length	Breadt
4	150	43	165	57
A 159 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 178 B 171		40	182	54
A 159 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173		41	225	57
A 159 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 178 B 171		42	184	49
		43	217	50
В	165	39	194	47
		44	181	45
Length A 159 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 158 B 168 A 168 A 178 B 168		41	216	56
		48	210	52
 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 178 B 171 A 158 		41	216	54
 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 178 B 171 A 158 		43	215	57
 B 154 A 183 B 185 A 165 B 165 A 163 B 160 A 177 B 173 A 151 B 155 A 178 B 171 A 158 		47	204	57
	178	50	196	50
B	171	43	213	49
		36	205	50
B	168	39	205	47
A	178	45	194	52
В	165	39	204	56
A	205	54	196	49
B	184	41	200	52
A	192	47	193	47
B	177	43	198	45
A	127	41	190	52
B	143	42	190	52

TABLE C1.

Series C. Correlation of Length with Breadth for All Conjugants.

Breadth in microns.

		6.88-08	33—35.9	86-38-9	6.17-68	6.44-24	6.47-94	4850.9	6.89-19	54-56.9	Totals
Length in microns.	$\begin{array}{c} 140 - 144 \\ 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ 200 - 204 \\ \end{array}$	1	1 - - - - 1		$egin{array}{cccc} 1 & 1 & 5 & 4 & 4 & 3 & 5 & 5 & 4 & 9 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	$ \begin{array}{c c} & - \\ & 4 \\ & 3 \\ & 8 \\ & 12 \\ & 10 \\ & 9 \\ & 10 \\ & 7 \\ & 8 \\ & 3 \\ & 1 \end{array} $	1 2 9 3 5 8 8 8				1 3 9 11 18 34 18 22 29 20 26 8 3
	Totals	1	2	20	47	77	39	14	1	1	202

TABLE C2.

Series C. Correlation of Length with Breadth for All Non-Conjugants.

Breadth in microns.

		6.17-68	6.44-24	6.24-9	6.09—87	6.83-19	54-56.9	6.69-19	6.2909	63—65.8	6.89—99	6-11-69	6.42-22	75-77.9	Totals
Length in microns.	$\begin{array}{c} 140 - 149 \\ 150 - 159 \\ 160 - 169 \\ 170 - 179 \\ 180 - 189 \\ 190 - 199 \\ 200 - 209 \\ 210 - 219 \\ 220 - 229 \\ 230 - 239 \\ 240 - 249 \\ 250 - 259 \\ \end{array}$		$ \begin{array}{ c c c }\hline 1 \\ \hline - \\ 2 \\ 1 \\ 5 \\ 3 \\ 1 \\ \hline - \\ - \\ - \\ - \end{array} $	4 2 6 2 	1 1 7 6 5 4 2 —	- - - - 5 6 7 7 3 1		$\begin{bmatrix} - \\ - \\ 1 \\ 4 \\ 1 \\ 6 \\ 11 \\ 3 \\ - \\ 1 \end{bmatrix}$							1 0 3 7 23 29 39 39 35 14 9
	Totals	2	14	14	26	36	54	27	15	8	4	1	0	1	202

TABLE C3.

Series C. Direct Homogamic Correlation. Length of A and Length of B. Each Pair entered Once.

T . 1	- 0			
Lenoth	of	A	111	microns.

ıs.		671—571	150-154	691—991	190-091	165—169	170-174	621—921	180—184	185—189	190-194	661—961	700-307	Totals
Length of B in microns.	$\begin{array}{c} 140 - 144 \\ 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ 200 - 204 \\ \end{array}$	1 - 1	1 2 - 2	1 1 1 1 - -	3 1 2 	1 1 1 -6 2 6 4 2 -1			2 1 4 1 4 -	1 5 1				1 1 4 7 12 10 9 11 17 13 13 2 1
	Totals	2	5	4	6	24	9	11	12	7	13	6	2	101

TABLE C4.

Series C. Direct Homogamic Correlation. Length of A and Length of B. Symmetrical Table.

Length of first conjugant in microns.

				()			J	0							
microns.		771-071	641-941	150-154	155—159	160—164	165—169	17.0-17.4	175-179	180-184	185—189	761-061	195—199	700-307	Totals
Length of second conjugant in	140—144 145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199 200—204	1	1 1 - 1	2 3 1 —	1 3 2 4 1 - -	4 2 8 1 1 2 —	1 1 3 1 8 4 8 4 3 -	1 1 8 2 2 2 1 - 1	- - 1 4 2 2 10 2 1 - -	$ \begin{array}{c c} & -1 \\ & -2 \\ & 3 \\ & 2 \\ & 10 \\ & 2 \\ & 4 \\ & 2 \\ & 3 \\ & -1 \end{array} $	1 2 4 10 3 —	$\begin{bmatrix} - \\ - \\ 1 \\ 2 \\ 3 \\ 14 \\ 4 \\ 1 \end{bmatrix}$	1 3 4		1 3 9 11 18 34 18 22 29 20 26 8
Lei	Totals	I	3	9	11	18	34	18	22	29	20	26	8	3	202

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TABLE C5.

Series C. Direct Homogamic Correlation. Breadth of A and Breadth of B. Each Pair entered Once.

Breadth of A in	microns

		Dice		-				•		
in microns.		30-32.9	33—35.9	86-38-9	6.14-68	6.44-24	6.24-94	6.09-87	6.25—19	Totals
Breadth of B in m	33—35·9 36—38·9 39—41·9 42—44·9 45—47·9 48—50·9 51—53·9 54—56·9] - - - - - -	1 - -	1 5 3 1 -	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 7 16 10 5 —	 2 3 5 6 1 	- 1 4 - - 1		1 10 22 37 22 8 0 1
	Totals	1	1	10	25	40	17	6	1	101

TABLE C6.

Series C. Direct Homogamic Correlation. Breadth of A and Breadth of B. Symmetrical Table.

Breadth of first conjugant in microns.

conjugant in		6.88—08	33-35.9	36-38.9	89-41.9	6.44-24	6.24-94	48-50.9	51-53.9	54—56.9	Totals
Breadth of second conj microns.	30-32·9 33-35·9 36-38·9 39-41·9 42-44·9 45-47·9 48-50·9 51-53·9 54-56·9	_ 1 _ _ _ _ _	- 1 1 - -	1 1 2 9 4 3 —	9 12 16 8 2	$ \begin{array}{c c} - & \\ 1 & \\ 4 & \\ 16 & \\ 32 & \\ 15 & \\ 9 & \\ - & \\ \end{array} $	- 3 8 15 12 1 -	_ 			1 2 20 47 77 39 14 1
Br	Totals	1	2	20	47	77	39	14	1	1	202

TABLE C7.

Series C. Direct Homogamic Correlation. Index of A and Index of B. Each Pair entered Once.

Index of A in p	er cent.
-----------------	----------

t.		6.81—81	6.61-61	6.02-02	6.12-12	6.82-38	6.22-33.6	6.42-42	6.92-52	6.92-92	6.12-12	6.88—88	Totals
Index of B in per cent.	$18-18\cdot 9$ $19-19\cdot 9$ $20-20\cdot 9$ $21-21\cdot 9$ $22-22\cdot 9$ $23-23\cdot 9$ $24-24\cdot 9$ $25-25\cdot 9$ $26-26\cdot 9$ $27-27\cdot 9$ $28-28\cdot 9$ $29-29\cdot 9$ $30-30\cdot 9$	- 1 1 - - - -		1 - 1	1 3 2 2 2 2 1 —	1 3 4 2 3 1 —	1 1 2 4 2 1 1 1	 3 2 2 2 2 1			- 1 - 1 1 1 1 1		1 0 6 5 16 14 13 15 14 11 2 2
	Totals	2	2	2	13	14	12	12	18	11	7	8	101

TABLE C8.

Series C. Direct Homogamic Correlation. Index of A and Index of B. Symmetrical Table.

Index of first individual in per cent.

										1					
per cent.		6.81—81	6.61-61	6.02-02	6.12-12	6.22-22	6.82-83	6.42-42	6.52-52	6.92-92	27-27.9	6.82-82	6.68-68	30-30.9	Totals
Index of second individual in	18—18·9 19—19·9 20—20·9 21—21·9 22—22·9 23—23·9 24—24·9 25—25·9 26—26·9 27—27·9 28—28·9 29—29·9 30—30·9	1 1 1 		1 - 4 - 1 1 - - -	$ \begin{array}{c c} 1 \\ -4 \\ 4 \\ 3 \\ 3 \\ -2 \\ 1 \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ -$	$egin{array}{c c} 1 \\ -1 \\ -3 \\ 6 \\ 4 \\ 5 \\ 6 \\ 3 \\ 1 \\ - \\ - \end{array}$	$\begin{bmatrix} -1 \\ 1 \\ 3 \\ 4 \\ 6 \\ 4 \\ 1 \\ 1 \\ 1 \\ - \end{bmatrix}$	- - 1 - 5 6 4 2 3 2 2 - -		$ \begin{array}{c} -\\ -\\ 1\\ 3\\ 1\\ 3\\ 9\\ 2\\ 4\\ 1\\ -\\ 1 \end{array} $	$ \begin{array}{c} $	1 2 2 1 3 -	1	1	3 2 8 18 30 26 25 33 25 18 10 2
Inc	Totals	3	2	8	18	30	26	25	33	25	18	10	2	2	202

TABLE C9.

Series C. Cross Homogamic Correlation. Length of A and Breadth of B.

Breadth of B in microns.

ons.		33—35.9	98—98	39—41.9	6.44-24	6.27-24	6.09—87	51-53.9	54—56.9	Totals
Length of A in microns.	$145-149 \\ 150-154 \\ 155-159 \\ 160-164 \\ 165-169 \\ 170-174 \\ 175-179 \\ 180-184 \\ 185-189 \\ 190-194 \\ 195-199 \\ 200-204$		1 2 3 2 - 1 1	$ \begin{array}{c c} 1 \\ 2 \\ 4 \\ 3 \\ 1 \\ 4 \\ -1 \end{array} $	$ \begin{array}{c c} & 2 \\ & 2 \\ & 1 \\ & 11 \\ & 3 \\ & 5 \\ & 3 \\ & 2 \\ & 4 \\ & 4 \\ & - \end{array} $	1 3 — 5 1 3 5 2 2	- 1 1 - 1 2 1 1			2 5 4 6 24 9 11 12 7 13 6 2
	Totals	1	10	22	37	22	8	0	1	101

TABLE C 10.

Series C. Cross Homogamic Correlation, Length of B and Breadth of A.

Breadth of A in microns.

os.		30-32.9	33-35.9	36—38.9	39—41·9	6.44-24	6.74-54	6.09—84	51—53.9	Totals
Length of B in microns.	$\begin{array}{c} 140 - 144 \\ 145 - 149 \\ 150 - 154 \\ 155 - 159 \\ 160 - 164 \\ 165 - 169 \\ 170 - 174 \\ 175 - 179 \\ 180 - 184 \\ 185 - 189 \\ 190 - 194 \\ 195 - 199 \\ 200 - 204 \\ \end{array}$		1	1 1 1 2 1 2 - 1	1 1 1 2 3 2 3 4 4 4 3 1	1 2 3 6 5 2 2 8 4 6 1			- - - - 1 - -	1 4 7 12 10 9 11 17 13 13 2
	Totals	1	1	10	25	40	17	6	1	101

TABLE C11.

Series C. Random Pairing. Length with Length for Conjugants.

Symmetrical Table.

Length of first individual in microns.

			130118	5			.11011				20110	•			
microns.		771-071	641—541	150—154	155—159	160—164	165—169	170-174	175-179	180—184	185—189	190—194	195—199	200-204	Totals
Length of second individual in	140—144 145—149 150—154 155—159 160—164 165—169 170—174 175—179 180—184 185—189 190—194 195—199 200—204			1 2 - 2 1 3	1 - 4 2 1 2 - 1	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{bmatrix} -1 \\ 4 \\ 2 \\ 8 \\ 4 \\ 1 \\ 5 \\ 5 \\ 2 \\ 1 \\ 1 \end{bmatrix}$		- - 1 4 1 3 8 2 - 1 1	2 2 5 3 2 6 2 5 2	$egin{array}{c c} 1 & - \ - \ 2 & 5 \ - \ 2 & 4 \ 4 \ - \ 1 \ \end{array}$	3 1 3 2 3 1 5 4 4	2 1 1 2 - 2		1 3 9 11 18 34 18 22 29 20 26 8 3
Len	Totals	1	3	9	11	18	34	18	22	29	20	26	8	3	202

TABLE C12.

Series C. Random Pairing. Length with Length for Non-Conjugants. Symmetrical Table.

Length of first individual in microns.

			0											
in microns.		671-071	150-159	160—169	170-179	180—189	190—199	200—209	210—219	676-076	230-239	642-042	250—259	Totals
of second individual	$\begin{array}{c} 140 - 149 \\ 150 - 159 \\ 160 - 169 \\ 170 - 179 \\ 180 - 189 \\ 190 - 199 \\ 200 - 209 \\ 210 - 219 \\ 220 - 229 \\ 230 - 239 \\ 240 - 249 \\ 250 - 259 \\ \end{array}$			2 - 1				- - 3 4 4 11 12 1 3 1	$\begin{array}{c} 1 \\ - \\ 1 \\ 3 \\ 7 \\ 11 \\ 10 \\ 3 \\ 1 \\ 1 \\ 1 \end{array}$	- 1 2 3 4 12 3 4 5 1			1 1 1	1 0 3 7 23 29 39 39 35 14 9
Length	Totals	1	0	3	7	23	29	39	39	35	14	9	3	202

TABLE C 13.

Series C. Random Pairing. Length of Conjugants with Length of Non-Conjugants.

Length of conjugants in microns.

		0 00													
microns.		771-071	641—541	150—154	155—159	191-091	165-169	170-174	175-179	180—184	185—189	761-061	195—199	200-204	Totals
Length of non-conjugants in	$\begin{array}{c} 140 - 149 \\ 150 - 159 \\ 160 - 169 \\ 170 - 179 \\ 180 - 189 \\ 200 - 209 \\ 210 - 219 \\ 220 - 229 \\ 230 - 239 \\ 240 - 249 \\ 250 - 259 \\ \end{array}$				5 1 2 2 1	1 2 2 7 2 2 2 2	- - - 8 6 5 2 6 3 3	1 1 2 2 5 3 2 2	- - - 4 3 3 6 2 1 3	$ \begin{array}{c} 1 \\ -1 \\ 1 \\ -2 \\ 6 \\ 7 \\ 5 \\ 4 \\ 1 \\ 1 \end{array} $	1 2 4 1 5 2 5 —		- 1 - 1 - 3 2 - 1	1 2	1 0 3 7 23 29 39 39 39 35 14
Ler	Totals	1	3	9	11	18	34	18	22	29	20	26	8	3	202

TABLE C14.

Series C. Random Pairing. Length with Length for the two Non-Conjugant Individuals nearest to each Pair of Conjugants Measured. Symmetrical Table.

Length of first individual in microns.

n microns.		671-071	150—159	160—169	621-021	180-189	661—061	602-002	612-012	622-022	230-239	642-042	250—259	Totals
gth of second individual in	$\begin{array}{c} 140-149 \\ 150-159 \\ 160-169 \\ 170-179 \\ 180-189 \\ 190-199 \\ 200-209 \\ 210-219 \\ 220-229 \\ 230-239 \\ 240-249 \\ 250-259 \end{array}$	1		- - 1 - 1 - -		1 2 2 4 3 3 6 1	$ \begin{array}{c c} 1 \\ - \\ 1 \\ 4 \\ 6 \\ 3 \\ 5 \\ 4 \\ 3 \\ 1 \\ 1 \end{array} $	$ \begin{array}{c} $	2 3 5 11 8 5 3 2		1 3 6 3 -	1 1 2 2 2 - 2	1 1 1	1 0 3 7 23 29 39 39 35 14 9
Length	Totals	1	0	3	7	23	29	39	39	35	14	9	3	202

TABLE D1.

Series D. Measurements in microns of the Length and Breadth of Conjugants and Non-Conjugants.

Conjug	ants	Non-Cor	njugants
Length	Breadth	Length	Breadth
A 150	40	197	51
B 189	43	189	50
$\begin{array}{cc} A & 200 \\ B & 202 \end{array}$. 38	$\frac{213}{189}$	50 50
$\begin{array}{cc} A & 189 \\ B & 191 \end{array}$	41 41	$\frac{206}{212}$	57 54
$egin{array}{ccc} A & 168 \\ B & 161 \end{array}$	43 43	$\frac{199}{213}$	50 50
A 180 B 184	44 45	$\frac{207}{217}$	50 49
$\begin{array}{cc} A & 180 \\ B & 200 \end{array}$	47 45	$\frac{223}{210}$	59 53
$egin{array}{ccc} A & 196 \ B & 182 \end{array}$	43 40	$\frac{225}{199}$	49 45
$egin{array}{ccc} A & 169 \ B & 184 \end{array}$	43 48	$\frac{203}{228}$	47 52
$egin{array}{ccc} A & 198 \\ B & 184 \end{array}$	36	216	51
	41	230	57
$\begin{array}{cc} A & 183 \\ B & 186 \end{array}$	37	232	54
	44	197	49
$egin{array}{ccc} A & 186 \\ B & 167 \end{array}$	45	217	56
	42	235	56
$egin{array}{ccc} A & 160 \\ B & 158 \end{array}$	43	168	44
	42	241	54
$\begin{array}{cc} A & 184 \\ B & 189 \end{array}$	43	243	57
	47	230	54
$\begin{array}{cc}A&175\\B&167\end{array}$	42	225	60
	44	· 241	60
$\begin{array}{cc} A & 194 \\ B & 189 \end{array}$	39	241	54
	43	230	56
A 188	44	223	54
B 188	44	266	56

TABLE E 1.

Series E. Correlation of Length with Breadth for All Non-Conjugants. Breadth in microns.

30 160—169 170—179 180—189 190—199 200—209	6.24-94 1	6.09-87	6.89-19	6.99—79	6.69-19	6.29-09	63—65.9	6.89-99	6.11.—69	72-74.9	6.2222	78—80.9	Totals
1 200 200	_ 1	1						1	l .			` '	
## 200—209 210—219 220—229 230—239 240—249 250—259 260—269 270—279		1 1 1 4	1	1 1 2 3 7	3 5 12 4 1 — —	- 1 6 5 9 8 - 1 - -	- 3 2 6 6 3 1 - 1	1 1 4 6 8 1 —			1 1 2	1	2 2 7 19 22 27 27 27 17 7 1 0

TABLE E 2.

Series E. Frequency Distribution of Length-Breadth Index for all Non-Conjugants.

Index in per cent.	23-23.9	6.42-42	25-25.9	6.9~9%	27-27-9	6.88-88	6.66—66	30-30.9	6.12-12	83-83.9	33-33.9	84-34.9	35-35.9	Total
Frequency	2	1	3	6	18	27	23	21	13	11	5	1	1	132

TABLE F1.

Series F Early. Direct Homogamic Correlation. Length of A, and Length of B. Each Pair entered Once. Micrometer unit = 8.6 microns.

Length of B in units.

ts.		6.12-12	6.22-22.0	23-23.9	6.42-42	25-25.9	6.9%-9%	2727.9	6.82-82	6.62-62	Totals
Length of A in units.	20-20·9 21-21·9 22-22·9 23-23·9 24-24·9 25-25·9 26-26·9 27-27·9 28-28·9 29-29·9	3 1 1 - -	1 3 4 3 1 —	- 2 4 3 2 2 1 -	- 3 1 1 3 3 3 - -	1 2 1 -	- - 4 3 1 1				4 6 9 11 16 10 8 2 2
	Totals	8	15	14	14	4	9	2	3	1	70

TABLE F 2.

Series F Early. Direct Homogamic Correlation. Length of A and Length of B. Symmetrical Table. Micrometer unit = 8.6 microns.

T	/1	a .						
Length	-10	first	-1nc	iivid	uat	1n	units.	

			· .									
in units.		6.02-02	6.12-12	6.22-22.0	63-33-6	6.42-42	25-25:0	6.92-92	27-27.9	6.88-88	6.67-67	Totals
h of second individual	20-20·9 21-21·9 22-22·9 23-23·9 24-24·0 25-25·9 26-26·9 27-27·9 28-28·9 29-29·9	3 1 	$ \begin{array}{c} $	1 6 6 6 4 1 —	1 6 8 4 3 2 1	$egin{array}{c} -4 & 4 & 4 & 6 & 5 & 7 & & & & & & &$	$\begin{bmatrix} - \\ 1 \\ 3 \\ 5 \\ - \\ 4 \\ - \\ 1 \end{bmatrix}$	$\begin{bmatrix} - \\ 2 \\ 7 \\ 4 \\ 2 \\ 1 \\ 1 \\ - \end{bmatrix}$	1 - 1 1 1		1 2	4 14 24 25 30 14 17 4 5
ength of	Totals	4	14	24	25	30	14	17	4	5	3	140

TABLE F 3.

Series F Late. Direct Homogamic Correlation. Length of A and Length of B. Each Pair entered Once.

Micrometer unit = 8.6 microns.

Length of B in units.

s.		$6.1\tilde{c}$ $-1\tilde{c}$	6.22-73.0	23—23·9	6.42-42	6.52-52	6.97-97	6.12-18	6.82 -82	6.62-62	30—30-9	81-01.9	Totals
Length of A in units.	20-20·9 21-21·9 22-22·9 23-23·9 24-24·9 25-25·9 26-26·9 27-27·9 28-28·9 29-29·9 30-30·9 31-31·9	1 1 - 1 - - - -	1 2 2 - 2 1 - -	2 3 4 5 3 - - -	1 7 2 1 1 7 2 1 1		1 - 4 1 1 1 -	2 1	1 3 - 1 .				2 6 5 10 14 21 8 6 3 0
	Totals	4	10	17	14	12	9	3	6	1	0	1	77

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TABLE F4.

Series F Late. Direct Homogamic Correlation. Length of A and Length of B. Symmetrical Table. $Micrometer\ unit = 8.6\ microns.$

Length of first individual in units.

			12011	5011	01 111	. St 1.	iidi v.	Idaa		um				
in units.		6.02-02	6.12-12	6.66-66	23-23.9	6.47-47	25—25.9	6.98-98	27-27.9	6.82—82	6.67-68	30-30.9	31-31.9	Totals
Length of second individual	20-20·9 21-21·9 22-22·9 23-23·9 24-24·9 25-25·9 26-26·9 27-27·9 28-28·9 29-29·9 30-30·9 31-31·9		1 2 2 3 -1 1 1 	1 2 4 3 2 - 2 1 - -	3 3 8 7 5 1 —			1 2 1 2 5 2 2 2 -	1 1 2 2 2 - 3					2 10 15 27 28 33 17 9 1 1
Ler	Totals	2	10	15	27	28	33	17	9	9	1	1	2	154

TABLE AA 1.

Series AA. Correlation of Length with Breadth for Conjugant A. Length of A in microns.

		691—091	170-179	180—189	190—199	200-209	210-219	220—229	230—239	672-072	250-259	692-092	270-279	280—289	Totals
Breadth of A in microns.	$33 - 35 \cdot 9$ $36 - 38 \cdot 9$ $39 - 41 \cdot 9$ $42 - 44 \cdot 9$ $45 - 47 \cdot 9$ $51 - 53 \cdot 9$ $54 - 56 \cdot 9$ $60 - 62 \cdot 9$ $63 - 65 \cdot 9$ $69 - 71 \cdot 9$ $72 - 74 \cdot 9$ $75 - 77 \cdot 9$ $78 - 80 \cdot 9$ $84 - 86 \cdot 9$		1	1 1 1 3 2 1 1 1 1 - -	- 1 1 1 3 3 1 3 2 3 - -	1 -1 -2 -6 11 -6 -5 -3 		$ \begin{array}{c c} 1 \\ -1 \\ 1 \\ 6 \\ 8 \\ 3 \\ 5 \\ 4 \\ 6 \\ 1 \\ 1 \\ 2 \\ - \\ 2 \end{array} $						- - - - 1 - - -	3 0 4 2 11 22 38 24 29 26 23 3 6 6 0 1
	Totals	1	2	11	18	36	41	41	24	18	4	3	0	1	200

TABLE AA 2.

Series AA. Correlation of Length with Breadth for Conjugant B.

Breadth of B in microns.

ons.		6.68-12	30-32.9	33-35.9	36-38.9	89-41.9	6.44-24	6.2494	6.09-84	61-53.9	54-56.9	57—59.9	6.29-09	63-65.9	6.89-99	6.1169	6.42-62	75-77.9	78-80-9	81—83.9	6.98-48	87—89-9	6.26-06	Totals
Length of B in microns	160—169 170—179 180—189 190—199 200—209 210—219 220—229 230—239 240—249 250—259 260—269	1					1 - 1 3 5 1 - -	 1 2 2 1 2 2 2 	1 1 1 4 6 3 1 —	$ \begin{array}{c c} & - & \\ & 2 & \\ & 16 & \\ & 7 & \\ & 6 & \\ & 3 & \\ & - & \\ $	$egin{array}{c c} 1 & -1 & 6 & 6 & 6 & 3 & 8 & -1 & -1 & -1 & -1 & -1 & -1 & -1 $	$ \begin{array}{c c} & - \\ & 1 \\ & 2 \\ & 10 \\ & 6 \\ & 3 \\ & 4 \\ & 2 \\ & 2 \\ & 2 \end{array} $	$\begin{bmatrix} - \\ - \\ 3 \\ 6 \\ 3 \\ 2 \\ 1 \\ - \end{bmatrix}$	$egin{array}{c} - \ - \ 4 \ 1 \ 2 \ 1 \ 1 \ 2 \ 1 \ \end{array}$			1 1 1		2	1				3 3 4 18 53 41 27 25 13 9 4
	Totals	1	0	0	0	5	11	12	18	36	31	32	18	12	2	14	3	0	2	1	0	0	2	200

TABLE AA 3.

Series AA. Direct Homogamic Correlation. Length of A and Length of B. Symmetrical Table.

Length of first individual in microns.

				0								•			
microns.		691-091	17.0-17.9	180—189	190-199	200-209	210-219	220-229	230-239	642-042	250-259	692-092	270-279	280-289	Totals
Length of second individual in	$\begin{array}{c} 160 - 169 \\ 170 - 179 \\ 180 - 189 \\ 190 - 199 \\ 200 - 209 \\ 210 - 219 \\ 220 - 229 \\ 230 - 239 \\ 240 - 249 \\ 250 - 259 \\ 260 - 269 \\ 270 - 279 \\ 280 - 289 \\ \end{array}$	1 1 1	1 - 1	1 1 4 3 4 1 — — —	$ \begin{array}{c c} 1 \\ 3 \\ 4 \\ 14 \\ 7 \\ 5 \\ 1 \\ 1 \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ -$	$egin{array}{c} - \ 4 \ 14 \ 30 \ 25 \ 9 \ 5 \ 1 \ 1 \ - \ - \ - \ \end{array}$	$ \begin{array}{ c c }\hline 1\\\hline -1\\\hline 7\\25\\22\\16\\5\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\-\\$	$ \begin{array}{c c} - & \\ 1 & \\ - & \\ 5 & \\ 9 & \\ 16 & \\ 10 & \\ 16 & \\ 7 & \\ 1 & \\ 2 & \\ - & \\ 1 \end{array} $		- 1 1 1 5 7 4 4 5 3 -				1	4 5 15 36 89 82 68 49 31 13 7 0
Len	Totals	4	5	15	36	89	82	68	49	31	13	7	0	1	400

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TABLE AA 4.

Series AA. Direct Homogamic Correlation. Breadth of A and Breadth of B. Symmetrical Table. Breadth of first individual in microns.

ró.		27-29.9	80-32.8	33-35.9	36-38.9	39-41.9	6.44-24	6.24-94	48—50.9	51—53.9	6.99—79	5759.9	6.29-09	63—65.9	6.8999	6.1%69	6.41-27	75-77.9	6.08-81	81—83.9	6.98-78	6.68—18	6.26-06	Totals
Breadth of second individual in microns.	$\begin{array}{c} 27 - 29 \cdot 9 \\ 30 - 32 \cdot 9 \\ 33 - 35 \cdot 9 \\ 36 - 38 \cdot 9 \\ 39 - 41 \cdot 9 \\ 42 - 44 \cdot 9 \\ 48 - 50 \cdot 9 \\ 51 - 53 \cdot 9 \\ 54 - 56 \cdot 9 \\ 60 - 62 \cdot 9 \\ 63 - 65 \cdot 9 \\ 66 - 68 \cdot 9 \\ 69 - 71 \cdot 9 \\ 72 - 74 \cdot 9 \\ 75 - 77 \cdot 9 \\ 78 - 80 \cdot 9 \\ 81 - 83 \cdot 9 \\ 84 - 86 \cdot 9 \\ 87 - 89 \cdot 9 \\ 90 - 92 \cdot 9 \end{array}$	1										$\begin{array}{c} - \\ - \\ - \\ - \\ 3 \\ 2 \\ 11 \\ 7 \\ 12 \\ 7 \\ 11 \\ - \\ - \\ - \\ 1 \\ 2 \\ - \\ 1 \\ 1 \end{array}$		1 	3 1 1					1	2			1 0 3 0 9 13 23 40 74 55 61 44 35 5 20 9 0 3 1 2
	Totals	1	0	3	0	9	13	23	40	74	55	61	44	35	5	20	9	0	3	1	2	0	2	400

TABLE AA 5.

Series AA. Cross Homogamic Correlation. Length of A and Breadth of B. Breadth of B in microns.

S.		6.62-12	30-32.9	33-35.9	36—38.9	6.14-62	6.44-64	6.14-54	6.02—87	51-53.9	6.99—79	57-59.9	6.29-09	63—65.9	6.89-99	6.11.—69	6.72-22	6.2292	7.8—80.9	81—83.9	6.98-78	87—89.9	90-92.9	Totals
Length of A in microns.	$\begin{array}{c} 160 - 169 \\ 170 - 179 \\ 180 - 189 \\ 190 - 199 \\ 200 - 209 \\ 210 - 219 \\ 230 - 239 \\ 240 - 249 \\ 250 - 259 \\ 260 - 269 \\ 270 - 279 \\ 280 - 289 \end{array}$					2 3	1 1 1 3 3 2 -	- - 3 5 4 - - -		1 3 4 11 8 3 1 1	- 3 3 8 3 8 2 4 - -	3 2 2 3 10 7 3 1 1	 1 4 5 2 2 3 1		1 - - 1 -	3 2 2 1 3 2 -				1			1	1 2 11 18 36 41 41 24 18 4 3 0
	Totals	1	0	0	0	5	11	12	18	36	31	32	18	12	2	14	3	0	2	1	0	0	2	200

TABLE AA 6.

Series AA. Cross Homogamic Correlation. Length of B and Breadth of A.

Breadth of A in microns.

ons.		33—35.9	6.88-98	6.17-68	6.4424	45-47.9	6.05-84	61-53.9	6.99—79	6.65-29	6.29-09	69-65-8	6.89—99	6.1169	6.42-22	75-77.9	6.08—81	6.58—18	6.98-48	Totals
Length of B in microns.	160—169 170—179 180—189 190—199 200—209 210—219 220—229 230—239 240—249 250—259 260—269	1 1 - 1 -		- - 1 3 - - - -		1 - - 5 3 - 2 - -	$ \begin{array}{c} -\\ -\\ 3\\ 8\\ 4\\ 3\\ 2\\ -\\ 1 \end{array} $	$ \begin{array}{c c} 1 \\ -1 \\ 7 \\ 7 \\ 9 \\ 5 \\ 6 \\ -2 \\ - \end{array} $	1 1 2 7 4 2 4 2 1	$ \begin{array}{c c} - & 2 \\ - & 1 \\ 10 & 6 \\ 2 & 3 \\ 2 & 2 \\ 1 \end{array} $	$\begin{bmatrix} 1 \\ - \\ 3 \\ 6 \\ 4 \\ 6 \\ 2 \\ 1 \\ 2 \\ 1 \end{bmatrix}$	10 2 4 2 3 1	 1 1	- - 1 - 2 - 2	 1 2 2 1 				- - 1 1 - - -	3 3 4 18 53 41 27 25 13 9 4
	Totals	3	0	4	2	11	22	38	24	29	26	23	3	6	6	0	1	0	2	200

THE ANTHROPOMETRIC CHARACTERISTICS OF THE INMATES OF ASYLUMS IN SCOTLAND.

By J. F. TOCHER.

(1) Introductory.

THE idea of making anthropometric observations on the inmates of asylums in Scotland originated with Dr Macpherson, Commissioner in Lunacy. At his suggestion and through his instrumentality the survey was carried out by the writer and his assistants. The survey forms part of a scheme, entertained by the Henderson Trust of Edinburgh, and has for its aim the making of an anthropometric examination of the physical characters of the Scottish people. In view of the fact that the data could be very easily collected, it was considered advisable, in the first instance, to commence with the asylum class of the population. Measurements were therefore begun on the inmates in December 1903, and with the assistance and cooperation of the medical superintendents and staffs of the various asylums, were carried out and completed by the end of 1904. The data. collected and classified, have just been published by the Henderson Trust in the form of a Report, which is reprinted as a supplement to this Volume of Biometrika. This Report is intended by the Trust to be, and is, a repository of facts at the disposal of those who make a special study of the head form of Man, but it advances nothing whatever by way of interpretation of the facts themselves. Since the Henderson Trust is interested only in the collection of data, it is not by omission, but by design that the Trustees have, very properly, excluded from their Report any statements purporting to interpret the results or to reach general conclusions. That task is now attempted here. As the organiser of the survey and the person responsible for the Report, the writer has been accorded the first opportunity of making the necessary statistical analysis which must precede any interpretation of the data. The results of this analysis, together with a statement of such conclusions as have been reached, are embodied in the present memoir.

Altogether 4436 males and 3951 females were observed, but from these numbers 55 males and 26 females were excluded from the general analysis, because they were held to be exceptional cases by the medical superintendents

under whose care they were. These persons were suffering from some congenital defect such as idiocy, or were rickety, syphilitic, or tuberculous, in such manner as directly to affect their anthropometric characters*. There were accordingly left 4381 males and 3925 females to represent the general lunatic population. Medical experts would no doubt agree that others might be excluded if a thorough knowledge of their history were available. It is therefore highly probable that an undetermined residue of exceptional cases remains. An elaborate investigation would, however, be required to reveal these cases, and as such an investigation was under the circumstances, out of the question, and would affect the results of the present enquiry only in a very slight degree, the 4381 males and 3925 females are taken to represent substantially what may be termed the ordinary normal asylum, or general insane population—i.e. those mentally affected, exclusive of the specific cases just mentioned. In view of the results of recent investigations by Pearl+ and Blakeman; establishing a direct connection between age and certain physical characters, an analysis of the data in age groups would have been useful, and would have furnished valuable additional information in the comparative study of the inmates of individual asylums. Since the age range in the asylums is a pretty wide one, there is little doubt that our information as to the physical characters of the inmates would have been more complete had an age analysis been made. In recording the measurements at the asylums, however, no note was made, at the time, of the age of the inmates, and it was only when the statistical analysis was being carried out that the importance of separation in age groups was fully recognised. It was then found that considerable additional expense would have been incurred in furnishing an accurate statement of the ages of those observed, and any treatment of the data with respect to age groups was therefore abandoned. Since, however, none but adults are included in the analysis, any conclusions reached are those based on an adult population.

As explained in the Supplement \S and in the Henderson Trust Report $\|$, observations were made on a selection of both measurable and non-measurable characters of inmates. The measurable characters observed and recorded were those of stature (S), head length (L), head breadth (B), and head height (H); the non-measurable characters were those of hair colour, eye colour and nose contour. Head length was measured from the most prominent point of the glabella to the occipital point. L is therefore maximum head length. The head breadth measured was the maximum breadth above the level of the ear. Head height was taken from the mid points of the auricular passages to the vertex; in some respects, as will be seen from the analysis, this is a somewhat indefinite measurement. The hair categories were red (R), fair (F), medium (M), and dark (D). Red included light, bright and dark red; fair consisted of white,

^{*} All cases of idiocy when recognised ab initio were excluded, or if measured were afterwards excluded under this head.

⁺ Pearl: Biometrika, Vol. IV. pp. 13-104.

[‡] Blakeman: Biometrika, Vol. IV. pp. 124-160.

[§] Biometrika, Vol. v. Suppl., p. 3.

^{||} Henderson Trust Report, Vol. 1. p. 14.

flaxen, and golden yellow; medium included chestnut and all shades of brown except dark brown and black. The eye categories were light, medium and dark. Light included light grey, blue or bluish grey. Dark embraced simply hazel brown and dark brown, while medium covered a mixed class (including grey) which were neither light nor dark. Hair if turned grey was not recorded. The nose shapes recognised and recorded were straight (S), Roman (R), Jewish (J), concave (C), and wavy (W).

It seems desirable at the outset to state the problems which, from the nature of the data, it appears necessary to deal with.

- (a) The fundamental problem clearly is: Does the insane population differ from the sane population? and this necessitates a comparison between sane Scots and insane Scots. No general comparison can, however, be made between these two classes since samples of the normal population in the various districts from which the insane population is drawn have not yet been measured. Only two or three short series are available for comparison. These will be dealt with under the districts to which they belong. Only pauper lunatics having been measured the population of each asylum is a local sample of the district served by that asylum.
- (b) Do the data differ in the form of their distribution from data already collected from other, presumably sane populations?
- (c) Do different parts of Scotland differ sensibly from each other, assuming the insane population to be an anthropometric sample of each local population?
- (d) Is there any reason for supposing greater homogeneity or heterogeneity in one part of Scotland than in another?
 - (e) What general conclusions on other points may be drawn?

(2) Relation between the Nature of the Distributions for Sane and Insane Populations. Problem (b).

In this section it is proposed to consider, not the absolute values of the type, variation and correlation of characters, but the general question of how closely the *form* of the frequency distribution is the same for these two classes of the general population. This may be done (1) by discussing the frequency curve for the distribution of a single character, or (2) by considering the nature of the regression curve for two characters.

(i) Distributions. It has been shown by a number of writers (Fawcett*, Pearson and Lee†, Macdonell‡, and Pearl§), that, with short series, frequency curves for anthropometric characters such as stature, head measurements, cranial measurements and indices follow closely, but not without sensible exceptions, the normal or Gaussian curve. It becomes therefore a problem of much interest to determine

^{*} Biometrika, Vol. 1. p. 443.

[‡] Biometrika, Vol. III. p. 227.

[†] Biometrika, Vol. 11. pp. 361-369.

[§] Biometrika, Vol. IV. p. 40.

whether there are more marked deviations with long series generally, or in the case of the insane, from this form. In the latter case, such would probably arise if the bulk of the insane were characterised by two or more special head shapes; for example, if the insane had special tendencies to macrocephaly and microcephaly.

As stated in the introductory paragraph, certain individuals have been excluded from the general analysis, because they were considered by their medical attendants to have characters affected by special causes, not characteristic of insanity in general. The differences arising in the frequency distributions, according as these cases—throughout this memoir, termed exceptionals—are included or excluded, will now be noted. The constants have been calculated for the "entire insane" population-4436 males and 3951 females-and also for the "general insane" population, i.e. without the exceptionals—4381 males and 3925 females. The values of the constants are given in the following table (Table I.). They show that the distributions are more or less skew, and that when the "entire insane" population is considered, the extremes in the range affect the goodness of fit considerably—in other words, while the skew or normal curves fitted to the distributions fairly describe their nature when considered as a whole, the most important contributions to defect of fit arise from the "tails." Even the "general insane" population shows for most characters excess frequency at the tails, indicating the probability that the homogeneity of the series is affected by the "undetermined residue" referred to above.

Considering the "entire insane" population first, we see that (a) the skewness measured by χ is probably significant in all cases since it amounts in each case to three, or more, times the probable error, (b) the kurtosis, η , is in all cases significant, amounting in every case to many times the probable error. In all the distributions, the positive values of η indicate leptokurtic curves, their magnitudes very largely depending on outlying observations, as will presently be seen*. Thus the skewness and leptokurtosis so affect the distributions that their frequencies cannot be represented by normal curves. Considering further the "entire insane" population, we see that κ_2 lies between 0 and 1 and therefore Type IV. is the actual form needed, but since κ_2 is in every case very small it is clear that the distributions will, if β_1 be very small and β_2 differ in excess significantly from 3, approach closely to Type IV. with symmetry. This actually occurs for all characters but stature, β_1 being less than '03 in all cases except one $(H_{\mathcal{S}})$ when it is only 1 and $\beta_2 = 3 + \eta$, differing very sensibly from 3. Thus it is seen that the "entire insane" population approaches to symmetry in distribution of head characters, and the deviation from normal frequency, accordingly, is not

^{*} In 10 out of 24 cases, C. D. Fawcett's series shows leptokurtosis, while Macdonell's English series shows 14 cases of leptokurtosis out of 26. Biometrika, Vol. 1. p. 442, Vol. 111. p. 228.

[†] Pearson: Phil. Trans. A. Vol. 197, pp. 443-459.

[‡] That is to the form: $y=y_2\left[1+x^2/\left\{2\sigma^2\left(m_2-\frac{1}{2}\right)\right\}\right]^{-(m_2+1)}$, where $\beta_2-3=6/(2m_2-3)$. Professor Pearson points out to me that there is an unfortunate interchange of m_1 and m_2 in the memoir, lines 2, 3, 4 and 5 from bottom. Biometrika, Vol. iv. p. 174.

 $[\]S$ Not absolute symmetry, because the values of β_1 , although small, do differ sensibly from zero.

TABLE I.

Analytical Constants of Curves.

"Entire Insane" Population.

$\frac{\beta_1}{\eta}$	0154 0219 1278 3317 0241 0219 0583		.0574 .0244 .1186 .0012 .0000 .5852
E_{χ}	-3.0215 -3.4322 9.3078 -12.2122 -3.7376 -3.3981 4.5872 -7.9097		-3.2336 -2.5960 7.9023 .4403 .0608 7.5301
$\frac{\eta}{E_{\eta}}$	15.2515 12.3249 15.9187 16.6303 17.3583 14.0817 6.9490 39.7930		2.6450 4.4686 10.4953 2.5694 6.9623 1.2928
×	- 0375 - 0426 - 1155 - 1521 - 0491 - 0447 - 0603		- 0404 - 0324 - 0986 - 0058 - 0008 - 0993
p g	- 0847 - 1177 - 3379 - 2203 - 1021 - 0749 - 1669 - 1434		0881 0869 -2756 -0118 -0013 -2689
Mode	195.7096 151.7359 136.0561 66.1119 186.6806 145.4232 130.6240 61.1852		195.7049 151.6776 136.1130 186.4083 145.2526 130.4558
Mean	195.4556 151.5005 136.7322 65.6712 186.3743 145.1985 130.9579 60.8983	tion.	195 · 4405 151 · 5037 136 · 6641 186 · 4436 145 · 2566 130 · 9935
K ₂	0060 0086 0613 0804 0958 0086 0241	Popula	.0236 .0952 .0552 .0004 .0000 1.8132
κ1	1.4787 1.1830 1.2769 2.8324 1.7586 1.4321 .6668 3.7108	"General Insane" Population.	.2413 .4299 .8615 .2705 .7344
u	7568 6116 7899 8283 9123 7404 3653 2:1000	neral In	.1320 .2231 .5240 .1355 .3672
√\β ₁	.1078 .1156 .3178 .5241 .1483 .1273 .1273	"Gen	.0871 .0738 .2493 .0127 .0020
β_1	.0116 .0134 .1010 .2747 .0220 .0162 .0213		.0076 .0054 .0621 .0002 .0000
$\mu_{\frac{1}{2}}$	97.8150 211.0586 278.0116 21.2949 72.9486 29.6032 197.4970 17.5026		71.3461 167.2315 214.9607 52.6389 24.3749 164.9277
μ3	-1.2422 -2.4439 7.9651 -1.5952 -1.3302 - 6006 3.0927 -1.0182		9076 -1.4256 5.4408 .1049 .0089 3.9643
μ_2	5.1026 7.6446 8.5648 2.1001 4.3181 2.8133 7.6607 1.8525		4.7728 7.2031 7.8103 4.0973 2.6905 7.3318
Unit	3 mm. 2 mm. 2 in. 3 mm. 3 mm. 3 mm. 2 in.		3 mm. 2 mm. 3 mm. 3 mm. 2 mm.
No.	4436 4436 4436 4401 3951 3951 3951 3951		4381 4381 4381 3925 3925
Cha- racter	なななななななななななななななななななななななななななななななななななななな		HAPA HAPA HAPA HAPA HAPA HAPA HAPA HAPA

in the main produced by a heterogeneity depending solely on the presence of a macrocephalic or of a microcephalic group alone. In the case of stature, the values of β_1 are considerably larger. The skewness of the distribution is more marked and is largely due in the case of females, and to some extent in the case of males, to the existence of a dwarf element in the "entire insane" population. This element in the females is in the main identical with the group termed "exceptionals," removed from the "entire insane" population in the manner already explained.

Some peculiarities of the "exceptionals" deserve to be noted. Among the males the head height of the group is much greater than that of the "general insane" population—in other words the male "exceptionals" are a hypsicranial group. The female "exceptionals" are small sized generally; in all characters the means are significantly less than the "general insane" population. The variability of the "exceptionals" for all head characters and for stature is very great indeed and is found to be due to excess frequencies on both sides of the range and a corresponding defect in the frequencies about the mean. The exceptionals are thus mainly a mixture of two groups, one, larger sized in all characters—a megameric group, and another smaller sized in all characters—a micromeric group. An inspection of the following table (Table II.) will serve to emphasize these points.

TABLE II.

Character	"Entire Insan	e" Population	" General Insa	Exceptionals		
Character	Mean	S. D.	Mean	S. D.	Mean	S. D.
<i>L</i> &	195.5	6.78	195.5	6.55	196.7	16:37
\vec{B} \vec{c}	151.5	5.53	151.5	5.39	151.7	13.42
$H \stackrel{\circ}{\circ} \dots$	136.7	5.85	136.7	5.58	147.2	20.75
8 8	65.7	2.90	65.9	2.84	65.4	4.22
L $\c Q$	186.4	6.23	186.5	6.04	176.5	10.97
$B \ \circ \ \dots$	145.2	5.03	145.3	4.91	142.9	13.17
H \bigcirc	131.0	5.54	131.0	5.43	125.3	14.62
S \circ	60.9	2.72	61.2	2.58	58.4	5.77

The mean is less than the mode for all characters except auricular height, δ and $\mathfrak P$, in which cases it is sensibly greater. Since the "general insane" population forms a pretty long series, one can hardly compare the asymmetry values with those of the very much shorter series of Fawcett and others, since the probable errors in these latter cases are relatively very large. Four long series from general sane populations are however available for stature: (α) Baxter's American recruits*, (β) Powys's New South Wales observations†, (γ) Weldon's Verona statistics‡ (Italian conscripts and recruits), and (δ) Macdonell's 3000 English

^{*} Pearson: Phil. Trans. Vol. 186 A, p. 385.

⁺ Powys: Biometrika, Vol. 1. pp. 43-46.

[‡] Pearson; Biometrika, Vol. IV. p. 506.

criminals. One long series is available for L and B, viz. Macdonell's criminals. In the case of the 25,878 American recruits there is a very distinct positive asymmetry (038 + 004) accompanied by mesokurtosis. The New South Wales males show quite significant negative asymmetry for the age groups 25-30 and 60 and over, perhaps significant negative asymmetry for the 40-50 and 50-60 groups, while the 20-25 and 30-40 groups are not significant although still negative. Mr Powys while noting that, for each group, $M_e < M_o$, observes that the skewness in all cases is small, but relatively this is not so, for at least the 25-30 and 60 upwards groups. The Italian conscripts and recruits both show very significant negative asymmetry, agreeing with the New South Wales males and the Scottish "general insane" population. The conscripts show very marked leptokurtosis, and the recruits significant platykurtosis. For four long series, then, viz. New South Wales males, Italian conscripts, Italian recruits and the Scottish general insane population, there is agreement as to asymmetry—in all four cases it is significantly negative; in one case, the American recruits, there is quite significant positive asymmetry. In two cases of very long series there is relative symmetry, viz. 15,117 N. S. W. males (30-40), and 5442 N. S. W. males (20-25) group. Macdonell's 3000 English criminals show slight negative asymmetry. Thus it is seen that in these long series of stature distributions, considered without reference to the ages of the adults in the populations measured, there is significant asymmetry in all cases except one; in three cases it is negative, in one only is it positive. It falls finally to be noted therefore that the negative asymmetry in stature of the "general insane" population is not specially characteristic of the insane; it is also a characteristic of some sane populations. As already stated, no very long series of head measurements are available for comparison with the exception of the 3000 English criminals, the skew curve of B for the series being given by Macdonell*. Here again negative asymmetry is found, and since the ratio $\frac{\chi}{E_{\gamma}} = 3.34$, the deviation from symmetry is probably significant. The L distribution of the same series also shows distinct negative asymmetry, the ratio $\frac{\chi}{E_x} = 3.40$ being found by the writer from the figures kindly supplied by Dr Macdonell. Thus in L and B, just as in stature, when long series are pitted against long series, there is agreement as to the nature of the distribution, which seems to be in the direction of negative asymmetry. The rule, therefore, as stated by Fawcett[†], Macdonell[‡] and Pearl[§] for short series of distributions of anthropometric characters does not appear to hold for long series.

For L and H, except the above case for L, only short series are at present available, and since there is no definite deviation in one direction more than another for these (Macdonell's English Crania, Fawcett's Naqada Crania, etc.), and since the probable errors are large, no comparison can profitably be instituted between them and the long Scottish series.

^{*} Macdonell: Biometrika, Vol. 1. p. 183.

[#] Macdonell; Biometrika, Vol. III. p. 227,

[†] Fawcett: Biometrika, Vol. 1. p. 443.

[§] Pearl: Biometrika, Vol. iv. p. 40,

The general "goodness of fit" of skew and normal curves for the "entire insane" population may next be considered. Taking first the normal curves, we find that in every case the fit is extremely bad; the skew curves show fairly good fits for head breadth (\mathcal{J} and \mathcal{I}), tolerable perhaps for H (\mathcal{J} and \mathcal{I}) and bad for stature and L (\mathcal{J} and \mathcal{I}). If now the values for the "general insane" population are examined, it is found that the fit of normal curves is very bad for stature and H (\mathcal{J} and \mathcal{I}), poor for B, and tolerable only for L. It must therefore be concluded that the rejection of the medically defined exceptionals does not convert the distributions into good normal curves. This can be seen from Table I., where the analytical constants are calculated for the "general insane" population. It is found that (i) the skewness still remains significant for L (\mathcal{J}), H (\mathcal{J}) and H (\mathcal{I}) and perhaps for B (\mathcal{J}), (ii) the leptokurtosis is still significant for B (\mathcal{J}) and \mathcal{I}), \mathcal{I} (\mathcal{J}) and possibly for \mathcal{I} (\mathcal{J} and \mathcal{I}). Summarising, good normal fits are not obtained for the "entire insane" population whether "general goodness of fit" is considered as in Table III., or the values of the analytical constants as in Table I.

TABLE III.

Goodness of Fit. Entire Insane Population. Summary of Tests.

	1	2	3	4	5	6	7	8	9	10
Character		Sex	Unit	Number	No. of in- dividuals especially affecting Fit	Percentage especially affecting Fit	$\begin{bmatrix} x = \frac{X - M}{\sigma} \end{bmatrix}^*$ Points affected x axis	Nature of Curve fitted	χ^2	P
L		ð	3 mm.	4436	5	·11	\(-4.79 \\ +4.95 \)	Type IV	67.75	Very Small
В		ð	2 mm.	4436	23	•52	$\begin{array}{c} 3 - 2.53 \text{ to } -4.34 \\ +4.34 \end{array}$	"	26.60	304
H		đ	2 mm.	4436	18	·41	-3.29 + 2.87	,,	35.20	.110
S		8	2 in.	4401	73	1.66	$\begin{array}{c} (-5.75) \\ +1.84 \text{ to} + 3.22 \end{array}$	"	65.90	Very Small
L		9	3 mm.	3951	25	.63	$\frac{3-5.67}{1+2.03}$	2)	54.10	,,
\boldsymbol{B}		9	3 mm.	3951	3	•08	-4.41	79	18.80	·328
H	• • •	Ý	2 mm.	3951	7	·18	-2.79 to -3.88	37	32.10	·115
S	• • •	9	2 in.	3915	93	2.38	$\begin{cases} -1.43 \text{ to } -4.37 \\ +2.24 \end{cases}$,,	68.50	Very Small
L		8	3 mm.	4381	10	.23	-3.12 to -4.03	Normal	22.10	·140
B_{-}		8	2 mm.	4381	8	·18	-3.36	,,	39.10	Small
H	• • • •	ð	2 mm.	4381	42	.96	+2.30 to +3.73	. ,,	84.20	Very Small
$S_{\underline{I}}$		₹ 0 ₹ 00+0+	2 in.	4393	38	-87	-3.13 to -4.54	"	495.80	22
L	• • •	¥	3 mm.	3925	29	.74	-1.89	***	23.50	.170
B	• • •	¥	3 mm.	3925	15	· 3 8	-3.30 + 3.40	22	43.00	Small
H	•••	9	2 mm.	3925	37	•94	$\{-2.49 \& -3.23 \\ +2.68 \& +3.42 $	37	54.40	Very Small
S		9	2 in.	3890	20	·52	(-3.17 & -3.94)	>>	3 25·50	19

^{*} M = Mean. X = Absolute magnitude of character. Relative scale is $\frac{X - M}{\sigma}$.

The removal of medically defined "exceptionals" tends to improve the goodness of a normal distribution, but it is far from making it essentially good.

On the other hand the only test made of the goodness of fit of skew curves for the "general insane" population is in the case of L (3), and this gives P=88, a splendid fit as compared with the P=14 of the corresponding normal fit, or the practical impossibility of fit at all for the "entire insane" population before the "exceptionals" are removed. It seems likely therefore that the skew curves would describe the "general insane" population satisfactorily in these cases where the normal curve fails. This is a case again of close approximation to symmetry, differing to some extent from normality. But until long series of sane populations are measured it cannot be said that in the "general insane" population there is a wider deviation from the normal curve than occurs in samples of the "general sane" population.

It seems desirable to notice more specially the H distributions, the physical constants of which indicate a wider deviation from the normal curve than exists in either of the two characters L and B. Dealing firstly with H_{d} , we find that, while the values of β_1 , β_2 , κ_1 and κ_2 are less than for the whole series (κ_2 still indicating Type IV.) significant leptokurtosis is associated with significant asymmetry, and that, owing to the emphasis on the positive side of the range between 2.30 to 3.73 on the relative scale, the normal curve fails to fit the distribution. The distribution of H shows a different type of curve from the one deduced for the "entire insane" population. The value of κ_2 being > 1 (1.813) a curve of Type VI, is indicated. A 5 mm. grouping however gives $\kappa_2 = .8$, indicating Type IV. Mesokurtosis occurs with significant asymmetry, and, compared with the normal curve, there is emphasis on both sides of the range. The emphasis occurs at the points 2.49 and 3.23 on the negative, and 2.68 and 3.42 on the positive side of the relative scale. Since the skewness in the character H is certainly significant, both in males and females, since a relatively greater proportion affects the goodness of fit of the normal curve, and since H shows greater relative variability it is evident that this character differs somewhat from L and B in the nature of its distribution. Here, however, the character head height, as defined in the first part. of this memoir, must be considered.

It should be noted that the character H in the living head, as measured from the mid points of the ear passages to the vertex, cannot properly be compared with any of the three similar measurements on the skull, even after due allowance is made for scalp-depth. These three measurements are as follows:

- (1) Basi-vertical height, i.e. height of skull, from the basion to the point on the top of the skull vertically above it, perpendicular to the horizontal plane of the Frankfurt Concordat—the German horizontal plane. This plane is determined by three points, the two highest points on the upper rims of the auricular passages and the lowest point on the under rim of the left eye socket.
- (2) Auricular height, i.e. the vertical height of the skull measured perpendicular to the German horizontal plane, in a line perpendicular to the auricular

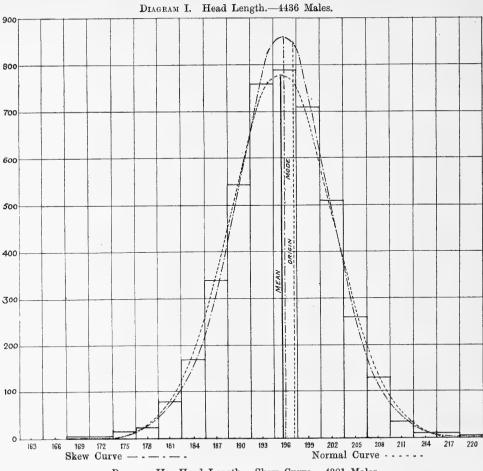
axis round which the skull swings when suspended from the uppermost points of the upper rims of the auricular orifices. This height is taken by some to the bregma.

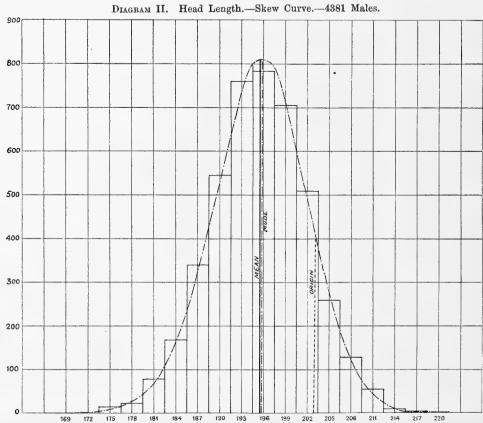
(3) Basi-bregmatic height, i.e. the height of the skull measured from the basion to the bregma.

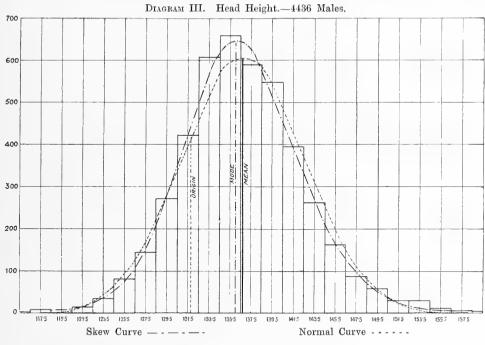
In (1) and (2) the highest point in the vault of the skull is determined by the German plane, and therefore these measurements may not be quite so satisfactory as (3), the basion and the bregma being two fairly definite anatomical positions. But in the living head, the conditions of (1), (2), and (3) are never reached. centre or mid points of the ear holes are not positions so definitely ascertained as the uppermost position on the temporal bone of the external auditory canal, as indicated by the suspension of a skull on two pointers. The soft tissue of the ear yields readily to the slightest pressure, and, therefore, with an instrument having blunt or spherical ends for the ear passages, the greatest care must be exercised in order to avoid drawing the ear up. Any error arising through this however in the asylum survey would be small, as the greatest care was exercised in determining the position. Probably the error is small also at the upper limit, although with the greatest care, one cannot expect the same precision as is obtainable with length and breadth, when it is remembered that the upper limit is "the top of the head, measured in a vertical plane when the eyes are directed to the horizon." What seem more important and real are the thickness of the scalp. the hair, and the slight variations in the pressure on the instrument. difficult to say whether the positive skewness in the distribution of head heights is due severally or jointly to (1) nature of the measurement, (2) nature of the instrument, and (3) to the observer, or (4) whether the positive skewness belongs to the character itself and is really in the nature of its distribution.

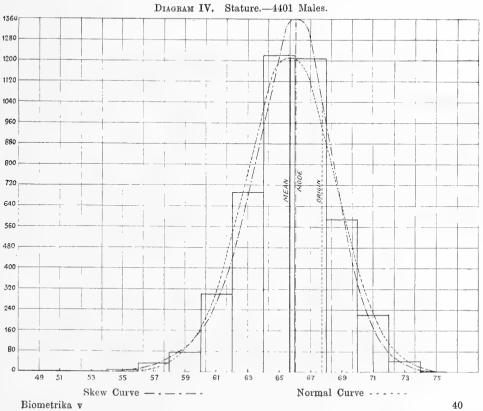
To summarise, it is clear that the distributions of the various characters, whether the "entire insane" or the "general insane" population is considered, may be described with fair accuracy by skew curves, with the exception of L (3 and 2 "general insane") which may be fairly described by the normal curve. (See Diagrams I. to VII.)

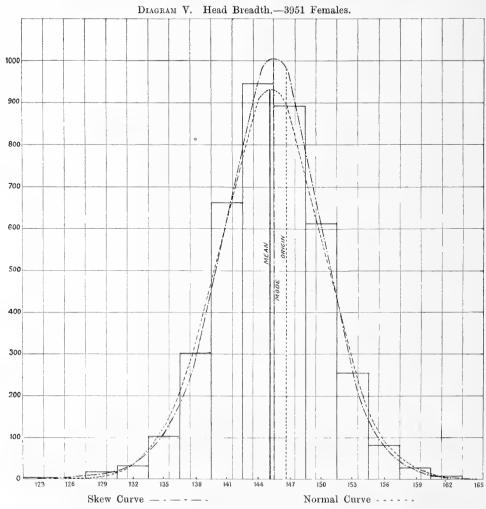
Further, it has just been shown that for long series, just as great divergencies from normality as exist among the "general insane," occur among the sane population, although greater divergencies are shown when the "entire insane" population is considered. It is not, however, established that there is not a difference in the form of distribution between the sane and the "general insane." So far as Scotland is concerned this cannot be definitely determined until a corresponding general survey is carried out. This analysis and discussion thereon merely show that when long series are pitted against long series, quite as great a divergence from normality, as measured by the kurtosis and asymmetry, occurs among the sane as among the insane. The question whether there is really a difference in the form of distribution between the sane and insane must be left an open one when it is remembered that, after the striking "exceptionals" are

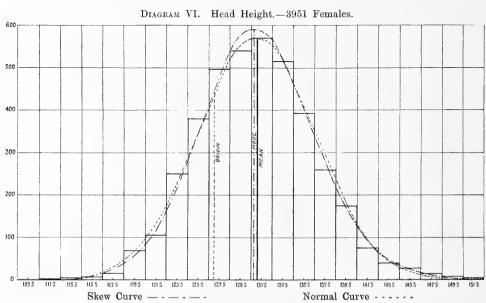


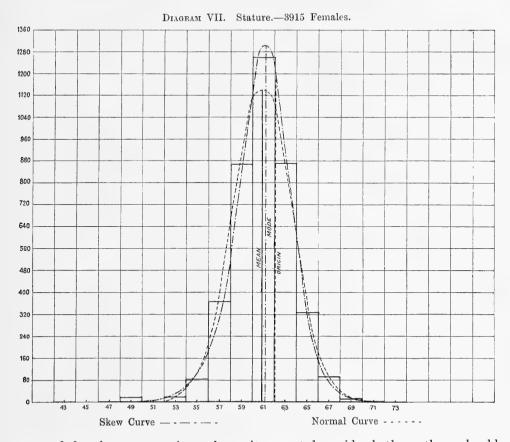












removed for the reasons given above, it cannot be said whether others should or should not be removed by a similar process of reasoning. Heterogeneity, however, may exist. If, for instance, local groups at each individual asylum are taken and their degrees of goodness of fit to the normal curve tested, it is found that, with a 5 mm. grouping, this curve gives very good fits in 125 cases out of 176 (see Table IV.). This, indeed, shows no more than that, for small samples of the insane, the normal curve describes the distribution within the probable errors of the constants, exactly as Fawcett, Macdonell, and others have shown for small cranial series. The divergence from normality in both the "entire insane" and the "general insane" populations of Scotland is therefore either (a) real because the greater numbers allow of more accurate determinations of the kurtosis and asymmetry constants, or (b) spurious and due to the introduction of local heterogeneity. The evidence for and against heterogeneity will presently be considered.

(ii) Correlations. The correlations and the nature of the regression curves for two characters will now be briefly considered. The first main point to be noted is that the values of the coefficients for the "entire insane" population are uniformly greater than those of the "general insane." This is chiefly due to the

TABLE IV.

Goodness of Fit. Normal Curve. Individual Asylums.

Value of P.

(For 5 mm. grouping.)

	L		В		H		S	
	Males	Females	Males	Females	Males	Females	Males	Females
Aberdeen	.916	.042	.911	164	.171	184	·831	350
Dumfries	·815	797	850	•281	-869	372	•915	.782
Dundee	.942	-797	.893	.636	920	•447	.730	•995
Edinburgh	.986	-880	311	221	995	934	.219	•341
Montrose	.770	973	.886	.660	925	.606	610	.860
Argyll	.758	238	273	663	042	.864	.756	.834
Ayr	.778	-834	.822	506	.730	180	885	.782
Banff	-998	.768	645	.860	044	-822	.977	.584
Elgin	.899	.954	.588	.255	.807	.732	.062	.413
Fife	.925	-983	.516	.600	016	296	.188	756
Glasgow (Gartloch)	629	-091	.107	.234	.516	.953	624	.612
,, (Lenzie)	678	719	.570	.304	.144	.195	.021	.183
Govan	.249	.444	.819	.403	.098	.382	.022	-875
Haddington	.720	-881	.136	.801	-954	.991	·612	296
Inverness	391	.943	.526	.963	-085	.900	.030	.333
Lanark	.163	.277	-948	.658	825	·169	-597	.056
Midlothian	.690	.749	.939	.277	-885	.779	.782	.331
Perth	.752	*834	072	.822	.214	.730	.612	.842
Roxburgh	.438	.680	.995	.139	·617	.837	.952	.544
Stirling	-885	.636	.903	.953	.701	.537	·811	•423
Greenock	.933	972	.964	.684	$\cdot 429$.901	·189	.393
Paisley	639	.420	986	.576	•343	·451	875	•959
Number of very ogod fits	19	18	17	14	13	15	15	14

"exceptionals" which are mostly "outliers" in the tables of pairs of distributions considered. The second main point to be noted is that the values for males and females are approximately equal and do not diverge to the extent shown in the values of the corresponding coefficients in most other published results. In the "entire insane" series the most highly correlated pair of characters is that of L & B, and then follow L & H, B & H, L & S, H & S, and B & S. The greatest divergence between the values of the coefficients for males and females appears in the case of the pair of characters L, S, the difference being 3284 - 2573 = 0711. There is closer agreement in the "general insane" series, the greatest difference, 0355, between the values for males and females occurring in the case of the pair of characters L, H.

The reader will find in Table V. a summary of the coefficients evaluated while the lines of regression of head length on stature, \mathcal{C} , and head breadth on head length, \mathcal{C} , are shown in Diagrams VIII. and IX. It will be seen from Table VII. that, taking head measurements,—to be directly comparable—there is a higher

Diagram VIII. Line of Regression; Head Length on Stature. 3915 Females.

Mean Length 186.42 mm. Mean Stature 60.9 in.

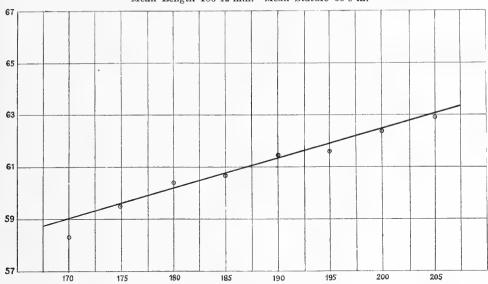
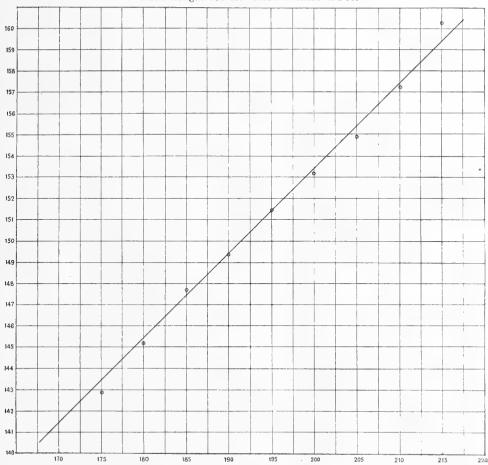


Diagram IX. Line of Regression; Head Breadth on Head Length.—4381 Males.

Mean Length 195'47. Mean Breadth 151'53.



degree of correlation in the pair of characters L, B among the "general insane" than among the 3000 English criminals or the 1000 middle class English, which show the lowest degree of the three classes. For the pair LS the values are very similar for "Entire Insane" males and English Criminals. The values of the

TABLE V.

Coefficients of Correlation.

"Entire Insane" Population		4436 Males	3951 Females
Head Length and Breadth	•••	·5026 ± ·0076	*5235 ± *0078
Head Length and Height		·4027 ± ·0085	*3566 ± *0094
Head Breadth and Height		·3761 ± ·0088	*3474 ± *0095
Head Length and Stature *		·3284 ± ·0091	*2573 ± *0101
Head Breadth and Stature *		·2002 ± ·0098	*2211 ± *0103
Head Height and Stature *		·2340 ± ·0096	*2357 ± *0102
"General Insane" Population		4381 Males	3925 Females
Head Length and Head Breadth	• • •	·4848 ± ·0079	·4672±·0084
Head Length and Head Height		·3755 ± ·0089	·3420±·0095
Head Breadth and Head Height		·3529 ± ·0090	·3325±·0096

corresponding coefficients for some series of skull measurements are given in the table. They show marked differences from the series of head measurements.

In Table VI. are given the values of the correlation ratio, η , and also their differences from the corresponding *comparable* values of r, (i.e. those found without

TABLE VI.

Test of Linearity of Regression.

"General Insane" Population.

Males	η	r	$\eta - r$	$\frac{\sqrt{N}}{67449} \cdot \frac{1}{2} \sqrt{\eta^2 - r^2} \dagger$
Head Length and Breadth Head Length and Height Head Breadth and Height Head Length and Stature	·4612	·4573	*0039	2·94
	·3547	·3546	*0001	·41
	·3390	·3299	*0091	3·83
	·3226	·3133	*0093	3·78
Females Head Length and Breadth Head Length and Height Head Breadth and Height Head Length and Stature	·4372	·4358	*0014	1·62
	·3241	·3216	*0025	1·94
	·3109	·3084	*0025	1·82
	·2489	·2488	*0001	·17

^{* 4401} Males and 3915 Females.

[†] Since $(\eta-r)/r$ is small this formula gives a good arithmetical approximation to the value of $(\eta-r)/E$. See Biometrika, Vol. iv. pp. 348, 349. Blakeman on "Linearity of Regression."

Ordinary method.
$$\theta$$
 method*. Contingency method †. r '5026 '5010 '5019.

(3) Means and their Differences. Problem (c).

In this section the following problem is considered: Do different parts of Scotland differ sensibly from each other, assuming the "general insane" population to be an anthropometric sample of each local population? This problem can be answered by discussing the individual asylum means and the extent of the difference of each from the remainder of the "general insane" population. Asylum means, no matter what character be selected, show differences as we pass from asylum Tables XV. to XXI. of Supplement give the values of the means of all the characters measured for each asylum, the general mean being the last line on every table. The probable errors are given in every case, but in order to note whether or not individual asylum means differ significantly from the means of the remainder of the "general insane" population, the differences have to be studied with respect to the standard deviation of sampling of these differences. If m =the mean of any character at any one of the asylums and M' = the mean of the same character for the remainder of the asylum population, m-M' is the difference between the local mean and that of the rest of the same population. Then, if σ = standard deviation of any character at any one of the asylums and Σ' = standard deviation of the same character for the remainder of the population,

$$\left(\frac{\sigma^2}{n} + \frac{\Sigma'^2}{N'}\right)^{\frac{1}{2}}$$

^{*} Using fourfold table. See Pearson, Phil. Trans. Vol. 195 A, pp. 1-47, 79-150.

⁺ See Drapers' Company Research Memoirs, Biometric Series 1, on "The Theory of Contingency, &c."
K. Pearson.

[‡] Biometrika, Vol. v. Supplement, pp. 92-96.

(where n = number of inmates at any asylum and N' = the remainder of the population of inmates) is the standard deviation of sampling of m - M'. This is the well-known expression for the standard deviation of the differences of two means, and the ratio

$$(m-M')\left/\left(\frac{\sigma^2}{n}+\frac{\sum'^2}{N'}\right)^{\frac{1}{2}}\right.$$

is a measure of the deviation of the local means from the mean of the rest of the population relative to the standard deviation of sampling, or, shortly, is the relative local difference $(RLD)_m$ expressed in a way enabling its significance to be tested. Professor Pearson, whose many suggestions in the course of this investigation the writer desires here gratefully to acknowledge, points out that the biometrician is not warranted in using the ratio

$$(m-M)\left/\left(\frac{\sigma^2}{n}+\frac{\sum^2}{N}\right)^{\frac{1}{2}}\right.$$

where M = general mean, and $\Sigma =$ standard deviation for the whole population, N, (although this is sometimes done), since the local sample is included in the determination of mean and standard deviation of the general population. In a note* kindly shown to the writer Professor Pearson shows that

$$(m-M')\left/\left(\frac{\sigma^2}{n}+\frac{\Sigma'^2}{N'}\right)^{\frac{1}{2}}=(m-M)\left/\left\lceil\frac{\Sigma^2}{N}+\frac{\sigma^2}{n}\left(1-\frac{2n}{N}\right)-\frac{n\left(M-m\right)^2}{N\left(N-n\right)}\right\rceil^{\frac{1}{2}},\right.$$

and is true whatever the magnitudes of N and n may be. In the present series where N=4381 and 3925 for males and females respectively, the term $\frac{n (M-m)^2}{N (N-n)}$ becomes small and may be neglected, so that the standard deviation of sampling of m-M' is given by (and can be conveniently calculated by using) the expression

$$\sqrt{rac{\Sigma^2}{N} + rac{\sigma^2}{n} \left(1 - rac{2n}{N}
ight)}$$
 ,

and the ratio applicable to the present data is thus

$$(m-M)\left/\sqrt{rac{\Sigma^2}{N}+rac{\sigma^2}{n}\left(1-rac{2n}{N}
ight)}\right.$$

The values of this ratio, if the samples are purely random ones, are simply the abscissal values of the normal curve whose equation is $y = 1/\sqrt{2\pi}$. $e^{-\frac{1}{2}x^2}$, and the corresponding ordinal values divide the curve into areas proportional to the probabilities of greater or lesser values occurring in future samples. For graphic representation in the following maps, the relative local differences have been grouped in the following manner. (See also Table VIII.) All values between $-\cdot 5$ and $+\cdot 5$ have been placed into one class, class 0, the central ordinate of the class corresponding to the abscissal value of the normal curve, x=0. All values between $+\cdot 5$ and $+1\cdot 5$; $+1\cdot 5$ and

^{*} Since published. Biometrika, Vol. v. pp. 181-183.

TABLE VII.

Coefficients of Cephalic Correlation.

		es					
	0+	.2573 ± .0101		1		1	
S pu	No.	3915				!	
L and	50	.3284 ± .009	I	.3399 ± .018		į	
	No.	4401		3000	1.		
	0+	·3474 ± ·0095	·3325 ± •0096			·340 ± ·056	.119 ± .052
B and H	No.	3951	3925	1		115	163
B ar	f 0	.3761 ± .0088	.3529 ± .0090	1		·233 ± ·059	·273 ± ·055
	No.	4436	4381			116	129
	0+	.3566 ± .0094	·3420 ± ·0095	-		.425 ± .051	.283 + .048
L and H	No.	3951	3925		1	1117	163
L aı	***	.4027 ± .0085	·3755 ± ·0089	ļ	-	.255 ± .058	.489 ± .044
	No.	4436	4381			120	134
	0+	.5235 ± .0078	.4672 ± .0084			.350 ± .051	.143 ± .049
L and B	No.	3951	3925	ļ	ļ	130	183
L an	50	.5026 ± .0076	.4848 ± .0079	.4016 ± .0123	·3450 ± ·0190	·240 ± ·055	·344 ± ·050
	No.	4436	4381	3000	1000	131	139
	Measurement	Head	Head	Head	Head	Skull	Skull
	Series	"Entire Insane" Pop. Scotland	"General Insane" Pop. Scotland	Criminals*, England	Middle Class†, English	Whitechapel ;, English	Naqada §

^{*} Macdonell: Biometrika, Vol. 1, pp. 181–188.
† Given by Macdonell: Biometrika, Vol. 1, pp. 181—188.
‡ Macdonell: Biometrika, Vol. 111. p. 233.
\$ Fawcett: Biometrika, Vol. 1, p. 455.

1, 2, and 3 respectively, the central abscissa of each class being once, twice, and three times the standard deviation of sampling respectively. It should be noted that the central abscissa of each class does not divide the class into two equal areas; it merely notes the centre of the range of the class. The last positive class is class 4, including values greater than 3.5 times the standard deviation of sampling. In a similar manner four negative classes have been instituted with the corresponding limits; class -1:-5 to -1.5; class -2:-1.5 to -2.5; class -3:-2.5 to -3.5; class -4: greater than -3.5. The object of this grouping is to arrange the relative local differences in the order of their significance, separating those which are fair samples of the general population from those which clearly are not. The following classes of relative local differences are thus created. (Table VIII.)

TABLE VIII.

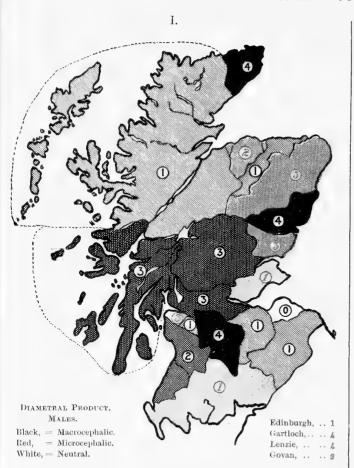
1	2	3	4		
The local mean, compared with the general mean is	Class	Range of class in terms of $(m-M)\left \sqrt{\frac{\Sigma^2}{N} + \frac{\sigma^2}{n}(1 - \frac{2n}{N})}\right $	greater deviations		
			Upper Limit Lower Limit		
Very much smaller Probably significantly less Less, but not quite significantly less Very slightly less Quite insignificantly different Very slightly greater Greater, but not quite significantly greater Probably significantly greater Very much greater Very much greater	$ \begin{array}{c c} -4 \\ -3 \\ -2 \\ -1 \\ 0 \\ 1 \\ 2 \\ 3 \\ 4 \end{array} $	-3.5 upwards -2.5 to -3.5 -1.5 to -2.5 - 5 to -1.5 + 5 to -5 + 5 to 1.5 1.5 to 2.5 2.5 to 3.5 3.5 upwards	0 :0233 ·0233 ·6210 ·6210 ·6·6807 ·6·6807 ·30·8537 30·8537 to 50* and 50 to 30·8537 ·6·6807 ·6·210 ·6·6807 ·0233 ·6·210 0 ·0233		

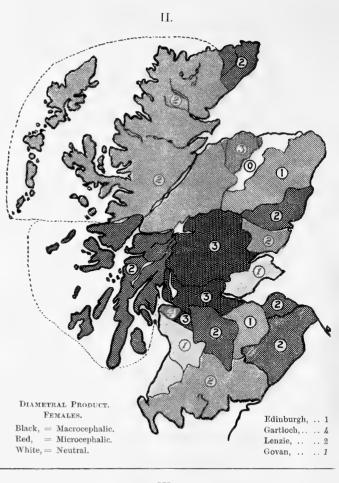
Relative local differences falling beyond +2 and -2 may be regarded as probably significant since the number of asylums is small (22), and since the probability that a greater deviation than that occurring at the furthest extreme on the range of this class is about 1 in 81, while the value for the central abscissa of this class is about 1 in 22. The figures in the fourth column obviously express the probable number of deviations from the general mean (per cent.) in future samples for the upper and lower limits of each class.

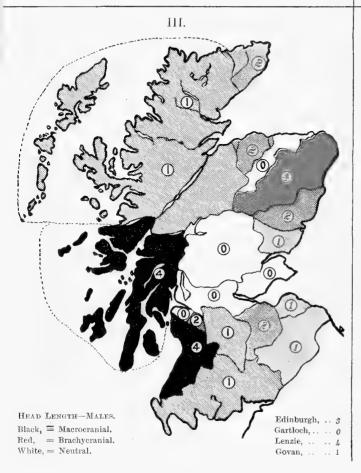
The distribution constants of each character for the whole population being used as a basis, the constants for each character in the various districts throughout Scotland will now be discussed. The relative differences between the local means and the rest of the population for each character are first considered.

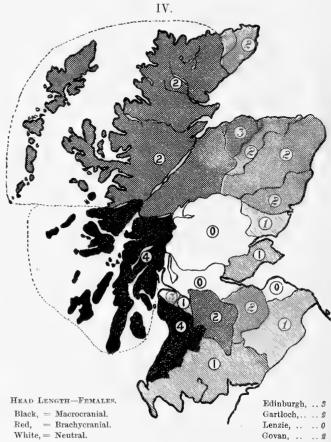
^{* 50=}P, for centre of this class,



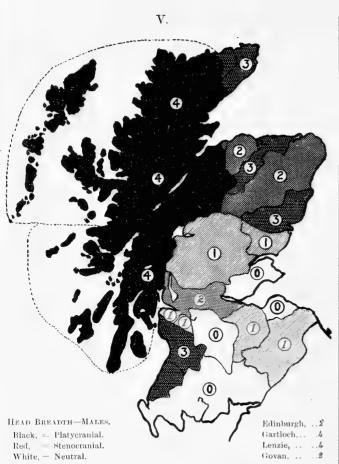


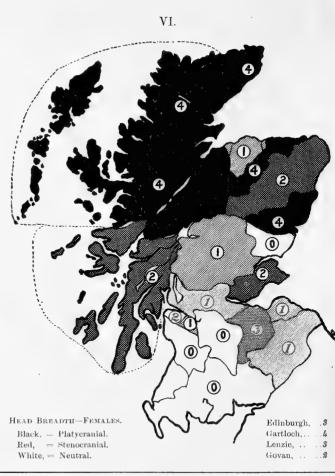


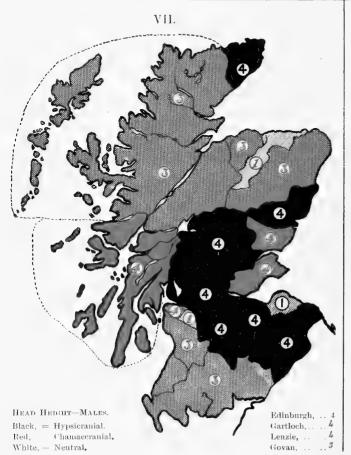


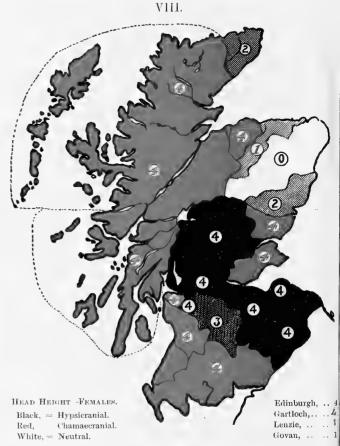


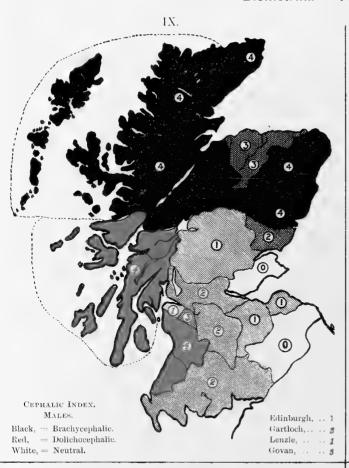
	,		

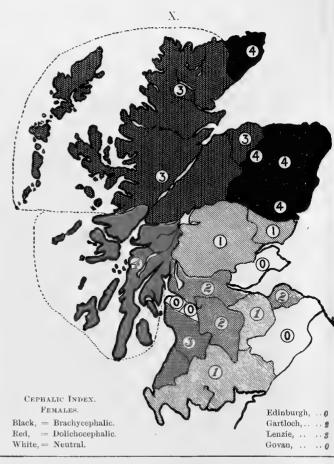


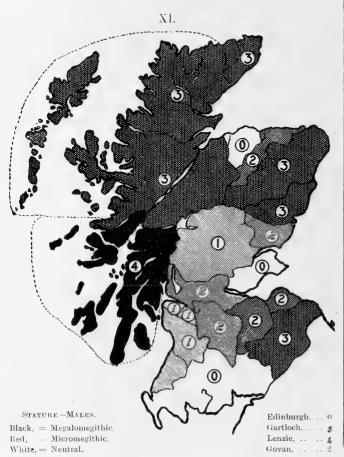














I. Individual Characters.—Head Length. (See Maps III. and IV.) An inspection of the accompanying maps reveals the fact that, exclusive of Glasgow, the west (and particularly the south-west) of Scotland has a long-headed or macrocranial population of inmates, while the north-east population is distinctly brachycranial. Edinburgh and Midlothian generally are slightly brachycranial. Among the Glasgow asylums, nothing striking in head length is noted, except among the males at Lenzie, who are as distinctly brachycranial* as the north-east population. The macrocranial inmates are those of Argyll, Ayr, and Renfrew, while the Inverness group (including Ross and Sutherland), and the Dumfries group (including Kirkcudbright and Wigton and Lanark) show this characteristic only in a slight degree. The Inverness females are more markedly macrocranial than the males. In a general way, a line drawn from the most northern part of the boundary between Sutherland and Caithness to the boundary between Dumfries and Cumberland on the Solway firth divides Scotland into a macrocranial and a brachycranial population.

Head Breadth. (See Maps V. and VI.) Quite a different grouping is shown among head breadths. The north of Scotland is distinctly broad-headed or platycranial, while the populous centres round about Glasgow and Edinburgh, and these towns themselves, show stenocranial characteristics or narrow-headedness. The female inmates of Edinburgh and Midlothian are more stenocranial than the males, while those of Argyll are less platycranial than the male inmates of the same asylum. The platycraniality of the Ayr males is probably significant. The inmates, of both sexes, at the Glasgow asylums, Gartloch, Lenzie and Govan, agree in showing distinct narrow-headedness or stenocraniality.

Cephalic Index. (See Maps IX. and X.) The ratio $i = 100 \, B/L$ is conveniently taken after the characters B and L. The results are even more striking than those of the characters just mentioned. The means and standard deviations were calculated from the formulae deduced by Pearson+, and the tables and maps show the differences, with respect to the standard deviations of sampling of these differences of means in the usual way. The north of Scotland is distinctly brachycephalic, while the south, particularly the south-west, is dolichocephalic, This condition of affairs is common to both male and female inmates, the only exceptions of significance being that of (1) Govan, the females there being mesocephalic or differing little from the general population, while the males agree with the surrounding population in being distinctly dolichocephalic, and (2) of Haddington, the females there being rather dolichocephalic, while the males show slight brach, cephaly. In such distinctly Highland counties as Argyll, Perth and Inverness, Argyll differs from the other two in being strikingly dolichocephalic, and from the whole population in actual size of head, as will be seen later. Perth and Fife are buffer counties, and the remaining portion of Scotland to

^{*} All the terms of this section are used in the sense indicated by C. D. Fawcett, Alice Lee and K. Pearson, in the memoir on Naqada crania: Biometrika, Vol. r. p. 462.

the west is divided off by Inverness in the north and Argyll in the south, thus bisecting the country north and south into a brachycephalic northern population and a dolichocephalic southern one.

LB product. If the product $L \times B = p_a$ be now considered, an idea may be gathered as to the magnitudes of the sectional areas in the length-breadth plane to which the products are proportional. The ratio $i=100 \ B/L$ deals only with the shape of the head in the same plane. An evaluation of the product enables an inspection to be made of the various mean values of p_a with the same or different mean values of i. It is to be observed that large sectioned and small sectioned groups may have the same cephalic index. Thus groups may be similar in shape but significantly different in size of section, due to greater or lesser length or breadth. A comparison of the values of length, breadth and cephalic index would of course bring out the facts, but it would be interesting to know the values of the means and standard deviations of the product in order to perceive by direct inspection significant differences of mean section. however, the means and standard deviations of these products can be evaluated \overline{p}_n and Σ_n have to be deduced in a manner similar to that employed for the ratio 100 B/L. Adopting the notation used by Pearson in the paper already referred to, if x_1, x_2 be the absolute magnitudes of any two correlated characters; m_1, m_2 their means; σ_1 , σ_2 their standard deviations; r_{12} their coefficient of correlation; \overline{p}_a the mean value of the distribution of x_1, x_2 ; Σ_{p_a} the standard deviation of the same distribution;

$$v_1 = \frac{\sigma_1}{m_1}$$
 and $v_2 = \frac{\sigma_2}{m_2}$; $\epsilon_1 = x_1 - m_1$ and $\epsilon_2 = x_2 - m_2$;

and finally n = the total number of pairs, then

$$\bar{p}_a = \frac{1}{n} S\left(x_1 x_2\right) = \frac{1}{n} S\left[m_1 m_2 \left(1 + \frac{\epsilon_1}{m_1}\right) \left(1 + \frac{\epsilon_2}{m_2}\right)\right]$$

$$= \frac{m_1 m_2}{n} S\left(1 + \frac{\epsilon_1}{m_1} + \frac{\epsilon_2}{m_2} + \frac{\epsilon_1 \epsilon_2}{m_1 m_2}\right)$$

$$= m_1 m_2 \left(1 + \frac{S\left(\epsilon_1 \epsilon_2\right)}{n m_1 m_2}\right)$$

$$\bar{p}_a = m_1 m_2 + r_{12} \sigma_1 \sigma_2 \dots (1).$$

and summing

or

The standard deviation is then found as follows:---

$$\begin{split} n \, \Sigma_{p_a}^2 &= S \, (x_1 x_2 - \bar{p}_a)^2 \\ &= m_1^2 m_2^2 \, S \, \left(\frac{\epsilon_1}{m_1} + \frac{\epsilon_2}{m_2} + \frac{\epsilon_1 \epsilon_2}{m_1 m_2} - r_{12} v_1 v_2 \right)^2 \\ &= m_1^2 m_2^2 \, \left[S \left(\frac{\epsilon_1}{m_1} \right)^2 + S \left(\frac{\epsilon_2}{m_2} \right)^2 + 2 \, \frac{S \, (\epsilon_1 \epsilon_2)}{m_1 m_2} \right. \\ &\quad + \frac{S \, (\epsilon_1^2 \epsilon_2^2)}{m_1^2 m_2^2} - \frac{S \, (\epsilon_1 \epsilon_2)}{m_1 m_2} \, r_{12} v_1 v_2 + r_{12}^2 v_1^2 v_2^2 + \frac{2S \, (\epsilon_1^2 \epsilon_2)}{m_1^2 m_2} + \frac{2S \, (\epsilon_1 \epsilon_2^2)}{m_1 m_2^2} \right]. \end{split}$$

Since $S(\epsilon_1^2 \epsilon_2) = S(\epsilon_1 \epsilon_2^2) = 0$ on the assumption of normal correlation, and since $S(\epsilon_1^2 \epsilon_2^2) = n\sigma_1^2\sigma_2^2(1 + 2r_{12}^2)$ on the same hypothesis, we have:

$$n\sum_{p_2}^2 = m_1^2 m_2^2 \left[nv_1^2 + nv_2^2 + 2nr_{12}v_1v_2 + nv_1^2v_2^2 (1 + r_{12}^2) \right].$$

The term $nv_1^2v_2^2 (1+r_{12}^2)$ does not appreciably affect the result and may be neglected. Thus

$$\Sigma_{v_{-}} = m_1 m_2 \left[v_1^2 + v_2^2 + 2 r_{12} v_1 v_2 \right]^{\frac{1}{2}} \dots (2).$$

An inspection of the relative local differences of \bar{p}_a , in Table IX., reveals the fact that the entire west of Scotland is large sectioned and that the east country south of the Forth is small sectioned, compared with the general population. These deductions can, of course, be made from the lengths and breadths themselves, but the facts do not come out so clearly. It is seen that Argyll and Ayr have large cross sections because of their long-headedness, while in the Inverness group's large section is due to the group's broad-headedness. It is also to be noted that both Edinburgh and Glasgow have small product means.

Diametrical Product. (See Maps I. and II.) This product $L \times B \times H = p_{\beta}$ is a useful character, supplying as it does, an estimate of the mean relative size of head in each of the asylum groups. The means and standard deviations were calculated from the following formulae, derived by the same process of reasoning and approximation as that employed to deduce the mean and standard deviation of the LB product.

$$\overline{p}_{\beta} = \frac{1}{n} S(x_1 x_2 x_3) = m_1 m_2 m_3 \left[1 + r_{12} v_1 v_2 + r_{13} v_1 v_3 + r_{23} v_2 v_3 \right] \dots (3)$$

and

$$\Sigma_{p_{B}} = m_{1}m_{2}m_{3} \left[v_{1}^{2} + v_{2}^{2} + v_{3}^{2} + 2r_{12}v_{1}v_{2} + 2r_{13}v_{1}v_{3} + 2r_{23}v_{2}v_{3} \right]^{\frac{1}{2}} \dots (4).$$

In the region of Scotland south of the Grampians and north of the Border and Galloway (that is, practically the Scottish Midlands), with the exceptions of the large towns of Glasgow, Dundee, Aberdeen and Greenock, the asylum inmates are large-headed or macrocephalic. In the above mentioned towns they are small-headed or microcephalic. Edinburgh and the rest of the country approximates to the mean diametral product. The large-headed or macrocephalic group consists of Argyll and Lanark (which are dolichocephalic), and Montrose, Perth and Stirling (which are brachycephalic). It is plainly evident that, excluding Edinburgh, the inmates of asylums in the great cities are smaller headed than those of the rest of the country, that is, they are a microcephalic population. The only significantly small-headed or microcephalic rural group is that of Elgin, where there are only 71 male and 89 female inmates. Aberdeen females are medium sized or mesocephalic, while Inverness females are smaller sized than the males. The distribution of relative size of head is shown as follows:—

TABLE VIII. (bis).

Diametral Product.

	ntly Large = cephalic	Medium = N	I esocephalic	Significantly Small= Microcephalic		
Males	Females	Males	Females	Males	Females	
Montrose Perth Stirling Lanark Argyll Ayr	Montrose Perth Stirling Lanark Argyll Roxburgh Haddington Paisley	Fife Banff Midlothian Edinburgh Inverness Roxburgh Haddington Dumfries Paisley	Fife Banff Midlothian Edinburgh Ayr Aberdeen	Gartloch Lenzie Govan Dundee Greenock Elgin Aberdeen	Gartloch Lenzie Govan Dundee Greenock Elgin Inverness Dumfries	

Head Height. (See Maps VII. and VIII.) The means of this character show greater variability than those of any other character do. This is at once seen from the interlocal constants, discussed further on. The inmates are divided sharply into two groups, (1) a high-headed or hypsicranial group, and (2) a low-headed or chamaecranial one. The Scottish Midlands are hypsicranial. Inverness, Aberdeen, Elgin, Argyll, Ayr, Galloway—all contiguous—are chamaecranial, as also are Fife and Dundee. Edinburgh city differs from Glasgow, Dundee and Aberdeen in being hypsicranial, agreeing with the surrounding country in this distinguishing feature. Males and females agree generally, the exceptions being Paisley, and to a lesser extent Haddington, Lenzie and Aberdeen.

Stature. (See Maps XI. and XII.) Glasgow and its environs, Paisley, Greenock, Lanark, Stirling and Ayr differ materially from the rest of Scotland with respect to stature. The inmates of this group are short-statured or micromegithic. The female inmates of Govan and Lanark, however, differ very little from the general mean. The males of the entire north (excepting Elgin, which is average statured or mesomegithic) and the border counties are tall-statured or megalomegithic. Galloway males approximate the mean. Taking the cases from the tallest downwards, the order of the asylums are as follows:—Argyll, Inverness, the Border counties, Aberdeen, Banff and Haddington. The shortest inmates are found at Lenzie, and then follow Gartloch, Stirling, Lanark and Dundee. Generally speaking the asylum population is shorter in the neighbourhood of the great cities and in these cities themselves than in the rest of Scotland.

The foregoing statements are based on results which are embodied in the following table.

TABLE IX.

(Values of
$$(m-M)\sqrt{\frac{\Sigma^2}{N}+\frac{\sigma^2}{n}\left(1-\frac{2n}{N}\right)}$$
.

Relative Local Differences of Means.

		L	B	H	p_a	p_{β}	i	S
Males								
Aberdeen		- 4.68	1.92	-3:40	-1.58	-2.74	6:40	2.77
Dumfries		1.41	- '35	-3.44	•59	-1.05	-1.66	.37
Dundee		56	1.27	-7.52	•40	-2.81	1.84	-1.67
Edinburgh		-2.55	-1.54	5.69	-2.40	1.04	.85	- 13
Montrose		-1.59	3.04	6.90	-82	3.96	4.55	2.79
Argyll		8.08	3.90	-4.29	6.82	3.21	-3.79	4.92
Ayr		5.98	2.51	-3.05	4.77	2.08	-3.82	-1.14
Banff		.22	2.80	-1.22	1.84	.76	2.71	1.77
Elgin		-1.60	1.51	-3.07	.08	-1.58	2.97	- 35
Fife		46	.39	-3.88	46	-1.30	05	- 12
Glasgow (Gart		39	-3.66	-5.95	-2.43	-4.46	-3.37	-3.42
\ \tag{T}		-5.42	-5.57	- 4.85	-6.46	-6.95	60	-7.76
Govan (Lenz		.76	-2.26	-3.33	-1.96	-2.21	-3.04	2.09
Haddington		72	05	-56	- 43	-05	-504	2.03
Inverness		1.23	4.57	-3.33	3.56	.64	3.72	3.43
Lanark		77	- 21	6.11	1.10	3.63	-2.44	-1.69
Midlothian		- 2.45	-1.31	5.98	-2.12	1.25	.64	1.58
Perth		- 37	+1.09	5.90	.45	3.37	1.43	1.49
Roxburgh	• • • •	- ·58	- ·83	3.95	- '84	1.09	- '31	2.89
Stirling	***	- '20	-2.14	7:71	-1.39	2.70	-1.95	-2.05
Greenock	• • •	- 20 ·14	- ·79	-6.80	- ·40	-3.15	96	-1.28
Paisley	• • •	1.72	-1.11	-1.03	.43	-69	-2.78	-1.13
Taisicy	••	1 (2	-111	-1 05	10	05	-270	-110
Females								
Aberdeen		-1.93	2.16	.49	.11	.56	4.04	.56
Dumfries		1.16	.37	-5.79	1.04	-1.79	73	1.79
Dundee		-1.28	30	-3.54	89	-2.26	.94	-1.68
Edinburgh		-3.04	- 2.85	6.68	-3.44	.92	23	-1.11
Montrose		-2.06	3.78	1.98	1.24	1.92	5.54	-1.01
Argyll		6.12	1.70	-3.61	4.58	1.70	-4.38	2.41
Ayr		4.02	45	-6.56	2.48	85	-3.20	-1.75
Banff		-1.73	4.36	-1.13	1.37	-28	5.73	2.94
Elgin		-2.62	'96	-4.78	94	-3.06	3.42	3.37
Fife		+1.38	1.51	-4.15	1.69	- '71	.23	3.50
Glasgow (Gart	loch)	-1.83	-4.40	-6.44	-3.64	-5.75	- 2.48	-2.45
" (Lenz		.00	-3.14	59	-1.86	-1.64	-3.07	-6.10
Govan		-1.76	-2.19	1.47	-2.32	-1.11	43	.18
Haddington		.35	-1.33	5.67	- 62	2.30	-1.68	1.71
Inverness		1.84	5.18	-8.83	4.09	-2.01	3.18	5.06
Lanark		1.62	50	2.71	.63	1.75	-2.05	•41
Midlothian		-1.51	-2.58	5.30	-2.36	1.11	95	.02
Perth		17	- 2.00	5.57	.56	2.73	.61	.02
Roxburgh		99	72	5.85	99	2.48	.09	2.33
Stirling		.13	-1.43	7.46	78	3.33	-1.56	-3.38
Greenock		-2.51	-1.64	-4.83	-2.38	-4.02	*43	-3.43
Paisley		.98	1.03	3.69	1.18	2.57	.06	1.17
	• • • •	00	1 00	3 00	- 10	0.	0.0	
					-			

II. Interlocal and Intralocal Characteristics. If the distribution of the differences of means of any one character throughout the whole of the asylums be considered, and the variability of the distribution for each character be determined,

an accurate estimate can be formed as to the relative homogeneity of the general population, with respect to each separate character. If the whole population be homogeneous the relative differences between the general and local means should be expressed by a random distribution. It should be again noted that the relative local differences (RLD) are the differences between the general mean M and the local means m reduced to a common scale by dividing each difference by its standard deviation, i.e. the ratios

$$(m-M)\left/\sqrt{\frac{\Sigma^2}{N}+\frac{\sigma^2}{n}\left(1-\frac{2n}{N}\right)}\right.$$

for each character at each asylum are considered interlocally. If the population be a homogeneous one with respect to the character considered, the standard deviation of the distribution of these ratios interlocally, or s, will seldom differ from unity by a quantity greater than three times the probable error of s, or $s = 1 \pm \frac{.67449}{\sqrt{2q}}$ where q is the number of districts considered. Thus s is an

interlocal constant determining the degree of homogeneity of the characters considered or the degree of character homogeneity. An attempt has also been made to discover the degree of district or local homogeneity, using the values of the relative local differences intralocally, but the writer has failed to find a solution of this interesting problem. As Professor Pearson has pointed out no attempt can be successful which neglects intralocal correlations, and since head characters are all more or less highly correlated, the reasoning employed with respect to the relative local differences interlocally is not applicable intralocally. It is to be hoped that Professor Pearson will find time to furnish anthropometricians with a solution.

The numerical portion of the following tables (Tables X. and XI.) gives the values of the interlocal constants, h being the mean of the distribution of (RLD) m interlocally and (s-1) the deviation from homogeneity of the general population for the various characters shown in the table. In the body of the table the distinguishing feature of each character is shown for each asylum, the terms employed to describe significant excess or defect of local means from the general mean being those already referred to in C. D. Fawcett's memoir, except where new terms are used, as defined in the text and in the "synopsis of terms." Where the blanks occur in the table, approximations to the general mean are This table should be examined in conjunction with the character maps and the diagrams of relative local differences. Confining attention in the first instance to one character at a time, it has already been noted that if the population had been an entirely homogeneous one, the value of s-1=0 and the groups at the various asylums would have simply been fair random samples of the whole. The magnitudes of many of the relative local differences show this is not the case.—The values of (s-1) for the character $H(\mathcal{J})$ and \mathfrak{P}), viz. 3.89 and 3.95, compared with their probable errors, are very large, thus indicating a very significant deviation from homogeneity interlocally. The values of (s-1) for all

TABLE X.
Specification of Asylum Population.—Males.

General Description	Mictomeric Isomeric Mictomeric Mictomeric Megalomeric Megalomeric Megalomeric Megalomeric Isomeric Mictomeric Micromeric Isomeric Micromeric Micromeric Micromeric Micromeric Micromeric Micromeric Isomeric Micromeric Micromeric Micromeric Isomeric Is	
82	Megalomegithic Megalomegithic Megalomegithic Megalomegithic Micromegithic Micromegithic Megalomegithic Megalomegithic Megalomegithic Megalomegithic Megalomegithic Micromegithic Micromegithic Micromegithic Micromegithic	.054
p_{β}	Microcephalic Macrocephalic Macrocephalic Macrocephalic Microcephalic Microcephalic Microcephalic Microcephalic Microcephalic Microcephalic Microcephalic Microcephalic Microcephalic Macrocephalic Macrocephalic Macrocephalic	077
	Brachycephalic Dolichocephalic Brachycephalic Brachycephalic Dolichocephalic Brachycephalic Brachycephalic Brachycephalic Brachycephalic Brachycephalic Dolichocephalic	.041
Н	Chamaecranial Chamaecranial Hypsicranial Hypsicranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Hypsicranial Hypsicranial Hypsicranial Hypsicranial Hypsicranial Chamaecranial Hypsicranial Hypsicranial	3.890
В	Platycranial Stenocranial Platycranial Platycranial Platycranial Platycranial Stenocranial	.167
L	Brachycranial Brachycranial Brachycranial Macrocranial Brachycranial Brachycranial Brachycranial Brachycranial Brachycranial Brachycranial	- ·015 1·855
	Aberdeen Dumfries Dumdee Edinburgh Montrose Argyl Ayr Banff Clasgow (Gart.) Do. (Lenzie) Govan Haddington Inverness Lanark Midlothian Perth Rayl	$\frac{h}{s-1}$

TABLE XI.
Specification of Asylum Population.—Females.

General Description	Mictomeric Mictomeric Mictomeric Mictomeric Mictomeric Megalomeric Mogalomeric Mictomeric	1
8	Megalomegithic Micromegithic Micromegithic Megalomegithic Megalomegithic Megalomegithic Micromegithic Micromegithic Micromegithic Micromegithic Micromegithic Micromegithic Micromegithic Micromegithic Micromegithic Megalomegithic Megalomegithic Micromegithic	.207 1.625
$_{eta}$	Microcephalic Macrocephalic Macrocephalic Microcephalic Microcephalic Microcephalic Macrocephalic	- ·073 1·384
į	Brachycephalic ———————————————————————————————————	•159 1·690
Н	Chamaecranial Chamaecranial Hypsicranial Hypsicranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Chamaecranial Hypsicranial	- 154 3.953
В	Platycranial Platycranial Platycranial Platycranial Platycranial Stenocranial Stenocranial Stenocranial Stenocranial Stenocranial Stenocranial	053
L	Brachycranial Brachycranial Brachycranial Macrocranial Brachycranial	- 158 1·123
	Aberdeen Dumfries Dumfries Dumdee Edinburgh Argyll Ayr Banf Elgin Fife Clasgow (Gartloch) Do. (Lenzie) Govan Inverness Lanark Midlothian Perth Roxburgh Stirling Greenock Paisley	$\frac{h}{s-1}$

the other characters, compared with $E_{(s-1)}$ also show that the differences, although not so large as in H, are all quite significant, and indicate that, passing from asylum to asylum, the means vary very considerably. In other words, while some local groups are fair samples of the "general insane" population for one or more characters, the majority of them are not fair samples. Individual asylum groups as a whole therefore cannot be said to form part of a "general insane" population of a homogeneous character. On the contrary, considered interlocally, asylum groups as a whole show great heterogeneity—greatest in the character H. An inspection of the table shows what has already been demonstrated regarding this character, its great variability from asylum to asylum. If the differences, grouped as already indicated, be arranged in the order of their frequency it is quite clear that the homogeneity curve $y = \frac{22}{\sqrt{2\pi}} e^{-\frac{1}{2}x^2}$ does not in the least fit the distribution,

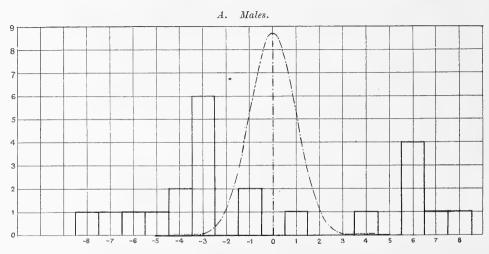
as Diagrams X (A and B) show. The frequency at the mean approximates to a minimum instead of a maximum value. The diagrams and maps show, what the analysis clearly indicates, that there are really two very distinct groups, a high-headed or hypsicranial and a low-headed or chamaecranial one.

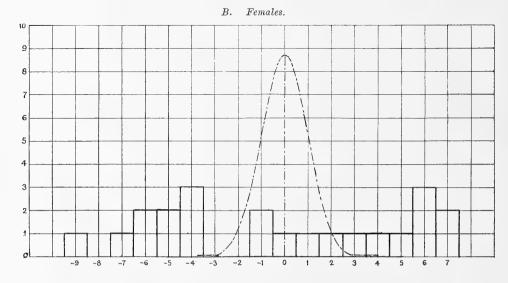
Examining now the relative local differences intralocally, we can form an idea of the anthropometric character of each individual asylum. Take striking cases: Argyll males and females show macro-, platy-, and chamae-craniality; they are therefore large sectioned. p_{θ} is large; they are thus large-headed or macrocephalic and they are tall-statured or megalomegithic. Viewing dolichocephaly as a defect of i, this is the only significant defect among the Argyll inmates. With the exception of p_{β} (?), all these characteristics are significant excesses from their respective means. Thus the Argyll group of inmates is the most significantly The group is a megalomeric one, most of its characters being megalo-By megalomeric is meant that the group possesses, on an average, greater magnitudes of the various characters measured than the general population of inmates. By megalometropic is meant that, in reference to the magnitude of any character, the value found is significantly greater than the value of the corresponding constant with which it is compared; by micrometropic, that the value is significantly less; and isometropic means that it is insignificantly different, with reference to the constant. Lenzie inmates show almost as great deviations as Argyll inmates do. The body of the table shows Lenzie to possess brachysteno-chamaecranial inmates, small sectioned and short-statured. The group is a micromeric one, having magnitudes of the various characters measured considerably smaller on an average than the general population, i.e. most of the characters are micrometropic. On the other hand, Paisley approximates to the general population in the magnitudes of its character means. Paisley males are slightly macrocranial, but distinctly dolichocephalic, their only distinguishing feature. Paisley females are hypsicranial. On the whole, the Paisley group is an isomeric one, the magnitudes of the characters of the group being mostly isometropic, or they are on the whole similar to the values found in the general population. The

megalomeric populations are those of Argyll, Ayr, Montrose and Banff, while the distinctly micromeric populations are those of Glasgow (Gartloch, Lenzie and Govan). Isomeric populations occur at Dumfries, Fife, Haddington, Perth, Greenock and Paisley. All the other groups are *mictomeric*. By this is meant that the group possesses on an average greater or equal magnitudes of some characters, and equal or less in others—the characters are in part megalo-, micro-, and isometropic. With respect to the general population, the significant differences or deviations are both positive and negative; or comparatively speaking, the mictomeric groups have a mixed specification.

DIAGRAMS X. (A and B). Relative Local Differences of Means.—Head Heights.

Equation to Curve $y=\frac{22}{\sqrt{2\pi}}$, $\ell^{-\frac{1}{2}x^2}$. The value of χ^2 is very large.





(4) Variabilities and their Differences. Problem (d).

Do the results for different parts of Scotland give any reason for supposing greater homogeneity or heterogeneity in one part than another? An endeavour can be made to answer this question after considering the variabilities in the distributions of the various characters. Under the character means, just dealt with, the sizes of the organs or characters were considered, differences in type noted, and the conclusion reached that the asylum population, as a whole, no matter what character is selected, is not a homogeneous one. An attempt will now be made to ascertain whether the separate district groups themselves can be described to be homogeneous; in other words, whether the groups in the various districts in Scotland are significantly more or less variable than the general asylum population.

If σ = the standard deviation of any character at any asylum, and Σ' = the standard deviation of the same character in the remaining population, then the ratio

$$(\sigma - \Sigma') / \sqrt{\left(\frac{\sigma^2}{2n} + \frac{\Sigma'^2}{2N'}\right)} = (RLD) \sigma$$

is the relative local difference in variability for any asylum. The values of this ratio for each character have been determined using the formula*

$$\sqrt{\left(rac{\sigma^2}{2n}-rac{\Sigma^2}{2N}
ight)}$$

where N = (n + N') = number in the whole population, in place of

$$\left\lceil \frac{\Sigma^2}{2N} + \frac{\sigma^2}{2n} \left(1 - \frac{2n}{N} \right) \right\rceil^{\frac{1}{2}},$$

Pearsons's full formula, which he shows to give the equivalent to

$$\left(\frac{\sigma^2}{2n} + \frac{\Sigma'^2}{2N'}\right)^{\frac{1}{2}}$$
.

The foregoing shorter formula has been used, on the assumption, warrantable in the present series, that the ratio $\frac{\Sigma^2}{2N}$ differs from $\frac{\sigma^2}{2N}$ by a quantity so small that

it may be put $=\frac{\sigma^2}{2N}$ without affecting the significance of the final result. In short, in this instance

$$\left(\frac{\sigma^2}{2n} - \frac{\Sigma^2}{2N}\right)^{\frac{1}{2}}$$

is a good approximation.

As expected, few districts show greater variability than the general population. Significantly greater variability occurs only in the character H among the Inverness

* Pearson, Biometrika, Vol. v. p. 183. The case considered in this note is the probable error of the difference between the mean of a subsample and the mean of a sample, but the same reasoning is applicable to the difference between the standard deviations of subsample and sample.

males, and the Aberdeen and Montrose females. On the other hand, significantly low variability is exhibited by the male inmates at Ayr for all the cranial characters and by the females in head height only. The male and female inmates at Dundee, Argyll, Lenzie and Govan also show selection in head height, agreeing with Paisley, Greenock and Gartloch males and Perth, Dumfries and Fife females

TABLE XII.

Relative local Differences of Variabilities.

$\it Males$		L	В	H	B/L	p_{α}	Рв	S
Aberdeen		-1:48	-2:38	-1.85	-1.60	-2.00	-2.11	- ·55
Dumfries		1.65	1.71	83	1.57	$\frac{-2.00}{1.70}$	-78	- '66
Dundee	* * *	67	- 28	-5.03	-24	20	-1.61	-1.56
Edinburgh	• • •	87	56	-3 03	58	83	- '37	$\frac{-1.30}{1.23}$
Montrose	* * *	20	- ·91	1.01	22	- 34	- 47	- 2.13
Argyll	• • •	.53	•47	-3.68	.01	- 77	58	20
	• • •	-3.46	-3.50	-3.08	-3.71	-3.10	-4.54	.12
Ayr Banff		- ·84	*43	- 36	03	- 08	- 17	.55
Elgin		-1.52	- 20	- 36	58	80	19	•48
Fife		- 32	-1.11	-2.30	76	- '69	- 2.83	-5.80
Gartloch		-1.23	-1:00	-6.38	-1.15	-1.18	-3.14	-70
Lenzie		- 14	1.00	-5.10	.77	.18	-1.88	1.77
Govan	• • • •	17	.74	-2.98	.25	.27	- 1.00	1.44
Haddington		63	.19	$\frac{-2.37}{2.27}$	09	20	89	.80
Inverness		-1.16	-2.34	4.18	-1.83	- 1.65	1.00	-2.39
Lanark		- 2.39	- '86	-2.24	-1.65	-1.49	-1.49	-2.27
Midlothian		-1.45	1.30	67	•46	.02	08	-2.15
Perth		- 01	25	2.46	- 11	13	1.17	- 34
Roxburgh		- 32	- 12	1.18	20	27	.43	-1.39
Stirling		+ .67	.67	1.52	-64	.61	1.19	-1.00
Greenock		36	1.36	-3.18	.93	.89	-61	1.18
Paisley		69	-1.87	-5.82	63	50	1.96	78
1 ansioy	• • •	00	101	002	00		100	
Females								
Aberdeen		2.15	.13	3.69	1.33	1.14	2.26	49
Dumfries	• • •	213	- 05	-6.10	- 02	-2.99	-1.96	-1.02
Dundee	* * *	.55	-34	-6.10 -4.40	- 53	-2 33	-1.33	$\begin{bmatrix} -1.02 \\ -1.02 \end{bmatrix}$
Edinburgh		-1.33	.79	- '48	.03	- '35	- 26	- 15
Montrose		- 29	2.10	2.98	1.36	1.05	2.01	- 31
Argyll		22	-1.87	-5.78	-1.48	88	-2.49	- '16
Ayr		10	1.75	-7.97	$-1.40 \\ -73$	-98	-1.84	.73
Banff	***	-1.66	-3.18	-1.11	-2.14	-2.33	-1.81	04
Elgin	• • •	- 12	- 3 16 - 26	63	'01	- 24	59	- 32
Fife		17	- 20	-2.99	31	.39	87	-2.84
Gartloch		- 25	-1.21	-2.47	74	90	-1.81	1.14
Lenzie		-2.04	-3.47	- 4·21	-2.90	2.86	-3.44	-1.32
Govan		-1.04	-1.88	-6.35	- 1.42	- 1.57	-3.16	+ .09
Haddington		- 24	-133	- ·53	.02	.03	.00	•47
Inverness		33	- 2·91	- 95	-1.60	1.43	59	69
Lanark		- ·45	- ·41	-1.78	58	- '42	- ·81	.54
Midlothian		1.10	.03	1.22	.62	.48	.89	42
Perth		14	.17	-4.48	.16	.18	-1.07	-1.30
Roxburgh		-1.62	25	1.34	53	66	-38	-1.19
Stirling		82	52	.75	- '71	70	.14	.64
Greenock	• • • •	-1.98	.18	- 2.52	53	- 88	- 1.94	86
Paisley	• • • •	46	37	-1.36	.00	.09	.27	- 84
2 201010		1.0		2 .50	0.7			
			<u>}</u>					

in having low variability in the distribution of that character. The male and female inmates at Fife are a selected group with respect to stature, their variability being significantly less than that of the general population. The variabilities of the diametral product (LBH) among the male inmates at Avr and Gartloch are significantly less than the general population, while the females at Lenzie and Govan are also significantly less. The variabilities for the remaining asylums approximate to the general mean with the exception of the females at Aberdeen and Montrose, which show for p_{θ} , as they do for H, significantly greater variabilities than the general population. The accompanying table (Table XII.) shows the values of the relative local differences in variabilities. Maps and diagrams have also been prepared to illustrate this variability, but their reproduction has been considered unnecessary, the only facts of note being as just The means and standard deviations of the differences, interlocally (shown in the table), measure (1) the fall in variability in passing from the general population to the individual groups for any one character, and (2) the amount of agreement, as to magnitude, among the differences themselves. It will be seen that H (\mathcal{J} and \mathcal{I}) has the greatest negative value among the means, and the greatest variability among the differences in passing from asylum to asylum.

So far as the question as to homogeneity or heterogeneity of district groups can be answered, it is answered in the following summary of differences probably significant.

TABLE XIII.

Variability Differences which are probably significant.

1			В	H		B/L		P_{eta}		S	
Greater	Less	Greater	Less	Greater	Less	Greater	Less	Greater	Less	Greater	Less
	Ayr		Ayr ♂ Inverness ♀ Banff ♀	Inverness & Aberdeen Q Montrose Q	Argyll Cond		Ayr of	Aberdeen Q Montrose Q	Ayr ♂ Gartloch ♂ Lenzie ♀ Govan ♀		Fife 3 and 9

(5) Differences between Male and Female Values of Coefficients of Variation.

In the Supplement to this memoir (pp. 5—96) the values of the coefficients of variation for the various characters are given alongside the values of the means and standard deviations. In determining the differences between the values for

males v_m and those for females v_f for each character at each of the asylums, the values of σ_v , the standard deviation of the coefficient of variation, were calculated from the usual formula

$$\sigma_v = \frac{v}{\sqrt{2n}} \left[1 + 2 \left(\frac{v}{100} \right)^2 \right]^{\frac{1}{2}}.$$

In the cases of B, B/L, and S,

$$\left\lceil 1 + 2 \left(\frac{v}{100} \right)^2 \right\rceil^{\frac{1}{2}}$$

was taken equal to 1.002, a sufficiently near approximation.

The following table (Table XIV.) shows the values of

$$(v_m - v_f)/(\sigma_{v_m}^2 + \sigma_{v_f}^2)^{\frac{1}{2}}$$

for L, B, H, B/L and S for all the asylums. In the foregoing formula, v_m = the coefficient of variation of any one character in any male group and v_f = the coefficient of variation for the corresponding character in the corresponding female group.

TABLE XIV.

Relative Differences of Coefficients of Variation.

Males and Females.

Values of
$$(v_m - v_f)/(\sigma^2_{v_m} + \sigma^2_{v_f})^{\frac{1}{2}}$$
.

Asylums	Head Length	Head Breadth	Head Height	Cephalic Index	Stature
Aberdeen	-1.84	68	-4.04	-1.55	- :34
Dumfries	1.50	1.95	2.51	1.56	.47
Dundee	.59	.19	87	.15	- '18
Edinburgh	.70	− ·25	.13	- 10	1.29
Montrose	.79	-1.46	-2.21	76	76
Argyll	.91	2.16	·91	1.32	.47
Ayr	-1.67	- 2.54	26	-2.43	07
Banff	.86	2.83	•43	1.75	.65
Elgin	- '71	•46	.97	18	.91
Fife	-42	- .51	-2.62	- '32	-1.16
Glasgow (Gartloch)	06	1.06	-1.72	·31	17
Do. (Lenzie)	2.09	4.00	26	2.84	2.56
Govan	1.07	2.59	2.28	1.66	1.13
Haddington	.04	·30	2.18	.06	•44
Inverness	.06	1.34	1.86	•37	- '51
Lanark	- 57	•71	- '61	- '14	-1.25
Midlothian	-1.34	1.48	-1:51	·16	92
Perth	•29	.31	4.46	.09	.97
Roxburgh	1.23	.36	21	.51	'13
Stirling	1.59	1.69	.24	1.37	76
Greenock	1.86	1.33	.07	1.34	1.46
Paisley	•48	- '40	-2.47	08	1.44
Totals	2.18	3.35	.96	1.71	1:39

Taking the series as a whole, we find the coefficients of variation in $B_{\mathcal{S}}$ differ materially from B?. On running through the values for the various asylums (see Table XIV.) this material difference is seen to be due to the inmates at Lenzie, where the sexual difference is very significant, and in a lesser degree to the inmates at Banff and Govan where the males also show greater relative variability, and at Ayr, where the females show the excess. In the other cases, the differences are not significant. The relative difference for L in the general population is perhaps hardly significant, but here again Lenzie stands out with a prominent difference. While the general coefficients for H are nearly equal, there are significant differences in the local values at Aberdeen and Perth and less significant ones at Fife, Paisley, Dumfries, Govan, Montrose and Haddington. Lenzie is again the disturbing factor in B/L and in S. The coefficients for B/L and S are approximately equal for most of the other asylums.

Thus, considering the differences between the sets of coefficients for both sexes at the individual asylums, we reach the conclusion that the variability among the males and females is very much alike, with the exception of the character B and a few local cases in the other characters. The conclusion is confirmed and amplified by considering the whole population where the males again appear more variable in B, the difference being probably significant, but in the other characters the variability among the males, although greater than among the females, is only slightly greater, and cannot be said to be at all significant.

(6) Pigmentation.

I. Distribution of Hair and Eye Colour. As already stated, the colours of the hair and eyes of most of the inmates were noted at the same time that the measurements were taken. A complete record of the observations is given in the Supplement to this memoir side by side with the record of observations on measurable characters.

In order to make a comparison between the pigmentation of the inmates at each asylum and the pigmentation of the "general insane" population, the values of χ^2 and $\log P^*$ were calculated for each asylum. In other words the actual frequencies for each colour were contrasted with their most probable values—the theoretical numbers which would occur on an even distribution of the "general insane" population. The approximate values of $\log P$ are given in Table XV. and XVI. and show that with the exception of a few cases, the local pigmentation diverges in character from the general distribution considerably. It is of interest to note that the divergence in colour of any locality from the remaining population may be measured by determining the mean square contingency coefficient

$$C_1 = \sqrt{\frac{\chi'^2/N}{1 + \chi'^2/N}},$$

where χ'^2 = the total square contingency[†]. Thus, to take a particular case, the distribution of hair colour in males at Aberdeen may be contrasted with the remaining population as in Table XVII. We find $C_1 = 1347$.

^{*} Elderton: Biometrika, Vol. 1. p. 155, χ^2 of Goodness of Fit.

[†] Pearson; Drapers' Company Research Memoirs, Biometric Series, 1. p. 16.

Anthropometry of Scottish Insane

TABLE XV. Divergency in Hair Colour.

Asylums		Ма	les	Fem	ales
v		$\operatorname{Log} P$	Q	Log P	Q
Aberdeen		<u>16.8</u>	.135	28⋅3	.186
Dumfries		$\overline{6}$ ·9	.080	<u>6</u> .8	.085
Dundee		5.7	.074	<u>4</u> ·9	.067
Edinburgh		1.1	.038	3.0	.066
${f Montrose}$		51.3	.238	<u>-6</u> ·5	.087
Argyll		$\overline{16} \cdot 1$	·137	$\overline{10}.2$	115
Ayr		$\overline{6}$.7	.083	12.0	125
Banff		6.2	.085	_2.9	.043
Elgin		$\overline{10}$ $^{\circ}4$.107	13.6	·127
Fife		$\overline{9}.9$.100	7.5	.094
Gartloch		$\bar{8}$ ·4	.098	$\overline{6}$ ·2	.089
Lenzie		$\overline{3} \cdot 2$.062	$\overline{\underline{1}} \cdot 1$.041
Govan		9.6	.102	2.0	.055
Haddington		1.8	021	1.6	.029
Inverness		$\overline{26}$ ·7	.171	$\overline{19}.7$	153
Lanark		1.4	.033	$\bar{1}.\bar{0}$.041
Midlothian	• • •	<u>2</u> ·9	.040	$\frac{\overline{4}\cdot 7}{\overline{3}}$.069
Perth		1 <u>3</u> ·5	.122	$\frac{\overline{2} \cdot 9}{\overline{1} \cdot 8}$.043
Roxburgh		<u>Ī</u> '7	.025		.023
Stirling		10.3	.110	7:1	.097
Greenock		$\overline{3} \cdot 2$.062	2.0	.056
Paisley		$\overline{4} \cdot 9$.063	3.1	.066

TABLE XVI. Divergency in Eye Colour.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Asylums		Ma	les	Fem	ales
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	nayidina		$\operatorname{Log} P$	Q	$\operatorname{Log} P$	Q
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Aberdeen		9.1	·101	ĪĪ:5	.117
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Dumfries			.064	4.6	.066
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Dundee		$\overline{5} \cdot 9$.068	2.6	.043
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.061	4.9	*064
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.075		.108
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Argyll					.003
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Ayr					.080
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						104
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						132
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			2.0			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					2.3	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		• • •				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		• • • •				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$						
$\begin{array}{cccccccccccccccccccccccccccccccccccc$						
Greenock $\overline{1}$ ·4 ·026 $\overline{1}$ ·9 ·011		• • •				
		• • •				
Paisley $\overline{1}$ ·6 ·021 $\overline{1}$ ·6 ·023	Greenock Paisley	• • •	$\frac{1.4}{1.6}$		$\frac{1.8}{1.6}$	011

TABLE XVII.

Males	Red	Fair	Medium	Dark	Totals
Aberdeen Remaining Population	8 58	16 259	78 2444	132 1240	234 4001
Totals	66	275	2522	1372	4235

In a private communication* Professor Pearson gives the following equivalent formula in terms of χ^2 , and thus obviates the necessity of determining each χ'^2 . If N = number in the general population and n = number in any locality;

$$C_1 = Q = \sqrt{\frac{\chi^2}{N - n + \chi^2}},$$

the measure of the divergence of the local group from the remaining population. Thus $\chi^2 = \chi'^2 (1 - n/N)$, and Q, the divergency coefficient, is determined directly from χ^2 . The values of Q are given alongside those of $\log P$ in Tables XV. and XVI. Both sets of values are approximations, sufficiently correct to enable their significance to be seen on inspection. Their relationship is shown in Diagram XI. All values of $\log P > \overline{3}$ (and thus, in this series, of Q > 0.55) are probably significant. A reference to the tables and to the colour divergency maps (where the values of Q and Q and Q have been classed) will show that the south east of Scotland is like the general population in hair colour (Q and Q) and eye colour (Q). Argyll, Ayr, Stirling and Fife, all contiguous, are least divergent among the males in eye colour. Generally speaking, the populous centres and environs are very like the general population, while in the sparsely populated parts the divergencies are the greatest.

Coming now to the cause of the divergencies (the excess frequencies of one or other of the various categories), the significance or non-significance of the various frequencies was determined in the following manner. Let y_s = total number of inmates in Scotland possessing any particular hair or eye colour; N = total number of inmates; m = number of inmates at any asylum, then m/N $y_s = y_s'$, the expected frequency. Let y_s'' = the corresponding observed frequency; $y_s/N = p$; 1 - p = q; then $(y_s'' - y_s')/\sqrt{mpq}(N-m)/(N-1)$ = the difference between the observed and the expected frequency relative to the standard deviation of y_s'' in the sample, m, of the population. The values of this rate for each category have been determined.

It has been recently shown by Pearson† that, in a population of N individuals, Np of which possess a given character, and Nq do not, the distribution of frequency in the character for random samples of magnitude m (when m is commensurable

^{*} Since published. Biometrika, Vol. v. pp. 198-203.

[†] Biometrika, Vol. v. pp. 172-175.

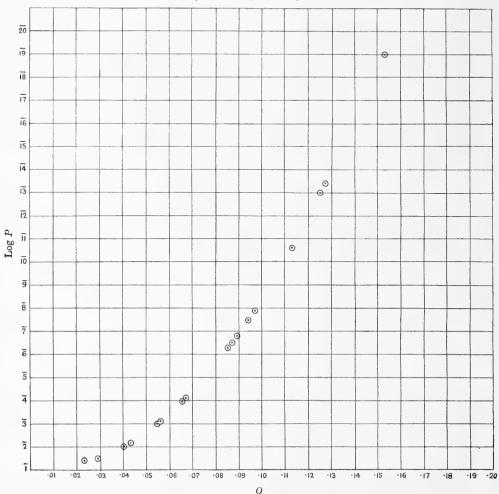


DIAGRAM XI. Relationship between Q and Log P.—Hair Colour, Females.

with N) is not a symmetrical one, but can be accurately described by a skew curve of either Type I. or Type IV. Thus, he points out that the tables of the probability integral cannot accurately give the areas on either side of the ordinate which divides the curve at the abscissal value $(y_s'' - y_s')/\sqrt{mpq} (N-m)/(N-1)$, and the probability of greater or lesser values occurring in future samples must be determined by other means. Since however the values of (m-1)/(N-1) in the present series are small (although not quite negligible), an approximate estimate of the significance of each difference can be obtained by determining the values of the ratio $(y_s' - y_s')/\sqrt{mpq}$, the distribution of these relative differences being assumed to follow the normal curve. The relative differences themselves are thus, on this basis, the abscissal values of the normal curve $y = 1/\sqrt{2\pi} \cdot e^{-\frac{1}{2}x^2}$. The ratios $(y_s' - y_s')/\sqrt{mpq} (N-m)/(N-1)$ and $(y_s' - y_s')/\sqrt{mpq}$ have both been

calculated for the present series of observations on hair and eye colours, the values of the latter ratio being given in Tables XVIII. and XIX. The values of the factor $\beta = 1/\sqrt{1-(m-1)/(N-1)}$ are also given in the tables, and these, if multiplied by the values of the relative local differences in the tables provide the corresponding values of $(y_s'-y_s')/\sqrt{mpq(N-m)/(N-1)}$ for comparative purposes.

Applying the foregoing test to all the hair and eye categories, it is found that Scotland north of the Forth is quite significantly darker than the south. Excepting Dundee, Fife and Argyll, which have a significant excess of medium hair, the country north of the Forth is significantly dark haired. The whole of the south-west is significantly brown haired, while a significant excess of fair occurs in the Stirling group (\mathcal{C}) and in Stirling, Perth and Montrose groups (\mathcal{C}). North of the Grampians there is a significant excess of red hair among the females and possibly also among the males, although Aberdeen is the only group which shows definite significance. Turning now to eye colour we see that north of the Grampians there is a significant excess of medium eyes, south of

TABLE XVIII.

Relative Local Differences in Hair and Eye Colours.

				Males				Values of
Asylums		H	air			Eyes		$\beta = 1 / \sqrt{1 - \left(\frac{m-1}{N-1}\right)}$
	Red	Fair	Medium	Dark	Light	Medium	Dark	
Aberdeen Dumfries Dundee Edinburgh Montrose Argyll Ayr Banff Elgin Fite Gartloch Lenzie Govan Haddington Inverness Lanark Midlothian Perth Roxburgh Stirling Greenock Paisley	2:39 -1:40 - :82 -74 -59 - :59 - :90 - :11 -:22 -1:34 -1:77 - :78 - :07 - :11 -:38 -:67 -:87 - :11 -:55 -:65 -:48	- 22 - 1 · 27 - · 31 1 · 89 14 · 58 - 3 · 63 - 1 · 63 - 2 · 16 - 1 · 54 - 1 · 34 - · 51 - 2 · 97 - 3 · 29 - 69 - 1 · 63 - 1 · 86 2 · 24 3 · 73 · 36 2 · 59 - 2 · 86 - 2 · 54	$\begin{array}{c} -6.51 \\ 5.13 \\ 4.60 \\ -1.94 \\ -9.52 \\ 8.70 \\ 6.34 \\ -3.71 \\ -5.83 \\ 6.31 \\ 5.97 \\ 3.29 \\ 6.28 \\ .87 \\ -9.67 \\ -1.80 \\ -7.70 \\ 1.36 \\ -6.90 \\ 3.51 \\ 3.72 \end{array}$	7·85 - 4·34 - 4·45 - 8·06 - 8·06 - 4·41 - 5·30 - 6·36 - 5·57 - 5·55 - 1·69 - 4·84 - ·27 10·91 1·12 - ·54 - 5·89 - 1·58 - 1·58 - 2·01 - 2·69	$\begin{array}{c} -5.41 \\ 4.01 \\ 3.85 \\ 1.89 \\ -4.37 \\ 38 \\ 2.01 \\ -6.94 \\ -6.58 \\ 3.04 \\ 1.68 \\49 \\ 2.79 \\ 4.25 \\ -9.74 \\ 4.16 \\ 4.27 \\ -5.94 \\ 5.15 \\ -1.99 \\ 1.61 \\ 1.24 \end{array}$	6·09 - 1·78 - ·86 - 3·81 1·27 - ·77 - ·14 8·63 7·67 - 1·53 - 3·01 - 3·77 - 2·68 - 2·89 12·42 - 3·76 - 2·85 1·40 - 3·09 - 14 - 1·08 - ·52	$\begin{array}{c}39 \\ - 2.79 \\ - 3.63 \\ 2.03 \\ 3.78 \\ - 1.33 \\ - 2.24 \\ - 1.18 \\52 \\ - 1.94 \\ 1.37 \\ 4.93 \\36 \\ - 2.11 \\ - 2.13 \\78 \\ - 2.04 \\ 5.68 \\ - 2.85 \\ 2.24 \\77 \\96 \end{array}$	1·029 1·014 1·017 1·022 1·031 1·023 1·029 1·008 1·007 1·026 1·037 1·047 1·033 1·008 1·026 1·049 1·016 1·021 1·017 1·038 1·011
(s-1)	03	2.75	4.57	3.98	3:35	3:38	1.51	

the Forth significant excess of light eyes, while Lenzie and the regions of Perth, Montrose, Edinburgh and Stirling are significantly dark eyed. Summarising the results of colour observations generally, it is found that, compared with the "general insane" population, the north of Scotland has excess of medium eyes, dark and red hair, the south-east is light eyed, the south-west brown haired and light eyed, while the midlands are mixed in character, having not only an excess of fair medium and dark hair but also of light and dark eyes. Considered interlocally, the non-measurable characters red hair δ , fair hair $\mathfrak P$ and dark eyes $\mathfrak P$ do not show significant departures from homogeneity [see values of (s-1), Tables XVIII. and XIX.]. The other colour characters show great heterogeneity interlocally. Thus the same conclusion is reached for non-measurable characters as was reached for measurable characters, namely: Individual asylum groups cannot be said to form part of a "general insane" population of a homogeneous character.

For a detailed examination of the pigmentation of the inmates the reader is referred to Tables XVIII. and XIX. and to the pigmentation maps, Maps XIII. to

TABLE XIX.

Relative Local Differences in Hair and Eye Colours.

			Values of					
Asylums		Н	air			Eyes		$\beta = 1 / \sqrt{1 - \left(\frac{m-1}{N-1}\right)^{n}}$
	Red	Fair	Medium	Dark	Light	Medium	Dark	
Aberdeen	7:48	.72	-9.84	7:41	-6.72	5.33	1.68	1.030
Dumfries	-1.34	.92	4.85	-4.82	3.91	-2.60	-1.52	1.020
Dundee	-2.21	.53	3.58	-3.13	2.39	72	-1:86	1.028
Edinburgh	- '42	.03	-3.79	3.97	3.17	-3.51	.29	1.029
Montrose	2.22	02	-5.07	4.46	-5.39	6.09	61	1.014
Argyll	-2.19	28	6.71	-6.03	06	18	- 13	1.027
Ayr	-2.04	-1.18	7.64	-6.72	6.04	-2.70	-2:32	1.035
Banff	.76	36	-2.45	2.37	-5.01	6.02	96	1.007
Elgin	5.77	.73	-6.13	4.18	-5.90	7.88	-1.98	1.009
Fife	-1.82	84	5.66	-4.89	3.20	2.95	35	1.029
Gartloch	-1.47	1.11	5.02	-5.02	3.11	-2.27	99	1.022
Lenzie	-1.86	-1.48	.92	·16	40	-1.99	2.59	1.040
Govan	-1.18	-1.04	3.27	-2.60	3.84	-3.37	.47	1.026
Haddington	.17	-1.48	1.15	71	.04	39	.38	1.010
Inverness	5.05	.71	5.71	6.96	-6.99	7.81	69	1.026
Lanark	-1.93	-1.37	05	1.11	3.79	-3.40	52	1.019
Midlothian	- '23	-1.05	-3.69	4.18	1.32	 55	- '86	1.020
Perth	.27	1.10	-2.52	2.09	-4.70	2.64	2.35	1.015
Roxburgh	- '71	.99	- 29	.85	2.81	-2.71	18	1.019
Stirling	1.29	3.00	-5.54	4.20	-5.08	1.59	3.90	1.035
Greenock	-1.57	.07	3.18	-2.76	.01	- '55	.58	1.014
Paisley	- '82	2.08	2.96	-3.46	1.10	.04	-1.26	1.013
(s-1)	1.66	.17	3.73	3.23	3.03	2.75	.53	

XVIII. the relative values being given in all cases in the tables*. The percentages are given in Tables XXIII, and XXIV, of Supplement.

II. Correlation of Hair and Eye Colour. Applying the contingency method to the data (see Table VIII. of Supplement) the following results were obtained. The author's results from the Aberdeenshire population and those of Pearson from Continental and British returns are also given, for the sake of comparison.

TABLE XX.

Correlation.—Hair and Eyes.

Population	Contingency Coefficient	Returns by
Male Asylum Inmates	.3039	J. F. Tocher
Female Asylum Inmates	2994	27
Adult Scottish Population	3673	"
Scottish Children †	·3802 ·2495	G. Retzius
Swedish Conscripts ‡ Prussian Children ‡	2495	R. Virchow
Italian Conseninted	3091	R. Livi
Jewish Children †	3381	R. Virchow
Baden Conscripts‡	3540	O. Ammon
British Schoolboys‡	•4203	K. Pearson

From this we see that there is no material difference between sane and insane populations in their degrees of correlation between hair and eye colours, although the result for the Scottish sane population is higher. The degree of correlation in the case of the Scottish children is slightly higher than that of the adult Scottish sane population. The continental results given above are not directly comparable, since while the children's data are available, those of the corresponding adult populations are wanting, and besides there are racial differences to consider. It would seem, however, from the foregoing that the correlation between hair and eye colours decreases in passing from a juvenile to an adult population. This is obviously due to a change of hair and eye colours in passing The correlation between age and the colour of hair from childhood to manhood. and eyes in man has been dealt with by Pearson & who shows from Uchida's results on Prussian and British data that, with a range of 13 years (7-19), the correlation between age and hair colour amounts to 158, and between age and eye colour '096. From Pfitzner's hospital results the value '451 was obtained for hair colour and age, but it is pointed out that, owing to the positive correlation between fairness and disease in childhood, this value is too high; probably 2 to 25 would

^{*} The foregoing is a short summary of the colour characteristics of the inmates. They will be dealt with in more detail in another paper when the results will be compared with the results of the Pigmentation Survey of Scottish School Children just carried out by the writer.

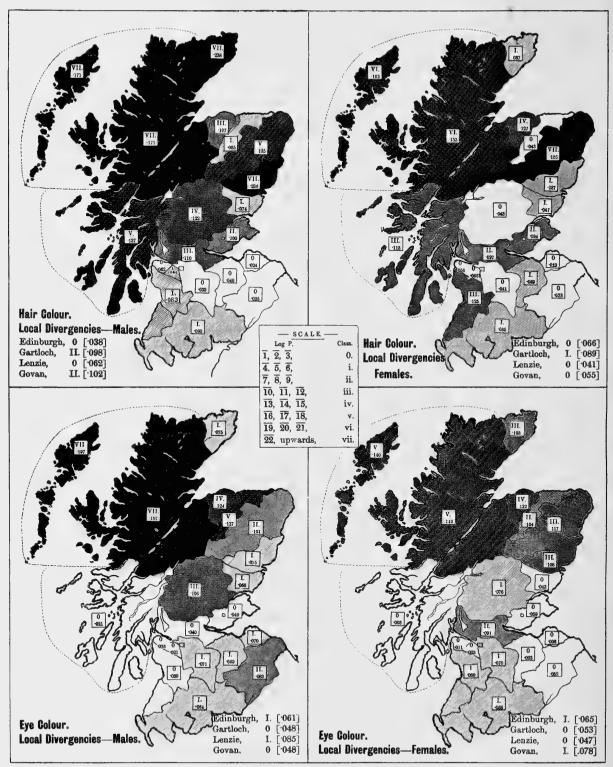
⁺ Not yet published.

[‡] Pearson: Biometrika, Vol. III. p. 461.

[§] Biometrika, Vol. III. pp. 462-466.

MAP XIII.

MAP XIV.



MAP XV.

MAP XVI.

be about the correct value. No British adult data are at present available to determine the constants involved. The change, however, in passing from juveniles (under 19) to adults can be approximately measured from the Aberdeenshire data. With the figures given in the following table, r=24, when we use Pearson's fourfold table method for characters not quantitatively measurable*.

TABLE	XXI.	Correlation	of	Age	and	Hair	Colour.
-------	------	-------------	----	-----	-----	------	---------

	Red	Fair	Medium	Dark	Totals	
Adults Children	 8 28·1	71 100·2	133 188·5	189 84·2	401 401	
Totals	 36.1	171.2	321.5	273.2	802	

III. Distribution of Colour among the Sane and the Insane. Since the Aberdeen data represent a local group, the colour observations on adults there cannot be contrasted with the colour data of the "general insane" population, as local groups may or may not be good samples of the general population. It has been shown for all characters that they are more likely not to be good The rate of change of hair and eye colour with age, however, is not so likely to vary in passing from one district to another. On the assumption that the rate of change is fairly uniform throughout Scotland, an approximate estimate can be made as to the probable distribution of hair and eye colours among the adult sane population from the Aberdeenshire data and the results of the observations from the Pigmentation Survey of School Children in Scotland about to be published. Let $p_1, p_2, \dots p_n = \text{percentage of either hair or eye colour}$ among school children in any district; $q_1, q_2, \dots q_n = \text{similar percentages among}$ the adults in the same district; $p'_1, p'_2, \dots p'_n = \text{similar percentages among the}$ children in the entire school population; $R = (1 + \epsilon/(100 - \epsilon))$; $\epsilon = a$ constant whose value depends on the nature of the distribution and n = number of categories then

$$\frac{p'_1q_1R}{p_1} + \frac{p'_2q_2R}{p_2} + \frac{p'_3q_3R}{p_3} \dots + \frac{p'_nq_nR}{p_n} = 100,$$

and gives the corresponding probable percentages of either hair or eye colour in the general adult sane population of the country. Applying this equation to the Scottish normal data, we obtain the following values, the corresponding values for the "general insane" population being given for comparison.

To judge from this result—a tentative one—there is an excess of light-eyed, brown and dark-haired persons in Scottish asylums and a corresponding defect in the other categories. The colour distributions of the "general insane" population cannot therefore be held to be fair samples of the general population of Scotland.

^{*} It is assumed that selection by hair-colour does not occur; the children are the distributions of 401 individuals on the base of the Pigmentation Survey, for Aberdeenshire; the division is taken between 'fair' and 'medium.'

TABLE	XXII.	Pigmentation	of	Sane	and	In sane.
-------	-------	--------------	----	------	-----	----------

	Hair per cent.				Eyes per cent.		
	Red	Fair	Medium	Dark	Light	Medium	Dark
Probable distribution of adult Sane Population General Insane Population	4·2 1·6	11·5 6·5	55·9 59·5	28·4 32·4	27·8 45·0	45·9 32·6	26·3 22·4
Difference	2.6	5.0	-3.6	-4.0	-17.2	13:3	3.9

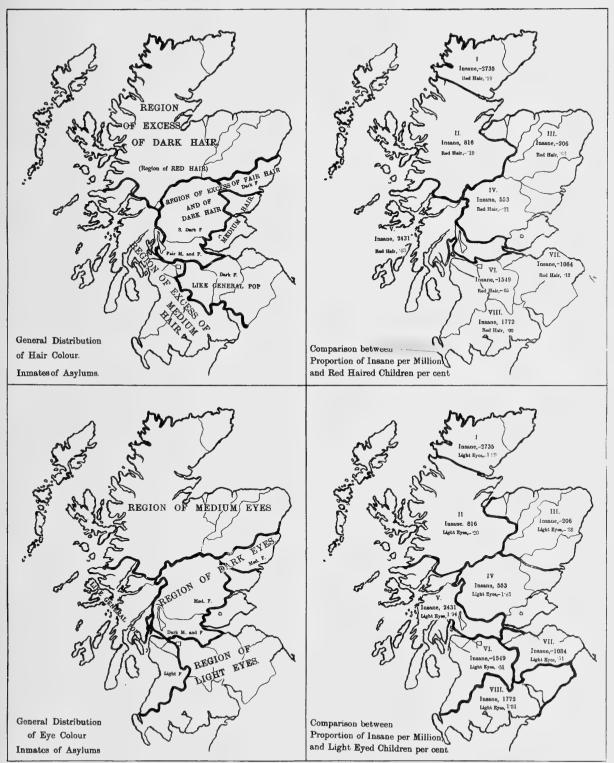
IV. Relationship between Colour and Insanity. This problem can be viewed from another standpoint, without dealing either with the observed colour distributions among the insane or the estimated values among the sane, just discussed. The various proportions of the insane among the whole population in each of the various districts in Scotland can be compared with the corresponding proportions of children possessing any particular hair or eye colour within the same areas. In the Report on the Scottish Census of 1901*, the proportion of lunatics per million of the population in each county and in the eight chief divisions of Scotland are given. From the results of the Pigmentation Survey of Scottish School Children recently carried out by the writer, the proportional colour distributions within the same areas can be found. Taking light-eyed children as an example the following table (XXIII.) was formed, x_1 being the deviation from the mean percentage of light-eyed children, and x_2 the corresponding deviation from the mean proportion of insane in the eight divisions under consideration.

TABLE XXIII.

Division	x_1	x_2
I III IIV V VI VII VIII	-1.99 20 38 -1.31 +1.94 +.15 +.51 +1.31	$\begin{array}{c} -2735 \\ +816 \\ -206 \\ +553 \\ +2431 \\ -1549 \\ -1084 \\ +1772 \end{array}$

The following values of r and of the ratio of r to its probable error E_r were obtained by comparing the percentages of the various colours successively with the proportion of insane in the eight divisions of Scotland. (Table XXIV.)

^{*} Eleventh Decennial Census of the Population of Scotland, 1901, with Report, Vol. 1. Table XVII, page xxix.



MAP XVIII.

MAP XX.

Colour	?'	$\frac{r}{E_r}$
Red Hair	5824	3.70
Fair Hair	0244	·10
Medium Hair	- 1283	•55
Dark Hair	•3396	1.61
Jet Black Hair	.0836	.35
Light Eyes	·6952	5.64
Blue Eyes	— ·0719	.30
Medium Eyes	- ⋅3222	1.51

- .4815

2.63

Dark Eves

TABLE XXIV. Correlation.—Hair and Eye Colours with Lunacy.

The results in the above table appear to be important, and confirm the deductions made from the pigmentation of the inmates. They show that on an average more persons became insane in parts of the country where there is an excess of light-eyed persons in the population, and in a much less degree where there is an excess of dark-haired persons. Lunacy is distinctly correlated positively to light eyes and in a much less degree to dark hair; and is distinctly correlated negatively to red hair and in a lesser degree to dark eyes. Thus there is a greater tendency to insanity among light-eyed and dark-haired persons, and a lesser tendency to insanity among red-haired and dark-eyed persons, compared in both cases with the general population. These are merely statistical facts, and no explanation is offered as to how or why presence or absence of pigment comes to be associated, as it is here found to be, with insanity.

(7) Comparison with other Data.

I. General. As has already been stated, no general Scottish data exist which can be directly compared with the Scottish "general insane" population, since a general survey of Scotland has not yet been carried out. Such British returns as are available can, however, be contrasted with the data under discussion. The following table shows the values of the means of L, B, and $100 \ B/L$.

TABLE	XXV	Comparative	Table	of L.	R.	and	100	B/L.
111111111111111111111111111111111111111	ZXZX 1 .	Compan week	1 0000	01 11.	w,	COLOUR	100	JU 1110 0

Population	Measure- ment on	L (mm)	B (mm)	$100rac{B}{L}$	Reference
General Hospital English Criminals Cambridge Graduates Scottish Lunatic Pop Scottish Habitual Crim. British Association Naqada Crania Long Barrow Skulls English Crania Scottish Crania	Head "" "" "" Cranium "" ""	190·4 191·7 193·5 195·5 196·3 198·1 185·1 190·6 189·1 186·8	149·3 150·4 154·0 151·5 153·1 155·5 134·9 142·5 140·7 144·3	78·5 77·2 79·6 77·6 78·0 78·2 73·0 74·9 74·3 77·3	Biometrika, Vol. IV. p. 126, Blakeman Biometrika, Vol. I. p. 204, Macdonell Biometrika, Vol. I. p. 351, Pearson This Memoir This Memoir Phil. Trans. Vol. 196 A. Lee and Pearson Biometrika, Vol. IV. p. 354, Fawcett Biometrika, Vol. IV. p. 354, Schuster Biometrika, Vol. III. p. 208, Macdonell R. S. E. Vol. 40, Part III. Sir W. Turner

II. Scottish Criminals. The writer is indebted to Dr J. F. Sutherland, Assistant Scottish Lunacy Commissioner, for kindly supplying the measurements on 375 Scottish habitual criminals. The analysis of these observations has provided interesting results. The criminals were divided into four classes; those convicted of (I) robbery and assault, (II) theft, (III) murder and assault, and (IV) offences against chastity. The following table gives the results of the analysis, stature, head-length, and head-breadth being considered.

TABLE XXVI.

Habitual Criminals in Scotland.

Mear	n ·	Standard Deviation
Stature:		2.27
Class No. I.	64·6± ·11	$2.37 \pm .08$ inches
" " II.	$65.0 \pm .18$ 65.3 + .20	2·68 ±·13 ,, 2·28 +·14 ,,
,, ,, III. ,, ,, IV.	65.2 + .42	0.56 1.20
Totals	64·8 ± ·09	$2.47 \pm .06$ "
Head Length:		
Class No. I.		$6.37 \pm .21 \text{ mm}$.
,, ,, II.	197·2 ± ·42	$6.06 \pm .29$,,
" " III.	198·4 ± ·63	$7.06 \pm .45$,,
" ,, IV.		4.02 ± .47 ,,
Totals	196·3 ± ·23	6·44 ± ·16 ,,
Head Breadth:		
Class No. I.	152·9 ± ·22	$4.70 \pm .16 \text{ mm}$.
" " II.		4·24 ± ·20 ,,
" " <u>III</u> .		4·83 ± ·31 ,,
" " IV.		$6.50 \pm .71$,,
Totals	$153.5 \pm .16$	$4.57 \pm .11$,,

Considering briefly in the first place the various classes of cruminals themselves, it is seen that those habitual criminals who have been convicted of murder and assault, and in a lesser degree those convicted of theft, differ considerably in head-length from those convicted of robbery and assault and other crimes. They have on an average longer heads. The difference in head-length between Classes I and III is 4.43 times its probable error, and Class III differs in its mean head-length from the remaining population by about 3.8 times the probable error of the difference. The distinctive feature here is that those convicted of murder and assault have significantly longer heads than the other criminal population. The difference in head-breadth between Classes I and II, and in stature between Classes I and III are possibly significant, but in all other cases the differences in the various characters among the criminals are insignificant—they are fair random samples of the short series of the general criminal population of Scotland. A longer series of measurements might of course reveal significant differences which appear in this series to be insignificant.

On comparing now the Scottish "general insane" population with the Scottish habitual criminals, we find that they differ considerably in type. An inspection of the differences (relative to their probable errors) will show this at a glance.

TABLE XXVII.

Between	Relative Difference	
Mean Head Lengths	3:40	
" Head Breadths	9.48	
" Statures	11.24	

That is, the Scottish criminal's head is on an average longer and broader than that of the inmate of a Scottish asylum, but he is somewhat shorter in stature; or, conversely, the insane person is smaller headed but taller in stature than the criminal. This result may or may not be independent of the racial nature of either population. It is to be noted, however, that 35 per cent. of the criminals in Scottish asylums are of Irish origin. A very much smaller proportion of the "general insane" population are of Irish extraction.

III. Scottish Crania. Sir William Turner, in his valuable memoir on the "Craniology of the People of Scotland," finds the mean length and mean breadth of the crania examined by him to be respectively 186.8 mm, and 144.3 mm. Making an allowance of 8 mm, for scalp depth for each character and comparing these values with those of the "general insane" population, we see that the differences are quite insignificant. From measurements kindly made for the writer by Dr Theodore Shennon, Pathologist at the Edinburgh Royal Infirmary, the average depth of the scalp is found to be less than that given above. Altogether 110 subjects were measured, in the temporal region at both sides, and at the glabella and occipital point. Measurements on subjects still continue to be made, but until a much larger number have been measured it seems desirable to adhere to the figure usually given. In any case, the above result is a purely tentative one, and no stress is laid on it. Besides, as Sir William Turner points out, the crania are not quite representative of the whole of Scotland, and the series is a short one.

IV. Local. One only of the asylum groups can be compared with the normal population of practically the same area—that of Aberdeen. The writer's values for head length, head breadth, and stature of the Aberdeenshire population are 193.93 mm., 153.40 mm. and 67.7 inches respectively. The difference in head length is insignificant, but the sane population of Aberdeenshire is significantly broader headed and taller than the corresponding asylum population. Roxburgh Volunteers have been found by J. F. Macpherson* to have an average stature of 67.89 inches, and this is significantly greater than the corresponding asylum population. It must be remembered, however, that the Volunteers are a selected

^{*} Stature of Roxburgh and Selkirk Volunteers: J. F. Macpherson.

population, so that the only normal local observations directly comparable with the local insane are those of Aberdeen.

V. Stature. Finally, stature generally falls to be briefly noticed. The following table shows the mean stature of the various Scottish populations measured by the writer, alongside those of other Anglo-Saxon populations whose values have been ascertained.

It will be observed that the first five classes in the table below are drawn from the normal or healthy populations, while the last five are either hospital patients, insane or criminals. So far as the Scottish populations are concerned it has been already pointed out that the sane are significantly taller than either criminals or

TABLE XXVIII.

Stature—Males,—Anglo-Saxon or British Populations.

Class	Stature (inches)	Reference
Cambridge Students	68.86	Biometrika, Vol. 1. p. 191, Macdonell
English Šons	68.86	Family data, Pearson
Roxburgh and Selkirk Volunteers	67.89	This Memoir
English Fathers	67.74	Family data, Pearson
Aberdeenshire Rural	67.72	This Memoir
General Hospital	67.16	Biometrika, Vol. IV. p. 126, Blakema
Criminals, New South Wales	66.88	Biometrika, Vol. I. p. 44, Powys
Scottish Insane	65.86	This Memoir
English Criminals	65:54	Biometrika, Vol. 1. p. 191, Macdonell
Scottish Criminals	64.84	This Memoir

the insane. It would thus appear that neither the criminals nor the insane are fair samples of the general population with respect to stature, these two classes being drawn more from the shorter section of the community.

(8) General Conclusions.

I. The fundamental problem (namely, does the insane population differ from the sane population?) cannot be answered from the data of this survey, at least with respect to measurable characters, since no corresponding complete survey of the sane population has been carried out. The mean stature of the Scottish insane, however, is significantly less than that of the sane population of any of the districts measured. With respect to the non-measurable characters, hair colour and eye colour, the colour data of the Scottish children being available, it has been found by direct and indirect comparison that the insane population does materially differ from the sane. On an average, the "general insane" population of Scotland is lighter-eyed and darker-haired than the sane population. There is a greater tendency to insanity among the light-eyed and dark-haired population than among any other colour class. Red-haired persons and dark-eyed persons seem less liable

to insanity. With regard to the remaining colour characters there is no material difference between the sane and the insane.

- II. In the one local district where the adult sane and insane populations can be compared—that of Aberdeen—it is found to agree, with respect to pigmentation, with the general conclusion just stated. With regard to measurable characters, the local sane population is broader headed and taller than the local insane.
- III. In the entire insane population there is a group whose characters are affected by special causes not characteristic of insanity in general. This group has on that account been excluded from the general analysis. The group is quite different in type from the "general insane" population, is both macrocephalic and microcephalic in character, and thus shows excessive variability.
- IV. (a) The distributions of the various characters in the general insane population are distinctly skew, with the possible exception of head length, which may be fairly described by the normal curve. Further, the distributions are leptokurtic and negatively asymmetric. For long series of the same characters, just as great divergences from normality occur among sane populations as are here found in the long general insane series. Asymmetry in distribution therefore is not a special feature among the insane. A difference in form, however, may exist between sane and insane populations. If it existed, it would be detected by a general survey of the sane population. In any case, heterogeneity would account for much of the asymmetry, and heterogeneity (see V. and VI.) has been found to exist among the insane.
- (b) There is a probably significant departure from linearity of regression among the males in the pairs of characters L & B, B & H, and L & S. Otherwise the regression is linear. The values of the correlation coefficients are somewhat higher in the entire insane population. In the general insane population the values approximate to those already found for the same pairs of characters among the sane population.
- V. Assuming the insane population in the various districts of Scotland to be, with respect to measurable characters, an anthropometric sample of each district, we find that local populations differ from each other sensibly in many respects.
- (a) The south-west of Scotland (exclusive of Glasgow) is long-headed or macrocranial, the north-east is short-headed or brachycranial. The north of Scotland is broad-headed or platycranial. Glasgow, Edinburgh, and the populous centres round them are stenocranial or narrow-headed. Again, the north of Scotland is distinctly brachycephalic, while the south-west is distinctly dolichocephalic. In the large towns (excepting Edinburgh, which approximates to the mean) the population is microcephalic or small-headed. The Scottish Midlands, excluding towns, are macrocephalic or large-headed. The rest of the country approximates to the average size—the population is mesocephalic. In head height, there are two sharply divided groups—a hypsicranial or a high-headed group in

the Midlands, and a chamaecranial or a low-headed one. The border counties are tall statured or megalomegithic. In the towns generally the population is significantly shorter—is micromegithic.

- (b) The interlocal constants evaluated show that the population is not a homogeneous one, no matter what character be considered. Intralocally, it is seen that in some groups the means of most characters exceed their respective general means, and are therefore megalomeric in character; in others the means of most of the characters are significantly less than the corresponding general means and are therefore micromeric. In others the groups exceed the means in some and are in defect in others, and therefore possess a mixed specification—they are micromeric groups.
- VI. Few districts show greater variability than the general population. Inverness males and Aberdeen and Montrose females show greater variability in head height. Male inmates at Ayr show significantly low variability for all cranial characters. Fife males and females are a selected group with respect to stature.
- VII. There is no significant difference between the two sexes in variability. The males, perhaps, appear more variable in head breadth, but otherwise males and females are very much alike in variability.
- VIII. While it has been shown to be exceedingly probable that the general colour distributions of the insane differ significantly in some respects from those of the adult sane population (see I.), the colour distribution of the insane throughout Scotland is by no means uniform. Generally speaking the north of Scotland is a region of excess of dark and red hair and medium eyes; the south-west of medium hair; and the south, of light eyes. The country lying directly between the Firth of Forth and Firth of Clyde has an excess of fair hair as well as of dark eyes; and the Montrose group (which includes Caithness and Shetland as well as Kincardine and North Forfar) has also an excess of fair hair in the male population.
- IX. Comparing the measurable characters of the Scottish insane population with the other available general Scottish data we find that (a) the insane are, on an average, probably shorter than the sane; (b) there is a distinct difference in type between the class or race material from which the insane and the criminals are drawn, the criminals being larger-headed and shorter men on an average than the insane. If the criminals and the insane belonged to the same race, or contained proportionally the same racial elements, it would be clear that the criminals were drawn from a physically different section of the community. About 35 per cent, of the habitual criminals in Scotland, however, are of Irish extraction, and the problem, thus complicated, cannot be solved without a knowledge of the physical characters of both races. Incidentally, the criminals differ little among themselves. They are a homogeneous group, excepting that the class convicted of

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murder and assault have significantly longer heads than the others; (c) so far as can be judged, comparing head and skull measurements, there is little difference between the asylum population and Turner's Scottish cranial series.

Synopsis of Terms. Specific Terms.

Character	Relation of the mean to which it	Reference			
	Greater	Less			
L B H B/L H/L B/H S	macrocranial platycranial hypsicranial brachycephalic hypsicephalic platycephalic megalomegithic (or macromegithic) macrocephalic	brachycranial stenocranial chamaecranial dolichocephalic chamaecephalic stenocephalic micromegithic (or brachymegithic) microcephalic	Biometrika, Vo	ol. I. Fawed	ett's Memoir ,, ,, ,, ,, ,, ,, ,,

General Terms.

Character or group	The value of the co- corresponding considering the	Reference			
	Significantly Greater	Insignificantly Different	Significantly Less		
Any character Any group, for all or most characters	megalometropic (or macrometropic) megalomeric (or macromeric)	isometropic isomeric	micrometropic micromeric	This memoir	
A mictomeric group is partly micromer	s one where the char tropic, with or withou			"	

ON THE ERROR OF COUNTING WITH A HAEMACYTOMETER.

By STUDENT.

When counting yeast cells or blood corpuscles with a hæmacytometer there are two main sources of error: (1) the drop taken may not be representative of the bulk of the liquid; (2) the distribution of the cells or corpuscles over the area which is examined is never absolutely uniform, so that there is an "error of random sampling."

With the first source of error we are concerned only to this extent; that when the probable error of random sampling is known we can tell whether the various drops taken show significant differences. What follows is concerned with the distribution of particles throughout a liquid, as shewn by spreading it in a thin layer over a measured surface and counting the particles per unit area.

Theoretical Consideration.

Suppose the *whole* liquid to have been well mixed and spread out in a thin layer over N units of area (in the hæmacytometer the usual thickness is '01 mm. and the unit of area $\frac{1}{400}$ sq. mm.).

Let the particles subside and let there be on an average m particles per unit area, that is Nm altogether. Then assuming the liquid has been properly mixed a given particle will have an equal chance of falling on any unit area.

i.e. the chance of its falling in a given unit area is 1/N and of its not doing so 1-1/N.

Consequently considering all the mN particles the chances of 0, 1, 2, 3... particles falling on a given area are given by the terms of the binomial $\left\{\left(1-\frac{1}{N}\right)+\frac{1}{N}\right\}^{mN}$, and if M unit areas be considered the distribution of unit areas containing 0, 1, 2, 3... particles is given by M $\left\{\left(1-\frac{1}{N}\right)+\frac{1}{N}\right\}^{mN}$.

Now in practice N is to be measured in millions and may be taken as infinite.

Let us find the limit when N is infinite of the general term of this expansion. The (r+1)th term is:

$$\begin{split} \left(1 - \frac{1}{N}\right)^{mN-r} \cdot \left(\frac{1}{N}\right)^r \frac{mN \left(mN - 1\right) \left(mN - 2\right) \dots \left(mN - r + 1\right)}{r!} \\ &= \left(1 - \frac{1}{N}\right)^{mN-r} \frac{m \left(m - \frac{1}{N}\right) \left(m - \frac{2}{N}\right) \dots \left(m - \frac{r - 1}{N}\right)}{r!} \\ &= \left(1 - \frac{mN - r}{N} + \frac{\left(mN - r\right) \left(mN - r - 1\right)}{N^2 \cdot 2!} - \dots \right. \\ &+ \left(-1\right)^s \frac{\left(mN - r\right) \dots \left(mN - r - s + 1\right)}{N^s \cdot s!} + \dots\right) \\ &\times m \frac{\left(m - \frac{1}{N}\right) \left(m - \frac{2}{N}\right) \dots \left(m - \frac{r - 1}{N}\right)}{r!} \cdot \end{split}$$

But when we proceed to the limit $\frac{1}{N}$, $\frac{2}{N}$... $\frac{r-1}{N}$ and $\frac{r}{N}$, $\frac{r+1}{N}$... $\frac{r+s-1}{N}$ are all negligeably small compared to m so that the expression reduces to

$$\left(1-m+\frac{m^2}{2!}-\ldots+(-1)^s\frac{m^s}{s!}\ldots\right)\times\frac{m^r}{r!}=e^{-m}\times\frac{m^r}{r!}.$$

That is to say that the expansion is equal to

$$e^{-m}\left\{1+m+\frac{m^2}{2\,!}+\ldots+\frac{m^r}{r\,!}+\ldots\right\}.$$

Hence it is this distribution with which we are concerned.

The 1st moment about the origin, O, taken at zero number of particles is

$$\begin{split} e^{-m} \left\{ m + \frac{2m^2}{2!} + \frac{3m^3}{3!} + \dots + \frac{rm^r}{r!} + \dots \right\} \\ &= me^{-m} \left\{ 1 + \frac{m}{1!} + \frac{m^2}{2!} + \dots + \frac{m^{r-1}}{(r-1)!} + \dots \right\} \\ &= m \times \text{total frequency.} \end{split}$$

Hence the mean is at m.

The 2nd moment about the point O is

$$\begin{split} &e^{-m}\left\{m+\frac{2^2m^2}{2\,!}+\frac{3^2m^3}{3\,!}+\ldots+\frac{r^2m^r}{r\,!}+\ldots\right\}\\ &=e^{-m}\left\{m+\frac{2m^2}{1\,!}+\frac{3m^3}{2\,!}+\ldots+\frac{rm^r}{(r-1)!}+\ldots\right\}\\ &=e^{-m}\left\{m+\frac{m^2}{1\,!}+\ldots+\frac{m^r}{(r-1)!}+\ldots+m^2+\frac{2m^3}{2\,!}+\ldots+\frac{(r-1)\,m^r}{(r-1)\,!}+\ldots\right\}\\ &=(m+m^2)\times \text{total frequency}. \end{split}$$

Hence the second moment-coefficient about the mean

$$\mu_2 = m + m^2 - m^2 = m.$$

By similar* methods the moment-coefficients up to μ_{ϵ} were obtained, as follows:

$$\mu_{1}' = m.$$

$$\mu_{2} = m.$$

$$\mu_{3} = m.$$

$$\mu_{4} = 3m^{2} + m.$$

$$\mu_{5} = 10m^{2} + m.$$

$$\mu_{6} = 15m^{3} + 25m^{2} + m.$$

$$\beta_{1} = \frac{\mu_{3}^{2}}{\mu_{2}^{3}} = \frac{1}{m},$$

Hence

and

$$\beta_2 = \frac{\mu_4}{{\mu_2}^2} = 3 + \frac{1}{m}$$
.

It will be observed that the limit to which this distribution approaches as m becomes infinite is the normal curve with its β_1 , β_3 , β_5 , etc., all equal to 0, and $\beta_2 = 3$, $\beta_4 = 15$, etc.

Further, any binomial $(p+q)^n$ can be put into the form $(p+q)^{nq/q}$, and if q be small and nq not large it approaches the distribution just given.

Thus if $1000 \ (\frac{99}{100} + \frac{1}{100})^{500}$ be expanded the greatest difference between any of its terms and the corresponding term of $1000 \ e^{-5} \left(1 + 5 + \frac{5^2}{2!} + \dots + \frac{5^r}{r!} + \dots\right)$

* The evaluation of the moments about the point O will be found to depend on the expansion of r^n in the form

$$\begin{split} r^n &= r \, \left. \left\{ \frac{(r-1)\,!}{(r-n-2)\,!} + a_1 \, \frac{(r-1)\,!}{(r-n-1)\,!} + a_2 \, \frac{(r-1)\,!}{(r-n)\,!} + \ldots + a_{n+1} \, \frac{(r-1)\,!}{(r-1)\,!} \right\} \right. \\ &= r \left. \left\{ \frac{1}{(r-n-2)\,!} + \frac{a_1}{(r-n-1)\,!} + \frac{a_2}{(r-n)\,!} + \ldots + \frac{a_{n+1}}{(r-1)\,!} \right\} \right. \left. (r-1)\,! \right\} \end{split}$$

Then if we form the series for n+1 from this it will be found that the following relations hold between a_1 , a_2 , a_3 etc. and the corresponding coefficients for n+1, A_1 , A_2 , A_3 etc.

$$\begin{split} A_1 &= a_1 + n, \\ A_2 &= a_2 + (n-1) \; a_1, \\ A_p &= a_p + (n-p+1) \; a_{p-1}. \end{split}$$

From these equations we can write down any number of moments about the point O in turn, and from these may be found the moments about the mean by the ordinary formulae.

The moments may also be deduced from the point binomial $(p+q)^{nq/q}$ when q is small and n large and nq=m, i.e. p=1, q=0, nq=m. We have

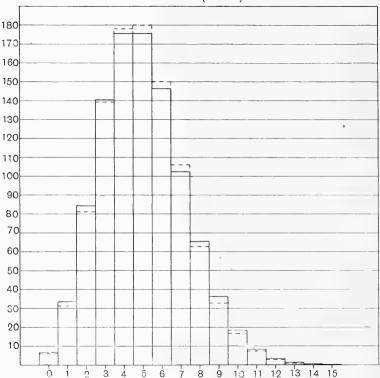
$$\begin{split} &\mu_1' = nq = m, \\ &\mu_2 = npq = m, \\ &\mu_3 = npq \; (p-q) = m, \\ &\mu_4 = npq \; \{1+3 \; (n-2) \; pq\} = m \; (1+3m) = 3m^2 + m. \end{split}$$

is never as much as 1, being about '8 for the term 1000 e^{-5} $\frac{5}{5!}$ which is 175.5 against 176.3 from the binomial.

Diagram I compares 1000 $e^{-5}\left(1+5+\frac{5^2}{2!}+\ldots+\frac{5^r}{r!}+\ldots\right)$ with the binomial 1000 $\left(\frac{19}{20}+\frac{1}{20}\right)^{100}$ which of course differ, but not by very much.

DIAGRAM I. Comparison of the exponential and binomial expansions.

Firm line represents $1000 e^{-5} \left\{1+5+\ldots+\frac{5^r}{r!}+\text{etc.}\right\}$. Broken line represents $1000 \left\{\frac{19}{20}+\frac{1}{20}\right\}^{100}$.



In applying this to actual cases it must be noted that we have not taken into account any "interference" between the particles; there has been supposed the same chance of a particle falling on an area which already has several particles as on one altogether unoccupied. Clearly if m be large this will not be the case, but with the dilutions usually employed this is not of any importance.

It will be shewn that the actual distributions which were tested do not diverge widely from this law, so we will consider the probable error of random sampling on the supposition that they follow it.

We have seen that $\mu_2 = m$.

Hence the standard deviation = \sqrt{m} .

So that if we have counted M unit areas the probable error of our mean (m) is $67449 \sqrt{\frac{m}{M}}$.

If we are working with a hæmacytometer in which the volume over each square is $\frac{1}{40000}$ mm. there will be 40,000,000 m particles per c.c. and the probable error will be $40,000,000 \times .67449 \times \sqrt{\frac{m}{M}}$.

Suppose now that we dilute the liquid to q times its bulk, we shall then have $\frac{m}{q}$ particles per square, and if we count M squares as before, our probable error for the number of particles per c.c. in the original solution will be $40,000,000 \times .67449 \times q \sqrt{\frac{m}{q} \times \frac{1}{M}}$. That is $40,000,000 \times .67449 \sqrt{\frac{mq}{M}}$.

That is we shall have to count qM squares in order to be as accurate as before.

So that the same accuracy is obtained by counting the same number of particles whatever the dilution, or, to look at it from a slightly different point of view, whatever be the size of the unit of area adopted.

Hence the most accurate way is to dilute the solution to the point at which the particles may be counted most rapidly, and to count as many as time permits: then the probable error of the mean is $67449 \sqrt{\frac{m}{M}}$ where m is the mean and M is the number of unit areas counted over, squares, columns of squares, microscope fields, or whatever unit be selected.

But owing to the difficulty of obtaining a drop representative of the bulk of the liquid the larger errors will probably be due to this cause, and it is usual to take several drops: if two of these differ in their means by a significant amount compared with the probable error (which is $67449 \sqrt{\frac{m_1 + m_2}{M}}$ where m_1 , m_2 are the means and M the number of unit areas counted), it is probable that one at least of the drops does not represent the bulk of the solution.

Experimental Work.

This theoretical work was tested on four distributions * which had been counted over the whole 400 squares of the hæmacytometer. The particles counted were yeast cells which were killed by adding a little mercuric chloride to the water in which they had been shaken up. A small quantity of this was mixed with a 10 °/°, solution of gelatine, and after being well stirred up drops were put on the hæmacytometer. This was then put on a plate of glass kept at a temperature just above the setting point of gelatine and allowed to cool slowly till the gelatine had set. Four different concentrations were used.

^{*} One of these is given in Table I.

In this way it was possible to count at leisure without fear of the cells straying from one square to another owing to accidental vibrations. A few cells stuck here and there to the cover glass, but as they appeared to be fairly uniformly distributed and were very few compared with those that sank to the bottom they were neglected: had the object of the experiment been to find the number of cells present they would have been counted by microscope fields, and correction made for them; but in our case they were considered to belong to a different "population" to those which sank.

Those cells which touched the bottom and right-hand lines of a square were considered to belong to the square; a convention of this kind is necessary as the cells have a tendency to settle on the lines.

There was some difficulty owing to the buds of some cells remaining undetached in spite of much shaking. In such cases an obvious bud was not counted, but sometimes, no doubt, a bud was counted as a separate cell, which slightly increases the number of squares with large numbers in them.

In order to test whether there was any local lack of homogeneity the correlation was determined between the number of cells on a square and the number of cells on each of the four squares nearest it; if from any cause there had been a tendency to lie closer together in some parts than in others this correlation would have been significantly positive.

Distributions 3 and 4 were tested in this way (Table II), with the result that the correlation coefficients were $+.016\pm.037$ and $.015\pm.037$. This is satisfactory as shewing that there is no very great difficulty in putting the drop on to the slide so as to be able to count at any point and in any order; as good a result may be expected from counting a column as from counting the same number of squares at random.

The actual distributions of cells are given below, and compared with those calculated on the supposition that they are random samples from a population following the law which we have investigated: the probability P of a worse fit occurring by chance is then found.

I. Mean = $.6825 : \mu_2 = .8117 : \mu_3 = 1.0876$.

Whence $\chi^2 = 9.92$ and P = .04.

Best fitting binomial $(1.1893 - .1893)^{-3.6054} \times 400$ for which P = .52.

II. Mean = 1.3225 : $\mu_0 = 1.2835$ μ_0 : = 1.3574.

	F-3 .						
	0	1	2	3	4	5	6
Actual	103	143	98	42	8	4	2
Calculated	106	141	93	41	14	4	1

Whence $\chi^2 = 3.98$ and P = .68.

Best fitting binomial $(.97051 + .02949)^{46.2084} \times 400$ for which P = .72.

III. Mean =1.80 : $\mu_2 = 1.96$: $\mu_3 = 2.529$.

Whence $\chi^2 = 9.03$ and P = .25.

Best fitting binomial $(1.0889 - .0889)^{-20.2473} \times 400$ for which P = .37.

IV. Mean = $4.68 : \mu_2 = 4.46 : \mu_3 = 4.98$.

Whence $\chi^2 = 9.72$ and P = .64.

Best fitting binomial $(.9525 + .0475)^{98.53} \times 400$ for which P = .68.

These results are given graphically in Diagram II. on the next page.

It is possible to fit a point binomial from the mean and the 2nd moment according to the two equations $\mu_1' = nq$, $\mu_2 = npq$ and these point binomials fit the observations better than the exponential series, but the constants have no physical meaning except that nq = m. And since the exponential series is a particular form of the point binomial and is fitted from one constant, while two are used for the "ad hoc" binomial, this better fit was only to be expected.

It will be noticed that in both I and III the 2nd moment is greater than the mean, due to an excess over the calculated among the high numbers in the tail of the distribution. As was pointed out before, the budding of the yeast cell increases these high numbers, and there is also probably a tendency to stick together in groups which was not altogether abolished even by vigorous shaking.

In any case, the probabilities '04, '68, '25 and '64, though not particularly high, are not at all unlikely in four trials, supposing our theoretical law to hold, and we are not likely to be very far wrong in assuming it to do so.

Let us now apply it to a practical problem: for some purposes it is customary to estimate the concentration of cells and then dilute so that each two drops of the liquid contain on an average one cell. Different flasks are then seeded with one drop of the liquid in each, and then "most of those flasks which show growths are pure cultures."

The exact distribution is given by

$$e^{-\frac{1}{2}}\left(1+\frac{1}{2}+\frac{(\frac{1}{2})^2}{2\,!}+\frac{(\frac{1}{2})^3}{3\,!}+\ldots\right),$$

which is

No. of Yeast cells	0	1	2	3	4
Percentage Frequency	60.65	30.33	7.58	1.26	.16

or approximately three-quarters of those which show growth are pure cultures.

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10 11 12 Where they coincide the firm line alone is given. Mean number 4.68. Cells per Square. Diagram II. Distribution of 400 Squares. Broken lines: Calculated from the Exponential Series. Mean number 1.80. Cells per Square. -0 Mean number 1.3225. Cells per Square. Firm lines: Actual Observations. o i 2 3 4 Cells per Square. Mean number 6825. 190 180 170 160 150 90 09 20 4 02

Number of Squares.

Conclusions.

We have seen that the distribution of small particles in a liquid follows the law

$$e^{-m}\left\{1+m+rac{m^2}{2\,!}+\ldots+rac{m^r}{r\,!}+\ldots
ight\}$$

where m is the mean number of particles per unit volume * and the various terms in the series give the chances that a given unit volume contains $0, 1, 2, \ldots r, \ldots$ particles. We have also seen that this series represents the limit to which any point binomial $(p+q)^n$ approaches when q is small, insomuch that even $(\frac{19}{20} + \frac{1}{20})^{100} \times 1000$ is represented by $e^{-5}(1+5+\frac{5^2}{2!}+\ldots+\frac{5^r}{r!}+\ldots) \times 1000$ with a maximum error of about 4.5 in 180.

For the rough calculation of odds with n small compared to $\frac{1}{q}$ the exponential series may be used instead of the binomial as being less laborious.

Finally, we have found that the standard deviation of the mean number of particles per unit volume is $\sqrt{\frac{m}{M}}$ where m is the mean number and M the number of unit volumes counted, so that the criterion of whether two solutions contain different numbers of cells is whether $m_1 - m_2$ is significant compared with $.67449 \sqrt{\frac{m_1}{M_1} + \frac{m_2}{M_2}}$.

TABLE I.

Distribution of Yeast Cells over 1 sq. mm. divided into 400 squares.

î		1			1		Ι	1		1		1			1		1		1
2	2	4	4	4	5	2	4	7	7	4	7	5	2	8	6	7	4	3	4
3	3	2	4	2	5	4	2	8	6	3	6	6	10	8	3	5	6	4	4
7	9	5	2	7	4	4	2	4	4	4	3	5	6	5	4	i	4	2	6
4	l	4	7	3	2	3	5	8	2	9	5	3	_	5	5	2	4	3	4
										_	-	1	9		_				
4	1	5	9	3	4	4	6	6	5	4	6	5	5	4	3	5	9	6	4
4	4	5	10	4	4	3	8	3	2	1	4	1	5	6	4	2	3	3	3
3	7	4	5	1	8	5	7	9	5	8	9	5	6	6	4	3	7	4	4
7	5	6	3 .	6	7	4	5	8 :	6	3	3	4	3	7	4	4	4	5	3
8	10	6	3	3	6	5	2	5	3	11 .	3	7	4	7	3	5	5	3	4
1	3	7	2	5	5	5	3	3	4	6	5	6	1	6	4	4	4	6	4
4	2	5	4	8	6	3	4	6	5	2	6	6	1	2	2	2	5	2	2
5	9	3	5	6	4	6	5	7	1	3	6	5	4	2	8	9	5	4	3
2	2	11	4	6	6	4	6	2	5	3	5	7	2	6	5	5	1	2	7
5	12	5	8	2	4	2	1	6	4	5	1	2	9	1	3	4	7	3	6
5	6	5	4	4	5	2	7	6	2	7	3	5	4	4	5	4	7	5	4
8	4	6	6	5	3	3	5	7	4	5	5	5	6	10	2	3	8	3	5
6	6	4	2	6	6	. 7	5	4	5	8	6	7	6	4	2	6	1	1	4
7	2	5	7	4	6	4	5	1	5	10	8	7	5	4	6	4	4	7	5
4	3	1	6	$\frac{4}{2}$	5	3	3	3	7	4	3	7	8	$\overline{4}$	7	3	1	4	4
7	6	7	-2^{-1}	4	5	1	3	12	4	2	2	8	7	6	7	6	3	5	4
1			_	_		1	9	12		-	-	0	•	0	1	J	9	9	
	!											1							

^{*} The prism standing on unit area.

It must be noted, however, that the probable error will always be greater than that calculated on this formula when for any reason the organisms occur as aggregates of varying size.

In conclusion, I should like to thank Prof. Adrian J. Brown, of Birmingham University, for his valuable advice and assistance in carrying out the experimental part of the enquiry.

TABLE II.
"Centre" Squares.

		1	2	3	4	5	6	7	8	9	10	11	12	Totals
"Adjacent" Squares	1 2 3 4 5 6 7 8 9 10 11 12	6 8 18 15 9 5 3 2 —	6 14 15 34 24 17 12 5 6 1 1	9 17 25 33 37 25 14 7 7 1	15 31 32 45 47 39 21 8 5 4	15 24 37 48 39 34 19 12 10 4 1	9 17 20 41 37 32 16 8 2 4 1	4 10 15 22 18 14 9 6 2	3 5 7 7 12 8 7 1 3 3	2 6 7 5 11 2 3 3 —	2 1 4 4 4 - 4 1 1	1 4 1 1 1 - -	1 - 2 1	69 134 171 258 247 186 106 57 38 18 8
	Totals	72	136	180	248	244	188	100	56	40	20	8	4	1296

Mean of "Centre" Squares, 4·6821 ; S. D., 2·139. Mean of "Adjacent" Squares, 4·7014 ; S. D., 2·116. $r=+\cdot016\pm\cdot037.$

Correlation table between the number of cells in a square and the numbers of cells in the four adjacent squares taken all over Table I.

MISCELLANEA.

On the Distribution of Severity of Attack in Cases of Smallpox.

By F. M. TURNER, M.D.

On Vol. iv. pp. 505-510 of *Biometrika*, Prof. Pearson gives reasons for believing that the distribution of severity among cases of smallpox is either normal, or not sufficiently skew to sensibly affect the calculations of correlation tables by normal curve formulae. His arguments are partly a priori; of direct evidence he only produces a list of cases of smallpox classified according to the length of time the patients were considered too ill to be bathed.

The following evidence to the contrary seems to me very strong. For over 10 years Dr Ricketts, formerly the Superintendent of the Hospital Ships, now Superintendent of all the smallpox hospitals of the Metropolitan Asylums Board, has divided his cases into six classes defined as follows:

Class I. Haemorrhagic cases.

.. II. Cases confluent in the vesicular stage.

. III. Cases confluent, but not before the pustular stage.

.. IV. Cases intermediate between classes III and V.

, V. Cases with from 100 to 500 pocks upon the face.

,, VI. Cases with less than 100 pocks on the face.

It will be seen that all the classes except I are defined by the severity of the eruption. In Class I the cases are so severe as to die, almost without exception, either before any eruption appears or before it is fully developed. It is almost certain that the cases of this class would belong to either Class II or III, if they lived long enough.

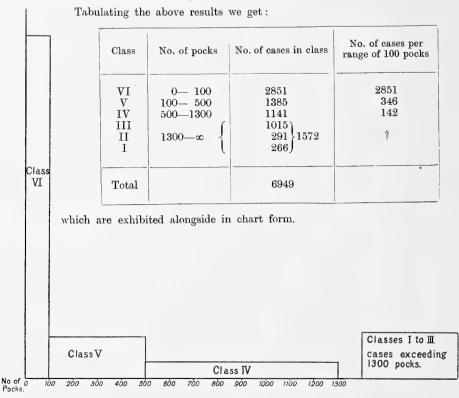
When I was working under Dr Ricketts two years ago, he generously put his records at my disposal, and I found that in the year 1902 the following number of patients were treated at Long Reach Hospital and the Hospital Ships:

Class	I.	266	4	Class	IV.	1141
,,	II.	291		29	V.	1385
"	III.	1015		,,	VI.	2851
				Т	otal	6949.

To get the comparative frequency of different degrees of severity of eruption we require a quantitative definition of the classes, which is given in Classes V and VI and may be ascertained with some approach to accuracy, as I shall shew below, in Classes II, III, and IV. That severity of disease in smallpox is very closely connected with severity of eruption is quite evident to me; and will, I believe, be admitted to be so by all who have had practical acquaintance of the disease.

To determine the superior limit of Class IV Dr Ricketts has sent me a photograph taken by his assistant, Dr Byles, which has been used as a standard, dividing Classes III and IV. The photograph is endorsed "Class III. Cases of less numerical severity fall into Class IV." The photograph is a profile view and on the half face I have counted 672 pocks. This number must not be taken as absolutely correct, partly because it is difficult to distinguish the individual pocks which have run together to form a group, partly because pocks are found of all sizes; besides those fully formed are others of small size, and others abortive, and it is difficult to draw a definite line in counting. Still the evidence shows that the division between Classes III and IV corresponds to about 1300 pocks.

For the number of pocks corresponding to Classes II and III I have only very rough evidence. In two large scale photographs of cases in these two classes I estimated the number of pocks at about 5000 and 2000 respectively. The pocks were so densely crowded that it was impossible to count them accurately. All I could do was to count those in one square inch of each photograph and multiply by the approximate area of the photograph. These photographs were of individual cases only and were not used as divisions between classes, nor as types. Consequently I have not used these figures in the table.



The skewness of the diagram is of a high order.

Further Remarks on the Distribution of Severity in Cases of Smallpox.

By KARL PEARSON, F.R.S.

In his paper in *Biometrika*, Vol. IV. pp. 483-504, Dr Turner obtained a series of values for the relation between severity of disease and vaccination, and in a discussion on these suggested that a normal distribution ought rather to be assumed for the whole population exposed to risk of infection than for the population actually attacked by the disease. He suggested that the attacked population is really a "curtailed" normal distribution and considered formulae for such "curtailed" distributions.

In a note on Dr Turner's memoir I took the only test of smallpox severity which was at my disposal, namely the distribution of intervals which the physicians at Glasgow allow to elapse between (i) onset and (ii) eruption and the first bath; this I have been assured is a rough but fair measure of the severity of the attack. I showed that in these cases the maximum severity

did not occur with the mildest attacks, or the distribution was not "curtailed" in the manner suggested by Dr Turner. Further, I indicated that curtailed distributions did not arise in such cases as Dr Turner anticipated, e.g. the stature distribution of selected soldiers. In fact most of our anthropometric distributions have been more or less selected, artificially or naturally, and they appear as a rule to be as normal as unselected material.

Dr Turner has replied to my criticism with some interesting further statistics of smallpox. He takes the number of pock marks as given by the scheme below:

Marks	0-100	100-500	500-1300	over 1300
Frequency	2851	1385	1141	1572

and suggests that they show a maximum frequency with the mildest cases. He does not, however, consider how far they approximate to that curtailed normal population, which as a whole he supposes to represent the total population which has run the risk of infection. Taking the four groups as they stand, the part of no normal curve whatever will even approximately fit them. It may be argued that the failure arises from a considerable number of the mildest cases, escaping notice at all. My assistant, Mr E. B. Ross, has therefore taken up the problem, omitting the first group altogether. Taking total population to rise by multiples of 10, he shows that the only way even to approach Dr Turner's numbers is enormously to increase the total population of which the above is to represent the tail, but millions and billions of population running the risk of infection will not suffice. In fact the ratio of the bases of

the two groupings $\frac{1300-500}{500-100}$ is 2, and the limit to this ratio for the given frequencies treated

as normal even if the risk-running population were infinite would only be 1·32. As a matter of fact the "spot maps" show how small was the population which ran the risk of infection even in the London epidemic of 1901–2. Thus whether we include or exclude the group 0 to 100, Dr Turner's data are wholly impossible even as an approximation to a curtailed normal curve. This want of any approach to normality suggests the question of whether the material is even approximately homogeneous. Is it possible that the number of pock marks may be different according to the extent of acquired immunity? Is it not also true that 5 or 10 pocks are almost as rare as haemorrhagic cases and the frequency increases from such values up to at least 100 pocks? In other words the modal severity is not as Dr Turner's diagram would lead one to suppose at the very mildest cases. If this be so, then the problem hinges on whether it is right to suppose severity a linear function of the number of pocks. Non-linear functions would not affect the application of fourfold-table methods, but they would affect the legitimacy of Dr Turner's argument.

I think it will be found that unvaccinated cases at least follow fairly closely a normal distribution of pocking. Dr J. Brownlee kindly provides me with all the material available from the Glasgow Epidemic, 1900–1. We have:

	Sparse	Abundant	Confluent	Haemorrhagic	Totals
Cases Deaths	9	41 12	61 42	4 4	115 59
Percentage Deaths ± P.E.	11·1±7·2	29·3 ± 4·8	68·9 ± 4·4	100 ± 9·8*?	51.3

Assuming the distribution normal I find:

```
Range of "Sparse" : from -\infty to -1.417\,\sigma; mean of group -1.868\,\sigma, , , "Abundant" : ,, -1.417\,\sigma to -0.164\,\sigma; , , , -694\,\sigma, , , "Confluent" : ,, -0.164\,\sigma to +1.815\,\sigma; , , , + .597\,\sigma, , , "Haemorrhagic": ,, +1.815\,\sigma to +\infty ; ,, , + .2.208\,\sigma.
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^{*} Deduced by an extension of Bayes' Theorem.

Fitting lineally by Least Squares (weighted with the number of observations) the means of the groups to the corresponding death-rates, we have if x be the abscissa of normal curve

Death-rate = $51.3 + 25.7x/\sigma$.

This gives:

Death-rate	Sparse	Abundant	Confluent	Haemorrhagic
Range Value at Mean of Class	0 to 15.0 3.4	15·0 – 47·2 33·5	$47 \cdot 2 - 97 \cdot 9$ $66 \cdot 7$	97.9 upwards 108.0*
Observed Value	11·1 ± 7·2	29·3 ± 4·8	68·9 ± 4·4	100±9·8?

These results are well within the errors of the samples given. The death-rate at the mean amount of pocking is 51.3. Thus, if we assume the amount of severity as given by pocking to follow a normal curve, the scale of severity obtained fits well the severity of the classes as found by a death-rate standard. It is further clear that the modal value lies in the confluent class and does not coincide with the slightest cases. Further there is a very high correlation between severity as measured by a normal scale of pock-marking, and severity as measured by death-rate in the case of no acquired immunity.

If an investigation similar to the present on cases vaccinated,—say within ten years—should show that a normal distribution of pock-markings fits in well there also with the death-rate severity scale, it would indicate that Dr Turner's severity skewness is due to a mixture of vaccinated and unvaccinated in his returns. Dr Brownlee's view that the disease is physiologically different in the two classes would thus be confirmed. The discussion having turned on the distribution of severity in disease, has got somewhat far from the original point, as to whether the case population, recovering and dying, could be represented by a normal curve. But clearly death on such a scale marks a certain intensity of the disease relative to the individual constitution; a scale of pock-marking cannot, we see from the above statistics, be equivalent to this scale; for deaths occur with all classes of pocking, and death cannot accordingly be made to correspond to a definite intensity of severity on a pocking scale. In short "power to resist disease when acquired" might obey a normal distribution although pocking did not, for failure to recover is not a fixed point on the scale of number of pocks.

If we have to dismiss entirely Dr Turner's suggestion of a curtailed normal curve, I cannot dismiss his severity statistics in the easy way in which he appears to dismiss mine. The bath test appears to me quite as valid as the pock test. It is further in accordance with a very considerable range of statistics for various diseases which have recently been published by Dr John Brownlee+, and which all go to show that the severity in other diseases is not such that the maximum frequency occurs at the minimum severity, but that the mean severity is approximately modal with milder and severer cases on either side.

It will thus be seen that the matter really demands further statistics. Is smallpox an exceptional disease for which the absolutely mildest cases are the most frequent? Or, may it not be that there is some method of reconciling the pock test of severity with the bath test of severity for which smallpox falls into line with other diseases? It appears to me that there are many other factors highly correlated with time and contributing to severity which may be largely overlooked by the numerical estimate of pocking as the sole test of severity and take their proper place and influence in the bath test, or what for our present purposes is more important than either, in a "power of resistance" test.

^{*} This is no impossible value, for the severity might be more than sufficient to kill the whole number of haemorrhagic cases.

⁺ Royal Phil. Soc. Glasgow Proceedings, November 7, 1906.

Supplement to Vol. V. of Biometrika.

ANTHROPOMETRIC SURVEY

OF THE

INMATES OF ASYLUMS IN SCOTLAND

BY

J. F. TOCHER.

APPENDIX I.—RECORD OF MEASUREMENTS AT THE VARIOUS ASYLUMS, PP. 5-80.

APPENDIX II.—TABLES OF CLASSIFIED DATA, PP. 81-ET SEQ.

[To accompany the memoir on "The Anthropometric Characteristics of the Inmates of Asylums in Scotland," by J. F. Tocher.]

Through the kindness of the Henderson Trust of Edinburgh, permission has been given to reprint the original data bearing on the Survey of the Inmates of Asylums in Scotland. The Editors beg to acknowledge their indebtedness to the Members of the Trust, and to thank them for their kindness in granting permission to reprint from their first Report such useful material.

Explanatory Note to Tables.

APPENDIX I.—Measurements.

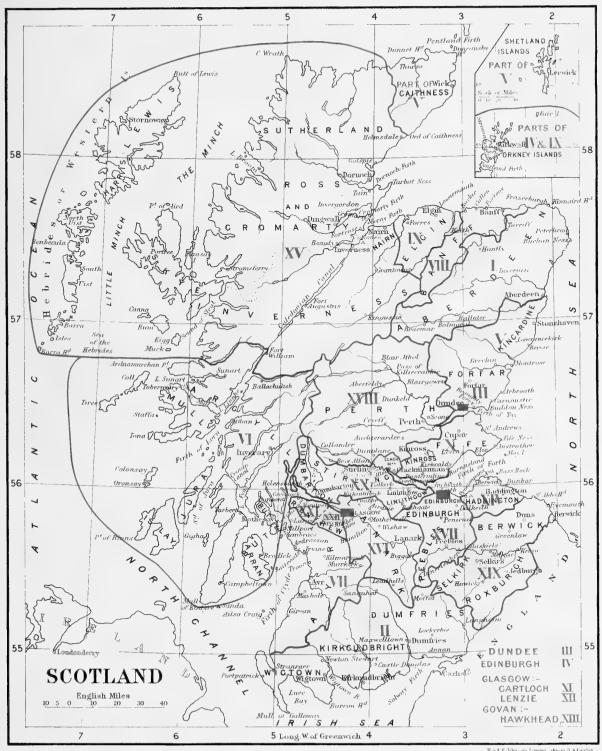
Observations were made on a selection of both measurable and non-The measurable characters observed and measurable characters of inmates. recorded were those of stature (S), head length (L), head breadth (B), and head height (H); the non-measurable characters were those of hair colour, eye colour, and nose contour. Head length was measured from the most prominent point of glabella to the occipital point, and was therefore the maximum head length. head breadth measured was the maximum breadth above the level of the ear. Head height was taken from the mid points of the auricular passages to the vertex. The types of nose recognised were straight (S), Roman (R), Jewish (I), concave (C), and wavy (W). The categories adopted for hair and eye colours were those used by the author in similar previous observations, and are the categories recognised by authorities in this country. The hair categories were red (R), fair (F), medium (M), dark (D). The letters B and M have, however, been inadvertently used in pages 5 to 14 to describe medium hair (i.e. in the Record of Observations on males at Aberdeen, Dumfries, Dundee, Edinburgh, Montrose, and Argyll), otherwise M is used in the hair column to describe medium hair. Red included light, bright, and dark red; fair consisted of white, flaxen, and golden yellow; medium included chestnut and all shades of brown except dark brown; dark embraced dark brown and black. The eye categories were light, medium, and dark (hazel brown). Where blanks occur in the table, no observations were made or recorded. The blanks in hair colour were chiefly due to absence of hair (baldness) or absence of pigment (grey hair).

APPENDIX II.—Classified Data.

In Appendix II, one table of frequency and several tables of correlation are given, inclusive of the hair and eye colour table. Where italics occur at the end of the range in any of the tables, a break in the continuity of the scale is indicated. No persons with intermediate dimensions were observed to occur. Tables of means and variabilities are also given in this appendix.

List of Asylums-Key to Map.

Asylum.	Counties in each Area.
I.—Aberdeen Royal Asylum	Aberdeen.
II.—Crichton Royal Institution	Dumfries, Kirkcudbright, Wigtown.
III.—Dundee District Asylum	Dundee.
IV.—Edinburgh Royal Asylum	Edinburgh (City) and Leith.
V.—Montrose Royal Asylum	Forfar, Kincardine, Caithness, Shetland.
VI.—Argyll District Asylum	Argyll, Bute, and Arran.
VII.—Ayr District Asylum	Ayr.
VIII.—Banff District Asylum	Banff.
IX.—Elgin District Asylum	.Elgin.
X.—Fife District Asylum	Fife, Kinross.
XI.—Glasgow District Asylum (Gartloch) Glasgow.
XII.— " " " (Lenzie).	•• ,,
XIII.—Govan District Asylum	,,
XIV.—Haddington District Asylum	Haddington.
XV.—Inverness District Asylum	Inverness, Nairn, Ross & Cromarty.
XVI.—Lanark District Asylum	Lanark.
XVII.—Midlothian District Asylum	Midlothian, Peebles.
XVIII.—Perth District Asylum	Perth.
XIX.—Roxburgh District Asylum	Berwick, Roxburgh, Selkirk.
XX.—Stirling District Asylum	Stirling, Dumbarton, Clackmannan, and Linlithgow.
XXI.—Greenock Parochial Asylum	Renfrew.
XXII.—Paisley Parochial Asylum	.Renfrew.



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APPENDIX I.—MEASUREMENTS.

				MALES.							MALES.				
No.	Col- Chara		of Nose.	Stature.		Crania Charact		No	Col Chara	our	of Nose.	Stature.		Cranial Characte	
	Hair,	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
1 2 3 4 5 6 7 8 9 10 1 1 2 3 3 4 5 6 7 8 9 10 1 1 2 2 3 2 4 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	D M	MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	nanananananananananananananananananana	265785569357 677866668506698704039	130 138 128 134 132 136 138 128 136 131 129 138 144 131 132 133 134 135 130 134 138 142 142 142 142 143 131 132 133 134 135 136 137 138 139 139 139 139 139 139 139 139	187 198 195 196 186 208 194 196 189 194 196 191 189 197 201 194 193 209 194 189 193 192 204 189 201 195 197 189 193 195 197 189 196 197 189 197 189 197 189 198 199 199 199 199 199 199 199 199	144 153 151 153 147 159 158 149 153 149 154 159 145 145 145 145 145 146 156 153 156 149 151 149 156 153 156 149 151 149 151 149 153 153 149 154 157 157 158 159 159 159 159 159 159 159 159 159 159	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 88 89 91 92 93 94 95 96 97 99 99 100 101 102 103 104 105 107 118 119 119 119 119 119 119 119 119 119	D D D D D D D D D D D D D D D D D D D	L D L D M L L D D D M M L M M D M M M D D M M L D M D L L L L	REARRANDE SA SA SA SA SA SA SA SA SA SA SA SA SA	$\begin{array}{c} 5 & 6 \\ 5 & 10 \\ 5 & 11 \\ 5 & 10$	140 134 134 128 135 134 138 130 131 135 131 129 144 129 135 140 135 136 136 136 136 136 136 137 141 145 128 137 140 133 141 145 128 137 140 133 141 145 128 137 140 133 141 145 128 137 140 133 141 145 128 137 140 138 133 141 145 129 131 144 145 129 131 144 134 129 131 134 129 131 134 129 131 134 129 131 134 129 131 141 145 128 137 140 138 133 141 145 128 137 140 138 133 140 140	199 193 199 189 199 199 199 199 191 201 189 191 202 207 198 181 199 194 191 179 186 198 207 201 199 189 184 196 193 204 191 189 198 193 198 197 191 189 198 198 197 191 189 198 193 198 197 191 189 198 193 198 197 197 199 198 193 198 193 198 197 198 193 198 193 198 197 198 198 199 198 199 198 199 198 199 198 199 198 199 198 199 198 199 199	15 14 15 14 15 15 15 15 15 15 15 15

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				MALES.								MALES.			
No.	Colo Chara		Shape of Nose.	Stature.	C	Cranial Characte		No.	Cole Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
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II.—Crichton Royal Institution.

				MAI	LES.								MALES.	•		
1 2 3 4 5 6 7 8 9 10 11 12 13 14	BBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB	L M D L L L M M M L L L L L L L	W W S S S W S S R S S S S W S	5 5 5 5 5 5 5 5 5 5 5 5 5 5	8 6 9 6 6 9 6 3 5 5 8 8 7 3	135 137 138 138 138 138 135 137 130 141 144 136 141 138	186 207 206 203 194 194 199 182 197 188 199 193 199 193 188	147 151 151 159 151 146 147 147 153 162 158 158 156 149 135	16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	B B B B B B B B B B B B B B B B B B B	L L M L M D L L L D L L L L	wwwww Summanna	5 7 6 5 5 8 5 7 4 5 5 5 4 5 5 5 5 5 5 5 5 5 5 5 5 5	144 141 134 135 127 130 133 133 132 135 138 133 132 133	208 199 186 211 188 193 191 193 199 210 201 196 189 189 200	166 149 145 153 147 156 151 153 157 156 151 146 157 146

				//	-Cri	chto	n R	oyal	i ins	stit	uti	on.			
				MALES.								MALES.			
No.		our acter.	J.	Stature.		Cranial Characte		No.	Col- Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.	i	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
31 32 33 34 4 35 36 37 38 40 41 42 44 44 45 50 51 52 53 54 55 66 66 67 68 69 70 71 72		L D L L L L M L L L L M L L L L D D M L L L L	and and and and and And And And And And And And And And A	510 510 786 955 55	135 139 136 139 138 135 132 143 132 134 135 136 136 125 128 136 125 128 137 137 137 138 137 137 138 139 136 125 136 125 137 138 139 139 139 139 139 139 139 139 139 139	206 200 196 201 193 193 194 203 203 203 207 197 197 199 188 191 194 195 191 206 197 188 191 194 195 205 198 199 199 199 205 199 199 199 205 199 199 199 199 199 199 199 199 199 19	153 152 149 157 153 154 148 154 154 154 151 149 151 155 156 149 149 149 149 149 149 149 149 149 149	73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 100 101 102 103 104 105 106 107 108 109 110 111 112 113	B B B B B B B B B B B B B B B B B B B	L L M L M D L L L L L D M L L L M M D L L L L	a Saranananananananananananananananananana	83958811578501174444730508714723182253831062 5545555555555555555555555555555555555	131 132 125 134 134 139 142 144 131 133 125 131 132 126 128 130 138 139 142 131 128 139 142 131 132 131 132 131 132 131 132 131 132 131 132 133 134 139 149 131 131 132 133 134 139 149 131 131 132 133 134 136 137 137 137 137 137 137 137 137	193 184 178 200 195 201 209 202 191 193 189 201 196 192 181 195 211 211 200 198 195 191 197 203 200 195 200 174 211 201 189 193 190 200 188 181 186 203 187	144 143 139 154 149 153 146 157 144 149 159 151 148 149 153 149 153 149 153 149 153 149 153 149 153 149 155 148 140 156 138 163 148 153 150 147 156 156
				JALES.	.—D	unde	e D	istri	ct A	4sy	lur	MALES.			
	В	L	ĺ	5 2	133	202	153	11	В	L	s	5 6	132	188	148
2 3 4 5 6 7 8 9	B B B B B B B B	L M L M L M L L L	and and and and and and and and and and	5 8 6 5 7 9 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	133 132 133 133 129 133 131 133 135 135	198 199 195 188 201 183 193 202 197	153 154 157 145 143 160 147 156 156	11 12 13 14 15 16 17 18 19 20	F B B B B B B B	L M L L L L M L M	vanan Anna	5 4 5 9 5 3 5 6 5 6 5 7 5 9 5 6 5 11	132 121 133 133 131 134 134 142 137 132	188 191 197 191 193 196 193 203 191 192	152 156 144 133 144 151 156 147 156

				111	I.—D	unde	e D	istr	ict .	Asy	/lui	n.			
				MALES								MALES.			
No.	Cole Chara		of Nose.	Stature.		Cranial Characte	er.	No.	Col Chara		of Nose.	Stature.		Crania Charact	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H. mm.	L.	B.
21 22 23 24 25 26 27 28 31 32 33 34 35 36 37 38 39 40 41 42 43 44 44 45 46 47 48 49 55 51 52 53 66 67 67 66 66 66 66 66 66 67 77 77 78 77 78 78 78 78 78 78 78 78 78	BBBBDDBDBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB	M L L M L L L L L L L L L L L L L L L L	O Reseau and a series of the s	55 55 55 55 55 55 55 55 55 55 55 55 55	130 127 133 129 132 134 136 130 135 131 137 135 135 130 131 137 136 138 128 124 136 128 128 124 136 137 136 137 137 138 139 142 138 139 139 139 139 139 139 139 139	183 188 193 185 189 202 200 195 212 188 195 203 198 199 200 198 207 183 188 185 195 196 204 181 192 200 198 202 193 199 198 184 192 208 189 189 184 192 208 189 189 184 192 196 196 202 193 199 198 189 184 192 196 198 189 184 199 198 189 184 199 198 189 184 199 198 189 189 189 189 189 189 189 189	143 151 151 146 152 153 155 153 156 152 159 160 149 154 154 156 148 156 149 146 155 146 149 154 151 160 152 151 160 152 151 152 151 152 153 160 152 154 160 160 160 160 160 160 160 160 160 160	82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 141 141 155 166 176 176 187 188 199 199 100 110 111 112 113 114 115 116 117 118 119 120 121 121 122 123 124 127 128 129 130 131 141 131 131 132 133 134 135 136 137 138 139 140 141 141 141 155 166 177 178 188 199 199 190 190 190 190 190 190	B B B B B D B D B B B B B D B B B B B B	M L D D L L M L L M L L L L L L L L L L	anananan Anananananan Anarananananan Anananana. ananananananananananananananan	$\begin{array}{c} 82 \ 43 \ 40 \ 66 \ 60 \ 75 \ 55 \ 55 \ 55 \ 55 \ 55 \ 55 \ 5$	138 134 124 135 133 136 138 138 139 135 139 136 141 138 139 135 139 136 141 138 140 135 132 126 133 131 143 132 129 138 132 129 138 132 129 138 132 129 138 132 129 138 132 129 138 132 129 138 132 129 138 132 129 138 132 131 143 132 134 137 136 138 139 139 138 139 130 140 126 134 133 135 132 144 137 136 138 139 138 139 139 138 139 139 139 139 139 139 139 139 139 139	186 187 192 196 197 198 205 211 195 197 199 203 185 203 196 205 204 192 191 193 191 193 195 180 181 196 186 217 186 185 197 186 185 197 186 185 197 186 187 199 190 193 189 193 199 190 193 189 193 199 190 193 189 189 189 189 189 189 189 189 189 189	155 155 146 152 144 163 162 154 144 163 153 149 145 150 154 153 153 149 145 153 149 145 153 149 145 140 142 143 153 148 153 149 147 152 147 155 150 150 150 150 150 163 163 163 163 163 163 163 163 163 163

				MALES.								MA	LES.			
No.	Colo Chara		Shape of Nose.	Stature.		Crania Charact		No.	Col Chara		of Nose.	Sta	ture.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H. mm.	L. mm.	B. mm
1 2 3 4 5 6 7 8 9 10 1 12 13 14 15 16 17 18 19 20 2 12 22 32 4 25 22 29 30 1 32 33 34 54 44 44 44 44 44 44 44 44 44 44 45 55 5	B B B F B	LLLUDLMDLLLLUDDLLLLLLUDDMDDLLLLLMLDLLBLDDLLLLDLDLDLMMLL	SSSS WSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	$\begin{array}{c} 26733535911147532091761\\ 5555555555555555555$	125 147 138 142 136 137 141 141 141 142 138 130 143 137 136 141 141 145 137 146 140 137 147 147 143 146 140 136 137 147 143 146 140 136 137 143 146 140 136 137 143 144 143 137 129 137 147 143 146 140 136 137 143 144 153 136 136 137 139 140 140 151 136 135 144 153 136 136 137 139 140 150 151 153 153 138 134 153 153 138 134 153 153 153 153 153 153	202 199 196 189 192 194 206 203 178 194 194 187 201 204 202 194 189 180 191 196 195 197 190 192 203 186 193 194 197 189 189 189 189 189 189 189 189 189 189	152 149 154 145 141 156 151 148 156 157 141 152 147 148 154 152 149 143 156 152 149 143 156 152 149 148 154 155 156 157 148 151 153 156 157 148 157 148 159 148 159 159 169 169 169 169 169 169 169 169 169 16	61 62 63 64 65 66 67 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 88 89 90 91 92 93 94 95 96 97 98 101 102 103 104 105 106 107 108 109 109 109 109 109 109 109 109 109 109	OFBBFOOBBBBFBOBOBBBBOODBBBBOOFBBOODMBBBBNNBNOBBBOODDOFBBN	M L M L L L L L M D L L L M D L L L M D L L L M D L D L	Assa Arasassassassassassassassassassassassassa	554555565555555555555555555555555555555	$\begin{smallmatrix} 651 \\ 687 \\ 302 \\ 543 \\ 342 \\ 671 \\ 154 \\ 087 \\ 785 \\ 003 \\ 644 \\ 705 \\ 897 \\ 154 \\ 668 \\ 764 \\ 294 \\ 574 \\ 554 \\ 895 \\ 4$	147 137 134 142 148 139 132 147 141 142 142 142 134 135 132 141 144 140 137 131 138 136 141 140 132 138 140 132 140 132 141 140 132 138 140 132 141 140 137 131 138 140 132 140 132 141 140 132 138 140 132 141 141 137 131 138 140 139 136 130 144 142 151 136 130 144 142 151 136 130 144 142 151 136 130 131 139 136 130 144 142 151 136 137 132 142 133 140 150 138 140 150 150 150 150 150 150 150 150 150 15	191 194 186 197 190 205 192 192 186 196 183 192 197 202 189 194 192 197 202 189 194 196 200 204 186 186 200 191 191 189 196 196 189 191 189 196 196 197 198 200 182 189 179 198 200 189 179 198 201 191 191 189 196 196 197 198 201 191 191 189 196 196 197 198 198 201 197 198 196 196 197 198 196 196 197 198 196 196 197 198 198 196 196 197 198 198 196 196 197 198 198 196 196 197 198 198 198 198 198 198 199 198 198 198	18 144 18 144 18 144 18 18 144 18 18 18 18 18 18 18 18 18 18 18 18 18

			I	MAL	ES.								MALES.			
No.	Col Chara		of Nose.	Stat	ture.	(Crania Characte		No.	Col Char		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
121 122 123 124 125 127 128 129 130 131 132 133 134 135 136 137 138 141 142 143 144 144 148 149 150	RBDBBBBBBBBBDDBBDBBBBNWBNDDBFDFN	LLDLLLLDM LLDM LLDLLLLW LDLLLLW LDLLLDD DLLLLDD		555555555555555555555555555555555555555	77 79 24 5 5 5 10 9 10 4 7 5 9 8 5 4 5 9 9 3 6 6 6 8 5 4 10 10 2 6 7	136 148 152 124 136 138 143 143 146 145 137 143 144 135 142 147 142 147 145 146 147 141 153	196 188 201 185 193 195 198 197 203 209 202 203 195 199 198 195 197 196 198 195 197 196 198 197 196 198 197 197 196 198 187 198 191 208 194 187 185 199	146 160 147 145 149 160 144 146 151 157 157 158 153 154 150 153 156 150 154 154 154 154 154 154 154 154 154 154	152 153 154 155 156 157 158 159 160 161 162 163 164 165 167 168 169 171 172 173 174 175 176 177 178 179	FDF BBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB			5 11 5 4 2 6 3 0 6 5 5 5 5 4 0 4 5 5 5 5 5 5 5 5 5 5 5 5 5	130 150 146 136 139 135 143 130 137 138 142 130 151 144 135 145 145 145 145 145 145 145 145 140 144 127 131 137	194 207 204 196 190 189 174 197 191 190 201 196 192 202 194 201 200 199 187 203 194 182 192 198 189 211 196	188 144 188 188 188 188 188 188 188 188

V.—Montrose Royal Asylum.

				MALES.								MALES.			
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	M F M D D B F M D F M D D D	L D L M M L D M M L D D M M M M	ananananananananan	MALES. 5 1 5 4 5 9 4 10 5 6 5 5 5 5 5 5 5 6 5 7 5 8 6 5 6 6	128 142- 121 132 137 144 131 135 142 126 145 138 138 134 146	179 192 175 187 196 191 200 196 200 208 182 208 195 196 196 195 198	142 152 142 146 154 151 156 149 155 154 156 158 158 158 151 153	21 22 23 24 25 26 27 28 29 30 31 32 33 34 35	D F F D F M F B F M M M F D D	L L L D M D L L L M D M D L L L M D M D		5 4 5 5 8 5 5 8 5 5 6 5 6 5 6 5 6 5 11 5 3 5 10 5 8 5 5 6 5 5 6 5 5 6 5 6 5 5 6 5 6 5 5 6 5 6	142 145 145 141 144 147 132 147 131 140 137 152 145 133 146 136	187 204 197 198 199 200 192 201 190 199 191 194 201 191 202 204 191	161 149 155 158 161 157 147 161 150 152 153 153 146 148
18 10 20	M D D	M M	SSS	5 4 5 6 5 8	129 136 127	189 191 196	155 152 152	38 39 40	D F M	M L L	SS	5 3 5 4 5 10	138 150 139	187 198 195	144 159 153

				V.	М	ontro	ose i	Roy	al A	ls <i>y</i>	lun	7.			
			1	MALES.				İ			Ŋ	MALES.			
No.	Cole Chara		of Nose.	Stature.	C	Cranial Characte		No.	Co Chara	lour acter.	of Nose.	Stature.	(Crania: Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
412 433 444 4456 447 448 449 551 552 553 661 663 664 665 667 771 777 777 777 777 777 777 777 777	FOMORFOF :RO :MM : :MOFMMBMOFFFDOFFOFFOMMMFMMFFFDFFFMFFRDOMDODOMD	f M $f M$ $f L$ $f D$ $f L$ $f M$ $f M$ $f D$ $f L$ $f L$ $f D$ $f M$ $f M$ $f D$ $f L$ $f L$ $f D$ $f L$ $f M$ $f M$ $f M$ $f D$ $f L$ $f L$ $f D$ $f L$ $f M$	and a superior of the superior of the superior and a superior of the superior	$\begin{smallmatrix} 102208953367442948731153067864266645544555687050863598779904985555545555555555555555555555555555$	154 134 140 129 134 137 142 140 130 142 140 140 130 141 141 132 146 144 138 141 140 135 134 140 140 135 134 141 140 135 141 140 135 141 140 135 141 140 135 141 140 135 140 140 136 137 140 140 138 140 140 138 140 140 130 130 130 130 130 130 130 130 130 13	194 192 190 188 195 198 201 208 185 194 198 205 192 185 195 197 201 198 199 193 190 203 202 192 194 198 199 193 197 198 199 198 199 198 199 198 199 198 199 199	148 152 156 144 146 156 164 155 156 145 155 156 148 152 159 151 149 150 151 154 153 153 153 164 155 153 164 155 156 157 149 149 149 149 150 151 147 149 149 149 149 149 149 149 149	101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 121 122 123 124 125 127 128 129 131 132 133 134 135 136 137 139 141 142 143 144 145 146 147 148 149 150 150 150 150 150 150 150 150 150 150			BROOK A KORONO A KORONO BOOK BOOK BOOK BOOK BOOK BOOK BOOK B	$\begin{array}{c} 7000655743761106335458777743705648989766668060899494576006656\\ 5555555555555555555555555555555$	127 139 148 131 137 142 140 142 143 159 134 133 134 133 134 137 136 133 134 147 136 133 134 147 136 137 147 148 149 149 149 149 149 149 149 149	190 200 203 193 196 199 190 200 195 201 195 202 198 191 182 198 183 183 200 204 189 191 200 204 196 196 197 200 197 201 199 187 201 199 187 201 199 199 199 199 199 199 199 199 199 1	1488 150 151 150 150 150 150 150 150 150 150

				MALES.				1				MALES.			
No.	Col Chara		of Nose.	Stature.	c	Cranial Characte		No.		lou r acter.	of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
161 162 163 164 166 167 168 170 171 172 173 174 175 176 177 178 181 182 183 184 185 189 191 192 193 194 199 200 201 203 204 206 206 207	FM DO FD DO DM M DO FF D M DO DM M D DM D M D M D M D M D M D		annanananan Zazanananananananananananananananananana	$\begin{matrix} 10\\25\\84\\01\\67\\74\\74\\67\\92\\40\\01\\69\\67\\09\\78\\4\\65\\63\\50\\98\\8\\5\\64\\0\\5\\65\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\5\\$	142 134 141 146 148 142 134 141 133 142 137 136 153 143 143 140 148 148 140 148 149 140 148 141 141 141 142 143 144 144 145 146 147 148 149 149 149 149 149 149 149 149 149 149	202 183 192 195 200 186 191 205 194 190 192 194 201 203 186 185 199 205 191 192 209 199 196 193 196 193 195 200 200 200 200 191 197 198 202 209 199 196 191 196 197 198 208 198 208 198 209 199 199 196 198 198 209 200 199 199 199 199 196 198 200 200 199 199 196 197 198 200 200 199 199 196 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 200 200 198 198 198 198 198 200 200 198 198 198 198 198 198 198 198	157 142 151 151 159 157 147 155 158 149 144 152 154 152 150 153 162 145 159 154 165 159 154 148 151 157 157 156 148 151 157 153 148 151 152 153 148 151 157 157 158 149 149 149 149 149 159 159 159 159 159 159 159 159 159 15	208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 227 228 230 231 232 234 235 234 235 234 241 242 243 244 245 246 247 248 249 251 252 253 254	FF M M M D FF FF M F D M M M M D F D D M R M D M D F D D M R M D F D D M R M D F D D M R M D M D F D D M R M D M D F D D M R M D M D M D R D D M D R D D M D R D D M D R D D M D R D D M D D M D D D M D D M D D D M D D D M D D D M D D D M D D D D M D D D D M D D D D D M D	L L M L L D M M L L D M M M D L M M M D L D M M D L M M D L D L	Substantian Assertation Assert	$\begin{array}{c} 5\\ 7\\ 5\\ 6\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $	138 148 135 145 135 140 139 148 137 144 134 134 131 135 129 152 147 136 140 139 149 140 140 140 140 150 147 144 133 129 131 145 139 139 139 140 140 142 137	188 203 193 202 184 195 190 188 192 197 201 198 194 177 193 195 200 198 185 194 197 205 200 203 197 200 201 198 197 200 201 198 197 200 201 198 197 200 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 197 200 201 198 198 199 200 201 198 198 199 200 201 198 198 198 198 198 199 200 198 198 198 198 198 198 198 198	144 153 144 153 153 153 153 154 155 156 156 156 157 157 157 157 157 157 157 157 157 157

VI.—Argyll District Asylum.

MALES.	MALES.
1 B D S 5 4 131 189 15 2 B L W 5 8 138 187 15 3 B M S 5 10 138 202 15 4 B L S 5 6 134 204 15 5 B L S 5 7 133 199 14	1 7 B L S 5 4 132 186 153 3 8 B L S 5 6 140 210 153 3 9 B L S 5 6 131 191 146

		-		ν	I.—A	rgy	II Di	stric	et A	syl	lum).			
				MALES.								MALES.			
No.	Cole Chara		Shape of Nose.	Stature.		Cranial Characte	er.	No	Col Chara	our acter.	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L. mm.	B.
11 12 13 14 15 16 17 18 19 20 12 22 23 24 25 26 27 28 29 30 31 32 43 43 44 44 46 47 48 49 55 56 66 66 66 66 66 66 66 67 66 66 66 66 66	ввавававававававаран вавававававававававававававававававав	M N D D D M M M M L D L L L M M L M L D L L M M L M L	annua sepantentan de la compansa de	$\begin{array}{c} 5 \\ 5 \\ 6 \\ 5 \\ 5 \\ 9 \\ 10 \\ 5 \\ 5 \\ 6 \\ 6 \\ 5 \\ 6 \\ 6 \\ 6 \\ 6 \\ 6$	142 139 134 140 137 140 138 137 140 138 133 136 136 132 137 138 135 136 137 144 130 131 142 130 131 132 133 136 145 145 149 131 131 131 131 131 131 131 131 131 13	200 203 189 208 202 200 197 196 211 194 197 195 202 201 203 199 201 203 195 213 201 201 207 216 203 210 197 216 203 210 197 216 203 210 197 216 203 210 197 216 203 210 197 210 207 196 199 196 191 202 209 197 210 207 198 199 196 191 202 209 197 210 207 198 199 196 191 202 209 197 218 201 197 203 204 207 208 192 197 203 204 207 208 192 197 203 204 184 196 193 205 195 195 185 206	151 156 148 156 153 158 153 152 148 153 152 152 149 160 159 151 156 166 157 152 157 156 168 153 148 152 153 148 152 153 148 153 154 155 156 157 158 158 158 158 158 158 158 158 158 158	71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 91 92 93 94 95 96 97 98 99 100 110 110 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 129 130	DDDDBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBBB	L D L L L M M M L L L L L L L L M D D L M D D L L L L	an A same and a same and a same a same and a same same	$\begin{smallmatrix} & & & & & & & & & & & & & & & & & & &$	133 125 128 141 145 144 141 139 155 132 138 136 136 134 139 138 136 137 129 131 133 136 137 129 131 133 136 137 129 131 133 135 136 137 129 131 133 136 137 138 139 138 137 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 138 139 139 139 139 139 139 139 139 139 139	188 195 194 210 201 200 204 201 216 190 199 194 194 199 208 192 199 183 193 195 200 200 200 201 212 206 200 203 212 194 199 195 202 204 201 197 199 195 209 199 195 209 199 195 209 199 195 209 200 200 200	140 141 142 164 163 154 155 160 147 150 152 157 143 159 152 154 153 150 159 152 160 149 153 150 158 143 152 156 154 155 163 148 149 143 152 166 154 157 165 160 158 157 165 160 158 157 165 160 157 148 152

	D 1 . 1 . 1 . 1	
VI.—Aravii	DISTRICT	Asvium.

				MALES.								MALES.			
No.	Cole Chara		of Nose.	Stature.		Cranial Characte		No.	Cole Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	II.	L.	B mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
131 132 133 134 135 136 136 137 138 139 141 142 143 144 145 146 147 148 151 151 152 153 154 155 156 157	M M M M M M M M M M M M M M M M M M M	L L M L L L L L L L L L L L L D L D L D	sananan Zanana Zanananananan	5 10 5 5 2 2 8 1 7 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	139 136 132 128 132 135 134 143 139 131 136 148 131 132 137 137 137 137 137 137 140 140 140 135	206 204 204 194 196 207 197 211 191 212 211 199 201 199 204 206 205 190 200 201 195 200 201	152 155 157 142 152 155 145 153 161 152 151 158 163 147 155 148 145 146 138 153 150 151	161 162 163 164 165 166 167 168 169 170 171 172 173 174 177 178 177 181 182 183 184 185 186	M M M M M M M M M M M M M M M M M M M	L L D M M M D L L M D D L L M L L L M D D D D		6 0 5 6 5 10 5 5 6 0 5 11 5 5 5 10 5 3 5 6 5 10 5 11 5 5 5 5 5 9 5 10 5 10 5 11 5 5 5 10 5 11 5 5 5 10 5 11 5 5 5 10 5 10	137 134 136 134 138 135 133 129 136 135 136 132 134 138 140 140 140 137 144 146 136 133 133 132 133	205 202 208 194 193 206 196 196 195 202 206 209 207 200 201 191 202 208 207 208 207 208 209 207 208	160 144 155 155 144 155 166 155 157 157 144 166 166 166 166 166 166 166 166 166
157 158 159 1 60	D D M	D M D M	SSSSS	5 7 5 5 5 7 4 6	135 134 145 137	199 200 220 195	$ \begin{array}{r} 148 \\ 156 \\ 162 \\ 150 \end{array} $	187 188 189 190	M M M M	D M D L		5 9 5 11 5 5 6 0	150 141 144 133	209 192 197 205	$ \begin{array}{c c} 15 \\ 14 \\ 14 \\ 15 \end{array} $

VII.—Ayr District Asylum.

			MAL	ES.								MALES.			
2	I L D M I L I M D M M I M D M I M I L I L I L I L I L I L I L I L I L I L	ananca Zanana Zananana	5 5 5 5	9 9 4 6 6 6 6 10 0 4 2 2 7 7 4 8 8 1 1 5 5 6 6 2 2 7 7 7 1 1 2 2 7 7 4	133 134 136 136 135 133 146 139 137 136 136 141 135 146 141 135 146	189 192 192 194 198 179 197 197 198 196 188 203 198 193 197 206 197 196 207 200	149 151 146 154 157 151 148 149 152 164 148 157 153 153 151 153 143 153 143	21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	M M M M M M M M M M M M M M M M M M M	D L L D M L L L M M M M M M M L L	and is a subsubsubsubsubsubsubsubsubsubsubsubsubs	5 9 4 5 5 8 5 2 2 5 3 8 5 5 7 5 8 8 5 5 2 5 5 8 8 5 5 5 7 5 5 8 8 5 5 5 5 5 5 8 8 5 5 5 5	139 133 147 143 137 136 143 139 135 142 135 131 130 134 141 137 147	199 197 189 197 194 189 191 204 200 193 193 200 189 202 194 204 194 208	147 143 160 153 149 146 147 152 162 148 151 149 146 153 149 156 149 156

				1	/11.—	Ayr	Dist	rict	: As	ylu	m.				
]	MALES.							7	MALES.			
No.	Col Chara		of Nose.	Stature.		Cranial Characte		No.	Col Chara	lour acter.	of Nose.	Stature.		Crania Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
41 42 43 44 44 456 477 488 49 551 52 534 556 66 67 751 77 77 77 77 77 77 77 77 77 77 77 77 77	MDDDDMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	$\begin{smallmatrix} MDL LLLLLMLMMLMMMDLLMMLLLLLLLDMLMMDLLMDLL$	Saus sau an an an an an an an an an an an an an	$\begin{matrix} 6844446066956849706389650868425976788934940999573825780283196 \\ 55555555555555555555555555555555555$	132 142 140 139 141 134 135 137 133 132 130 137 140 134 123 136 137 137 137 137 137 137 137 137 137 137	194 204 185 203 198 197 193 194 201 193 200 203 200 203 200 207 193 200 207 194 194 194 194 194 194 194 194	152 157 148 144 160 149 152 154 151 149 153 153 153 147 143 149 146 146 146 146 146 146 146 146	101 102 103 104 105 106 107 108 110 111 112 113 114 115 116 117 118 119 121 122 123 124 125 126 127 128 129 131 132 133 134 135 134 135 136 141 142 143 144 145 146 147 148 149 151 153 154 156 157 158 158 158 158 158 158 158 158 158 158	M M M M D D D M M M M M M M M M M M M M	LLMOMM DOLDLLLLMLMLMLLDLLMLDDLDMLLMMMMDMDMDMLLLMDMLLL	nonnannannannanna Afanannanna Affanannanna Affan Annannanna	$575562714622152555567550311547662252543053558452878911588580591\\55555555555555555555555555555555555$	139 132 129 136 137 124 138 135 134 132 131 130 136 131 134 140 139 134 139 134 139 136 137 145 143 133 132 135 134 133 132 135 134 137 145 143 137 145 143 137 145 143 137 145 138 137 145 138 137 145 138 137 147 139 136 137 139 136 137 139 136 137 139 136 137 139 136 137 139 136 137 139 136 137 139	209 204 197 202 200 196 198 197 202 201 193 200 194 201 194 196 207 209 205 208 202 205 201 194 196 192 206 191 209 203 198 200 201 202 198 200 197 198 188 192 202 198 201 188 199 200 197 198 188 199 200 197 198 188 199 200 197 198 201 188 204 196 209 201 202 203 198 200 197 198 198 201 188 204 191 195 204 208 209 209 209 200 197 198 200 197 198 201 188 204 209 209 209 209 200 197 198 200 197 198 201 188 204 209 209 209 209 200 201 200 201 202 203 203 203 204 205 205 206 207 207 208 208 208 209 209 200 201 200 200	162 160 155 154 159 148 147 146 156 151 158 151 152 148 151 152 160 151 155 154 154 148 151 154 149 156 156 157 148 157 158 158 158 159 159 159 159 159 159 159 159 169 169 169 169 169 169 169 169 169 16

				MAL	ES.				<u> </u>				MAL	ES.			
No.	Col Chara		of Nose.	Statu	ure.	_	Cranial Characte		No.	Col Chara		of Nose.	Stati	ure.	1	Cranial haracte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B, mm.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
161 162 163 164 165 166 167 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 189 191 192 193 194	M M M M M M M M M M M M M M M M M M M	L D M L L M M D L L M M M L L D M M L L L M D L L L M L L L L		555555555555555555555555555555555555555	44495869533736911536686167593541944806770	136 134 133 138 134 133 140 137 142 144 130 135 138 138 138 138 138 140 135 135 134 144 140 134 142 128 138 138 138 138 138 139 139 139 139 139 139 139 139 139 139	195 196 187 202 208 195 201 206 191 190 197 203 193 199 197 197 200 198 199 191 202 202 202 202 183 195 200 193 207 198 197 208	149 148 145 155 150 153 155 151 150 154 159 149 153 152 150 145 152 149 159 151 160 155 159 151 160 155 159 151 160 155 159 151 160 155 159 153 158 159 151 150 153 149 157 150 1553	198 199 200 201 202 203 204 205 206 207 208 209 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 227 228 229 231 232 233	D M M M M M M M M M M M M M M M M M M M	M D L L L L L D L L L L D L L L L L L L	assas Assas As Tasas as Tasas Assa Assa	555555555555555555555555555555555555555	$\begin{smallmatrix} 5 & 6 & 5 & 5 & 3 & 6 & 6 & 7 & 3 & 9 & 4 & 6 & 6 & 11 & 7 & 9 & 7 & 5 & 9 & 9 & 4 & 8 & 8 & 6 & 9 & 2 & 5 & 6 & 3 & 8 & 8 & 7 & 6 & 9 & 3 & 3 & 11 & 11 & 11 & 12 & 12 & 12 &$	135 139 137 135 136 134 136 139 136 139 136 132 132 134 142 142 139 132 131 132 133 138 135 130 137 132 133 134 135 136 137 137 138 139 131 131 132 133 134 135 136 137 137 138 139 130 137 137 138 139 130 137 137 138 139 130 137 137 138 139 130 137 137 138 138 139 139 130 137 137 138 138 139 139 130 137 130 137 137 138 138 139 139 139 139 139 139 130 130 130 130 130 130 130 130	196 203 205 192 189 202 203 196 198 201 199 198 201 199 198 196 200 189 197 210 174 191 192 202 196 191 197 200 199 198	15 16 15 15 15 15 15 15 15 15 15 15 15 15 15

				V	///.—E	Banf	f Di	stri	ct /	4sy	lun	n.			
				MALES.							I	MALES.			
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	M D D D D D D D D D D D	M M M M M D D M M M M	aa qaacaaaaaaaa	5 11 5 7 5 9 5 2 5 7 4 11 5 5 5 10 5 8 5 4 5 7 5 2	137 130 137 133 132 143 132 141 138 132 133 134 136 131	195 186 194 202 196 198 191 185 196 211 193 207 201 183	150 145 152 142 143 153 157 151 159 151 163 156 159 156	16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	D D M M M D M M M	M M L M L M D M M M M M M		5 10 5 9 5 5 5 7 5 5 5 7 5 5 5 7 5 5 5 7 5 5 5 7 5 5 5 7 5 7	137 143 128 137 130 136 136 136 138 135 145 145 158 134	187 200 198 195 197 194 207 193 199 195 204 197 211 203 195	150 155 144 158 159 153 157 148 154 155 155 162 155 143

				MALES.								MA	LES.			
No.	Col Chara		of Nose.	Stature.		Cranial Characte		No.	Colo Chara		of Nose.	Sta	ture.		Cranial Characte	
31	Hair.	Eyes.	Shape	ft. in.	H.	L. mm.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57	M D D M D M D M D M D M D D M D D D D D	M M M M M M M M M M M M M M M M M M M		5 8 5 11 5 6 5 8 5 6 5 9 5 7 5 10 5 6 5 9 5 7 5 6 5 9 5 7 5 6 5 5 7 5 5 6 5 5 7 5 5 6 5 7 5 5 6 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7	145 139 131 133 134 131 136 132 136 132 137 132 153 143 133 132 125 135 135 134 143 131 135 136	204 200 190 197 182 195 198 197 193 195 189 192 194 195 199 201 200 194 202 206 188 190 193	157 154 149 154 155 151 157 150 155 151 156 154 151 158 154 146 152 146 149 153 154 146 149 153 154 146 153	58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 80 81 82 83 84	D D D D M M M D D D D D M M D D D M M M D D D M M M D D D D M M D D D M M D D D M M D D D M M D D D M M D D D M M D D D M M D D D M M D D D M M M D D D D M M M D D D D M M M M D D D D M M M D D D M M M D D D D M M M M D D D D M M M M D D D D M M M M D D D M M M M D D D D M	D M M M M M M M M M M M M M M M M M M M	anananananananananananananan	555555555555555555555555555555555555555	9 7 5 3 6 3 9 9 8 5 9 6 3 5 7 5 0 8 6 1 1 4 2 6 6 7 5 0 8 6 6 7 5 0 8 8 6 7 5 0 8 8 7 5 0 8 8 6 7 5 0 8 8 7 5 0 8 8 8 7 5 0 8 8 8 7 5 0 8 8 8 7 5 0 8 8 8 7 7 5 0 8 8 8 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	136 130 143 137 132 128 144 136 140 129 143 141 133 134 144 147 140 141 135 139 140 137 142 131 131	208 192 194 190 191 193 193 199 186 199 187 191 185 202 206 189 197 190 191 198 191 198 191 198 191 198	15 15 15 14 14 14 15 13 15 15 15 15 15 15 15 15 15 15 15 15 15

IX.—Elgin District Asylum.

				MAl	LES.							MALES.			
1 2 3 4 4 5 6 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	D M D D D D D D D D D D D D D D D D	M L M D D D M M M D D D M M M M M M M M	Wassassassassass Cons	555555555555555555555555555555555555555	$\begin{array}{c} 5 \\ 6 \\ 7 \\ 8 \\ 5 \\ 7 \\ 7 \\ 6 \\ 3 \\ 6 \\ 7 \\ 4 \\ 5 \\ 0 \\ 5 \\ 0 \\ 7 \\ 7 \\ 4 \\ 7 \end{array}$	127 134 133 135 138 135 130 135 120 131 139 133 125 122 134 133 135 122 134 135	184 199 196 197 193 204 202 182 201 198 196 188 185 191 185 191 195 198	141 151 149 155 161 155 163 152 144 150 156 150 145 145 145 145 145 145 145	26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 44 45	R D D M M D M R F M D M D D M	M M M M M M M M M M M M M M M M M M M	5 5 7 5 5 7 5 5 8 8 5 7 11 5 5 8 8 4 11 5 5 5 10 5 7 7 5 5 8 4	131 124 131 142 145 136 132 144 135 145 131 139 140 131 139	195 185 196 205 200 197 200 194 201 190 197 189 195 203 198 198	150 153 154 158 157 150 143 153 163 151 147 155 148 155 138 154 155 138
21 22 23 24 25	D D D D	M M M D M	SSSCS	6 5 5 5 5	0 3 1 4 4	135 136 135 120 132	201 184 191 191 193	161 154 153 145 155	46 47 48 49 50	D D D D	M M M D D	5 6 5 7 5 9 5 6 5 2	137 139 134 138 138	185 185 196 195 182	154 151 157 152 153

			_
/X.—	Eiain	District	Asylum.

				MALES.								MA	LES.			
No.	Colo Chara		of Nose.	Stature,		Cranial Characte		No.	Col Chara		of Nose.	Stat	ture.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in	H,	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
51 52 53 54 55 56 57 58 59 60	M D D M D	M M L D M M M M M M	$\alpha\alpha\alpha\alpha\alpha\alpha\alpha\alpha\alpha\alpha\alpha\alpha$	5 7 5 8 5 4 5 2 5 7 5 9 5 10 5 10 5 7	139 139 129 131 139 133 143 134 138 136 137	199 206 186 188 196 192 202 204 195 196 193	148 155 148 159 151 151 153 162 153 156 159	62 63 64 65 66 67 68 69 70 71	M M D M D D D M D	M M M M M M M M M	Canananana	5 5 5 5 5 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	7 6 8 6 6 11 9 11 7 6	133 130 129 140 129 128 123 133 127 131	199 194 196 189 193 193 190 194 199	157 151 153 154 147 143 143 157 155 161

X.—Fife District Asylum.

	MALES.		,	MALES.	
1 M L S 3 M L S 4 M L S 5 D L S 6 M L S 7 M M M S 9 D D S 10 F L S 11 D L S 11 D L S 11 D L S 11 D L S 11 D L S 11 D L S 11 D L S 11 D L S 12 M M S 14 M L S 15 M L S 17 F L W 18 M D S 20 M D S 21 M L S 22 M M L S 22 M M L S 24 M L S 25 M L S 26 M M M S 27 M M M S 28 M L S 29 M M M S 29 M M M S 30 M D S 31 M L S 32 D L W 33 M L S 34 M L S 35 M L S 36 D D S 37 M D S 38 M L S 39 M L W 40 M L W	5 7 138 19 5 6 138 19 5 6 138 19 5 7 129 18 5 7 128 19 5 7 128 19 5 5 134 20 5 6 139 20 5 5 138 19 5 8 132 19 5 5 8 132 19 5 5 9 138 19 5 9 140 19 5 5 11 136 20 5 5 1136 20 5 6 142 20 5 6 142 20 5 7 136 19 5 9 138 19 5 9 138 19 5 9 138 19 5 9 138 19 5 1 136 20 5 1 136 19 5 7 1 141 1 20	8 154 42 4 148 43 4 148 43 4 156 44 4 154 44 4 154 45 4 151 47 6 146 48 3 147 50 9 146 51 8 154 52 151 53 54 2 151 53 2 153 59 3 154 60 3 154 60 4 153 64 5 151 63 5 151 63 4 153 64 6 154 66 6 155 65 6 151 63 6 148 65 6 154 66 6 156 66	R	5 7 136 5 6 135 5 4 135 5 8 138 5 7 136 5 5 141 5 9 130 5 6 138 5 10 137 5 2 136 5 8 150 5 7 136 5 8 150 5 7 135 5 6 132 5 6 132 5 6 132 5 6 132 5 7 135 5 8 130 5 8 130 5 8 130 5 6 132 5 8 133 5 7 135 5 7 135 5 7 135 5 7 135 5 7 135 5 8 133 5 8 130 5 8 133 5 9 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 9 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 8 133 5 9 133 5 8 133	193 150 193 141 195 157 201 154 204 151 202 151 192 149 201 156 195 150 196 146 191 152 213 172 190 150 199 156 188 155 190 153 194 144 190 159 207 158 200 151 188 153 200 151 188 154 200 154 200 154 190 150 200 153 200 151 188 147 201 154 202 159 189 149 203 160 186 147 187 142

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X.—Fite	District	Asvlum.

				MALES							,	MALES.			
No.	Colo Chara		of Nose.	Stature.		Cranial Characte		No.	Colo Chara		of Nose.	Stature.		Cranial Tharacte	r.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 139 130 131 141 141 151 161 171 181 182 183 184 185 186 187 187 188 189 180 180 180 180 180 180 180 180	M M M M M M M M M M M M M M M M M M M	LM LD LL LM L D L L L M L M L M L L L L	Actual and a contract	$\begin{array}{c} 58737646605775803555555555555555555$	140 135 136 134 135 136 135 136 137 136 136 137 136 136 140 134 135 136 140 134 135 136 146 140 134 135 136 137 136 137 136 137 136 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 137 136 137 138 139 134 135 136 137 138 139 134 135 137 136 137 138 139 134 135 136 137 138 139 134 135 136 137 138 139 134 135 136 137 138 138 138 138 138 138 138 138	196 198 197 189 203 195 189 198 195 206 194 197 186 193 188 204 201 185 189 201 189 197 191 203 189 197 194 192 194 197 189 189 206 193 191 196 198 206 193 191 196 198 206 187 198 199 202 187 198 189 206 187 198 199 201 189	153 145 158 149 154 144 148 150 152 160 152 158 147 152 155 140 145 155 156 157 153 145 155 151 155 151 155 151 155 151 155 155 151 155 155 157 155 155	141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 166 157 158 169 161 162 163 164 165 166 167 168 169 170 171 178 178 176 177 178 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196	M M M M M M M M M M M M M M M M M M M	L D M L M D L L M D L M L L L L L L L L	SC Nananananananananananananananananananan	5677917594758869764466678388675017456577770137556337880177668 5555555555555555555555555555555555	140 139 142 143 141 136 136 136 136 137 136 137 136 137 136 137 136 137 136 137 138 139 125 139 134 135 137 138 137 138 139 139 140 131 131 132 133 135 136 137 138 139 139 139 139 139 139 139 139 140 141 139 140 141 140 141 140 141 140 141 140 141 140 141 140 140	202 200 198 195 198 195 198 196 197 212 203 195 191 194 192 201 205 181 192 203 196 189 201 203 196 189 203 196 189 203 196 189 198 198 199 201 205 189 199 199 199 199 199 199 199 199 199	150 154 155 152 155 147 159 151 152 156 143 158 149 152 148 151 150 152 147 163 136 146 141 151 154 148 151 154 148 151 152 147 163 136 146 151 151 152 147 153 148 151 151 152 147 153 148 151 151 152 147 153 154 154 154 154 154 155 155 155 156 156 157 157 157 158 158 158 158 158 158 158 158 158 158

	X.—Fife	District	Asylum.
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			1	MAI	ES.								MAI	LES.			
No.	Col- Chara		of Nose.	Sta	ture.		Cranial Characte		No.	Col Chara		of Nose.	Sta	ture.		Cranial Characte	
	Hair.	Eyes.	Shape			н.	L.	В.		Hair.	Eyes.	Shape			Н.	L.	В.
		Ξ.		ft.	in.	mm.	mm.	mm.			H	·~	ft.	in.	mm.	mm.	mm.
201	D	$\hat{\mathbf{r}}$	S	5	6	139	192	159	208	M	L	\mathbf{s}	5	9	135	195	153
202 203	M M	L D	S	5	$\frac{11}{2}$	142 131	$\frac{209}{182}$	$160 \\ 145$	209 210	M M	M L	S	5 5	5 5	$\frac{140}{141}$	$\frac{209}{201}$	$152 \\ 151$
204	M	L	\mathbf{S}	5	6	134	199	158	211	M	M	S	5	3	138	195	143
205 206	M M	$egin{array}{c c} \mathbf{L} & \\ \mathbf{L} & \end{array}$	S R	5 5	$\frac{1}{8}$	133 139	$\frac{192}{197}$	$\frac{148}{157}$	212	M D	$\frac{L}{M}$	S	5 5	5 2	$\frac{135}{127}$	193 194	$155 \\ 151$
206	M	Ľ	S	5	8	135	196	146	213	D	D W	8	5 5	7	132	186	148

XI.—Glasgow District Asylum (Gartloch).

	MALES.	MALES.
1 M L S 3 M D S 4 D M S 5 M M S 6 M L S 8 M L S 8 M L S 9 M M L S 10 M L S 11 D D S 11 D D S 12 D L S 13 M L S 14 F L S 15 D D C 16 M D S 20 D M S 21 F L S 22 D M W 22 D M S 24 D D S 25 M L S 26 M L S 27 D L S 28 D L S 29 M L S 31 M L S 31 M L S 32 M M S 34 M M S 35 F L S 36 M L S 31 M L S 31 M L S 31 M L S 32 M L S 33 M L S 34 M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 38 M M S 39 M D S 30 M L S 31 M L S 31 M L S 32 M L S 33 M L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 38 M M S 39 M D S 38 M M S 39 M D S 38 M M S 39 M D S 31 M L S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 31 M L S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 31 M L S 31 M L S 32 M L S 33 M L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 31 M L S 31 M L S 32 M L S 33 F L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 38 M M M S 39 M D S 31 M L S 31 M L S 32 M L S 33 F L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 38 M M M S 39 M D S 31 M L S 31 M L S 32 M L S 33 F L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 31 M L S 31 M L S 32 M L S 33 M L S 34 M M S 35 F L S 36 M L S 37 M M S 38 M M S 39 M D S 38 M M M S 39 M D S 30 M L S 31 M L S 31 M L S 32 M L S 33 F L S 34 M M S 35 F L S 36 M L S 37 M M M S 37 M M M S 38 M M M S 39 M D S 31 M L S 35 F L S 36 M L S 37 M M M S 37 M M M S 38 M M M S 39 M D S	S 5 7 130 190 S 5 6 131 193 S 5 6 136 193 S 5 6 130 184 Y 5 7 132 198 S 5 5 130 184 Y 5 7 132 198 S 5 5 130 200 S 5 5 133 200 S 5 5 133 200 S 5 5 133 199 S 5 6 138 199 S 5 6 138 199 S <t< td=""><td>46 M L S 5 3 136 197 147 47 M L S 5 4 130 185 148 48 M L W 5 9 136 195 150 49 L W 5 5 133 190 147 50 M M S 5 7 142 210 154 51 M L S 5 6 133 194 144 52 M D S 5 2 139 202 153 53 M D S 5 2 139 202 153 54 M M S 5 6 133 194 144 47 M M S 5 8 132 195 149 55 M L S 5 8 132 195 149 55 M L</td></t<>	46 M L S 5 3 136 197 147 47 M L S 5 4 130 185 148 48 M L W 5 9 136 195 150 49 L W 5 5 133 190 147 50 M M S 5 7 142 210 154 51 M L S 5 6 133 194 144 52 M D S 5 2 139 202 153 53 M D S 5 2 139 202 153 54 M M S 5 6 133 194 144 47 M M S 5 8 132 195 149 55 M L S 5 8 132 195 149 55 M L

-				Glas MALES.	sgov	v Dis	stric	t As	sylu	m (MALES.	h).		
No	Colour Character		of Nose.	Stature.	(Cranial Characte		No.	Col Chara		of Nose.	Stature.		Cranial Characte	r.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 123 124 125 129 130 131 134 135 136 137 138 144 144 145 146 147 148 149 150 160 160 160 160 160 160 160 16	M M M M M M M M M M M M M M M M M M M	D D M D L M M L L L L M D L L L L L D L L M M L M D D D L L M L L L D M M D L M M L M L	assessessessesses Assessessesses Assessessessessessessessessessesses	$\begin{smallmatrix}2&3&7&3&8&0&9&6&2&2&9&5&7&1&6&8&2&7&6&3&3&9&6&8&8&2&6&8&7&3&0&6&6&2&8&5&5&6&4&2&5&9&1&6&4&8&5&3&6&1&7&7&6&2&8&1&5&4&2&6\\5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5$	131 134 137 134 127 137 137 134 132 137 131 132 131 132 131 132 131 130 133 129 134 139 140 139 127 135 133 129 134 139 121 130 135 129 121 130 135 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 129 121 130 133 135 129 121 130 133 135 129 121 130 133 135 129 134 141 152 139 134 141 137 135 136 136 136 136 137 133 134 144 133 127 133	186 192 194 189 201 199 203 193 196 192 189 188 186 203 181 190 200 207 210 207 194 195 190 200 187 179 200 211 188 196 195 190 201 201 190 201 190 201 187 179 200 211 188 196 195 190 190 190 191 181 194 195 190 190 190 191 181 184 195 193 196 187 191 184 195 193 196 187 191 184 200	150 149 153 148 152 151 155 152 151 155 152 151 153 156 146 153 159 156 146 152 147 148 134 149 159 149 152 147 149 153 153 159 149 159 159 147 147 149 159 159 149 149 149 149 149 149 149 149 149 14	151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 170 171 172 173 174 175 176 177 178 177 181 182 183 184 185 186 187 189 190 191 192 193 194 195 196 206 207 208 209 210	M M M M M M M M M M M M M M M M M M M		RESERVED TO SERVED $\frac{42245153968596979111450270862175667244634244569065922380348532}{55555555555555555555555555555555555$	140 138 132 135 137 142 133 137 142 134 131 136 138 133 132 135 128 144 140 136 138 128 131 132 133 132 133 132 135 142 136 137 142 138 144 140 136 137 142 143 144 140 140 140 140 140 140 140	199 196 186 195 182 196 199 192 203 192 202 195 181 196 199 195 190 193 189 200 189 200 189 201 180 200 189 203 197 195 194 180 200 189 194 188 190 193 186 183 177 195 188 198 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 188 199 194 189 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 194 195 198 199 199 199 199 199 199 199 199 199	15% 144 144 155 154 144 145 155 156 157 157 157 157 157 157 157 157 157 157	

			X1	Glas	gow	<i>Di</i> s	trict	As	ylui	n (Ga		h).		
	Colo		lose.	MALES.		Cranial				our	Nose.	MALES.		Cranial	
No.	Chara		Shape of Nose.	Stature.	Н.	Characte	B.	No.	Character.		Jo	Stature.	H. L.		в.
	Hair.	Eyes.	Sha	ft. in.	mm.	L.	mm.		Hair.	Eyes.	Shape	ft. in.	mm.	mm.	mm.
211 212 213 214 215 216 2217 2218 2219 2221 2224 2225 2224 223 2224 223 223 234 234 231 232 234 231 232 234 241 242 243 244 245 246 247 248 249 241 242 243 244 245 246 247 248 249 247 248 249 249 241 249 241 241 242 243 244 245 246 247 248 249 249 249 241 241 241 241 241 241 241 241 241 241	D M D M M M M M M M M M M M M M M M M M	D L L L D D D D L L D D M L D L L L L L	a A Ausananananana Ausananananana Ausana Ausananana	4933811832477678480759137343198428957642425 555555555555555555555555555555555	131 136 134 134 137 136 121 122 122 122 123 134 131 136 139 136 141 143 136 141 143 136 141 143 136 141 143 139 139 139 139 139 139 139 13	199 205 210 199 202 194 164 190 189 181 190 195 202 206 190 202 206 190 202 191 185 185 189 191 195 198 197 192 200 195 189 196 199 188 187 192 198 197	145 145 157 152 157 151 140 148 143 151 144 150 152 159 157 151 145 157 151 145 145 149 157 153 150 149 150 152 151 148 145 149 150 152 151 148 145	254 255 256 257 258 259 260 261 263 264 265 266 267 268 269 271 272 273 274 275 276 277 278 280 281 282 283 284 285 289 290 291 292 293 294 295	M M M M M M M M M M M M M M M M M M M	M L D L L L L L L L D L M M L D D D L L L M D L D D L L L M D L D D L L L M L L D M L D M L D D D L L L M L L D M L L D M L D D D D	Sesson Andrew Andrews and and andrews and andrews Andr	56 55 <	143 140 142 140 135 135 131 134 133 137 137 138 130 140 134 138 141 133 134 133 131 131 133 134 132 133 131 131 133 134 132 138 134 138 131 131 133 134 138 131 131 133	208 204 203 196 194 184 195 201 201 198 191 197 177 189 207 188 196 189 202 193 198 186 200 204 194 194 195 205 194 195 205 194 195 206 206 207 207 207 207 207 207 207 207 207 207	169 150 155 149 155 149 155 157 149 149 157 160 155 149 161 155 161 155 161 155 161 161 155 161 161
			X	MALES.		ow E	Distri	ict /	4syl	lum	(1	Lenzie MALES			
1 2 3 4 5 6 7 8 9	M M D M M F R M M M	L D L M M L D	R SW R SS SS SS SS	5 8 5 4 5 8 5 6 5 3 6 0 5 5 5 10 5 1	131 137 136 132 134 134 138 137 123 134	197 195 201 190 187 206 197 194 179	140 149 156 154 147 159 146 154 132	11 12 13 14 15 16 17 18 19	M M M M M M M M M	M D L M L L L		5 4 5 9 5 6 5 8 5 7 5 3 5 7 5 7 5 9	137 144 134 127 130 137 137 136 141	205 209 197 199 190 201 196 199 209	16: 150 149 15' 149 149 144 144 15

			ΧI	I.—GI	asgo	w D	istri	ict A	ls <i>yl</i>	um	(L	.enzie	·).		
				MALES.								MALES.			
No	Colour Character. Stature. H. L. B.							No.	Colour Character.		e of Nose.	Stature.	Cranial Character.		
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
21 22 23 24 25 26 27 28 29 30 31 32 33 34 43 44 45 46 47 48 49 50 51 52 53 54 66 57 57 58 66 67 77 77 78 80 80 80 80 80 80 80 80 80 80 80 80 80	MM MM MM MM MM MM MM MM MM MM MM MM MM	LLLDMLLLLLDLLLLDLLLLMDLLLLMDDDLLLDLLLLMDDDLLLDLLLLMDDDDLLDLL	asasasasasasasasasasasasasasasasasasas	634355763866656374866955493349547784442519305686243533966554 555555555555555555555555555555555	130 135 135 135 136 137 138 139 135 134 135 134 135 136 137 138 137 138 137 138 137 138 137 138 137 138 137 138 137 138 137 138 137 138 137 138 137 138 139 137 138 139 137 138 139 139 139 139 139 139 139 139	202 200 193 209 202 197 196 196 197 199 189 190 189 191 194 202 185 191 194 205 193 190 189 190 189 195 191 194 205 193 190 189 190 190 189 190 190 190 190 190 190 190 19	142 149 152 154 153 149 151 154 156 146 154 147 147 148 147 148 147 154 148 147 154 148 147 148 147 148 149 151 148 149 151 148 149 151 149 149 149 149 149 149 149 149 149 14	81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 111 112 113 114 115 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 139 130 130 130 130 140 150 160 170 180 190 190 190 190 190 190 190 19	M D D D D D D D D D D D D D D D D D D D	$\begin{smallmatrix} L M L L L M D D L D L L M M L L L D M D L D L$	a Assarbase Assa	835388323532440319201787651186518676770330111672735454856127179	140 141 134 128 129 134 139 135 136 137 142 121 135 136 137 142 123 135 136 137 141 132 135 136 134 140 135 136 134 141 132 135 136 134 141 132 135 136 134 141 132 135 136 137 131 132 134 135 136 137 131 132 133 134 135 136 136 137 131 132 133 134 135 136 136 137 131 132 133 134 135 136 137 131 132 134 137 131 132 134 137 131 134 137 131 132 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 134 137 131 133 134 137 138 138 138 138 138 138 138 138	191 194 188 191 178 192 189 200 189 188 187 185 188 189 202 207 200 194 186 199 199 198 197 188 197 188 196 196 196 192 200 192 192 187 191 186 194 187 191 186 194 187 197 190 182 197 190 182 197 197 190 182 197 197 190 182 197 197 197 197 197 197 197 197 197 197	148 156 159 137 147 134 151 148 151 148 151 129 149 150 155 142 150 155 142 160 145 145 146 151 148 150 155 142 150 141 153 151 148 151 148 151 148 151 148 151 155 148 150 155 148 150 155 148 150 150 150 150 161 161 161 161 161 161 161 161 161 16

	\		χ	(II.—G	lasg	ow I	Distr	rict	Asy	lur	n (l	Lenzi	e).		
				MALES								MALES			
No.	Col Chara	lour acter.	of Nose.	Stature.		Cranial Charact		No.	Col Chara	lour acter.	of Nose.	Stature.		Crania Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
141 142 143 144 145 146 150 151 152 153 154 155 166 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 177 178 181 182 183 184 185 186 187 188 189 190 191 192 193 194 199 199 200	DFDMMMMMDMMMMDMMMMDDDMMMMDDMMMMMDDMMMMMDDMMMM		SSA ASSESSESSESSESSESSESSESSESSESSESSESSESSE	7649574785995865209053483517354677795113858742046885867446675014 555555555555555555555555555555555555	138 136 140 138 132 135 135 133 139 136 130 140 140 134 139 131 134 139 131 134 139 131 134 139 131 134 139 131 134 139 131 134 139 135 147 144 139 131 134 133 135 147 144 139 131 134 133 135 147 144 139 131 134 133 135 147 144 139 131 134 133 135 147 144 139 131 134 133 135 147 144 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 131 139 139	196 203 188 190 198 1992 208 1992 208 1992 190 185 193 193 200 188 193 196 218 197 191 201 180 200 198 193 199 200 185 193 198 201 198 193 198 201 198 193 198 201 187 187 200 203 199 200 185 194 202 182 191 187 187 200 203 199 191 187 187 200 203 199 191 187 187 200 203 199 191 187 187 200 203 199 191 187 187 200 203 199 191 187 187 200 203 199 191 187 187 200 203 199 191 189 193 194 196 189 193 199 191 189 192 176	151 152 147 146 149 155 156 149 160 156 143 151 154 152 153 147 140 154 149 159 159 158 150 140 141 155 158 150 141 155 158 150 141 155 158 159 159 160 160 160 160 160 160 160 160 160 160	201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 221 222 223 224 225 228 229 230 231 232 233 234 235 236 237 238 239 240 241 242 242 243 244 245 246 247 248 249 240 251 251 261 271 271 271 271 271 271 271 27	M	M M L L D M M D D L M M M D L L M M L L D D L L L M M L L D D L L L M L L D D L L L M M L L L D D L L L M M L L L D D L L L M M L L L M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L L L M M M L M	SSWWSSSSSSSWWWWWWWSSSSSSSWWSSWWWWWWWWW	$\begin{array}{c} 3 \\ 6 \\ 6 \\ 3 \\ 7 \\ 8 \\ 11 \\ 0 \\ 5 \\ 6 \\ 5 \\ 4 \\ 10 \\ 0 \\ 5 \\ 6 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5$	140 132 134 136 139 149 136 137 133 136 142 135 135 135 137 133 136 143 131 144 132 143 144 134 143 144 135 137 133 136 134 136 134 136 134 136 134 136 134 136 134 136 134 136 134 136 134 136 136 134	204 187 208 199 195 189 193 185 202 195 202 185 190 192 189 188 185 205 192 190 192 193 200 192 201 190 185 191 190 187 194 202 201 199 201 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 187 194 190 188	163 1536 1536 1546 1546 1546 1546 1546 1546 1546 154

			:	MALES.								MALES.			
No.	Colo Chara		of Nose.	Stature.		Cranial haracte	r.	No.	Colo Chara		of Nose.	Stature.	1		
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
261 262 263 264 265 2664 2266 2267 2273 2274 2274 2274 2274 2278 2282 2282 2282	M M F M M D M D M M M M M	D M D M D L L L M M L D D M M L D D L L M D L D L	Annuar annuar Annuar an	$\begin{array}{c} 6 \ 57 \ 40 \ 68 \ 176 \ 168 \ 580 \ 641 \ 523 \ 246 \ 0110 \ 284 \ 33 \ 3775 \ 1171 \ 832 \ 000 \ 011 \\ \hline \\ 6 \ 57 \ 57 \ 57 \ 57 \ 57 \ 57 \ 57 \ $	131 135 143 145 139 137 142 137 135 142 125 148 149 153 134 131 131 131 131 131 131 131 131 13	196 201 207 204 192 191 193 193 188 189 195 202 197 195 197 195 197 196 182 199 186 186 201 182 193 185 194 189 191 182 193 185 194 189 191 182 196 196 196 196 196 196 197 197 198 198 199 191 185 196 196 196 197 197 198 198 199 191 185 196 196 196 197 198 199 191 185 196 196 197 198 198 199 191 185 196 196 196 197 198 198 198 199 198 198 198 198 198 198	151 150 161 158 148 152 157 155 143 142 154 150 151 156 148 149 143 153 153 154 153 153 154 156 147 143 146 159 151 156 147 148 147 146 159 151 156 148 149 151 151 156 149 151 153 153 154 155 157 158 158 158 158 158 158 158 158 158 158	317 318 319 320 321 322 323 324 325 326 327 328 329 330 331 332 333 334 341 342 343 344 345 346 357 358 360 361 362 363 364 365 366 367 368 369 371	M D D M M D M M D M M M D M M M D M M M D M M M D D M M M D D M M M D D M M M D D M M M D D M M M M D D M M M M D M M M D M M M M D M M M M D M M M M D M M M M M D M M M M M D M M M M M M M D M		BAAACCURUUUAAACAUUUAAAAAUUUUAAAAAUUUUAAAAAAAA	2 4 7 6 2 5 3 8 0 6 0 4 5 5 6 3 4 6 7 5 1 0 4 5 1 1 1 1 5 4 1 1 5 4 3 7 3 5 7 5 6 4 6 6 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5	130 130 130 132 136 132 133 133 133 135 135 135 138 129 129 139 133 133 132 133 137 138 134 141 126 143 136 139 139 139 138 131 137 138 139 139 139 139 139 139 139 139 139 139	203 198 190 200 186 196 184 198 190 201 193 188 195 197 192 188 187 199 197 183 189 197 183 184 182 191 200 194 195 197 196 197 196 198 199 199 199 199 199 199 199 199 199	18 14 14 15 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16

				X	///.—	Gova	an E	istr	ict	Asj	/lu	m.			
				MALES.							1	MALES.			
No.		our acter.	Jo.	Stature.		Crania Characte		No.		lour acter.	of Nose.	Stature.		Crania Charact	
	Hair.	Eyes.	Shape	ft. in.	H. mm.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
1 2 3 4 4 5 6 6 7 8 9 10 112 13 14 15 16 17 18 19 20 12 22 32 4 25 27 28 29 30 31 32 33 34 41 42 43 44 45 6 47 48 49 50 51 52 53 54 55 56 57 8 59 60	MM MM MM MM MM MM MM MM MM MM MM MM MM	$\begin{smallmatrix} L & M & M & L & L & D & D & L & L & L & M & M & L & L & D & D & L & L & L & D & D & L & L$	annanana Kon Kon Kanananana Kon Kana Kana	$\begin{matrix} 681856789473989178796767786085205664347796079153690416646854 \\ 55655555555555555555555555555555555$	145 131 137 138 137 138 137 138 139 132 132 133 138 154 137 145 137 145 137 145 137 145 137 141 141 130 135 141 141 133 134 136 132 138 134 131 135 133 134 136 132 142 143 135 141 141 135 135 142 142 143 139 149 140 135 135 145 137 146 146 141 132 142 144 124 132 142 144 124 132 142 144 124 132 144 132 144 132 144 134 136 146 141 132 142 144 134 137 146 146 141 132 142 144 134 136 137 146 146 141 132 142 144 134 137 146 146 141 132 142 144 134 137 146 146 141 132 142 144 134 137 146 146 141 132 142 144 134 137 146 146 141 132 142 144 134 135 136 136 137 137 138 139 149 140 135 135 135 135 135 135 135 135 135 136 137 137 138 139 139 149 140 135 135 135 135 135 135 135 135 135 136 137 137 138 139 149 140 135 135 135 135 135 135 135 135 135 136 137 137 137 138 139 139 139 139 139 139 139 139 139 139	199 191 194 197 198 203 181 190 196 189 196 204 206 197 210 201 190 198 201 199 197 193 194 197 193 183 191 200 204 202 196 189 199 205 192 199 200 200 196 210 199 219 219 219 219 219 219 219 219 219	155 145 145 151 154 152 148 147 151 148 157 163 154 151 144 152 163 154 148 145 148 145 148 145 148 147 148 153 144 145 146 153 154 157 163 163 163 164 165 165 165 165 165 165 165 165 165 165	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 110 102 103 104 105 106 110 110 111 111 115 116 117 118 119 110 111 111 111 111 111 111 111 111	D M D D D M M D D D M M M M M M M M M M		ananananasanasanasanasanananananananana	$\begin{smallmatrix} 6&6&6&117&9&9&8&7&8&8&8&6&7&11&8&5&7&6&6&3&1&6&1&9&5&8&5&7&6&8&2&2&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5&5$	124 123 139 137 136 136 137 135 139 142 138 136 139 134 141 147 138 136 139 134 134 134 134 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 133 135 141 142 135 143 141 142 143 143 144 144 147 148 148 149 149 141 141 141 141 141 141 141 141	191 193 203 203 193 192 192 196 198 199 201 189 193 195 189 193 196 196 197 199 191 189 193 196 196 197 198 199 199 195 189 191 189 199 199 199 199 199 199 199	146 146 148 153 143 143 146 149 154 157 150 146 159 158 154 142 155 150 147 151 148 154 150 141 148 154 150 141 150 141 150 141 150 141 150 141 150 141 150 141 150 141 150 141 150 141 150 141 150 140 140 140 140 140 140 140 140 140 14

				XI	//,	Gova	ın D	istr	ict .	Asy	lui	n.			
	1 m			MALES.							-	MALES.			
No.		lour acter.	Jo J	Stature.	C	Cranial Characte		No.		lour acter.	of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
121 122 123 124 125 126 127 128 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 161 162 163 164 165 167 168 169 170 171 172 173 174 175 176 177 178 179 180	M M M M M M M M M M M M M M M M M M M	M L M M L D L L D L L D L L D L L D L L D L L D L L D L L D L L D L D L D L L L D	a Azoros a consequence a conse	$\begin{matrix} 681094398128597518556993761712666489843391120638000802175745 \\ 55555555555555555555555555555555$	129 139 133 141 140 133 134 134 138 137 142 139 138 141 131 136 135 137 128 136 135 134 133 158 141 127 133 141 140 132 135 130 125 130 125 130 127 128 131 140 132 135 130 127 127 127 127 127 127 127 127 127 127	193 194 180 202 197 208 197 210 196 178 189 202 193 197 192 191 194 191 195 198 201 188 195 202 183 198 184 204 198 195 208 189 197 200 180 180 180 180 191 201 196 208 189 191 201 196 208 189 191 201 196 208 189 191 201 196 208 189 197 206	147 152 147 153 157 152 141 151 144 158 155 150 145 155 150 145 155 150 147 148 155 150 147 148 155 150 147 148 157 149 153 154 155 147 147 148 158 157 159 160 160 161 160 161 160 161 160 161 160 160	181 182 183 184 185 186 187 188 190 191 192 193 194 195 196 200 201 202 203 204 205 206 207 208 209 211 212 213 214 215 216 217 218 219 220 221 223 224 225 226 227 228 229 230 231 232 233 234 235 238 239 240	D M M M M M M M M M M M M M M M M M M M	L M L O L L L L D O L M L L D O M M M L L D D M M M L L L L L M M L L L L	anna farannannannannannannannann fannannann fannannannannannannannannannannannannann	$\begin{array}{c} 9847167576686706664726010984651101462333911611456674830578888757 \\ 5555555555555555555555555555$	135 139 134 134 136 135 135 135 136 148 136 136 137 141 140 140 140 141 142 144 126 137 141 141 129 141 141 129 137 141 142 137 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 142 136 137 141 141 141 142 136 137 141 141 141 142 136 137 141 141 141 142 136 137 141 141 141 141 141 131 142 136 137 141 141 141 141 141 141 141 14	199 200 197 193 191 194 194 194 199 190 195 192 198 193 200 195 201 199 173 201 199 173 201 199 173 201 199 173 201 199 173 201 199 173 201 199 173 201 199 179 206 198 202 188 195 185 202 201 199 189 200 195 191 197 206 202 194 184 198 207 214 202 290 193 202 203	153 152 152 142 150 151 145 148 147 148 151 155 154 157 155 146 159 160 152 157 144 152 161 152 159 161 152 154 161 153 153 154 161 163 153 154 161 163 163 163 163 163 163 163 163 163

XIIIGovan	District	Asylum.
AIII.—GUYUII	DISTING	Maylulli.

			1	MAL	ES.								MAI	LES.			
No.	Cole Chara		of Nose.	Stat	ure.		Cranial Characte		No.	Col Chara		of Nose.	Stat	ure.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
241 242 243 244 245 246 247 248 249 250 251 252 253	M M M M M D M M M M M	D L M M L M L D L	SSC Noss Noss S	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	5 7 10 8 8 6 3 9 7 6 8 6 7	133 137 141 135 134 141 135 134 139 137 136 138	195 200 200 192 201 193 185 195 200 203 190 195 194	144 150 155 144 155 154 148 151 156 153 138 158 152	254 255 256 257 258 259 260 261 262 263 264 265	D M M M M M M M M M M	M D L L L L L L L L L	SSS RSSSSSSS W	5555555655	10 7 9 2 6 6 7 5 1 5 4	138 135 138 139 125 133 130 133 133 134 140	200 196 188 190 207 195 189 191 198 194 201 211	154 147 150 155 158 150 152 145 155 151 157 158

XIV.—Haddington District Asylum.

	MALES.	MALES.
2 M L S S M L S S S S S S S S S S S S S S	S	35 D L S 5 11 142 202 153 36 M L S 5 10 139 200 153 37 M D S 5 11 138 193 156 38 D M S 5 5 129 195 153 39 D L S 5 8 139 192 145 40 M L W 5 1 137 198 151 41 M L S 5 7 139 190 159 42 M L S 5 3 126 191 138 43 M L S 5 1 145 205 154 44 D D S 5 8 143 198 157 45 M L S 5 8

				XV.	-/n	/ern	ess l	Dist	rict	As	ylu	ım.			
				MALES.								MALES	•		
No.	Colo Chara		of Nose.	Stature.		Cranial Characte	r.	No.	Colo Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft in.	H.	L.	B.	ir.	Hair.	Eyes.	Shape	ft. in.	H. mm.	L.	B. mm.
1 2 2 3 4 4 5 6 7 8 9 10 1 1 2 2 1 3 2 4 4 1 1 1 2 1 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	M	M M L D D M M L M L M L M L M M M M M M	and and and and and and and and and and	5561420131670924397585072579734711479935378648736575981487854 555555555555555555555555555555555	131 139 131 131 131 131 131 131 131 131	193 198 191 190 205 209 194 202 187 192 200 199 189 201 192 200 193 194 197 200 196 202 183 199 187 196 202 183 199 197 196 200 198 198 200 198 198 200 191 193 196 193 196 193 196 197 196 198 197 196 198 197 198 200 199 197 198 200 199 197 198 200 199 193 198 200 199 193 198 200 199 193 198 200 199 193 198 200 199 193 198 200 199 193 193 196	151 153 146 158 154 154 153 157 150 154 147 151 152 160 154 151 152 160 154 151 152 156 154 151 155 151 155 151 155 151 155 155	61 62 63 64 65 66 67 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 88 89 90 91 92 93 94 95 100 101 102 103 104 110 110 111 112 113 114 115 116 117 119 119 119 119 119 119 119 119 119	FD DD FD M :: :: :: :: :: :: :: :: :: :: :: :: :	M M M D L M L L L M M M M L M L M M M M		$\begin{array}{c} 5 & 5 & 5 & 4 & 8 & 7 & 11 & 7 & 6 & 1 & 11 & 6 & 7 & 6 & 5 & 3 & 6 & 6 & 11 & 9 & 4 & 5 & 6 & 4 & 6 & 3 & 6 & 6 & 3 & 6 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	140 147 140 139 132 131 133 143 132 125 140 155 138 134 132 125 131 153 158 139 130 151 153 158 139 130 141 141 140 144 136 137 131 133 144 134 135 146 137 137 138 139 130 131 131 131 131 133 143 144 136 137 137 138 139 130 131 131 131 131 131 131 131 131 131	203 198 197 196 197 201 198 198 198 198 196 196 196 196 196 196 196 196 196 197 198 200 185 188 205 205 194 199 185 197 186 207 198 207 198 207 198 207 198 207 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 199 183 195 201 197 193 201 191 196 196 196 196 196 197 197 198 200 198 201 197 198 201 198 201 198 201 197 198 201 201 201 201 201 201 201 201 201 201	1555 1546 1576 166 1577 166 1576 1536 1551 1548 1551 1551 1551 1551 166 152 166 152 166 152 166 152 166 152 166 153 166 166 167 168 169 169 169 169 169 169 169 169 169 169

				XV.	_Inv	erne	ess <i>L</i>	Dist	rict	As	yμ	ım.			
				MALES.								MALES.			
No.	Colo Chara		of Nose.	Stature.		Cranial Characte	er.	No.	Col Chara		of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 138 139 140 141 142 143 144 145 150 151 151 151 151 156 161 162 163 164 161 162 163 164 167 170 171 172 173 174 175 176 177 178 179 180	M D D	M M D M M M M M M M M M M M M M M M M M	ananananasanasanananananananananananana	$\frac{1585724584888954781711300343148626467999908766603287647699}{55555555555555555555555555555555555$	136 141 146 141 145 131 138 134 145 143 138 134 145 142 136 131 136 139 124 139 125 130 136 126 129 138 125 130 136 126 121 126 137 134 138 137 140 135 130 140 136 131 136 131 136 131 136 131 136 131 137 140 135 130 140 136 131 133 134 135 131 133 134 135 131 133 134 135 131 133 134 135 131 133 134 135 131 133 134 135 136 131 133 134 135 136 137 137 138 138 138 138 138 138 138	198 199 203 207 204 200 198 198 198 198 198 191 184 204 195 191 199 195 197 194 192 199 196 188 190 200 188 199 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 197 203 208 198 199 197 200 184 191 198 198 197 192 197 200 188 188	145 158 150 152 158 160 152 144 149 156 156 157 150 158 148 151 160 155 148 151 150 160 155 153 155 148 147 150 155 146 150 155 153 155 148 147 150 155 148 147 150 155 148 147 150 155 146 150 155 155 166 150 157 153 150 151 155 146 152 159 153 150 155 156 160 1656 160 1656 160 1656 1655	181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 200 201 202 203 204 205 206 207 208 209 210 212 213 214 215 216 217 218 220 221 222 223 224 225 226 227 228 229 230 231 232 234 235 236 237 238 239 240	DM	D M L D M M M L M M M M M M M M M M M M	a a a a a a a a a a	56 58 88 65 58 88 78 97 84 51 50 44 17 76 36 66 73 07 86 87 9 5 5 5 5 5 <	129 140 126 138 133 134 139 130 144 153 139 131 126 127 139 135 136 128 134 138 149 131 138 149 131 138 140 139 141 133 127 145 136 135 147 136 135 147 136 135 147 136 135 143 143 143 142 135 144 132 135 145 145 145 136 137 145 145 145 145 145 145 145 145 145 145	198 197 185 198 196 199 198 197 199 198 197 199 198 192 182 193 195 196 201 199 197 191 182 206 203 186 204 195 201 193 197 190 206 193 197 190 206 193 197 198 202 196 193 197 198 202 196 193 197 198 202 196 193 197 199 197 198 199	1555 1611 1477 1577 1511 1499 152 1546 1545 1566 1544 1577 1555 1566 1544 161 153 1577 154 1571 1571 1571 1571 1571 1571

XVInverness	District	Aevlum.
VAIIIIACLIICOO	DISTINGT	MSylulli.

				MALES								MA	LES.			
No.	Colo Chara		of Nose.	Stature.		Cranial Characte		No.	Col Chara		of Nose.	Stat	ture.		Cranial haracte	
	Hair.	Eyes.	Shape of	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L. mm.	B. mm.
241 242 243 244 245 246 247 248 250 251 252 253 255 256 267 262 263 262 263 264 264 265 265 266 267 262 263 264 264 265 266 267 266 267 268 268 269 269 269 269 269 269 269 269 269 269	M D D D D D D D D D D D D D D D	M M L L D M M M M M M M M M M M M M M M	anna Pananananananananananananananananan	5 4 5 11 5 7 5 10 5 4 5 5 6 5 5 10 5 5 6 6 5 5 6 7 5 5 6 6 5 10 6 7 7 7 8 7 8 7 8 7 8 7 8 7 8 7 8	139 134 133 139 131 124 129 139 137 131 120 126 138 137 131 129 126 138 137 131 129 139 137 131 129 139 137 131 129 139 139 137 131 129 139 139 139 139 139 139 139 13	196 206 193 199 195 186 191 202 193 190 195 187 195 175 191 185 204 176 196 199 198 202	150 159 156 157 150 149 158 151 161 149 152 141 154 145 153 132 149 155 149 155 149	267 268 269 270 271 272 273 274 275 277 278 279 281 282 283 284 285 286 287 288 289 290	D M M M D R D D M D D D D M M D D D D M M D D D D	M M M M M M M M M M M M M M M M M M M		555565555555565555555555555555555555555	$\begin{array}{c} 5\\ 7\\ 7\\ 7\\ 0\\ 7\\ 9\\ 3\\ 7\\ 8\\ 8\\ 0\\ 7\\ 8\\ 3\\ 4\\ 7\\ 7\\ 6\\ 8\\ 6\\ 10\\ \end{array}$	132 139 140 147 138 126 137 126 133 127 133 137 159 138 140 142 134 127 134 121 136 131 136 131 136 131	186 194 196 217 198 187 198 190 201 191 192 203 193 206 202 197 193 193 204 195 199 198 205	151 146 151 164 150 148 161 150 157 149 151 164 153 152 157 148 153 153 153 155 157

XVI.—Lanark District Asylum.

				MALES.								MALES.			
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 22 23 24 25	M D D M M M D D M M M M M M M M M M M M	L D M L L D L L L M M M L L D D L L L L	SWSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	5 7 9 4 8 6 4 6 5 5 6 6 5 5 5 5 4 8 6 5 5 5 5 5 5 6 6 5 5 5 5 5 5 6 6 5 5 5 5 6 6 5 5 5 5 6 6 5 5 6 6 5 5 6 6 5 5 6 6 5 6 6 5 6 6 5 6 6 5 6	137 135 137 134 139 133 137 137 139 141 140 139 138 148 142 141 133 125 143 144 136 143 151	198 196 194 193 201 187 183 190 194 198 199 196 198 199 204 188 187 203 198 204 193 206 208 194	153 151 153 154 161 146 149 156 147 143 158 149 153 153 144 149 156 145 152 152 152	26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50	M M D D M M R D D D M M D D D D M M M D D D D	L L L L L M D L D D L L L L M L L M M L L D M M L D M M L D M M L D M	WSSWSSRSRWWWWSRSSWSSSSSSSSSSSSSSSSSSSS	5 5 6 6 6 3 4 4 5 9 7 1 5 6 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	129 141 139 151 145 138 138 136 136 136 136 136 136 137 141 142 142 143 141 137 135 142 144	196 194 199 212 217 197 198 202 203 192 193 203 186 198 199 187 193 200 187 193 200 187 193 200 187 204 199 198 201 205	151 149 153 157 160 158 162 149 155 146 159 150 158 146 151 152 143 151 149 152 143 156

				MAI	LES.							1	MAL	ES.			
No.	Col- Chara		of Nose.	Sta	ture.	C	Cranial Characte		No.	Col Chara	our acter.	of Nose.	Sta	ture.		Crania Characte	
	.:	s,	be (H.	L.	В.		:	y,	be (Н.	L.	В
	Hair.	Eyes.	Shape	ft.	in.	mm.	mm.	mın.		Hair.	Eyes.	Shape	ft.	in.	mm.	mm.	mn
 51	D	M	s	5	7	144	202	164	111	M	M	s	5	6	134	195	15
52	M	L	w	5	5	142	196	156	112	M	M		5	5	126	190	14
53	D	\mathbf{D}	S	5	6	144	205	158	113	M	M	S	5	7	130	190	15
54	D	D	S	5	5	137	194	141	114	D	L	S	5	9	141	204	16
55	M	Ļ	S	5	9	139	199	150	115	M	Ļ	S	5	1	126	187	14
56	D M	$\frac{L}{M}$	$\frac{\mathbf{W}}{\mathbf{S}}$	5 5	4 5	$\frac{150}{136}$	$\frac{203}{188}$	$\frac{147}{150}$	116 117	M	L L	$\frac{S}{W}$	5	2 3	130 135	$\frac{196}{195}$	$\frac{15}{15}$
57 58	M	M	S	5 5	8	134	201	155	118	M M	L	S	5	6	138	198	lå
59	D	L	S	5	6	135	193	143	119	M	L	S	5	9	139	202	15
60	M	M	$\tilde{\mathbf{s}}$	5	7	143	203	164	120	Ď	$\vec{\mathbf{p}}$	$\tilde{\mathbf{s}}$	5	9	139	195	15
61	D	L	S	5	6	145	203	160	121	D	M	W	- 5	5	141	201	15
62	M	M	S	5	7	139	196	152	122	D	M	W	õ	5	142	197	15
63	D	L	W	5	7	137	199	158	123	M	D	S	5	5	130	190	14
64	M M	M L	S	5 5	$\begin{bmatrix} 5 \\ 2 \end{bmatrix}$	$\frac{138}{142}$	$\frac{193}{204}$	$\frac{153}{162}$	124	M	L	S	5 5	4 6	132 133	$\frac{195}{195}$	15
65	M	M	S	5	9	139	204	146	125 126	M D	M D	$_{ m W}^{ m C}$	5	8	136	198	$\frac{14}{15}$
67	M	L	s	5	9	142	199	160	127	Ď	Ď.	w	4	6	133	185	15
68	D	$\bar{\mathbf{D}}$	$\tilde{\mathbf{S}}$	5	7	142	207	153	128	M	Ĺ	S	5	7	140	190	15
69	M	M	R	5	4	132	186	146	129	D	D	S	5	9	142	193	14
70	M	M	W	5	1	137	193	156	130	R	L	S	5	7	141	204	15
71	M	L	R	5	7	143	200	153	131	D	D	W	5	3	146	190	15
72	M	M	R	5	5	135	198	154	132 133	M	T.	S	5 5	2 4	137	188	14
$\frac{73}{74}$	D F	D L	\mathbf{v}	6 5	1 6	131 142	193 196	$\frac{149}{155}$	134	D D	L M	S	5 5	4	138 142	$\frac{191}{196}$	$\frac{14}{15}$
7 5	M	M	C	5	0	139	199	148	135	D D	M	S	5	8	131	197	14
76	D	$\mid \mathbf{D} \mid$	š	5	8	139	192	147	136	M	L	S	5	6	130	194	14
77	D	M	w	5	5	137	190	154	137	D	Ĺ	$\tilde{\mathbf{s}}$	5	5	131	189	13
78	D	D	W	5	4	129	200	144	138	D	D	S	5	5	133	201	15
79	D	L	S	5	4	133	193	148	139	D	D	S	5	3	138	201	15
80	M	M	S	5	2	129	186	153	140	D	L	W	5	3	136	191	13
81	M F	$\begin{array}{ c c } L \\ \end{array}$	S	5	4	133	184	140	$\frac{141}{142}$	M	M	S	5 5	4	140	$\frac{193}{200}$	15
82 83	M		S	5 5	6	134 142	$\frac{188}{194}$	$\frac{143}{152}$	142	1) M	$\begin{array}{c c} \mathbf{L} \\ \mathbf{L} \end{array}$	C R	5 5	3 5	139 136	192	15 14
84	D	L	S	5 5	4	121	183	140	144	M	L	W	5	7	140	192	15
85	M	M	S	5	8	140	199	144	145	M	L	s	5	5	139	195	14
86	D	D			10	140	202	153	146	M	L	S	5	4	143	201	15
87	M	M	SSS	5	11	135	197	151	147	F	L	W	5	3	133	188	14
88	M	L	S	5	4	136	189	147	148	D M	M	S	4 5		137	187	15 14
29	M	L	S	- 5	3	143	191	152	149					1 1	132	189	

No.			of	Sta	ture.				No.			Jo	Star	ture.			
	i.	es.	tpe			H.	L.	В.		ij.	s, di	ıpe			H.	L.	В.
	Hair.	Eyes.	Shape	ft.	in.	mm.	mm.	mın.		Hair.	Eyes.	Shape	ft.	in.	mm.	mm.	mm.
51	D	M	s	5	7	144	202	164	111	М	М	g	5	6	134	195	155
52	M	L	w	5	5	142	196	156	112	M	M	S	5	5	126	190	142
53	D	$\widetilde{\mathbf{D}}$	S	5	6	144	205	158	113	M	\dot{M}	$\tilde{\mathbf{s}}$	5	7	130	190	156
54	D	D	S	5	5	137	194	141	114	D	L	$\tilde{\mathbf{s}}$	5	9	141	204	160
55	M	L	S	5	9	139	199	150	115	\mathbf{M}	L	S	5	1	126	187	148
56	D	L	W	5	4	150	203	147	116	M	L	S	5	2	130	196	152
57	M	M	S	5	5	136	188	150	117	M	\mathbf{L}	W	5 5	3	135	195	150
58	M	M	S	5	8	134	201	155	118	M	L	S	5	6	138	198	154
59	D	L	S	5	6	135	193	143	119	M	F	S	5	9	139	202	153
60	M	M	S	5	7	143	203	164	120 121	D	D	S	5 5 5	9	139	195	$154 \\ 153$
61 62	D M	L M	S	5 5	6	145 139	203 196	$\frac{160}{152}$	122	D D	M M	W	- 5 - 5	5 5	$\frac{141}{142}$	$\frac{201}{197}$	152
63	D	L	W	5	7	137	199	158	123	M	D	s	5	5	130	190	140
64	M	M	s	5	5	138	193	153	124	M	L	Š	5	4	132	195	153
65	M	L	$\tilde{\mathbf{S}}$	5	2	142	204	162	125	M	M	$\tilde{\mathrm{C}}$	5	6	133	195	147
66	M	M	S	5	9	139	201	146	126	D	D	W	5	8	136	198	152
67	M	L	S	5	9	142	199	160	127	D	D	W	4	6	133	185	150
68	D	D	S	5	7	142	207	153	128	\mathbf{M}	L	S	5	7	140	190	150
69	M	M	R	5	4	132	186	146	129	D	D	S	5	9	142	193	142
70 71	M	M	W	5	<u>1</u>	137	193	156	130	R	L		5	7	141	204	153
71	$_{ m M}^{ m M}$	L	R	5	7	143	200	153	131 132	D	D	W	5 5	3 2	$\frac{146}{137}$	190	153 147
72 73	D	M D	$\frac{R}{W}$	5 6	5	135 131	198 193	$\frac{154}{149}$	133	\mathbf{D}	$egin{array}{c} \mathbf{L} \\ \mathbf{L} \end{array}$	S	5	4	138	$\frac{188}{191}$	147
74	F	L	S		6	142	196	155	134	$-\mathbf{D}$	M	20	5	4	142	196	150
75	M	M	Č	5 5	0	139	199	148	135	D	M	20000	5	8	131	197	149
75	D	D	š	5	8	139	192	147	136	M	L	š	5	6	130	194	149
77	\mathbf{D}	M	W	5	5	137	190	154	137	D	L	$\tilde{\mathbf{s}}$	5 5 5	5	131	189	136
78	\mathbf{D}	D	W	5	4	129	200	144	138	D	D	S S W	5	5	133	201	154
79	D	L	S	5	4	133	193	148	139	D	D	S	5	3	138	201	153
80	M	M	S	5	2	129	186	153	140	D	L	W	5 5	3	136	191	139
81	M	Ļ	S	5	4	133	184	140	141	M	M	S	5	4	140	193	150
82	F	Ļ	S	5	6	134	188	143	142	1)	Ļ	C	5	3	139	200	151
83	\mathbf{D}	L	S	5 5	$\frac{6}{4}$	142 121	194 183	$\frac{152}{140}$	143 144	M M	L	$\frac{R}{W}$	5 5	5	136 140	$\frac{192}{199}$	$\frac{147}{159}$
84	M	M	S	5	8	140	199	144	145	M	L	S	5	7 5	139	195	145
85 86	D	D	S	5	10	140	202	153	146	M	L	S	5	4	143	201	159
87	$\widetilde{\mathbf{M}}$	M	$ \tilde{s} $	5	11	135	197	151	147	F	$\tilde{\mathbf{L}}$	$\widetilde{\mathrm{w}}$	5	3	133	188	147
88	M	L	S	5	4	136	189	147	148	$\bar{\mathbf{D}}$	$\overline{\mathbf{M}}$	S		11	137	187	150
89	M	L	S	5	3	143	191	152	149	\mathbf{M}	L	S	5	1	132	189	146
90	M	\mathbf{L}	S	5	7	144	205	149	150	D	D	S	5	5	128	183	142
91	M	M	S	5	7	137	192	154	151	M	M	S	5	9	139	196	150
92	M	ho	S	5	10	136	188	160	152	M	M	S	5	5	127	193	152
93 94	D M	Ľ	SSS	5 5	6 5	$135 \\ 145$	202 193	$\frac{150}{154}$	153 154	D	D L	0	5 5	$\begin{bmatrix} 4 \\ 6 \end{bmatrix}$	$\frac{135}{134}$	183 191	$\frac{143}{150}$
95	M	Ď	w	5	5 5	139	202	$\frac{154}{160}$	155	Ď	M	SSS	5	4	136	197	153
96	D	Ď	w	5	4	140	202	147	156	M	L	S	5	8	145	198	154
97	M	Ĺ	S	5	6	142	209	157	157	Ď	M	$\ddot{\mathbf{s}}$		ıŏ	148	203	164
98	M	M	S	5	9	146	201	159	158	$\widetilde{\mathbf{M}}$	L	$\tilde{\mathbf{s}}$	5	9	139	192	150
99	D	M	S	5	10	133	193	146	159	\mathbf{D}	L	W	5	4	142	198	148
00	D	M	S	5	1	142	206	156	160	F	D	W	5	4	141	196	151
.01	M	M	S	5	6	140	196	154	161	D	D	S	5	7	141	204	152
02	M	L	S	5	6	133	189	144	162	M	L	W	5	6	131	183	134
103	M	M	S	5	7	130	186	148	163	M	Ļ	S	5	7	140	196	144
104	F M	L	W	5 5	8	135	$ \begin{array}{c c} 199 \\ 202 \end{array} $	$\frac{158}{149}$	164	M M	$_{ m L}^{ m L}$	$\frac{s}{w}$	5 5	$\begin{bmatrix} 4 \\ 10 \end{bmatrix}$	$\frac{138}{152}$	$\frac{203}{206}$	$\frac{153}{159}$
05	M	L	R	5 5	$\frac{6}{6}$	138 140	191	$149 \\ 152$	165 166	M	M	S	5 5	7	144	208	159
$106 \mid 107 \mid$	F	L	S	5	6	130	191	$152 \\ 152$	167	M	L	w	5	7	139	198	157
108	M	L	Š	5	5	134	203	154	168	\mathbf{p}	$\ddot{\mathbf{D}}$	S	5	ó	144	191	153
109	M	M	S	5 5 5	6	138	197	148	169	M	$\tilde{\mathbf{L}}$	$\widetilde{\mathbf{w}}$	5	8	143	197	153
110	D	L	S	5	2	133	192	149	170	M	L	W	5	4	143	203	156
110				-										-			

XVI.—Lanark District Asylum.

				MAI	ES.								MALES.			
No.	Colo: Charac		Shape of Nose.	Stat	ure.		Cranial haracte	r.	No.	Colo Chara		of Nose.	Stature.	(Cranial Characte	
	Hair.	Eyes.	Shape	ft	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
171 172 173 174 175 176 177 178 180 181 182 183 184 185 190 191 192 203 204 195 206 207 201 202 203 204 211 212 213 214 215 216 227 228 229 230	M D M D M M M M	MLDLLLMLLMDLLDMMLMMLMDMLDLMDLLDM :: LLLDLLLLLMLDDDMLMLDLLLLLDMM	asasasasasasasasasasasasas Andre And	455555555555555555555555555555555555555	$\begin{array}{c} 11 \\ 81 \\ 66 \\ 59 \\ 87 \\ 75 \\ 68 \\ 811 \\ 55 \\ 52 \\ 11 \\ 72 \\ 28 \\ 53 \\ 28 \\ 55 \\ 79 \\ 23 \\ 74 \\ 33 \\ 98 \\ 86 \\ 35 \\ \ldots \\ 27 \\ 846 \\ 85 \\ 266 \\ \end{array}$	142 136 127 131 140 135 150 146 131 133 144 138 138 142 141 132 136 140 131 131 136 142 131 131 136 140 131 131 131 131 131 131 131 131 131 13	198 195 174 201 195 200 206 203 184 200 192 196 192 202 177 190 196 190 201 205 193 191 203 191 195 190 202 193 188 194 193 207 198 197 201 186 187 201 189 197 202 187 198 209 163 197 198 209 163 197 198 209 167 198 209 169 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 197 202 189 193 206	148 150 130 148 150 158 161 142 162 151 152 149 150 155 152 145 158 150 157 153 147 149 152 153 148 151 152 153 148 151 152 155 148 156 149 152 155 148 156 149 152 155 148 156 149 155 158 156 149 155 158 156 149 155 155 148 136 149 155 155 148 136 149 155 155 148 136 149 155 155 148 136 149 155 155 148 136 149 155 155 148 136 149 155 155 156 161 150 155 155 156 161 156 161 156 161 156 165 155 15	231 232 233 234 235 236 237 238 239 240 241 242 243 245 250 251 252 256 260 267 268 269 270 271 272 278 278 279 280 283 284 285 289 280 290	M M M M M M M M M M M M M M D D D M M M D D D M M D D D D M M M D D D D M M M D D D D M	L D L L L M M D L L L D D L L D D L L L D D L D L	No No No Sand Andrew Constant	93332534458594676448804666656631655712667117433685888755451566154519428 555555555555555555555555555555555555	134 136 135 138 137 139 138 129 139 142 142 135 144 142 135 144 142 133 128 141 150 155 144 141 150 151 141 142 139 136 149 149 149 149 149 149 149 149 149 149	189 192 196 197 197 195 201 208 208 208 209 193 200 199 193 201 192 199 190 185 201 197 197 194 199 190 190 191 206 199 194 199 190 190 191 206 199 194 199 190 190 191 206 199 194 199 196 199 196 199 196 199 196 199 196 199 196 199 196 199 196 199 196 199 196 198 198 199 196 198 198 198 199 196 198 198 198 198 198 198 198 198 198 198	1389 157 151 144 155 156 144 155 156 146 157 157 158 158 158 158 158 158 158 158 158 158

			1	MAL	ES.				1				MALES.			
No.		our acter.	of Nose.	Stat	ure.	(Cranial Characte		No.	Col Char	our acter.	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H. mm.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
291 292 293 294 295 296 297 298 301 302 303 303 304 305 310 311 312 313 314 315 316 321 322 323 324 325 327 328 329 321 322 323 331 332 332 332 332 332 332	M M M M M M M M M M M M M M M M M M M	L L L L L L L L L L L L L L L L L L L	SSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	555555555555555555555555555555555555555	$\begin{array}{c} 11 \\ 9 \\ 3 \\ 10 \\ 5 \\ 5 \\ 8 \\ 4 \\ 8 \\ 6 \\ 3 \\ 7 \\ 0 \\ 6 \\ 1 \\ 6 \\ 4 \\ 4 \\ 5 \\ 5 \\ 5 \\ 4 \\ 4 \\ 0 \\ 6 \\ 9 \end{array}$	139 131 144 135 142 140 135 139 139 140 138 139 140 138 134 128 130 142 129 136 134 132 142 135 126 140 141 137 138 134 134 136 136 134 134 137 137 137 137 137 137 137 137 137 137	198 200 202 200 206 198 201 197 197 190 204 185 201 198 190 192 191 201 198 198 199 190 192 191 201 198 189 189 188 191 185 190 204 198 198 198 198 199 196 191 198 199 196 191 198 199 196 191 198 199 196 191 198 199 198 199 199 199 199 199 199	161 145 152 157 157 152 154 147 152 153 144 155 150 147 148 148 149 160 146 148 147 157 152 143 145 153 144 157 152 148 147 157 153 144 157 152 148 147 157 153 148 147 157 153 148 147 157 157 158 158 158 158 158 158 158 158 158 158	339 340 341 342 343 344 345 346 347 348 350 351 352 353 354 355 358 359 360 361 362 363 364 363 364 363 364 367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 381 381 381 381 381 381 381	M M M M M M M M M M M M M M M M M M M	L L L L M L L L L M M D L L L L M M L L L L	As Aucous Arsensus As Assess Assess Assess Assess	0 5 5 6 6 1 8 9 8 8 4 8 7 6 5 <td>129 142 144 141 148 144 140 141 132 143 143 144 142 134 144 139 146 141 137 165 134 141 135 135 134 141 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 134 137 135 134 141 139 137 132 133 142</td> <td>187 197 193 185 194 198 190 205 192 200 188 191 200 207 194 188 204 204 192 195 195 199 228 197 199 209 183 200 188 201 183 201 188 201 188 201 188 201 188 201 188 201 188 201 201 201 201 201 201 201 201 201 201</td> <td>144 155 144 155 151 151 151 151 151 151</td>	129 142 144 141 148 144 140 141 132 143 143 144 142 134 144 139 146 141 137 165 134 141 135 135 134 141 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 131 137 135 134 146 134 137 135 134 141 139 137 132 133 142	187 197 193 185 194 198 190 205 192 200 188 191 200 207 194 188 204 204 192 195 195 199 228 197 199 209 183 200 188 201 183 201 188 201 188 201 188 201 188 201 188 201 188 201 201 201 201 201 201 201 201 201 201	144 155 144 155 151 151 151 151 151 151
				XI	/// _x -	<i>IVI i</i>	dloti	hian	Dis	tric	t A	sy	lum.			
1 2 3 4 5 6 7	D D M F D F M	D D L M M L L	S W S W S S	5 5 5 5 5 5 5 5	8 2 6 1 3 4	150 131 146 157 128 133 141	196 197 195 218 182 190 187	162 141 149 157 138 152 152	8 9 10 11 12 13 14	D M D M D M M	L M L L L L L	SSS WSSS	5 8 .5 6 .5 9 .5 6 .5 7 .5 5 5 .5	148 145 143 141 155 141 141	192 194 198 206 191 198 202	163 153 160 154 150 149 152

				XVII.	[V] i	idlot	hian	Dis	stric	et /	4sy	dum.			
]	MALES.								MALES.			
No.	Cole Chara		of Nose.	Stature.		Cranial Characte	er.	No.	Col Chara		of Nose.	Stature.		Cranial Characte	er.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
15 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 16 17 18 18 18 18 18 18 18 18 18 18 18 18 18	M D D M M M M D D M M M D D M M M M D D M	L L L L L M M D M D L L M L L L L L L L	ossassassas Azassassassassassassassassassassassassass	93624191161367488395878311676085118425724666572970582117084 $555555555555555555555555555555555555$	145 142 145 137 141 149 132 125 141 140 141 145 137 140 141 145 137 139 133 128 147 137 139 133 128 147 137 139 136 141 142 143 132 141 136 140 152 150 129 140 130 140 149 140 145 136 140 149 140 143 139 134 139 134 139 134 139 134 139 144	202 202 206 199 189 196 198 190 190 190 190 190 192 185 194 197 193 192 196 204 197 193 192 196 204 197 188 197 199 199 199 199 199 199 199 199 199	159 155 151 155 150 146 157 147 140 157 155 146 157 151 150 159 155 147 161 155 149 144 160 150 157 143 158 151 154 155 150 148 150 148 150 148 150 148 150 148 150 148 151 156 148 157 150 166 153 158 154 155 158 154 158 155 158 154 158 155 158 154 158 155 158 159 158 159 158 159 158 159 158 159 158 159 158 159 158 159 158 159 158 159 159 158 159 159 159 159 159 159 159 159 159 159	75 76 77 78 78 79 80 81 82 83 84 85 86 87 89 90 91 92 93 94 95 96 97 100 101 102 103 104 105 110 111 112 113 114 115 116 117 118 119 120 121 123 124 125 126 127 128 130 131 132 133		MOLILLE MEDOMOLOLE MILLLLLLLLLLLLLLLLL MOLLMMMDOMLLLLLMLMLLLLLMLL	ananananawa 3: ananananananana 3an Ananananana 3an anananana	55306070417659617587487913786798473482304757487845865854629 $555555555555555555555555555555555555$	145 135 143 156 135 142 133 146 142 133 140 131 140 131 140 137 142 133 140 131 140 137 145 138 134 145 139 138 134 145 139 138 134 145 139 138 134 145 139 131 140 149 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 139 131 145 134 148 140 140 143 142 148 140 143 148	195 190 201 202 191 195 191 200 193 206 194 195 192 191 194 192 183 197 194 196 191 198 200 193 197 188 197 198 197 189 198 197 188 197 188 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 198 197 189 199 191 181 195 190 192 205 196 191 181 195 196 162 192	158 149 162 158 150 146 146 148 156 155 152 151 148 140 145 151 145 150 150 158 143 150 150 158 143 141 156 151 142 154 151 157 158 149 154 151 143 147 156 148 157 151 149 154 151 143 147 156 149 156 149 156 145 152

				MALES.							-	MALES			
No.		lour acter.	of Nose.	Stature.		Cranial Characte		No.		lour acter.	of Nose.	Stature.		Crania Charact	
	Hair.	Eyes.	Shape o	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape o	ft. in.	H.	L.	B,
12334 5 6789 10 1123144 15 16171819 20 22234 25 2627829 33 13233344442434445 5 553554 5 566789 6 0	D M M D D D D M D D D D D D D D D D D D		BERESE AUGUSTUS AUGUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AUGUSTUS AU	163742773787565867785289618547306795887599356678070559070715 555555555555555555555555555555555	138 142 148 141 135 127 142 138 136 136 136 136 136 137 150 140 134 142 137 150 140 134 142 137 150 140 134 141 143 152 129 138 148 149 149 139 138 149 149 149 149 149 149 149 149 149 149	195 198 194 190 190 195 208 197 183 186 197 193 187 195 199 193 197 199 191 203 199 195 191 193 197 199 195 191 193 197 199 195 191 193 197 199 195 191 193 197 199 195 191 201 201 201 201 201 201 201 201 201 20	151 155 154 147 149 175 155 157 156 161 152 156 149 153 148 156 149 153 148 156 149 153 144 152 152 153 144 155 156 156 157 146 156 157 147 157 156 157 149 157 157 149 159 159 159 159 159 159 159 159 159 15	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 81 82 83 84 85 88 89 91 92 93 94 94 95 99 100 102 103 104 105 106 107 118 119 110 111 111 112 113 114 115 116 117 118 119 110 111 111 111 111 111 111 111 111		L D M L M D D D M L M D D L D M M L L L L	assesses Augus and Augus a	$\begin{array}{c} 5 & 11 & 3 & 7 & 8 & 9 & 6 & 5 & 5 & 10 & 8 & 5 & 9 & 10 & 9 & 3 & 4 & 7 & 2 & 3 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	136 134 127 136 141 135 150 131 142 128 131 141 138 129 154 136 136 139 149 132 134 151 146 137 148 142 140 141 141 143 145 137 147 138 137 139 137 139 137 139 141 141 140 141 140 141 140 141 140 140	196 202 181 194 192 193 203 190 182 206 192 215 202 210 187 189 195 202 210 187 189 191 191 191 199 191 191 199 191 191	13 16 15 15 15 15 15 15 15 15

					χv	///	Per	th D	istr	ict	Asj	/lu	m.				
				MA	LES.								MAL	ES.			
No.	Col Chara		of Nose.	Sta	ture.	(Cranial Characte		No.	Cole Chara		of Nose.	Statu	rre.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	II.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H. mm.	L. mm.	B. mm.
121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 137 138 139 140 141 142 143 144 145	D M M F F R D D D D D M M M D D D D D D D D D D D	D L M M L L L L D D L L M M D D L L L M M M D D L L L M M M D D L L M M M D L L L M M M D L L M M D L L M M D L L M M D L L M M D L L M M D L L M M M D L M M D L M M D L M M D L M M M D L M M M D L M M M D L M M M D L M M M D L M M M D L M M M D L M M M M	asasasasasasasasas Rayasyasa	555555555555555555555555555555555555555	$\begin{array}{c} 4 \\ 10 \\ 75 \\ 8 \\ 77 \\ 84 \\ 86 \\ 67 \\ 08 \\ 65 \\ 88 \\ 58 \\ 410 \\ 61 \\ 87 \\ \end{array}$	148 147 143 139 144 140 143 135 138 149 136 128 149 142 139 142 139 143 141 142 134 141 137	199 206 199 201 201 188 201 193 197 187 199 193 193 191 201 185 204 194 194 197 206 198 207 196 198 207	151 166 154 155 159 161 146 151 143 154 151 159 139 156 153 156 153 156 151 154 152 149 162	147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170		M M M D M D M M M M M M M M M M L D M M M M	SSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	55555555555555555555555555555555555555		150 139 143 130 153 146 142 143 153 137 128 139 146 148 131 133 134 141 141 155 142 142 142 151	202 199 205 198 198 201 196 201 196 202 192 193 189 203 208 200 197 196 190 195	158 154 158 154 156 156 151 156 149 153 150 143 153 153 154 155 156 161 149 156 149 157

XIX.—Roxburgh District Asylum.

			MA	LES								MALES			
1 M 2 M 3 M 4 D 5 M 6 M 7 D 8 D 9 D 10 M 11 M 12 M 15 D 14 M 15 D 16 F 17 M 18 M 19 M 20 D 21 D 22 D 23 D 24 D 25 D	L L M L D D D L L M L L L D D D L L L D D D D	W S S S S S S S S S S S S S S S S S S S	555555555555555555555555555555555555555	447555567515687574384237666	141 149 134 133 144 147 138 126 146 132 140 140 140 140 140 140 137 137 134 136 134 136 138 126 138	190 198 196 194 198 208 203 187 181 193 193 193 193 194 191 191 194 188 187 184	149 151 153 147 155 148 162 149 147 149 153 147 157 147 155 162 144 144 155 160 142 154 148	26 277 288 29 30 31 322 333 34 35 36 37 38 39 40 41 42 43 44 44 45 46 47 48 49 50	M M D D D D D D D F F M M M M M M M M	M D L L L L L L L L L L L L L L L L L L	sesses Assesses Assesses Assesses	5 7 5 5 2 5 9 5 6 3 6 0 6 5 10 5 10 5 10 5 10 5 7 5 10 5 7 5 5 10 5 7 5 5 10 5 7 5 10 5 7 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10	141 138 147 134 133 152 136 141 128 136 140 145 138 145 138 140 141 143	191 192 210 181 198 193 193 200 196 191 193 194 198 203 194 198 188 203 192 196 200 194 191 195 196 200 196 191 199 199 199 199 199 199 199 199	152 139 163 145 154 152 149 160 154 147 151 148 150 156 144 152 153 149 153 148 153 148 153 153 153 153 153 153 153 153 153 153

				XIX MALES	R	oxbu	rgh	Dis	tric	t A	syl	MALES.			
No.	Col		of Nose.	Stature.		Cranial Characte		No.	Col		of Nose.	Stature.	(Cranial Characte	
110.	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.	140.	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
512 553 554 555 566 578 599 661 62 63 64 66 66 67 712 72 74 775 778 881 82 83 845 889 991 993 994	M R M M R D M M M M M M M M M M M M M M	M D L L L L L L L L L L L L L L L L L L	Assessed Canada Assessed Assessed Assessed Canada and Assessed Ass	5 7 5 11 5 6 6 8 9 5 7 5 10 5 5 6 8 9 5 7 5 10 5 5 6 6 0 6 5 5 10 5 5 6 6 0 6 5 6 8 4 5 7 5 5 8 9 5 11 5 5 6 7 9 5 10 5 5 7 7 5 9 5 10 5 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	136 142 137 146 141 139 136 150 144 138 130 141 142 142 143 139 139 135 145 130 151 141 147 126 133 131 158 138 147 128 148 144 141 154 153 147 153 147 154	190 196 198 198 203 192 191 204 204 198 200 192 200 192 207 203 200 192 207 203 200 192 204 188 203 192 204 193 205 192 193 205 192 195 195 195 196 196 196 196 196 196 196 196 196 196	150 152 153 151 151 150 145 152 150 153 154 153 154 155 156 146 155 156 148 149 137 155 158 148 146 151 153 148 146 151 153 148 154 154 155 156 146 157 167 167 167 167 167 167 167 167 167 16	95 96 97 98 99 100 101 102 103 104 105 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138	M D M M M M M M M M M M M M M M M M M M	L M D L M L L L L L M L L L L L L L L L	Annuanannunununga Karana Kananahan Kankan Kankan	86574038866388665525256958566977811818688888055 555555555555555555555555555555555555	153 143 139 142 142 129 139 142 121 142 129 133 147 137 147 133 142 131 143 133 140 143 133 140 143 135 138 141 143 137 140 145 139 149 139 139 149 149 149 149 149 149 149 149 149 14	205 201 195 194 196 194 192 202 178 199 189 189 184 199 200 190 190 190 190 190 191 197 197 194 197 197 194 197 198 199 194 197 197 198 199 199 199 199 199 199 199 199 199	155 144 155 144 155 144 155 144 155 146 155 166 153 156 156 157 166 144 155 156 157 156 157 156 157 157 157 157 157 157 157 157 157 157

XX.—Stirling District Asylum.

			MA	LES.								MALES.			
1 M 2 M 3 F 4 F 5 D	M D M D	S S S W	5 5 5 5 5	4 7 6 8 8	125 138 147 143 144	184 194 191 196 201	143 152 156 153 150	6 7 8 9 10	D F D M	D M M D D	s s w s	5 8 5 10 5 4 5 11 6 0	143 144 125 146 141	202 202 182 198 194	149 147 148 147 153

					XX	.—S	tirlin	g D	istr	ict .	Asy	/lui	m.			
					MALES.								MALES.			
I	۷o.	Colo Chara		of Nose.	Stature,		Cranial Characte		No.	Col Chara		of Nose.	Stature.	C	Cranial Characte	
		Hair.	Eyes.	Shape	ft. in	H, mm.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L. mm.	B.
	112134 14516617819 1202223422222222222222222222222222222222	RMMFMDDDDMMDRMMRDMDFMDFMDFDMMDDDDDMMMMMMDDDDDFDDMDDDDDDD		RSSSWSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	$\begin{array}{c} 7509957753750290786405414899945435\\ 555555555555555555555555555555555$	137 143 146 138 137 142 141 155 144 140 150 130 136 148 138 146 147 149 141 159 144 137 141 141 141 141 141 141 141 141 141 14	186 194 199 194 196 202 203 194 199 191 202 202 197 194 206 199 188 200 187 194 201 189 199 199 197 186 194 187 188 191 199 187 188 191 199 187 188 191 199 189 189 181 199 190 191 205 181 193 190 191 205 181	145 154 164 148 145 154 156 153 156 145 151 151 158 154 156 161 161 162 148 153 159 157 154 149 150 153 149 150 151 148 153 149 150 151 148 153 159 157 152 164 147 156 158 153 157 152 153 148 153 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 157 152 153 148 151 156 148 158 153 157 152 153 148 151 157 152 153 148 151 156 158 158 153 157 152 153 148 151 157 152 153 148 151 156 158 158 159 153 153 157 152 153 148 151 157 152 153 148 151 156 158 158 159 153 153 157 152 153 148 151 157 159 152 153 153 153 153 153 153 153 153 153 153	71 72 73 74 75 76 77 78 81 82 83 84 85 86 87 98 99 99 99 99 99 100 101 102 103 104 105 110 111 112 113 114 115 116 117 118 119 120 121 121 122 123 124 127 128 129 130	M D D D D D M M M D D D D D M M M D D D D D M M M D D D D F M M D D M D M	DMMMDLMDDDDLLLDMDDDDLLMLMMLDDMMLLDDMMMLLDDMMMDDDMMDDDDLLLDMMMDDDMMMLMMDDDMMMLLDDMMMMMM	SAME SAME SAME SAME SAME SAME SAME SAME	443631869379753233968655575024617715623442267806955507314917 555555555555555555555555555555555555	140 143 138 145 150 135 147 140 144 141 132 137 145 140 143 141 141 141 141 141 141 141 141 141	187 194 196 190 186 186 194 194 206 194 208 183 190 208 202 197 199 204 197 203 190 209 189 199 189 203 188 194 195 196 197 199 199 189 199 199 189 199 189 199 19	153 148 146 156 152 151 149 147 152 150 150 151 145 154 157 147 151 155 152 157 147 151 155 157 144 147 151 147 151 147 151 147 151 147 151 148 147 151 147 151 147 151 147 151 147 151 147 151 147 151 147 151 147 151 147 151 147 151 147 151 151 147 151 147 151 151 147 151 151 147 151 151 147 151 157 157 157 157 157 148 157 157 157 157 157 157 157 157 157 157

				4	XX	,-S	tirlin	g D	istri	ict i	Asy	lur	n.			
				MAL	ES.								MALES	·		
No.	Cole		of Nose.	Stati	ure.		Cranial Characte	r.	No.	Col- Chara		of Nose.	Stature.	(Cranial Characte	
	Hair.	Eyes.	Shape	ft	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 167 168 169 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 187 188 189 180		MDMDLDDDLMLLLLMLLLLMLLLLDLLDLLDDDDLLDMMLDLDMLLMDLLDMMMLLMLL	SWSSSSRSSSRSSSSSSSSSSSSSSSSSSSSSSSSSSS	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	$\begin{smallmatrix} 596523353363537116744845789892673873046097077475776569501166652 \end{smallmatrix}$	134 141 134 135 128 141 129 135 130 130 139 130 131 145 143 145 143 140 135 140 135 140 135 140 135 140 135 141 142 153 144 145 140 135 140 141 142 153 144 145 140 140 140 140 140 140 140 140 140 140	196 193 186 191 191 203 199 193 198 191 197 190 188 212 201 192 193 196 188 193 198 196 198 199 184 209 184 209 189 184 198 203 185 190 198 194 199 201 201 204 199 200 181 192 201 201 204 199 200 181 192 201 201 202 200 208 208 204 205 200 196 205 198 192 203 193	156 151 147 141 141 152 144 155 152 147 149 146 153 159 150 157 149 155 152 151 160 156 146 155 148 156 148 156 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 143 151 149 145 150 155 148 156 158 148 157 165 158 148 156 155 148 147 154 148	191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 211 212 213 214 215 216 217 218 219 220 221 223 224 225 226 227 228 229 231 232 224 225 236 237 228 229 231 232 244 245 245 246 247 248 249 250	M D D D D D D D D D D D D D D D D D D D	MLLLDMMLDMCLMLLLLMLMMDMMLLLLLLLLLLLLLLMLMLL :LM :LDDLMMDODD	Wank Cananan Kananan K	$\begin{smallmatrix} 8 & 6 & 4 & 0 & 1 & 2 & 2 & 9 & 6 & 3 & 2 & 4 & 3 & 0 & 2 & 1 & 5 & 4 & 5 & 3 & 4 & 7 & 1 & 0 & 0 & 7 & 3 & 4 & 5 & 3 & 4 & 9 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	145 138 144 135 134 137 146 133 141 139 140 140 143 134 127 140 142 137 138 142 137 138 142 137 138 142 137 138 142 137 138 149 140 140 141 127 137 138 149 140 140 141 141 141 141 141 141 141 141	198 191 192 195 202 193 194 199 210 188 190 193 200 206 205 194 189 193 200 195 197 198 196 194 202 197 195 199 190 201 198 172 191 195 198 196 194 199 190 201 198 172 191 195 198 196 198 172 191 195 198 190 198 172 191 195 198 190 198 172 191 195 198 190 198 172 191 195 198 190 198 172 191 195 198 190 198 210 198 190 198 210 198 199 190 198 210 198 210 198 199 190 198 210 198 200 198 200 198 200 198 200 198 200 200	154 148 142 153 135 142 141 155 156 154 149 145 155 156 154 147 157 157 151 154 146 157 151 154 147 153 167 151 154 146 151 153 154 147 147 153 167 151 154 146 151 153 154 147 145 149 144 151 155 146 157 151 153 154 147 155 156 156 157 156 156 157 156 156 156 156 156 156 156 156 156 156

XX.—Stirling District Asylui	n.
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				MA	LES.								MA	LES			
No.	Col Chara		of Nose.	Sta	ture.		Cranial Characte		No.	Cole Chara		of Nose.	Sta	ture.	(Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
251 252 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 271 272 273 274 275 277 278 279 280 281	D D D D D D D D D D D D D D D D D D D	L L D L L L D D M L L L L D M L D D L L L L	Waasassassas Kaasassassassassassassassassassassassass	555555555555555555555555555555555555555	$\frac{65}{65} \frac{65}{42} \frac{42}{46} \frac{67}{777} \frac{79}{90} \frac{47}{42} \frac{73}{85} \frac{85}{44} \frac{44}{78} \frac{67}{67} \frac{43}{105} \frac{105}{88}$	140 143 140 130 137 149 149 140 148 139 152 137 144 146 134 135 141 136 137 143 141 136 141 137 143 144 141 145 146 147 147 148	191 199 194 197 202 196 194 203 190 196 201 199 193 195 187 191 184 198 194 197 188 196 196 189 197 188	147 140 151 150 155 145 151 145 141 146 155 143 146 157 144 158 148 148 148 144 154 154 155 156 144 157	282 283 284 285 286 287 291 292 293 294 295 297 298 299 301 302 303 304 305 306 307 308 309 310	D M M D D D M M M D D D M M M D D D M M M D D D D M M M D D D D D M M D D D D D M M D D D D M D D D D M D D D D M D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D M D D D D D M D D D D D M D D D D D M D D D D D D M D D D D D D M D		RSWSWSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	555555555555555555555555555555555555555	5684777488455155874647777556759	143 137 148 142 141 136 142 134 146 131 124 140 144 135 135 137 146 147 137 146 147 135 146 147 135	202 189 194 208 196 197 178 186 195 192 188 181 195 195 185 198 199 189 189 189 189 189 189	148 144 148 155 154 150 151 142 158 150 164 161 155 149 148 143 143 145 159 150 147 157 157 147

XXI.—Greenock Parochial Asylum.

			MALES								MALES			
1	M L L L	Wassas Assassas	5 8 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	128 122 133 135 123 130 128 126 133 143 136 139 138 135 130 137 141	201 178 195 192 195 183 198 204 194 194 191 205 187 191 200 185 200	143 134 149 144 146 151 154 147 162 155 151 153 158 151 154 142 157	21 222 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	M D M D M M M M M M M M M M D D M D D	D M L M D L L L L D L L D L	SSW SSW SSW SW SS SSW SSW SSW SSW SSW S	5 10 5 2 5 10 5 2 5 10 5 2 5 8 5 5 2 5 5 8 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7	138 127 130 132 129 128 135 131 131 131 132 131 132 133 134 132 135 129 138 133	198 183 199 200 192 197 204 184 187 186 203 188 192 194 193 181 194 205	152 148 156 149 152 147 157 148 140 141 148 146 144 146 143 148

				X	X1	-Gre	eno	ck F	Paro	chi	al i	Asy	/lum.			
				MA	LES								MALES			
No.	Col Chara		of Nose.	Sta	ture.		Cranial Characte		No.	Col- Chara	our cter.	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
41 42 43 44 45 46 47 48 49 50 51 52 53 55 55 66 61 62 63 64 66 66 66 66 67 77 77 78 79 80	M M M M M M M M M M M M M M M M M M M	LLDLDDDDMMLLLLMMMLLMMMDDDMLLDLLLM	SEA A SEE SEE SEE SEE SEE SEE SEE SEE SE	565555555555555555555555555555555555555	$\begin{smallmatrix} 8 & 0 & 1 & 4 & 6 & 6 & 5 & 5 & 7 & 4 & 6 & 8 & 3 & 3 & 7 & 2 & 5 & 7 & 6 & 8 & 6 & 7 & 6 & 3 & 2 & 7 & 8 & 5 & 8 & 4 & 7 & 2 & 6 & 6 & 6 & 8 & 5 & 3 & 1 & 5 & 7 & 5 & 8 & 4 & 7 & 2 & 6 & 6 & 6 & 8 & 5 & 3 & 1 & 5 & 7 & 6 & 8 & 6 & 7 $	138 139 128 131 141 136 135 141 138 132 142 130 128 135 136 137 128 137 128 137 128 137 128 137 128 137 128 137 128 137 128 137 137 138 137 137 138 138 139 139 139 139 139 139 139 139 139 139	197 199 186 195 200 195 190 193 198 194 195 191 188 204 190 201 202 195 199 191 200 188 193 207 194 197 190 203 200 199 199 191 195 199 200 199 199 191 195 199 200 199 200 199 200 199 200 199 200 199 200 199 200 199 200 199 200 199 200 199 200	151 152 153 153 156 155 149 154 152 150 144 153 148 157 161 152 160 144 157 161 151 151 151 151 151 148 148 147 151 153 160 153 160 154 155 160 160 160 160 160 160 160 160 160 160	81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 119 1112 113 114 115 116 117 118 119	D D D M M M M M M M M M M M M M M M M M	L M D M L L L M M M L L L L L D M L L L L	mananananananana Sanananas Asan Kasaa	5 0 7 5 5 5 5 8 9 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	126 134 133 137 129 134 130 134 130 134 132 132 132 132 139 128 131 136 133 134 136 137 143 137 143 137 143 137 138 136 137 138 137 138 137 138 139 139 139 139 139 139 139 139 139 139	189 191 188 211 198 189 195 200 197 199 188 195 195 192 201 197 198 203 207 202 196 189 185 203 205 195 187 200 194 175 195 195 195 197 200 194 175 195 195 197 200 194 175 195 204 198	133 144 144 166 144 166 155 155 151 144 166 155 154 144 155 154 151 151 166 151 151 161 161 161 161 161

XXII.—Paisley Parochial Asylum.

MALES.				MALES.			
2 M L S 5 7 1 3 D D S 5 9 1 4 M M S 5 7 1 5 M M S 5 8 1 7 D D S 6 0 1 8 D M S 5 5 1 9 D M S 5 0	148 148 148 148 148 148 148 152 153 150 153 150 153 150 153 150 153 146 194 146 144 197 154 153 209 159 151 137 189 151 137 194 152 151 152 154 152 154 152 154 154 155 155	11 M 12 D 13 D 14 R 15 R 16 M 17 M 18 M 20 M	L S S L S S L S M W S	5 2 5 5 5 0 5 2 5 5 5 4 5 5 5 6 5 4 5 10	132 142 137 139 134 142 135 138 144 152	193 200 191 199 186 192 195 206 195 193	153 152 145 145 144 162 150 154 151 153

				XXII	.—Pa	zisle	y P a	roc	hia	I A	s <i>yl</i>	um.			
				MALES.								MALES.			
No.	Cole	icter.	e of Nose.	Stature.		Crania Charact		No.	Col Chara	acter.	of Nose.	Stature.		Cranial	
	Hair.	Eyes.	Shape of	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H. mm.	L. mm.	B. mm.
21 22 23 24 25 26 27 28 29 30 31 32 33 34 41 42 43 44 45 50 51 51 52 53 54 57	M M M M M M M M M M M M M M M M M M M	M M L M D L D L L L L L M L M L D L D L	Wan zanananananananananananananananananan	$\begin{smallmatrix} 5 & 6 & 11 & 5 & 5 & 2 & 2 & 6 & 6 & 14 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & $	147 133 135 128 137 144 133 141 138 136 135 133 136 133 136 133 135 134 138 138 139 139 135 138 138 137 139 141 138 137 139 141 138	199 182 194 178 192 190 213 196 203 201 196 189 188 186 192 194 200 197 190 208 194 188 216 192 195 196 188 202 200 208 197 188	152 141 158 145 156 158 150 161 152 149 147 146 149 147 153 153 153 154 154 148 148 148 148 148 154 154 149 141 144 145 154 147 148 148 149 149 149 149 149 149 149 149 149 149	58 59 60 61 62 63 64 65 66 67 70 71 72 73 74 75 76 77 78 81 82 83 84 85 86 87 88 89 90 91 92 93 93 94 95 96 96 97 97 97 97 97 97 97 97 97 97	M M M M M M M M M M M M M M M M M M M	L M L L L L L L L D L D L L L D D M L L L L	Rananananananananananananananananananan	$\begin{array}{c} 5 & 8 \\ 5 & 5 \\ 5 & 7 \\ 5 & 8 \\ 5 & 5 \\ 5 & 8 \\ 5 & 7 \\ 7 \\ 5 & 10 \\ 7 \\ 5 & 10 \\ 4 \\ 8 \\ 5 \\ 7 \\ 5 \\ 11 \\ 4 \\ 10 \\ 6 \\ 5 \\ 11 \\ 5 \\ 10 \\ 6 \\ 2 \\ 4 \\ 10 \\ 10 \\ 10 \\ 5 \\ 5 \\ 8 \\ 5 \\ 5 \\ 9 \\ 2 \\ 8 \\ 5 \\ 5 \\ 5 \\ 8 \\ 5 \\ 5 \\ 5 \\ 8 \\ 5 \\ 5$	137 141 137 135 138 134 137 133 137 135 134 132 141 141 140 141 140 141 139 142 138 137 133 143 121 130 130 130 134 143 143 137 137 138 137 138 137 138 139 139 139 139 139 139 139 139 139 139	203 209 197 194 200 196 201 197 200 203 191 195 204 202 199 195 197 194 203 200 192 199 188 205 188 209 198 209 198 209 198 203 198 209 198 198 198 198 198 198 198 198 198 19	152 158 150 148 145 149 164 148 150 153 156 152 158 156 145 149 151 151 151 151 151 151 154 157 154 157 154 151 154 155 156 159 159 159 159 159 159 159 159 159 159

					—Ab	erde	en i	Roy	al A	ls <i>y</i>			2		
No.		lour acter.	Nose.	Stature		Cranial Characte		No.		lour acter.	Nose.	Stature.		Cranial Characte	
1101	Hair.	Eyes.	Shape of	Stature. ft. in.	H.	L.	B.		Hair.	Eyes.	Shape of	ft. in.	H.	L.	B.
1 2 2 3 4 4 5 6 7 8 9 10 11 12 13 14 15 16 17 7 18 19 20 1 12 22 3 24 25 6 22 8 29 30 1 32 33 33 34 4 4 4 5 5 6 5 5 5 5 5 5 5 5 5 5 5 5 5	DDRD ::RDDDDDDMMDDDD ::M :: :: :: :: :: :: :: :: :: :: :: ::		assocs Charcakas Caracas assachas assac	$\begin{array}{c} 2 \\ 5 \\ 5 \\ 2 \\ 10 \\ 21 \\ 31 \\ \\ 5 \\ 21 \\ 23 \\ 30 \\ 31 \\ 27 \\ 37 \\ 90 \\ 10 \\ 20 \\ 41 \\ 10 \\ 20 \\ \\ 44 \\ 55 \\ 55 \\ 55 \\ 55 \\ 55 \\ 5$	132 134 131 134 130 140 136 132 133 141 132 132 139 129 136 133 131 132 123 133 131 128 132 127 128 127 132 127 131 140 122 153 153 153 154 157 157 158 158 158 158 158 158 158 158 158 158	180 187 187 187 187 187 188 171 188 178 194 183 167 186 191 186 191 187 188 191 186 171 188 189 189 189 186 171 188 181 188 171 188 189 189 189 189 189 189 189 189 18	141 143 146 152 147 141 142 146 141 153 153 144 151 153 144 151 153 149 141 153 149 141 153 149 141 153 149 141 153 149 141 153 149 141 153 149 141 153 149 141 141 153 149 141 141 153 149 141 141 153 149 141 141 153 149 149 149 149 149 149 149 149 149 149	61 62 63 64 65 66 67 71 72 73 74 75 76 77 78 80 81 82 83 84 85 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 109 110 1112 113 114 115 116 117 118 119 110 110 1112 1113 114 115 116 117 118 119 110 110 110 110 110 110 110 110 110	M	L M D D D L D L M M M M M M M M M M M M	and and and and and and and and and and	$\begin{array}{c} 5 & 1 \\ 4 & 10 \\ 3 & 2 \\ 3 & 3 \\ 1 & 0 \\ 4 & 10 \\ 1 & 0 \\ 7 & 3 \\ 1 & 5 \\ 5 & 5 \\ 3 & 1 \\ 0 & 0 \\ 2 & 3 \\ 9 & 1 \\ 3 & 1 \\ 4 & 5 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 3 \\ 9 & 1 \\ 3 & 1 \\ 4 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 5 \\ 5 \\$	120 128 130 128 132 132 127 127 120 124 132 137 139 149 131 140 125 128 129 138 131 130 131 135 124 128 138 131 135 123 124 128 138 132 135 136 131 135 126 123 133 1324 128 138 132 135 136 130 131 135 136 130 131 135 136 130 131 135 136 130 131 135 136 137 138 139 128 130 131 135 135 136 130 131 135 136 130 131 135 136 130 131 137 128 138 139 126 130 130 130 130	179 183 182 187 186 180 181 181 182 178 194 187 194 185 197 176 190 179 179 192 190 188 182 189 184 191 177 187 182 169 188 177 186 182 176 188 177 186 181 177 187 186 182 176 188 177 187 186 181 177 187 187 188 187 188 189 199 207 187 187 187 187 187 187 187 187	1421 1431 1431 1431 1431 1431 1431 1431

				I.	—Ab	erde	een l	Roy	al A	ls <i>y</i>	lun	7.			
			FI	EMALES							F	EMALES	5.		
No.	Cole Chara		of Nose.	Stature.		Cranial Characte		No.	Cole Chara		of Nose.	Stature.		Cranial Characte	er.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B: mm.
121 122 123 124 125 126 127 128 130 131 132 133 134 135 136 137 149 141 145 146 147 148 149 150 166 157 158 166 167 168 169 170 171 178 176 177 178 180	M M D D M	M M M L L L M M L D D D M M L D D D M M D D D M M D D D M M M M		$\begin{array}{c} 5 & 5 & 2 & 1 & 6 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0$	128 133 126 139 140 150 125 128 138 121 126 139 130 138 121 129 132 130 138 134 137 122 132 133 126 128 132 140 139 140 147 127 125 140 139 148 132 134 128 132 133 134 144 134 137 130 126 128 132 133 133 134 144 134 137 138	187 199 189 181 202 180 187 190 183 179 184 189 184 193 187 184 193 187 188 193 182 188 199 186 196 187 188 199 186 176 189 185 186 176 186 176 189 189 186 176 189 189 186 176 189 189 186 176 189 189 189 189 189 189 189 189 189 189	148 162 130 148 151 143 150 140 150 145 143 141 147 142 146 152 146 149 143 147 133 146 148 137 145 150 149 143 146 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 140 143 141 141 149 150 143 144 149 150 143 144 149 150 146 147 143	181 182 183 184 185 186 187 188 189 190 191 192 203 204 205 206 207 208 209 210 211 212 213 214 215 226 227 228 229 230 231 231 234 235 234 235 236 237 238 2340	MRRDMDD :: :DDFDDD :: :FDM ::RDDDDDD :: :DD :: :DD :: DMDDDDDDMMDDDDDDMMDDDDDDMMDDDDDDMMDDDDDD	M L M D L M M M M M M M M M M M M M M M	agaranganangananganangangangangangangangananga	$\begin{array}{c} 1151111248520232422513304611131538042013110112641212333321111302032 \\ 454555545555555555555555555555555555$	131 141 138 138 138 131 132 125 128 128 134 145 134 137 125 138 130 126 129 134 127 127 126 129 134 129 126 123 128 134 129 126 123 128 134 129 126 123 128 137 121 121 121 121 121 121 121 121 121 12	187 197 188 189 184 183 185 189 188 181 186 184 192 180 181 190 181 199 183 183 183 189 191 199 183 183 189 191 177 178 178 178 178 178 178 178 178 185 183 187 181 175 185 183 187 181 175	154 153 142 151 141 145 148 152 150 140 146 140 146 140 146 140 145 152 147 151 152 143 145 145 145 145 145 145 145 145

	houdoon	Daval	Asylum.
1.—A	verueen	noyai	Asylum.

			F	EMALE:	S.						F	EMALES	5.		
No.	Col Chara		of Nose.	Stature.	C	Crania Characte		No.	Col Chara		of Nose.	Stature.		Crania Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
241 242 243	D D M	D M M	20202	5 4 5 4 5 1	133 126 132	182 185 186	145 146 145	269 270 271	R D D	M M M	SSC	5 1 5 4 5 0	134 133 126	192 176 190	147 143 148
244 245 246 247	D	M M M	BBBBB	5 1 5 3 5 0 4 10	125 135 126 120	188 190 196 183	142 149 150 143	272 273 274 275	R D D R	M D M M	SSCS	$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	126 126 122 126	189 172 187 172	151 144 145 140
248 249 250 251	M M D D	M M M M	www.	5 2 5 3 4 10 4 10	123 132 123 120	182 192 183 189	$ \begin{array}{r} 145 \\ 150 \\ 138 \\ 141 \end{array} $	$\begin{vmatrix} 276 \\ 277 \\ 278 \\ 279 \end{vmatrix}$	D D	D D M		$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	127 130 133 119	194 200 184 189	146 158 135 144
252 253 254 255	D D D	M M D	S W S	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	125 135 119 126	183 199 174 189	141 150 136 151	280 281 282 283	D	D L M M	8888	$\begin{bmatrix} 5 & 0 \\ 5 & 1 \\ 5 & 0 \\ 5 & 3 \end{bmatrix}$	136 126 129 128	193 183 180 181	150 146 143 145
256 257 258 259	R D R D	M D L D	00000	5 4 5 1 5 4 5 4	132 124 125 138	185 178 180 186	146 145 142 142	284 285 286 287	R M D	D M M	2000	$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	148 136 132 125	$184 \\ 190 \\ 184 \\ 178$	148 148 147 143
260 261 262 263	D	M M D L	8880	5 1 5 1 5 0 5 3	133 135 132 139	177 196 190 188	143 147 149 149	288 289 290 291	D	M D M M	00000	5 1 5 1 5 3 5 1	126 134 128 126	190 189 194 178	153 145 145 148
264 265 266 267	 D М	M M M M		5 5 5 0 5 2 5 1	143 119 136 132	184 191 187 186	147 147 152 150	292 293 294 295	D D D	D M M	SSCC	5 1 5 4 5 2 5 2	133 126 126 132	202 194 179 201	149 154 146 148
268	M	M	ŝ	5 5	129	185	150	296	Ř	M	š	5 4	132	183	150

II.—Crichton Royal Institution.

]	FEMAL	ES.						F	FEMALE	S.		
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 .17 18 20	M M M M M M M M M M M M M M M M M M M	L L L D M L L D M D M D L L L	assas/sassassassassassas	5 2 4 9 5 1 0 5 0 0 5 0 0 5 1 7 5 3 2 5 5 7 5 1 1 0 1 7 5 5 5 2 2 5 5 3	ES. 131 131 129 124 131 129 132 131 129 131 129 131 129 131 131 129 135 131 130 135 130	190 190 187 186 185 177 188 190 188 196 196 198 185 186 198 185 188 198	144 139 146 150 143 143 150 149 151 139 146 144 148 152 150 141 149	26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45	M M M M M D M M M M M M M M M M M M M M		S S S S S S S S S S S S S S S S S S S	5 4 5 0 5 7 4 11 4 11 5 2 5 0 5 2 5 2 5 4 5 2 5 2 5 4 5 2 5 2 5 4 5 3 4 8 5 0 6 4	S. 134 129 133 124 129 129 132 124 130 128 132 135 124 132 130 124 131 128 131	199 180 192 186 192 195 179 178 179 185 182 177 185 183 193 183 193 183	147 141 149 146 149 147 151 139 144 141 152 144 148 146 156
21 22 23 24 25	M M M M M	M M L D	s s w s s	5 0 5 3 5 4 5 2 5 0	129 124 129 134 129	186 190 181 192 192	152 147 140 148 144	46 47 48 49 50	M M D D M	M D D L D	88088	5 4 4 11 5 1 5 0 4 8	129 128 123 129 124	178 181 182 185 177	148 140 141 144 135

				//	-Cric	chto	n Ro	yal	Ins	tit	utio	on.		11.	
			F	EMALES	•						F	EMALES	5.		
No.	Col Chara		of Nose.	Stature.	C	Cranial Characte		No.	Col- Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L. mm.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 77 77 77 77 77 77 77 77	M M M D D D M M M M M M D D M M M M M D D M M M M M D D M M M M M D D M M M M M D D D D M	L D L D L D L D L D L D L L L L L M M D D D L L L L	ananananananananananananananananananan	$\begin{array}{c} 5 & 3 \\ 4 & 11 \\ 1 & 3 \\ 1 & 5 \\ 5 & 3 \\ 2 & 4 \\ 3 & 6 \\ 11 & 0 \\ 2 & 4 \\ 4 & 2 \\ 6 & 5 \\ 11 & 2 \\ 0 & 4 \\ 4 & 5 \\ 5 & 4 \\ 11 & 5 \\ 5 & 2 \\ 2 & 1 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 4 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 2 \\ 2 & 1 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 5 \\ 5 & 5 \\ 5 & 4 \\ 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 2 \\ 2 & 5 \\ 5 & 5 \\ 4 & 10 \\ 2 & 2 \\ 2 & 2 \\ 2 & 2 \\ 2 & 3 \\ 3 & 4 \\ 4 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 4 & 2 \\ 5 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 4 & 2 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 4 & 2 \\ 5 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 4 & 2 \\ 5 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 5 & 5 \\ 5 & 5 \\ 5 & 5 \\ 4 & 10 \\ 5 & 5$	128 128 126 124 139 126 131 136 132 130 128 126 125 128 127 130 130 127 126 125 138 132 136 139 127 126 125 138 132 136 139 127 130 130 130 127 126 125 138 132 127 130 130 132 127 132 130 133 129 129 128 125 121 121 121 122 122 122	200 198 190 197 189 188 188 196 196 196 190 182 191 186 186 186 187 191 191 186 183 202 205 192 191 194 184 183 183 184 185 185 187 187 189 189 189 189 189 189 189 189 189 189	148 150 141 152 142 146 152 146 146 152 146 143 147 140 141 143 149 146 153 152 153 153 157 152 147 151 133 150 142 144 151 143 144 151 143 145 146 147 148 149 146 153 153 153 147 153 153 147 153 153 164 165 165 165 165 165 165 165 165 165 165	98 99 100 101 102 103 104 105 106 107 118 119 121 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 140 140 140 140 140 140 140	M M M M M M M M M M M M M M M M M M M	LLLLLMMM M LLMM M D LLD LLM D LM LM LLLLLLLMM LLMM LLMM LLLLLL MM LLMM	unan Aunanan aunanan aunanan aunan Aunan Aunan Aunan	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	130 126 123 131 132 131 129 128 133 129 128 133 129 124 133 131 127 136 124 123 121 125 121 131 125 121 136 127 125 127 125 127 125 127 125 127 127 128 129 129 129 129 129 129 129 129 129 129	181 181 175 185 185 185 186 190 183 178 183 188 193 185 187 204 189 181 175 180 175 180 175 184 180 175 184 180 181 193 181 189 181 189 181 189 181 189 189 189	144 144 144 144 144 144 145 155 156 157 144 133 144 143 144 144 144 144 144 144
						ınde	e Di	stri	ct /	1sy					
			FI	EMALES							F	EMALES			
1 2 3 4 5	D D M M	D L D L M	SSSJS	$\begin{array}{cccc} 6 & 0 \\ 5 & 3 \\ 5 & 0 \\ 4 & 11 \\ 5 & 0 \end{array}$	129 138 133 126 124	191 188 184 183 183	153 141 141 147 135	6 7 8 9 10	M M D D	M D L L D	S R S S	$\begin{array}{c cccc} 4 & 11 & \\ 5 & 5 & \\ 5 & 1 & \\ 5 & 2 & \\ 4 & 11 & \\ \end{array}$	131 131 136 133 123	187 188 186 195 187	148 153 140 146 141

			F	EMALES		und	ee D	istr	ict	Asj		m. EMALES			
No.	Col Chara		of Nose.	Stature.		Cranial Characte		No.	Col Chara	our acter.	of Nose.	Stature.		Cranial Characte	er.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
11 12 13 14 15 16 17 18 19 20 12 22 33 31 32 22 24 25 26 27 28 29 29 33 33 44 44 44 44 44 44 46 66 66 66 66 66 66	M D M M M M M M M M M M M M M M M M M M	DDLLLMLDLLLMLLLMLLLMMMMLLLMMMMMLLLMMMMMLLLMMMMMLLLMMMM	andanananananananananananananananananan	$\begin{smallmatrix} & & & & & & & & & & & & & & & & & & &$	134 136 126 136 129 132 129 133 128 135 130 125 132 129 124 124 129 132 121 125 132 121 128 131 131 131 125 137 132 125 128 139 131 125 132 129 124 134 135 130 130 130 130 130 130 130 130 130 130	191 192 187 195 189 174 190 193 192 183 187 172 193 189 189 189 189 189 189 189 189 181 188 186 187 193 181 188 186 187 193 181 188 186 187 193 181 188 193 181 188 193 181 188 193 181 188 193 181 188 193 181 188 193 181 188 193 181 188 186 187 190 189 187 189 189 178	153 144 145 143 151 141 149 152 140 144 141 141 142 144 151 144 151 144 151 144 145 150 141 144 147 148 145 145 145 145 145 145 145 145 145 145	71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 119 111 112 113 114 115 116 117 118 119 120 121 123 124 125 126 127 128 129 130	D M M M M M M M M M M M M M M M M M M M	LLLLLMMDD MLLLLMMMLMDLMLLLLLLLLLLLLLLLL	CausanaChausananananananananananananananananaCausanaCausaskanakanananananananananananananananan	$\begin{array}{c} 5 & 1 \\ 5 & 5 & 2 \\ 2 & 5 & 5 \\ 5 & 1 & 10 \\ 2 & 9 & 9 \\ 1 & 1 & 2 \\ 2 & 9 & 9 \\ 1 & 1 & 2 \\ 2 & 4 & 4 \\ 1 & 1 & 3 \\ 1 & 9 & 0 \\ 0 & 2 \\ 1 & 4 & 1 \\ 2 & 1 & 2 \\ 2 & 4 & 4 \\ 2 & 1 & 2 \\ 2 & 1 & 3 \\ 2 & 2 \\ 2 & 3 \\ 3 & 4 \\ 4 & 4 \\ 2 & 2 \\ 2 & 3 \\ 3 & 4 \\ 4 & 5 \\ 5 & 5 \\ 3 & 3 \\ 1 & 3 \\ 4 & 5 \\ 5 & 5 \\ 5 & 3 \\ 3 & 1 \\ 3 & 4 \\ 5 & 5 \\ 5 \\$	129 132 129 126 134 126 131 130 122 137 133 128 126 126 126 133 125 130 125 131 130 128 129 130 125 131 130 128 129 130 128 129 130 128 129 130 120 128 131 139 127 125 131 139 127 125 131 139 127 127 128 134 129 130 129 130 120 120 121 131 139 127 127 127 128 134 129 130 129 130 120 120 120 120 120 120 120 120 120 12	182 193 197 190 192 178 182 179 199 182 172 188 182 172 188 182 172 188 189 175 180 180 179 180 175 181 190 201 188 175 181 185 187 199 185 187 199 185 187 189 189 189 189 189 189 189 189 189 189	133 144 145 144 145 144 145 144 144 144 144

				///	.—D	unde	e Di	istri	ict /	4sy	lur	n.			
			I	FEMALE	S.						F	EMALE	S.		
No.	Cole Chara		of Nose.	Stature.		Cranial Characte		No.	Cole Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	S ft. in. m		H.	L.	B. mm.
131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 151 152 153 154 155 156 161 161 162 163 164 165	M M M D M M M M M M M M M D D M M D D M M D D D D D D D D D D		ananakanananananananananananananananana	$\begin{array}{c} 5 & 3 \\ 4 & 10 \\ 5 & 4 \\ 11 \\ 5 & 3 \\ 4 & 11 \\ 5 & 5 \\ 2 \\ 4 & 11 \\ 5 & 5 \\ 2 \\ 4 & 11 \\ 5 & 5 \\ 5 & 0 \\ 5 & 1 \\ 4 & 11 \\ 5 & 3 \\ 4 & 10 \\ 5 & 2 \\ 4 & 11 \\ 4 & 11 \\ 5 & 3 \\ 4 & 10 \\ 5 & 2 \\ 4 & 11 \\ 5 & 3 \\ 4 & 11 \\ 5 & 3 \\ 4 & 11 \\ 5 & 1 \\ 5 & 1 \\ 5 & 1 \\ 5 & 1 \\ 5 & 2 \\ 4 & 11 \\ 5 & 2 \\ 4 & 11 \\ 5 & 3 \\ 5 & 3 \\ 6 &$	127 130 132 137 130 130 122 132 133 128 131 129 135 134 125 132 137 134 125 132 137 134 125 132 137 134 125 132 137 134 125 132 137 138 128 139 130 130 130 130 130 130 130 130 130 130	183 178 199 190 192 178 183 182 178 186 186 186 186 182 181 187 183 184 182 198 173 183 177 190 180 180 184 195 195 195 195 195 195 195 195 195 195	149 145 152 146 145 144 137 146 149 146 142 141 157 149 146 143 156 142 144 155 137 137 142 144 155 137 133 137 142 144 147 138 138	166 167 168 169 170 171 172 173 174 175 176 177 178 181 182 183 184 185 186 187 189 190 191 192 193 194 195 198 199 200	M D D M M M M M M M M M M M M M M M M M		Razazazazazazazazazazazazazazaz	4 10 5 1 5 5 2 5 0 5 1 8 5 5 3 5 0 5 1 8 5 5 3 5 0 4 11 5 0 4 10 5 1 5 4 4 11 4 11 5 0 4 11 5 0 4 11 5 0 4 11 5 0 4 11 5 0 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1	125 137 135 133 131 125 125 134 129 136 136 137 128 137 123 123 123 129 131 126 125 138 137 123 123 129 131 126 125 135 136 136 137 128 137 128 131	174 180 188 185 192 185 184 194 194 182 185 181 182 195 178 184 182 188 196 177 183 184 196 187 191 198 199 187 191 198 199 199 199 199 199 199	148 148 148 149 146 148 138 145 153 140 152 138 140 153 145 145 145 145 145 145 145 145 145 145

IV.—Edinburgh Royal Asylum.

			FI	EMALES	S		-				F	EMALES	S.		
1 2 3 4 5 5 6 7 8 9 10 11 12 13 14 15	D D M D D M M D D M M M M M	D D M D L L L L L M D M D L	www.wwwwwwwww	5 3 5 6 5 3 5 0 5 1 8 4 8 8 5 2 4 11 5 0 5 5 3 5 1 5 0	133 135 140 124 126 129 133 128 139 129 134 127 140 133	187 182 182 178 177 177 189 179 184 187 198 188 179	145 150 142 139 138 139 146 139 138 139 160 147 132 149	16 17 18 19 20 21 22 23 24 25 26 27 28 29	M F D D D D M M M M M D	M M D L D D L D M L L D L L	Acamananamananan	5 3 5 0 4 11 5 1 5 2 5 4 9 5 1 4 5 4 10 4 10	140 131 137 134 141 135 132 139 135 131 132 136 132 126	191 179 176 186 190 183 192 189 185 186 185 191 186 173	151 136 149 141 145 147 146 142 142 147 141 151 145 129

				IV.	–Ed	inbu	rgh	Roj	al.	Asy	lui	n.			
			F	EMALES	i.						F	EMALE	S.		
No.		lour acter.	of Nose.	Stature.	(Cranial Characte		No.		lour acter.	of Nose.	Stature.	. (Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
31 32 33 34 35 36 37 38 39 40 412 43 44 44 45 55 55 57 58 59 60 62 63 64 66 67 77 77 77 77 77 77 77 77 77 77 77		MM MM M D L L L L L L L L L D L M D L L L D L D	as Mana Mana Mana Mana Mana Mana Mana Ma	$\begin{smallmatrix} 5 & 3 & 6 & 4 & 0 & 1 & 0 & 0 & 5 \\ 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	137 138 144 136 132 127 142 124 133 134 136 137 139 135 142 128 127 131 126 138 120 131 135 131 138 132 129 128 130 131 135 130 130 130 130 130 130 130 130	187 193 188 193 181 181 182 181 182 185 182 183 192 188 191 193 177 191 181 188 181 177 181 185 187 181 183 184 183 184 183 184 183 184 183 184 183 184 185 187 188 189 189 189 189 189 189 189 189 189	147 151 148 145 144 138 153 139 144 141 156 148 146 138 142 143 146 143 146 146 143 146 147 146 147 148 149 149 149 149 149 149 149 149 149 149	91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 118 119 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 149 150	M D D D M M D D D D D D D D D D D D D D	$\begin{smallmatrix} L & D & L & L & L & M \\ L & L & L & L & L & L & L & L \\ L & D & L & L & D & L & L & M \\ M & D & D & D & D & D & D \\ D & D & D & D$	asaakasaasaasakaasaasaasaasaasaasaasaasa	$\begin{array}{c} 4 & 11 \\ 4 & 0 \\ 4 & 5 \\ 5 & 5 \\ 6 & 4 \\ 11 & 1 \\ 11 & 0 \\ 11 & 1 \\ 11 & 0 \\ 11 & 1 \\ 11 & 0 \\ 11 & 1 \\ $	136 132 133 138 136 126 137 130 133 136 133 136 135 122 127 124 131 135 134 131 142 141 137 139 131 142 141 135 131 142 141 135 139 131 128 131 135 136 137 138 139 131 142 141 135 136 137 138 139 131 142 141 135 136 137 138 139 131 142 141 141 141 141 142 141 141 141 14	184 182 191 194 193 182 189 175 181 183 194 183 190 187 182 181 190 187 185 185 185 185 185 185 187 179 189 179 189 179 189 179 189 179 189 179 189 179 189 179 189 189 179 189 189 179 189 189 189 189 179 189 189 189 189 189 189 189 18	136 141 148 150 143 140 154 146 145 136 145 131 148 142 148 142 148 148 149 141 148 141 148 149 143 150 147 146 149 143 151 145 145 145 145 145 145 145 145 145

				IV.	–Ed	inbu	rgh	Roy	al i	Asy	lui	n.			
			F	EMALES	5.						F	EMALES	5.		
No.	Cole		e of Nose.	Stature.	(Cranial Characte		No.	Col Chara		of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
151 152 153 154 156 157 158 159 161 162 163 164 167 168 169 171 172 173 174 175 176 177 178	D D D D D D D D D D D D D D D D D D D	M D L D L L L L L L L L L L L L L L L L	WSCCsskssskssssckssssckksssss	5 0 5 0 5 1 5 2 5 3 4 10 4 11 5 4 11 5 4 11 5 5 1 4 10 4 10 4 10 5 3 5 3 5 0	141 137 136 135 141 141 133 134 129 135 135 135 135 135 135 135 129 129 124 129 129 129 129 138 145 139	187 180 192 186 188 180 190 176 183 176 187 192 188 195 182 188 187 196 188 187 196 188 187 196 186 187 196 183 185 186 187 196 186 186 186 186 186 186 186 186 186 18	143 138 156 146 152 145 145 133 140 142 124 141 152 144 149 141 140 152 144 143 143 143 143 143 145 152	180 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207	M D D D M M D D D M M D D M M D D M M D D M M D D M M D D M M D D D M M M D D D M M M M D D D M M M M D D D D D M M M M D D D D D M M M D D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M M D D D D D D M M M M D D D D D D M M M M D D D D D D M M M M D D D D D M M M M D D D D D M M M M D	M L L D M D L L M L M L D L M L D L M L L L D L L L L		5 1 4 11 5 - 0 4 11 5 - 9 5 1 4 11 5 5 2 5 3 4 10 5 5 3 5 5 7 4 7 6 0 4 10 5 5 3 5 5 5 3 5 5 5 5	134 131 126 132 151 128 132 133 135 141 128 133 142 133 142 133 142 133 142 143 137 130 141 129 146 145	182 187 184 191 198 180 193 185 169 183 194 188 181 172 195 187 188 183 177 188 183 177 188 189 194 195 195 195 197 198 199 199 199 199 199 199 199 199 199	140 139 150 149 150 149 140 144 139 144 142 144 133 153 145 149 148 146 146 146 146 146 146 146 146 146 146

V.-Montrose Royal Asylum.

		F	EMALES	5.						F	EMALES	S.		
1 D D 2 D D D D D D D D D D D D D D D D	M D M M D M M M M M M M M M M M M M M M	anananananananananan	4 11 4 10 4 10 4 10 4 10 5 0 4 10 5 2 5 1 5 0 4 10 4 5 5 2 5 1 5 0 5 0 5 1	131 129 133 123 148 129 126 120 138 139 128 129 130 128 127 131 134 127	186 177 181 180 191 182 174 181 183 188 183 184 173 181 182 185 195 197 186 184	145 138 141 140 154 147 145 146 149 140 139 149 145 146 151 150 154	21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	D M D R D D D D D D D D D D D D D D D D	M M M L M M D M M D D M M M M M M M M M	anananananananananana	5 0 4 9 4 10 5 0 5 1 5 2 5 4 5 0 5 3 4 10 5 4 5 0 4 11 5 0 4 11 5 1 4 11 5 4 1 11 5 4	125 144 119 132 122 131 132 122 132 122 132 123 129 131 130 127 128 128 129 135 129	182 198 172 185 178 186 185 178 192 185 191 184 195 180 183 187 176 176 175	144 155 138 153 143 148 148 147 142 142 142 143 149 150 158 143 139 142

			F	EMALI	ES.						F	EMALES	S.		
No.	Col- Chara		of Nose.	Stature		Cranial Characte		No.	Col Chara		of Nose,	Stature.	6	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B, mn
41 42 43 44 44 45 50 51 52 53 53 54 55 56 66 66 66 66 66 66 67 77 77 77 77 77 77		M D D L M M M M M M M M M M M M M M M M	anananani Ca ananani Cananananananananananananananananananan	5 1 7 2 0 1 6 5 5 0 1 1 5 5 6 2 4 11 0 5 5 6 0 0 5 5 5 5 1 1 5 5 5 5 5 5 5 5 5 5 5 5	124 143 122 131 130 136 132 123 128 127 129 124 121 131 128 127 129 124 121 131 135 143 135 143 135 143 135 143 135 143 135 127 139 125 136 136 138 128 122 121 130 139 127 145 136 136 136 138 149 127 140 135 138 138 142 121 130 139 127 145 136 136 136 136 137 149 149 149 149 149 149 149 149 149 149	189 188 196 182 185 186 182 180 181 184 193 185 189 180 181 191 181 191 188 189 188 189 188 189 188 181 175 183 181 175 183 181 175 183 191 182 186 179 187 184 195 191 186 188 184 195 191 186 188 189 188 184 195 191 186	151 147 144 136 148 141 149 157 146 149 157 146 149 149 149 149 149 149 149 149 144 145 152 150 144 144 145 151 151 151 153 144 145 151 151 151 151 151 151 151 151	97 98 99 100 101 102 103 104 105 107 108 109 110 111 112 113 114 115 116 117 118 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 151	M :: D :: D :: D :: M :: D :: M :: D :: M :: D :: D :: M :: D :: D :: M :: D :: D :: M :: D :: D :: M :: D :: D :: M :: D :: D :: M :: D :: D :: M D	L M D L L M M M M M M M M M M M M M M M	ananananananananananananananananananan	$\begin{array}{c} 5 & 3 \\ 4 & 11 \\ 4 & 10 \\ 5 & 4 \\ 11 \\ 5 & 2 \\ 2 & 6 \\ 5 & 2 \\ 2 & 6 \\ 5 & 5 \\ 2 & 10 \\ 4 & 10 \\ 5 & 5 \\ 5 & 2 \\ 2 & 6 \\ 5 & 5 \\ 2 & 1 \\ 0 & 5 \\ 5 & 2 \\ 2 & 6 \\ 5 & 5 \\ 2 & 1 \\ 0 & 5 \\ 5 & 2 \\ 2 & 3 \\ 4 & 11 \\ 10 & 4 \\ 2 & 0 \\ 2 & 1 \\ 2 & 5 \\ 5 & 5 \\ 5 & 5 \\ 2 & 1 \\ 2 & 2 \\ 2 & 3 \\ 3 & 4 \\ 4 & 11 \\ 4 & 10 \\ 4 & 10 \\ 4 & 11 \\ 5 & 5 \\ $	126 125 132 135 140 139 134 150 137 133 135 128 131 140 126 128 139 141 140 126 128 139 134 134 134 134 134 135 138 130 131 132 138 133 133 133 133 128 148 131 135 131 132 137 125 139 128 138 131 132 137 125 139 128 138	184 184 184 192 185 175 191 189 175 186 186 184 184 185 191 185 190 179 182 196 180 191 183 180 193 185 183 180 193 185 183 180 193 185 186 188 196 189 177 188 188 173 190 193 174 178	18 14 14 14 14 14 14 14 14 14 14 14 14 14

				V	I.—A	rgyl	I Dis	stric	t A	sy/	um).			
			F	EMALE	s.						F	EMALES	5.		
No.	Colo Chara		of Nose.	Stature,	(Cranial Characte		No.	Col Chara	lour icter.	or Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in	H.	L.	B, min.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
1 2 3 4 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 6 27 28 29 30 31 32 23 33 4 35 36 37 7 38 39 40 41 42 43 44 45 6 5 5 6 5 5 6 5 5 6 5 5 6 5 6 5 7 8 5 9 60	M M M M M M M M M M M M M M M M M M M	MOLLLLL MMOMMMLLM DOMMLOMOLLD MOMMOLD MLDOLLM MLDLLM MLLLM MLLLM MLLLM MLLLM MLLLM MLLLM MLLLM MLM MLLM MLLM MLLM MLLM MLLM MLLM MLLM MLLM MLLM MLLM MLLM ML	ananananananananananananananananananan	3590113502094325200222252603114742656131215311256412052412 $5444555555555555555555555555555555555$	138 133 135 137 129 124 129 133 130 122 133 124 124 124 127 129 136 137 139 129 131 129 131 129 131 129 131 132 133 129 131 132 133 129 131 132 133 134 135 136 137 138 139 139 139 139 139 139 139 139	201 188 181 191 184 187 188 181 192 193 182 196 182 181 191 181 184 205 196 187 189 181 193 179 181 183 195 191 179 201 183 195 191 190 184 193 195 196 187 188 195 196 187 188 197 198 198 198 198 198 198 198 198	141 148 144 144 143 137 148 144 147 134 149 144 147 151 153 144 151 150 150 144 151 150 146 143 147 151 150 146 143 147 150 146 143 147 150 146 143 146 147 150 146 147 150 146 147 150 146 147 150 148 149 149 149 149 149 149 149 149	61 62 63 64 65 66 67 70 71 72 73 74 75 76 77 78 81 82 83 84 85 88 89 91 92 93 94 95 96 97 100 101 102 103 104 105 107 108 109 110 111 112 113 114 115 116 117 118 119 119 119 119 119 119 119 119 119	M M M M M M M M M M M M M M M M M M M	LLMMMLDLLDMMMMLLMMLDLLMMLLLMMMDDMMMLLLLMMLDLLLLDLMMMLDD	annananananananananaganagananananananan	$\begin{smallmatrix} 4 & 11 & 2 & 3 & 2 & 5 & 5 & 1 & 3 & 5 & 2 & 1 & 9 & 1 & 1 & 1 & 9 & 1 & 8 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	128 127 137 119 125 132 137 126 129 133 131 127 123 124 129 132 132 134 130 121 130 132 131 130 131 131 130 132 131 130 132 133 134 130 132 135 131 130 132 135 131 130 132 135 131 130 132 133 134 130 132 135 131 130 132 135 131 130 132 133 134 130 132 135 131 130 132 133 134 130 132 135 136 137 138 139 130 130 130 130 130 130 130 130	185 186 190 181 189 193 186 182 201 193 190 188 188 185 184 194 172 179 194 185 182 189 194 185 182 189 195 184 190 185 186 190 187 188 189 190 189 189 189 189 189 189 189 189 189 189	141 142 148 148 148 141 156 153 143 144 150 144 142 150 146 143 135 144 149 146 144 148 141 149 151 151 140 144 138 150 146 144 148 151 151 140 144 138 150 146 144 148 141 149 151 151 140 144 138 150 146 144 144 155 143 138 151 144 155 143 138 151 144 155 143 138

					VI.—	l <i>rgy</i>	II Di	s <i>tri</i> e	et A	syl	um					
			F	EMALE	ES.						F	EMA.	LES	Š.		
No.	Cole Chara		of Nose.	Stature		Cranial Characte	er.	No.	Cole Chara		of Nose.	Stati	ıre.	(Cranial Characte	
	Hair.	Eyes.	Shape	ft in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H. mm.	L.	B.
121 122 123 124 125 126 127 130 131 132 133 134 135 136 137 138 149 140 142 143 144 145 151 152 156 151 155 156 156 157 158 159	M M M M M M M M M M M M M M M M M M M	L L M L L D M M D D D M M L L L D M M D D D D	ananananananananananananananananananan	$\begin{array}{c} 4 & 11 \\ 5 & 2 \\ 5 & 0 \\ 5 & 5 \\ 2 & 3 \\ 5 & 7 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 5 & 3 \\ 4 & 11 \\ 5 & 5 \\ 5 & 3 \\ 4 & 11 \\ 5 & 5 \\ 5 & 3 \\ 4 & 10 \\ 5 & 5 \\ 5 & 3 \\ 5 & 5 \\ 5 & 3 \\ 5 & 5 \\ 5 & 3 \\ 5 & 5 \\ 5 & 5 \\ 5 & 3 \\ 5 & 5 \\ 5 &$	125 125 132 132 135 130 127 131 132 133 128 128 124 120 130 137 131 132 132 127 130 127 127 121 132 121 132 127 121 132 127 130 127 131 132 133 133 134 135 137 137 137 137 137 137 137 137 137 137	179 188 185 197 183 185 187 179 191 186 198 185 197 200 184 191 188 185 192 189 191 179 195 189 187 189 186 189 181 190	141 149 146 155 141 148 148 141 149 148 147 146 149 143 143 143 144 151 140 141 154 138 148 148 141 145 145 146 143 147	160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 181 182 183 184 185 186 187 189 190 191 192 193 194 197	D M M M M M M M M M M M M M M M M M M M	M L D M L D M L D D L L L L D D L L L L L M M L D L L L L L M M L D L L L L	ananananananananananananananananananan	55555555555555555555555555555555555555	$\begin{smallmatrix} 2 & 3 & 1 & 2 & 2 & 2 & 0 & 0 & 1 & 1 & 2 & 2 & 2 & 2 & 2 & 2 & 2 & 2$	130 128 132 126 129 131 128 126 133 135 137 132 141 135 132 141 135 134 127 127 127 126 130 134 131 130 134 131 130 131 131 131 131 131 131 131 131	186 183 185 179 187 197 196 192 196 195 194 193 196 184 199 191 190 188 194 189 192 194 185 185 188 199 199 196 188 189 196	148 149 145 144 142 145 143 150 148 148 144 151 148 148 148 148 148 149 149 146 145 151 150 139 147

VII.—Ayr District Asylum.

		F	EMALES). ·						F	EMA	LES	S.		
2 3 4 5 6 7 8 9	M M L M L M M D M M L M L M D D L L M L	ss As Assass	4 10 5 0 4 11 5 0 4 11 5 1 4 10 5 1 5 5 5 5	129 129 134 131 129 130 134 127 138 132	191 179 189 192 184 182 193 181 189 188	138 149 145 153 141 147 146 143 139 147	11 12 13 14 15 16 17 18 19 20	D M D M M M M D M	M L L M L D D L M M	$\omega \omega $	5555555555	5 2 0 0 2 1 1 5 0 4	132 129 134 132 120 131 130 138 129 134	185 185 184 185 192 185 194 207 187 190	143 146 156 147 142 147 142 157 143 143

					VII	-Ayı	· Dis	tric	t As	sylu	ım				
			FF	EMALES	•						F	EMALES	S.		
No.	Cole Chara		of Nose.	Stature.		Cranial Characte		No.	Col Chara		of Nose.	Stature.		Oranial haracte	er.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
21 22 23 24 256 27 28 29 30 31 32 33 34 44 45 46 47 48 49 50 51 52 53 55 56 66 67 68 69 70 71 72 78 78 78 78 78 78 78 78 78 78 78 78 78	MM MM MM MM MM MM MM MM MM MM MM MM MM	MLLLDLLDLLLDLMLLLLMMLDMLLD ::MLLMLLLDMLDMDLMLDLDLLLLDLDDDLL :L	acanananananananananananananananananana	$\begin{smallmatrix} 1&2&3&2&0&3&1&5&0&2&0&2&1&1&1&7&1&4&2&2&1&4&0&0&0&4&1&1&7&2&2&9&1&8&4&2&1&3&0&3&3&3&1&8&1&1&2&6&2&2&5&1&5&1&0&0&1&1&1&1&1&1&1&1&1&1&1&1&1&1$	135 131 133 131 129 130 130 130 130 130 130 130 130 130 124 129 132 129 129 129 129 129 129 129 129 129 12	193 188 186 183 185 189 190 192 194 185 183 200 185 183 200 185 189 184 189 183 190 192 188 196 180 186 186 199 180 186 186 199 180 181 186 186 190 181 186 190 201 181 186 190 191 196 190 191 189 187 178	150 142 147 139 153 149 151 146 150 138 141 144 145 147 141 142 139 145 147 141 142 148 145 146 149 151 148 145 146 149 151 148 149 141 149 141 149 149 141 149 149 149	81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 130 131 140 140 150 160 170 180 180 190 190 190 190 190 190 190 19	D M M M M M M M M M M M M M M M M M M M	LLMLDLLLMDLLLLMMDMLLLDLLLLMMMLLLLLDMMMMDLLMLDDLMLMMMDLMLLMMMLLL	a Augus Cuangus ang ang Augus Cacangus ang ang ang ang ang ang ang ang ang ang	$\begin{smallmatrix} 4 & 11 & 1 & 5 & 1 & 1 & 2 & 2 & 1 & 1 & 1 & 2 & 2 & 1 & 1$	124 125 133 124 132 123 121 123 121 125 130 129 136 131 135 137 131 129 120 134 124 132 130 128 129 130 128 129 130 128 129 130 128 129 130 128 129 130 131 129 130 131 131 131 135 137 137 137 137 137 138 139 130 130 130 130 130 130 130 130 130 130	180 184 194 184 191 194 178 171 175 190 195 198 197 183 188 197 172 191 187 188 183 180 191 197 185 180 181 187 189 191 187 189 189 189 189 189 189 189 189	146 135 145 139 144 146 142 137 147 149 151 158 140 145 150 154 144 145 144 145 146 147 148 146 147 148 147 148 149 149 149 149 149 149 149 149 149 149

			F	EMALE	S.						F	EMALES	8.		
No.	Colo Chara		of Nose.	Stature.		Cranial Characte		No.		our acter.	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B
141 142 143 144 145 146 147 148 149 151 152 153 154 155 166 167 168 169 170 171 172 173 174 177 178 177 178 182 183 184 185 186 187 189 199 199 199 199 199	D D D D M M D M M M M M D D M M M M D D M M M M D D M M M M D D M M M M M D M		ana Jan Janananan Canadana Janananan Janananananananananananana	4 8 2 5 1 4 9 8 9 1 1 5 5 1 1 0 0 0 4 10 1 0 5 5 1 1 4 5 5 5 5 6 6 5 5 5 5 6 6 5 5 5 5 6 5 5 5 6 6 5 5 5 6 6 5 5 5 6 6 5 6 5 6 5 6 6 5 6 6 5 6	127 136 127 131 125 126 126 126 127 127 130 131 128 131 128 131 129 132 131 132 127 131 128 131 129 129 131 131 128 131 129 129 131 131 128 131 129 131 131 129 131 131 128 131 129 131 131 132 131 131 132 131 131 132 131 131	187 196 182 190 189 175 188 181 183 173 191 185 192 190 192 190 192 190 192 190 192 190 192 190 192 190 192 190 192 183 185 183 187 189 189 189 189 189 189 189 189 189 189	143 149 148 145 146 142 137 138 146 142 139 145 148 143 154 144 145 145 147 148 149 140 140 140 141 141 141 141 145 146 140 141 141 141 141 141 141 141 141 141	195 196 197 198 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 229 223 224 225 226 227 228 229 230 231 232 233 234 235 234 245 246 247 248	M M M M M M M M M M M M M M M M M M M	LMLMMLMMLLLLLLLLLL	an fanananananananananananananananananan	4 8 4 10 3 3 4 11 4 10 5 3 4 11 4 10 5 5 5 5 5 5 1 1 1 5 5 5 5 5 5 5 5 5	125 134 125 135 135 125 134 135 126 123 133 128 124 129 127 130 125 129 127 130 120 125 133 133 131 137 130 120 125 133 133 131 137 130 121 125 130 127 130 131 131 132 133 133 134 137 137 138 139 130 130 130 130 130 130 130 130 130 130	174 191 178 207 188 194 195 183 189 192 193 189 186 190 189 186 191 200 189 183 180 194 196 183 181 198 183 184 199 186 183 181 199 186 183 189 189 189 189 189 189 189 189 189 189	19

				V	///.—E	Banf	f Di	stric	et A	ls <i>y</i>	lun	ı.			
			F	EMALES							F	EMALE	S.		
No.	Colo Chara		of Nose.	Stature.		Cranial Characte		No.	Col- Chara		of Nose.	Stature	C	Cranial Characte	
	Hair.	Eyes.	Shape of	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H. mm.	L. mm.	B. mm.
1 2 3 3 4 4 5 5 6 6 7 7 8 8 9 9 100 11 11 12 13 14 14 15 16 17 18 12 22 23 24 25 26 27 28 29 30 31	M D M M M D D D D D D D D D D D D D D D	M M M M M M M M M M M M M M M M M M M		$\begin{array}{c} 5 & 5 & 1 \\ 4 & 11 & 0 \\ 5 & 5 & 2 \\ 2 & 6 & 3 \\ 3 & 2 & 5 \\ 5 & 5 & 5 \\ 5 & 5 & 5 \\ 4 & 11 & 2 \\ 4 & 5 & 5 \\ 5 & 4 & 11 \\ 2 & 4 \\ 5 & 5 & 3 \\ 4 & 5 & 2 \\ 3 & 11 & 1 \\ 2 & 4 \\ 5 & 5 \\ 4 & 5 \\ 5 & 5 \\ 4 & 5 \\ 5 & 5 \\ 4 & 5 \\ 5 & 5 \\ 5 & 4 \\ 5 & 5 \\ 5 & 5 \\ 4 & 5 \\ 5 & 5 \\$	136 126 129 120 128 123 137 130 123 135 135 135 125 131 133 125 136 127 127 123 127 127 132 125	183 187 178 182 182 183 183 183 187 189 175 190 181 182 178 186 181 189 174 189 174 189 176 183 185 185 187	152 146 147 142 148 150 143 141 148 152 151 146 149 146 146 151 144 153 148 149 144 150 142 145 151 149	32 33 34 35 36 37 38 39 40 41 42 43 44 45 48 49 50 51 52 53 54 55 57 58 59 60 61 62	D D M D D D D D D D D D D D D D	M D D M M M M M M M D D M M M M D D M M M D D M M D D M M D D M M M D D D M M M D D D M M M D D D M M M D D D M M M M D D D M M M D D D M M M M D D D M M M M D D D M M M M D D D M M M M M D D D M M M M D D D M M M M M D D D M M M M M D D D M M M M M D D D M		5 3 3 3 5 2 4 10 8 8 5 5 5 2 2 1 9 1 1 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	132 139 130 134 131 134 125 130 131 132 135 132 123 138 138 122 123 138 124 129 127 133 131 129	184 189 192 184 188 188 185 197 180 182 176 188 197 182 192 180 189 192 188 184 186 187 189 192 189 192 189 199 199 199 199 199 199 199	149 154 156 146 145 143 147 151 150 152 147 146 147 149 148 147 144 140 146 146 149 152 153

IX.—Elgin District Asylum.

/X	Flain	District	Asylum,
// i —	LIUIII	DISHIGE	MONIMILE

		F	EMALE	S.			FEMALES.									
			Colour Character.		Stature.		Cranial Characte		No.	Colo Chara		of Nose.	Stature.		Cranial Characte	
Hair	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.		
41	L M M M M M M M M M M M M M M M M M M M		5 5 7 6 6 5 2 1 5 5 6 6 5 5 6 6 5 5 5 5 5 5 5 5 5 5 5	131 132 135 123 126 129 132 135 131 137 127 119 129 136 117 134 123 120 134 130 130 135	181 188 200 186 183 180 180 181 180 187 197 188 183 189 184 176 188 182 180 191 185 184 173 179 184	143 149 146 139 144 143 144 145 155 145 155 146 148 151 147 148 144 148 147	66 67 68 69 70 71 72 73 74 75 76 77 78 81 82 83 84 84 85 86 87 88 89	D D D R R D M D D B R	M M M M D M M M M L M M M M M M M M M M		4 11 5 1 5 0 5 2 5 7 4 9 5 5 4 9 5 1 5 0 5 1 5 2 4 11 5 5 5 3 4 10 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1	129 121 124 128 129 124 136 127 127 120 129 129 129 129 123 118 131 123 118 131 128 126 115	179 171 184 188 190 182 195 179 182 186 186 185 169 195 181 183 184 177	142 135 148 145 151 150 145 139 146 144 144 145 129 144 143 149 148 146 143 141 139 142 139		

X.—Fife District Asylum.

			FI	EMALES	•					F	EMALES	S.			
No.	Colour Character.		of Nose.	Stature.	C	Cranial Characte		No.	Col Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
51 52 53 54 57 57 58 59 60 61 62 63 64 66 66 67 77 77 77 77 77 77 77	M M D D M M	DLM LDDL MLLLDLLLDDM LLLDDLLLDM LLLDDLLLDM LLLDDLLLDDLLDM LLLDDLLDM LLLDDLLDM LLLDDLLDM LLLDDLLDM LLLDDLLDM LLLDDLLDM LDLLDM LLLDDLLDM LDLLDDLLD	ananananananananananananananananananan	$\begin{smallmatrix} 4&2&5&4&2&5&5&4&1&0&2&3&9&0&1&4&1&7&4&0&5&4&2&5&2&3&1&3&3&0&6&0&2&3&1&3&2&3&1&0&2&1&1&2&2&0&2&6&1&4&0&4&6&6&4&9&8&3&4&1&1&2&2&0&2&6&1&2&2&2&2&2&2&2&2&2&2&2&2&2&2&2&2&2$	138 126 131 133 130 130 130 131 128 120 136 125 124 128 135 134 130 137 127 129 130 127 127 128 132 130 127 127 128 132 130 127 125 130 127 125 130 127 125 130 127 125 130 131 131 132 126 141 131 137 138 130 133 129 127 136 125 128 130 133 129 131 127 136 125 128 130 130 133 129 131 127 136 130 137 137 138 130 139 127 136 125 128 130 130 131 137 137 138 130 139 127 136 125 128 130 130 131 137 137 138 130 139 127 136 125 128 130 130 130 129 131 127 134	189 179 185 186 184 191 190 186 189 189 180 173 190 190 186 189 185 183 194 189 185 187 179 180 186 185 190 179 180 179 180 179 180 186 185 190 179 181 196 184 185 183 192 181 196 183 192 181 196 182 177 188 183 198 178 189 196 181 181 196 182 197 180 181 181 185 183 198 178 183 198 178 189 181 181 181 181 181 181 181 181 18	152 149 141 145 142 153 144 142 150 151 145 146 145 146 145 147 138 149 142 150 145 144 140 143 145 147 148 149 149 149 149 149 149 149 149 149 149	111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 130 131 132 134 135 136 137 138 139 140 141 142 143 144 145 155 156 157 158 159 160 161 162 163 164 167 168 170	M M M M M M M M M M M M M M M M M M M	LMLDLMDDMLDDMDLDMLLDMLDMMMDDDDLLMMDLDLLLLDLDDLD	anna Annanana Enananananananana Annan Annananananana Annananana	$\begin{smallmatrix} 3 & 3 & 0 & 3 & 0 & 1 & 1 & 8 & 3 & 4 & 0 & 9 & 0 & 5 & 2 & 4 & 0 & 4 & 4 & 4 & 1 & 3 & 9 & 8 & 1 & 2 & 1 & 1 & 3 & 0 & 5 & 1 & 3 & 9 & 1 & 0 & 9 & 0 & 0 & 0 & 4 & 3 & 3 & 1 & 9 & 0 & 2 & 1 & 1 & 1 & 0 & 4 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	131 131 131 134 133 130 128 131 129 135 116 117 137 134 124 124 126 136 125 124 126 128 128 127 128 128 129 120 125 128 121 128 127 128 129 120 120 120 120 120 120 120 120 120 120	190 196 195 188 192 194 187 187 193 187 187 193 187 187 192 186 200 194 181 181 181 181 181 181 181 181 181 18	144 144 144 144 144 144 144 144 144 144

W		4	4 1	
X.—Fit	re <i>Di</i> s	trict i	4SVI	um.

			I	FEMALE	S.			FEMALES.								
No.	Colour Character.		of Nose.	Stature.		Cranial Characte		No.	Cole Chara		of Nose.	Sta	ture.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	II.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.
171 172 173 174 175 176 177 178 180 181 182 183 184 185 186 187 188 189	D M M M M D M D M D M D M D M M M M M M		Wassascasses : Wass	5 5 1 4 11 5 5 3 5 0 5 0 5 0 5 2 5 0 4 11 5 2 2 5 1 4 10 5 2 5 3 4 10 5 0 5 0 4 11	137 127 127 124 134 128 127 128 130 128 130 128 132 121 125 121 125 124 123 124 127	196 188 191 183 184 176 183 189 187 192 188 151 187 189 184 199 185 184 199	150 147 155 133 145 134 147 153 146 153 132 140 138 142 153 145 138 145 138 148 152	191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207 208 209	M D M M M M M M M M M M M M M M M M M M	L L L L M M L M L L L M M L L M M L L M M L L M M M L M	sananana yyanananan	555555555555555555555555555555555555555	3 2 3 1 0 2 0 0 3 3 0 0 11 4 3 2 3 6 0 0 2	127 131 135 123 140 134 127 124 130 128 130 128 130 134 124 132 133 134 134 128	152 187 194 185 195 191 183 187 180 182 182 194 179 195 195 184 183	127 144 138 155 152 141 146 148 143 139 145 149 133 147 148

XI.—Glasgow District Asylum (Gartloch).

		1				
]	FEMALES.		FE	EMALES.		
1 D M S 2 M L S 3 M M C 4 D L S 6 M L S 7 M L S 8 M L S 9 D D S 10 D D S 11 D L S 12 M L S 12 M L S 12 M M S 14 M D S 16 M M S 16 M M S 16 M M S 16 M M S 20 M D S 21 M L S 22 M L S 23 M L S 24 M D S 24 M D S 25 M L S 26 M L S 27 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S 29 M L S	8 4 9 127 193 138 C 4 10 128 188 144 S 5 4 128 180 147 S 4 10 133 192 146 S 5 1 125 165 133 S 5 1 122 189 135 S 5 0 128 187 141 S 5 2 128 186 139 S 5 2 128 186 139 S 5 2 127 178 137 S 5 3 130 191 146 S 5 3 130 191 146 S 5 4 11 122 179 141 S 5 4 11 122 179 141 S 5 3 120 184 135 S 5 1 126 188 144 S 5 1 126 188 146 S 5 1 124 180 141 <	31 D 32 M 33 M 33 M 35 M 36 M 37 D 38 M 39 M 40 M 41 M 42 M 43 M 44 M 45 M 46 M 47 M 48 M 51 M 52 M 51 M 52 M 53 M 54 M 55 M 56 D 58 M 59 D 60 F	M S S S S S S S S S S S S S S S S S S S	4 8 125 5 0 126 5 4 128 5 2 129 5 7 126 5 0 127 5 2 131 5 1 127 5 2 140 4 11 119 5 1 124 5 2 125 5 3 129 5 4 134 5 5 2 133 5 5 2 139 5 4 134 5 5 1 128 5 0 137 6 130 6 1	185 194 193 180 179 181 185 186 183 183 184 193 181 187 182 183 187	153 142 154 141 147 142 140 144 138 138 140 146 138 146 144 145 146 147 144 141 151 144 141 151 144 144 145 146 146 146 147 147 148 149 149 149 149 149 149 149 149 149 149

			FI	EMALES	S						F	EMALES	i.		
No.	Colc Chara		of Nose.	Stature.	C	Cranial haracte		No.	Chara	our acter.	of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape c	ft, in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B
61 62 63 64 65 667 77 77 77 77 77 80 81 82 83 84 85 88 89 99 99 99 99 99 99 99 99 99 99 99	M M M M M M M M M M M M M M M M M M M	MOMMEL: LOOLLIMIN :: MULLILMOMELM LOMMLOLLLO :: LOLMLOOMLM ::LL	ac Ananananana anananananana Anananananana	$\begin{smallmatrix}2&3&1&1&1&1&1&1&1&1&1&1&1&1&1&1&1&1&1&1&$	128 125 127 126 127 127 126 124 132 127 127 133 128 128 129 123 133 131 127 126 129 123 133 131 127 128 129 121 120 121 122 127 128 134 129 129 121 120 121 121 121 122 123 133 133 131 127 128 129 129 120 120 120 121 121 121 122 123 124 125 126 127 128 129 129 120 120 120 120 120 120 120 120 120 120	185 187 186 191 181 188 191 186 198 194 186 185 183 183 183 183 194 170 193 196 188 190 187 187 187 187 187 187 187 187 189 181 180 191 180 191 180 191 180 191 180 191 191 191 191 191 191 191 191 191 19	148 151 142 143 142 140 149 144 145 141 151 141 140 142 141 152 147 138 153 149 144 149 141 140 152 142 141 140 152 142 141 140 152 142 141 141 140 152 142 141 141 141 141 141 141 141 141 14	114 115 116 117 118 119 120 121 123 124 125 126 127 128 129 130 131 131 135 136 137 138 139 140 141 142 143 145 146 147 151 151 156 157 158 159 160 161 162 163 164 165 166	FM MM DM MM MM DM MM DDM MM MM MM MM MM M		Cananananananananananananananananananan	$\begin{smallmatrix} 4 & 10 \\ 5 & 4 & 10 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 3 \\ 9 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 3 \\ 9 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 3 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 3 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 2 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 0 & 1 & 2 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 2 & 10 & 1 \\ 1 & 1 & 2 \\ 2 & 3 & 2 \\ 2 & 10 & 1 \\ 2 & 1 & 2 \\ 2 $	126 132 122 126 130 127 136 139 130 129 131 128 123 128 121 130 129 131 128 127 130 129 131 133 127 134 128 127 127 128 133 126 126 121 133 135 127 128 131 133 127 128 129 131 133 129 131 138 127 128 129 131 133 129 131 133 129 131 133 121 133 122 133 133 123 134 129 131 133 133 128 136 136 137 138 138 138 138 138 138 138 138 138 138	178 182 184 189 183 182 188 185 181 171 182 183 189 183 189 183 189 181 190 181 190 181 190 181 190 181 190 181 190 182 184 191 193 193 194 191 189 190 185 184 191 189 190 185 184 191 189 190 185 184 191 189 190 185 184 191 189 190 185 184 191 185 185 185	1: 1: 1: 1: 1: 1: 1: 1: 1: 1: 1: 1: 1: 1

			F	EMALES	5.			}]	FEMALE	ES		
No.	Colo Chara		of Nose.	Stature.		Cranial Characte		No.	Col Chara		or Nose.	Stature.	(Cranial Characte	
	Hair.	Eyes.	Shape	ft. in	H, mm.	L.	B.		Hair,	Eyes.	Shape	ft. in.	H.	L.	B.
1 2 3 4 4 5 6 7 8 9 101 12 13 14 15 16 17 8 19 20 1 12 22 3 24 25 6 27 8 29 20 20 20 20 20 20 20 20 20 20 20 20 20	MM MM MM MM MM MM MM MM MM MM MM MM MM	MLLLMMDMDDLDMMMDLLDLLLLLMMMDMDLLDMDMLLDLLMMMLMDLLLMMLLDLLMMLLDLLMMLLMLL	annana Annana Annana Annana Annana Annana Annana Annana Annanana Annana	$\begin{smallmatrix} & & & & & & & & & & & & & & & & & & &$	138 137 138 131 129 124 136 138 137 129 134 134 138 135 130 127 125 130 124 128 129 130 132 127 128 129 131 133 129 131 133 129 128 121 131 133 129 125 131 128 127 128 131 132 134 128 127 135 134 128 127 127 135 134 138 127 127 137 138 136 131 138 136 131 138 136 132 130 131 138 136 132 130 131 128 130 131 138 136 132 137 138 136 132 137 138 138 138 139 131 138 138 138 139 131 138 138 138 138 138 138 138 138 138	181 195 190 191 190 187 188 187 184 191 182 189 201 187 184 181 180 194 187 179 183 189 192 181 187 191 188 187 191 188 187 191 188 187 191 188 187 191 191 193 188 187 191 191 193 193 193 193 193 193 193 193	151 143 146 151 143 148 137 149 142 148 145 149 151 145 141 145 141 145 141 147 143 141 147 141 143 141 145 141 147 141 145 141 145 141 145 141 145 141 145 141 145 147 148 149 141 147 148 149 149 149 140 140 140 140 140 140 140 140 140 140	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 86 89 90 91 92 93 94 95 100 101 102 103 104 105 106 107 108 109 109 109 109 109 109 109 109 109 109	D M M D D D M M M M M M M M M M M M M M		annana fananana fananananananananananana	$\begin{array}{c} 4 & 10 \\ 5 & 10 \\ 4 & 10 \\ 4 & 10 \\ 4 & 10 \\ 4 & 10 \\ 5 & 5 \\ 4 & 10 \\ 4 & 10 \\ 5 & 5 \\ 4 & 10 \\ 5 & 2 \\ 4 & 10 \\ 5 & 5 \\ 4 & 10 \\ 5 & 2 \\ 4 & 10 \\ 5 & 2 \\ 4 & 10 \\ 5 & 2 \\ 4 & 10 \\ 5 & 2 \\ 5 & 4 \\ 4 & 10 \\ 5 & 2 \\ 5 & 4 \\ 4 & 11 \\ 5 & 3 \\ 4 & 11 \\ 5 & 5 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 5 & 5 \\ 4 & 11 \\ 5 & 5 \\ 5 & 5 \\ 6 & 5 \\ 6 & 5 \\ 7 & 5 \\$	137 131 134 133 128 132 128 130 134 129 133 130 127 124 123 133 132 128 138 129 131 132 128 138 129 131 132 128 130 129 129 120 130 128 131 128 131 129 129 120 123 128 128 131 129 129 129 120 120 121 121 123 124 129 123 124 129 121 124 129 129 129 129 129 129 129 129 129 129	189 184 187 176 182 190 188 177 180 189 192 187 197 196 198 183 191 182 181 185 189 191 184 184 199 179 181 176 183 185 200 178 180 180 178 191 180 180 178 191 180 180 178 191 186 193 191 190 189	144 144 143 144 144 144 144 144 144 144

			F	EMALE	S.						F	EMALES	S.		
No.	Col Chara		of Nose.	Stature		Cranial Characte		No.	Col Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B
121 1223 124 125 126 127 128 129 131 133 134 141 143 144 144 145 146 147 157 166 166 167 177 177 177 177 177 177 17	M		ananananananananananananananananananan	$\begin{array}{c} 4\ 11\\ 4\ 11\\ 4\ 10\\ 6\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 5\\ 2\\ 2\\ 4\ 10\\ 1\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\ 5\\$	140 140 127 137 124 129 133 131 134 134 139 125 136 127 130 120 124 140 135 136 127 130 129 124 140 135 136 127 130 129 124 140 135 136 129 127 141 130 129 123 129 127 141 130 129 123 129 127 141 134 137 134 136 133 133 133 133 134 139 121 136 138 139 121 136 138 139 121 136 138 139 121 136 138 139 121 136 138 139 121 136 137 134 139 121 136 137 134 139 121 136 139 121 136 136 137 139 129 127 141 134 135 139 128 130 121 136 137 138 139 129 121 134 135 139 121 136 136 137 139 129 138 139 129 138 139 129 138 139 129 139 140 141 141 141 141 141 141 141 141 141	199 190 188 182 180 192 183 178 184 184 184 180 185 176 183 178 178 179 196 187 188 189 188 187 188 188 187 188 188 187 188 188	140 152 143 147 148 153 143 154 144 143 143 150 144 143 143 150 146 148 149 148 149 149 149 149 149 149 149 149 149 149	181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 201 202 203 204 205 206 207 208 209 211 212 213 214 215 216 217 218 221 221 223 224 225 228 229 230 231 232 233 234 235 236 237 238 239 240	D D D D D D M M M D D D D D M M D D D D		a Aachanananananananana Aachanananananananananananananananananana	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	136 138 133 130 123 134 133 135 134 124 125 123 136 127 131 129 124 121 120 134 127 128 127 128 127 128 127 128 131 127 128 131 127 128 131 127 128 131 127 128 131 127 128 131 127 128 137 130 132 136 133 132 136 133 132 136 133 132 136 133 132 136 133 132 136 133 132 136 133 132 136 133 132 138 132 138 139 131 127 129 131 123 136 135 130 129 131 127 129 138 137 130 129 131 123 136 135 128 137 130 129 131 123 136 135 128 137 130 129 138 137 129 138 137 129 138 139 139 130 129 131 123 128 137 129 138 139 139 139 139 130 139 130 130 129 130 130 130 129 130 130 130 129 130 130 130 129 130 130 130 129 130 130 130 130 130 130 130 130 130 130	195 187 174 179 192 185 180 188 189 175 178 185 188 181 195 177 179 186 177 179 186 177 179 186 177 179 188 181 182 189 189 186 175 193 182 184 181 195 185 172 184 181 195 185 172 184 181 195 185 184 181 195 185 184 181 195 185 184 181 195 185 184 181 197 193 188 186 194 187 193 188 186 194 187 193 188 186 194 187 193 188 186 194 186 187 181 179 184 185 179 184 185 179 184	14 14 14 14 14 14 14 14 14 14 14 14 14 1

XII.-Glasgow District Asylum (Lenzie).

			F	EMALES	3.						F	EMALES	S.		
No.	Cole Chara	cter.	of Nose.	Stature.	(Cranial Characte		No.	Cole Chara	cter.	e of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
241 242 243 244 245 247 248 249 251 252 253 254 255 256 257 258 259 260 261 262	D D M M D D M D D D M D D D D D D D D D	D D D M L D D L L D D L L D D L L D D		4 11 4 6 5 0 4 10 5 1 4 8 4 0 5 1 5 2 5 1 5 1 5 0 5 1 5 0 5 0 5 0 5 0 5 0 5 0 5 0 5 0	126 131 127 123 130 125 129 127 132 129 125 133 136 133 129 123 127 128 123 131	190 173 189 187 185 177 186 186 183 187 190 186 182 191 171 184 191 175 194	146 136 142 146 142 141 142 137 148 149 140 143 147 147 150 140 155	263 264 265 266 267 268 269 270 271 272 273 274 275 278 279 280 281 282 283	M M D D D D M M M M D D D D F	M M L D D L M M D D D D D D D L L D D D D	accasasaccasasasasas	5 1 4 11 4 18 4 10 5 1 5 0 5 1 5 2 5 2 5 2 5 1 5 2 5 1 5 0 5 1 5 1 5 0 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1	131 134 137 136 127 133 124 120 124 118 136 130 123 137 123 136 132 124	184 185 182 186 186 181 183 178 184 185 183 188 185 190 183 189 188	150 137 146 144 152 141 142 146 146 145 137 150 147 149 147 148 144 154 144

XIII.—Govan District Asylum.

		Fl	EMA	LES	S.						F	EMALES	S		
1 2 3 3 4 4 5 6 6 7 8 8 9 100 111 12 13 114 15 16 17 18 19 20 21 22 23 24 25	M D D M M D D M M D M M M M M M M M M M		5 5 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	$\begin{array}{c} 2\\ 1\\ 4\\ 11\\ 4\\ 3\\ 3\\ 2\\ 1\\ 2\\ 4\\ 0\\ 0\\ 2\\ 0\\ 1\\ 2\\ 1\\ 3\\ 9\\ 5\\ 2\\ 0\\ 5\\ 0\end{array}$	131 137 129 130 132 130 131 130 129 135 124 129 128 137 129 127 131 135 132 132 135 132 137	189 181 168 178 193 184 184 186 188 178 178 178 178 179 177 185 199 177 185 191 177 198 176 201 181 195	144 153 144 147 143 146 143 142 144 139 146 147 145 154 138 148 148 148 149 148 143 143 143 143 143 143 143	26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50	M D M M M M M M M M M M M M M M M M M M	L D M D L L L L L D M L L M L L L L L M L L L L	SSSSW SCSSSSSSW WSW SWS	5 1 6 0 5 1 5 0 4 0 4 11 4 10 4 11 4 11 5 0 5 3 5 2 4 10 4 9 5 1 5 1 5 2 5 2 4 10 4 11 4 10 4 11 5 1 5 2 5 2 4 10 4 11 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1	131 133 124 139 136 132 130 128 132 129 129 129 123 133 132 127 123 135 125 131 127 132 133 132	195 197 179 185 193 184 192 186 185 171 181 191 186 185 179 181 192 181 179 181 179 181 179 181	149 153 141 146 142 150 142 146 147 149 145 145 147 139 143 134 148 148 148 144 144 144 144

						Gova	n Di	stri	ct A	ls <i>y</i>						
	1		F.	EMALES								EMAI	LES	•		
No.	Colo Chara		Shape of Nose.	Stature.		Cranial Characte	r.	No.	Colo Chara		of Nose.	Statu	ıre.		Cranial Characte	r.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H. mm.	L. mm.	B. mm
51 52 53 54 55 56 66 66 66 66 66 66 67 77 77 7	M D D D D D M M M M M M M M M M M M M M		Constant and and and and and and and and and and	$\begin{matrix} & & & & & & & & & & & & & & & & & & &$	131 125 128 139 130 120 121 132 127 133 126 123 131 128 133 130 132 135 131 130 133 135 131 137 130 133 135 125 131 137 130 133 135 137 137 138 139 139 139 139 139 139 139 139 139 139	179 189 186 199 179 184 186 182 189 181 189 182 189 181 189 182 199 182 199 182 199 182 199 182 191 185 186 186 185 184 181 191 187 188 189 189 189 189 189 189 189 189 189	147 149 140 140 143 149 142 148 146 136 140 144 147 147 147 149 146 148 140 152 155 145 145 145 145 141 144 149 134 141 145 140 140 141 147 147 149 136 140 140 141 147 144 145 140 140 141 147 144 145 140 140 141 147 144 145 140 140 141 147 144 145 140 141 147 144 145 140 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 147 144 145 140 141 149	111 112 113 114 115 116 117 118 119 120 121 123 124 125 126 127 128 130 131 132 133 134 135 136 137 140 141 142 143 144 145 147 148 149 140 151 151 152 163 164 165 166 167 168 169 170	M M D D D M M M M M D D M M M M D D D M M D D D D M M D D D D D M M M M M D D D D D M	L L M L L L L L M D L L L M D L L M L L D D D D	nan Zaran Zaran Sananan nan nan Sana Sana Sana Sana	555555555555555555555555555555555555555	1 10 2 3 4 8 2 3 2 7 0 1 0 2 3 4 5 6 7 0 0 3 9 2 9 2	135 135 135 129 129 140 135 128 131 135 130 130 142 136 129 133 130 134 134 137 138 139 130 131 131 135 131 135 131 135 130 130 130 130 130 130 130 130 130 130	195 179 189 195 186 186 195 187 181 190 192 184 188 193 187 187 187 187 189 190 201 177 192 190 185 184 187 182 190 172 185 186 191 188 183 184 191 188 183 184 191 188 183 184 191 188 183 184 191 188 183 187 187 187 187 187 1885 199 190 184 187 187 187 187 187 1885 199 190 184 187 187 187 187 1886 1883 187 187 1888 1876	144 144 144 144 144 144 144 144 144 144

XIII.—Govan	District	Asvlum.
AIII: GUVUII	DISTIFLE	лоунини

			F	EMALES	S.						F	EM	ALE:	S.		
No.	0							No.	Col Chara		of Nose.	Sta	ture.		Crania Characte	
	Character. No Stature. Character. Stature. H. L. mm. mn				L.	B. mm.		Hair,	Eyes.	Shape	ft.	in.	H.	L.	B. mm.	
171 172 173	M M M	L M L	2222	$\begin{array}{cccc} 5 & 0 \\ 4 & 11 \\ 5 & 1 \end{array}$	128 127 133	184 191 186	147 140 145	180 181 182	M M D	L L D	SSS	5 4 5	5 8 1	135 126 136	183 178 185	146 137 147
174 175 176 177	M M D M	M D M L	SOSS	$\begin{array}{ccc} & \cdots & & \\ 5 & 0 & & \\ 5 & 0 & & \\ 5 & 2 & & \end{array}$	123 130 131 133	179 192 192 185	138 140 147 147	183 184 185 286	M M D M	$egin{array}{c} \mathbf{D} \\ \mathbf{L} \\ \mathbf{M} \\ \end{bmatrix}$	SSSS	5 4 5 4	$\begin{array}{c} 2\\ 9\\ 0\\ 8 \end{array}$	133 137 133 140	190 189 186 189	147 143 143 149
178 179	M M	L L	S	4 9 5 5	129 136	181 185	$\frac{140}{148}$	287	D	M	S	5	3	129	188	148

XIV.—Haddington District Asylum.

	FEMALES	5.				F	EMALES	5.		
1 M L 2 M L 3 M L 4 M L 5 M L 6 D D 7 M M 8 D D 9 D M 10 D L 11 M L 12 M L 13 M D 14 D D 15 M D 16 M M 17 D D 18 M D 19 D M 20 M L 21 D M 22 M L 23 D M 24 R L 25 M M 26 M M 27 M D 28 M L 29 D D 30 M L 31 M L 32 D M 33 M L 34 M L 35 D M 36 M M 37 M L	8 4 10 0 5 5 3 2 2 1 3 5 5 2 2 1 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	144 187 127 178 135 163 130 181 135 186 138 189 137 186 143 185 134 184 139 197 129 180 141 198 141 192 136 189 134 188 128 194 126 181 133 188 128 178 139 183 136 193 138 184 136 191 130 180 138 195 123 181 134 196 129 183 135 185 134 183 135 185 134 183 135 186 135	138 136 149 144 144 150 147 142 150 143 150 149 138 144 143 144 143 144 143 144 143 144 143 144 143 146 143 146 143 146 147 147 148 149 138 146 147 148 149 149 138 149 149 149 149 149 149 149 149	38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 61 62 63 64 65 66 67 68 69 70 71 72 73 74	D M M D M M D M M M D D D D D M M M D D D D D D M M M D D D D D M M M D D D D D M M M D D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D M M M D D D D D D M M M D D D D D M M M D D D D D D M M M D D D D D D M M M D D D D D D M M M D D D D D D M M M D D D D D D D M M M D D D D D D D D D D D D M M M D	Assassassassassassassassassassassassassa	5 3 4 2 2 2 0 7 11 9 4 4 11 9 9 9 11 1 4 4 11 5 5 5 5 5 5 5 5 1 1 5 5 5 5	138 137 128 130 145 137 135 121 127 135 121 127 136 134 133 141 136 137 126 136 131 141 141 141 141 142 133 141 141 135 129 134 132 129 134 132 129 134 135 136 137 136 137 137 137 137 137 137 137 137 137 137	184 192 189 182 184 183 185 178 188 188 180 183 194 180 185 176 192 176 192 176 192 197 196 192 185 185 185 185 186 192 185 185 185 186 187 188 189 189 189 189 189 189 189 189 189	146 143 141 136 142 143 149 146 141 136 142 141 142 151 155 136 145 154 155 155 140 139 155 145 155 147 150 129 136 142 142

				XV.	- <i>In</i> 1	/ern	ess i	Dist	rict	As	sylι	ım.			
			FI	EMALES	•			1			F	EMALES	S.		
No.	Col Chara		of Nose.	Stature.	C	Cranial Characte		No.	Col Chara		of Nose.	Stature.		Cranial Characte	er.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
1 2 3 4 4 5 6 6 7 8 9 10 11 12 13 14 15 16 17 8 19 20 21 22 23 24 25 6 27 28 29 30 31 32 33 34 44 44 45 44 45 51 52 53 54 55 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	DD	D D M M M M M M M M M M M M M M M M M M		$\begin{smallmatrix} 1 & 1 & 9 & 0 & 4 & 1 & 1 & 2 & 0 & 1 & 1 & 2 & 1 & 6 & 1 & 0 & 0 & 3 & 1 & 1 & 3 & 2 & 1 & 3 & 0 & 2 & 1 & 3 & 2 & 2 & 2 & 5 & 1 & 2 & 1 & 2 & 2 & 4 & 4 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5$	111 127 126 132 133 127 129 116 117 125 1227 127 130 120 120 120 120 120 120 120 120 120 12	178 186 193 196 183 187 180 184 180 184 198 191 171 192 180 186 189 187 188 184 179 178 188 184 179 178 188 181 191 179 178 180 187 181 181 191 179 178 180 187 181 181 191 179 178 180 187 181 181 191 179 178 180 187 181 181 181 191 179 178 180 187 181 181 181 181 181 181 181 181 181	141 143 144 149 138 152 139 144 141 145 150 142 150 145 150 145 150 147 153 146 147 153 147 152	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 107 108 109 109 109 109 109 109 109 109 109 109	DD :R :: :: DDDDDD :R :: :D :: DDDD ::M :: DDDDDDDDDD	M M M D D D D D D D D D D D D D D D D D		$ \begin{array}{c} 4\ 11 \\ 4\ 10 \\ 6\ 02 \\ \vdots \\ 4\ 11 \\ 11 \\ 5\ 5 \\ 2 \\ 4\ 11 \\ 11 \\ 11 \\ 2 \\ 02 \\ 2 \\ 11 \\ 10 \\ 2 \\ 11 \\ 10 \\ 2 \\ 2 \\ 3 \\ 10 \\ 10 \\ 2 \\ 3 \\ 10 \\ 10 \\ 2 \\ 3 \\ 10 \\ 4 \\ 10 \\ 3 \\ 3 \\ 6\ 0 \\ 5 \\ 5 \\ 4 \\ 10 \\ 3 \\ 3 \\ 4 \\ 10 \\ 3 \\ 3 \\ 4 \\ 10 \\ 3 \\ 3 \\ 6\ 0 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\$	112 120 129 116 123 131 126 130 126 129 128 149 123 138 127 136 125 131 124 127 128 128 127 128 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 127 128 129 129 129 129 129 129 129 129 129 129	182 171 176 183 192 196 184 191 186 187 175 194 186 197 190 188 187 187 187 187 187 189 184 181 190 180 195 188 181 191 188 181 191 188 188 181 191 188 188	143 139 147 145 152 153 145 150 148 144 144 151 145 150 139 146 150 149 144 141 141 149 149 143 153 144 141 149 149 149 149 149 149 149 149

				XV.	–/nv	ern	ess i	Dist	rict	As	ylu	ım.			
			F	EMALES	· .						F	'EMALES	S.		
No.	Col Chara		of Nose.	Stature.		Cranial Characte		No.	Col Char	our acter.	of Nose.	Stature.	C	Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 144 145 146 147 148 149 150 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178	::M M		Randanananananananananananananananananan	4 11 5 3 4 4 10 5 5 5 3 4 4 9 6 5 5 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	127 132 121 126 119 134 135 130 132 128 139 120 134 121 122 123 134 121 124 121 124 123 134 121 124 125 123 134 126 127 128 129 120 131 121 122 123 134 125 126 127 127 128 129 120 121 121 122 123 124 125 126 127 127 128 129 120 120 121 121 122 123 124 125 126 127 127 127 127 127 127 127 127	186 187 182 191 182 191 190 191 196 199 199 192 173 185 187 188 187 188 187 188 187 189 191 194 189 180 189 191 180 191 181 189 180 190 191 187 188 187 189 189 189 189 189 189 189 189 189 189	140 153 144 152 140 158 150 147 145 152 146 151 146 151 146 151 153 145 145 145 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 146 151 153 147 141 144 154 156 157 167 167 167 167 167 167 167 16	181 182 183 184 185 186 187 188 1890 190 191 192 193 194 195 196 197 198 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 221 223 224 225 223 224 225 226 237 228 229 230 231 232 233 234 235 2340	D M M D C C C C C C C C C C C C C C C C	M M M M M M M M M M M M M M M M M M M	апители Витители по по по по по по по по по по по по по	$\begin{array}{c} 5 & 3 & 5 & 5 & 5 & 5 & 5 & 5 & 5 & 5 &$	131 134 136 128 125 123 128 127 125 134 131 130 125 124 125 132 125 132 127 142 117 142 117 128 130 128 130 127 142 117 130 128 131 128 130 127 142 118 130 127 130 128 131 128 130 127 142 118 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 128 131 128 130 127 130 131 128 131 128 130 131 128 130 130 130 130 130 130 130 130	186 194 187 193 179 190 184 177 185 192 188 195 187 191 190 174 181 180 189 191 192 187 181 180 189 191 192 187 188 191 192 187 188 193 187 188 193 187 188 193 187 188 193 188 193 188 193 188 193 188 193 193 193 193 193 193 193 193 193 193	149 148 143 142 150 144 145 144 146 151 145 149 152 138 147 145 146 150 152 138 147 145 146 150 149 152 138 147 145 146 150 149 141 145 146 150 141 145 146 150 141 145 146 140 146 140 146 140 146 140

				λ	(V	-/nv	erne	ess l	Dist	rict	As	ylι	ım.			
			I	EM	ALE	S.					ì	F	EMALES	5.		
No.	0						No.	Colo Chara		of Nose.	Stature.		Cranial Characte			
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
241 242 243 244 245	D M D D	M M M M	202220	5 5 5 5 5	0 2 2 2 5	135 129 126 134 130	173 185 180 182 195	143 147 146 152 148	246 247 248 249 250	D M M	M L M M D	200000	5 5 4 10 5 1 4 8 4 11	137 128 130 131 139	195 188 180 184 183	150 146 143 148 147

XVI.—Lanark District Asylum.

	FEMALES	3.				F	EMALES	S.		
1 M L 2 D L 3 M M M 4 M L 5 M L 6 D L 7 D M 8 D M 10 M M M 11 M L 12 D M 12 D M 14 M M L 15 R L 16 D L 17 D M 18 M L 19 D M 18 M L 19 D M 20 M L 22 M D 23 M L 22 M D 24 D D 25 D L 22 M D 24 D D 25 D L 28 M L 29 M M L 31 M L 32 M D 34 D M 35 M D 31 M L 32 M D 34 D M 35 M D 31 M L 32 M D 34 D M 35 M D 31 M L 32 M D 34 D M 35 M D 31 M L 32 M D 34 D M 35 M D 36 M L 37 M M M 38 D D 39 F L 40 M M L 41 D M 42 D D 43 M M M 44 M L 45 M L	S	137 191 131 187 128 178 136 187 127 187 124 178 128 181 125 186 127 188 134 194 128 184 130 185 127 183 133 184 127 180 128 188 135 186 137 186 129 189 134 183 130 181 132 184 127 180 128 188 135 186 137 186 129 189 134 183 130 181 132 184 127 183 131 181 132 184 127 183 133 181 132 184 127 183 133 181 132 184 127 183 133 181 133 187 120 195 135 186 140 182 128 185 131 187 142 186 137 188 124 191 128 196 133 188 124 191 128 196 133 188 124 191 128 196 133 188 124 191 128 196 133 188 134 181 135 185 132 173 131 181 133 183 130 179 142 202 129 176 131 188 133 184	151 142 143 151 147 136 151 148 148 142 141 142 144 145 140 145 140 145 141 137 144 139 142 147 147 148 151 148 151 149 149 149 149 149 149 149 149 149 14	46 47 48 49 50 51 52 53 54 55 56 62 63 64 66 67 68 69 77 77 77 78 77 77 77 77 77 77 77 80 81 82 83 84 86 87 88 88 89 89 89 80 80 80 80 80 80 80 80 80 80 80 80 80	D L L D L D M M M M D M M D D L L L L L	sasseRAscassassascassassasAscassasAsca	4 5 4 3 3 2 2 2 1 1 2 3 3 1 1 1 1 3 4 8 8 2 6 9 2 2 2 0 3 3 0 3 2 1 1 3 9 1 2 1 1 3 1 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	133 137 136 143 139 133 130 131 131 133 137 139 136 122 123 121 146 142 128 131 132 132 135 137 139 131 132 132 135 137 139 131 132 132 135 137 139 131 132 132 133 137 139 131 131 132 133 137 139 139 130 130 130 130 130 130 130 130 130 130	182 198 188 202 185 183 190 195 187 187 197 191 177 178 185 199 197 191 195 185 186 190 178 172 183 190 174 185 190 178 185 183 190 178 185 186 188 189 189 189 189 189 189 189 189 189	140 151 146 156 142 148 148 146 150 147 148 138 135 151 150 149 151 145 145 140 144 156 143 137 144 145 140 141 142 142 143 144 156 143 145 146 147 147 148 149 147 148 149 147 148 149 149 147 149 149 149 149 149 149 149 149 149 149

				XI	/1,—1	Land	ırk L	Disti	rict	As,	ylu	m.			
			F	EMALE	S.						F	EMALE	S.		
No.	Col Chara	our acter	of Nose.	Stature.	C	Cranial Characte		No.		lour acter,	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H. mm.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B,
91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 110 111 112 113 114 115 116 117 118 119 120 121 123 124 125 126 127 128 129 131 132 133 134 135 136 137 138 139 140 141 141 142 143 144 145 146 147 148 149 140 141 141 142 143 144 145 146 147 148 149 140 141 141 142 143 144 145 146 147 148 149 140 141 141 142 143 144 145 146 147 148 149 140 140 141 141 142 143 144 145 146 147 148 149 140 140 141 141 142 143 144 145 146 147 148 149 140 140 140 140 140 140 140 140		MLD M L M LD M L M D M LD M LLDLLLD M LLDLLLLD M DLDLLLDDDLLLLDDD M LLL M D M LD M L	ana Sananananana Sananana Sananana Sanananan	$\begin{smallmatrix} 4 & 11 & 1 & 0 & 9 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0$	128 129 131 131 126 132 128 130 132 134 134 127 135 138 129 134 133 133 133 133 129 131 120 131 120 131 121 120 131 121 120 131 121 120 131 121 120 131 131 120 131 131 120 131 131 131 131 131 131 131 131 131 13	193 186 184 177 183 173 185 184 194 190 189 187 188 193 185 187 195 184 188 181 184 188 189 181 193 181 187 195 193 187 195 198 197 198 198 198 198 198 198 198 198 198 198	148 149 138 135 138 146 147 141 146 150 146 145 148 145 144 146 141 145 148 141 145 146 141 145 146 141 145 146 141 145 146 147 146 147 147 146 148 149 140 140 140 140 140 140 140 140	151 152 153 154 155 156 157 158 159 160 161 162 163 164 167 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 188 189 191 192 193 194 195 197 198 199 200 201 202 203 204 206 207 208 209 201 200 201 201 201 201 202 203 204 206 207 208 209 209 200 200 200 200 200 200 200 200	MM DD DD MM DD DM MM DD DM MM DD MM MM M	$\begin{array}{c} D D M D M D L D D L L L M M L L L L L$	ananananananananananananananananananan	$\begin{matrix} 3 & 0 & 2 & 1 & 1 & 1 & 2 & 2 & 0 & 4 & 5 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	149 133 130 126 128 134 135 122 127 131 132 139 136 136 137 131 123 120 140 139 140 139 140 139 140 139 140 139 140 130 127 131 123 120 140 139 140 139 140 130 127 133 131 136 137 138 139 135 126 137 136 131 137 136 137 137 136 137 137 136 137 137 136 137 137 138 139 139 139 139 139 139 139 139 139 139	197 189 188 183 183 184 190 174 184 193 188 185 182 191 180 174 187 198 196 187 179 185 181 188 198 181 185 187 179 185 181 188 198 186 191 181 188 198 186 191 181 181 188 198 186 191 181 181 188 198 186 191 181 181 181 188 198 186 191 181 181 181 188 198 186 191 181 181 181 188 196 191 181 181 181 181 181 188 198 186 191 181 181 181 181 181 181 185 186 191 181 181 181 181 181 181 181 181 181	158 143 147 139 142 143 135 1450 150 141 145 1448 141 148 141 142 151 147 146 143 139 155 150 141 147 152 146 146 145 141 153 145 141 153 144 144 144 144 144 145 147 146 148 145 147 148 148 153 144 144 144 144 148 145 147 144 146 148 145 147 144 148 145 147 144 148 145 147 144 148 145 147 144 148 145 147 144 148 145 147 144 148 145 147 144 141 146 142 155 134 148 145 147 144 141 146 142 155 134 148 145 147 144 141 146 142 155 134 148 145

				X	/IL	.ana	rk C	istr	ict	Asj	/lui	m.			
			F	EMALES	5.						F	EMALES	S.		
No.	Col- Chara		of Nose.	Stature.		Cranial Characte	r.	No.	Col Chara		of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
211 212 213 214 215 216 217 228 229 223 224 225 226 227 228 229 234 241 245 252 256 257 256 267 257 268 259 260 261 262 263 264 267 268 267 268 269 270	M M M M D D D M M D D D M M D D D D M M D D D D D D D D D D D D D M M D D D D D M M D D D D M M D D D D M M D D D D M M D D D D D M M D D D D D M M D D D D D M M D D D D D M M D D D D D D M M D	$\begin{array}{c} \textbf{D} \textbf{L} \textbf{L} \textbf{L} \textbf{L} \textbf{L} \textbf{M} \textbf{M} \textbf{L} \textbf{D} \textbf{L} \textbf{D} \textbf{L} \textbf{D} \textbf{L} \textbf{L} \textbf{L} \textbf{L} \textbf{L} \textbf{L} \textbf{L} L$	Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and an analysis of the Assessed and Assessed	$\begin{array}{c} 3 & 2 & 3 & 1 & 4 & 2 & 0 & 2 & 5 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	131 131 134 130 133 136 125 131 135 134 131 132 139 121 130 131 132 133 128 133 128 133 128 134 126 133 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 120 131 130 130 130 130 130 130 13	192 190 192 195 193 180 186 189 183 186 190 177 190 191 181 190 176 184 185 188 188 198 186 192 194 188 187 190 184 191 181 197 190 184 197 190 184 197 190 184 197 190 184 197 190 184 197 197 189 189 189 189 189 189 189 189 189 189	154 148 147 151 147 143 137 147 140 151 155 140 141 144 147 146 133 152 141 144 140 153 146 140 153 144 148 147 153 144 148 147 153 144 148 147 153 144 145 145 146 147 153 146 147 153 146 147 153 146 147 153 148 149 149 149 149 149 149 149 149 149 149	271 272 273 274 275 276 276 277 281 282 283 284 285 289 291 292 293 294 295 294 295 298 299 300 301 302 303 304 305 307 308 307 308 307 311 312 313 314 315 316 327 328 329 329 329 329 329 329 329 329 329 329		LLLM DD LDD DD MLM MM MD LLLLD DD MM LLM LL	and an an an an an an an an an an an an an	$\begin{smallmatrix} 5 & 11 & 2 & 3 & 1 & 1 & 2 & 3 & 1 & 1 & 2 & 3 & 2 & 1 & 4 & 1 & 2 & 3 & 2 & 1 & 4 & 1 & 2 & 2 & 3 & 2 & 1 & 4 & 2 & 2 & 2 & 3 & 2 & 1 & 4 & 2 & 2 & 2 & 2 & 2 & 2 & 2 & 2 & 2$	132 123 148 142 137 133 125 136 143 126 133 127 129 141 136 129 124 128 139 136 124 138 127 136 128 137 136 137 138 127 138 129 136 137 138 129 130 131 138 129 130 131 131 132 136 137 138 137 138 139 130 130 131 131 132 136 137 138 137 138 139 130 131 131 132 133 134 135 131 131 132 133 134 137 138 139 130 130 130 130 130 130 130 130	181 179 189 191 188 185 188 181 200 191 192 182 189 174 191 188 181 185 177 181 185 177 181 185 195 198 185 187 181 185 185 187 181 185 187 181 185 185 187 181 185 185 186 192 188 187 181 185 185 186 197 181 185 185 185 186 197 181 185 185 185 185 186 197 181 185 185 185 185 185 185 185	149 143 150 144 150 140 157 139 141 153 146 145 151 147 144 150 146 146 135 149 151 152 144 151 149 151 149 151 149 151 149 151 149 141 141 149 140 144 147 140 144 147 145 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 136 143 144 149 139 147 140 151 135 148 142 148

XVI.—Lanark District Asylum.

			F	EM	ALE	S.							FEN	IAL	ES		-
No.	Col- Chara		of Nose.	Sta	ture,	(Cranial Characte		No.	Col Chara	our icter.	of Nose.	Sta	ture.		Crania Charact	
	Hair.	Eyes.	Shape			Н,	L.	В.		Hair.	Eyes.	Shape			H.	L.	B.
	=	<u> </u>		ft.	in	mm.	mm.	min.		_ 	——— E		ft.	in.	mm.	min.	mm.
331 332 333 334 335 336	D D M D	L D L D M	s s s s s s s	5 5 5 4 5	$\begin{array}{c} 2 \\ 3 \\ 0 \\ 2 \\ 10 \\ 2 \end{array}$	129 133 125 131 137 138	183 192 183 189 186 188	146 147 145 148 147 148	346 347 348 349 350 351	M D D M D	L M L M M	www.cw	5 5 4 4 5 4	3 5 11 2 3	133 137 132 131 128 131	185 192 183 179 182 186	140 153 144 146 140 142
337 338 339	D D M	M M M	CSS	5 4 5	3 8 4	135 130 133	193 179 180	147 138 144	352 353 354	M D D	L L L	20.00.00	5 5 4	$\begin{array}{c} 2 \\ 0 \\ 10 \end{array}$	133 132 136	185 188 188	143 141 140
340 341	D	M D	$\frac{s}{w}$	5 5	1	130 130	186 186	146 150	355 356	$_{ m D}^{ m M}$	$egin{array}{c} ar{L} \ L \end{array}$	S	5 5	4 2	121 123	186 191	137 143
342 343	M M	L	W S	5 5	3	133	184 187	140 149	357 358	D D	L	S W	5 5	$\frac{0}{1}$	127 129	175 186	· 145
344 345	D M	$_{ m L}^{ m M}$	S	5 5	$\frac{2}{2}$	127	180 187	148 147	359	M	L	S	5	0	127	180	137

XVII.—Midlothian District Asylum.

		F	EMALES	8.					I	FEMALE	S.		
1 2 3 4 4 5 6 7 7 8 8 9 9 10 11 12 13 14 14 15 16 17 7 28 22 23 24 25 26 27 28 29 33 13 22 33 34 35 35	L M L L L L M L M M D L M L D L D L D L	WWW.caasasasaswassassassassassassassassassass	5 2 3 6 5 5 3 5 6 5 5 3 5 6 5 5 5 1 0 4 10 4 10 4 10 4 10 5 1 1 5 5 2 1 1 1 5 5 2 2 4 11 1 5 5 5 2 2 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	138 135 128 130 141 120 132 130 142 124 133 129 130 135 133 132 124 145 136 142 145 133 132 127 131 129 130 140 125 130 130 141 127 131 129 130 130 135 130 130 130 130 130 130 130 130 130 130	193 193 186 193 186 196 181 188 190 184 177 177 170 182 186 188 187 183 193 187 189 191 191 190 174 180 192 177 175 189 189	152 142 148 152 152 133 133 147 148 145 128 146 145 152 145 144 143 143 143 147 145 138 147 145 138 147 145 138 147 145 138 147	36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 67 68 66 67 68 69 70	L M M M L D L M L L L D M L L L D M L L L D M L L L D M L L L D M L L L D M L L L D M L D L L L D M L D L L L D M L D L L D M L D L L L D M L D L L L D M L D L L L D M L D L L L D M L D L L D M L D L L D M L D L L L D M L D L L D M L D L L D M L D L L D M L D L L D M L D L L D M L D L L D M L D L L D M L D L L D M L D L D		5 2 5 2 5 2 5 5 2 5 5 0 4 10 5 2 5 5 0 5 1 4 5 0 5 3 5 3 4 11 4 10 5 1 4 10 5 2 4 11 5 2 4 11 5 2 5 0 4 11 5 2 5 0 6 1 7 5 0 7 5 0 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1 8 1	127 132 134 127 137 130 123 128 135 126 135 147 126 136 135 126 131 132 133 139 130 131 132 133 130 131 132 133 136 137 137 138 190 181 178 177 182 176 179 187 188 188 175 189 187 180 184 180 181 187 177 177 180 172 188 177 177 188 177 177 186 187 187 187 187 187 188 188 175 188 188 175 189 187 187 188 188 188 188 188 188 188 188	139 145 149 141 137 139 145 142 141 151 128 152 138 136 144 142 145 148 149 146 148 149 146 148	

XVII.—Midlothian	District	Asylum.

			F	EMALES	S.						F	EMALE:	S.		
No.	Col	our acter.	of Nose.	Stature.		Cranial Characte		No.	Col Chara	lour acter.	of Nose.	Stature.		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in:	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B. mm.
71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 89 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106	M M M M M M D D D M M D D M M D D D M M D D M M D D M M M D D M M M D D D M M M D D D M M D D D M M D D D M M D D D D M M D D D D M M D D D D M M D D D D M M D D D M M D D D M M D D D D D M M D D D D D M M D D D D D M D D D D M D D D D M D D D D M D D D D D D M D	D L L L D L L L D M L L L L D M D L L L M M D L D L	a Sasasa Angasa Angasa Angasa angasa	4 11 4 18 5 3 4 7 5 1 4 10 4 11 5 4 5 1 5 1 5 1 5 5 2 5 3 5 1 5 5 2 5 5 1 5 5 2 5 5 1 5 5 2 5 5 1 5 5 2 5 5 1 5 5 2 5 5 1 5 5 2 5 5 1 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 2 5 5 5 5 2 5 5 5 5 2 5 5 5 5 2 5 5 5 5 5 2 5 5 5 5 5 5 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	139 126 138 132 134 132 132 132 127 140 130 126 138 139 145 130 131 133 131 133 131 133 131 133 131 133 131 133 131 133 131 133 131 133 134 137 137 138 139 139 139 139 139 139 139 139 139 139	186 174 186 184 190 198 175 187 189 179 184 190 187 199 187 199 187 199 187 199 187 199 187 191 193 181 181 182 196 188 188 188 188 188 188 188 188 188 18	143 141 146 147 151 148 139 145 148 147 153 137 161 142 148 146 146 146 146 146 146 147 145 143 147 145 143 147 147 145 143 147	107 108 110 111 112 113 114 115 116 117 118 119 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 137 138 137 138 137 138 137 141 142	DD DM F M M DD DD DD BR M M DD DD DD BR M M DD DD DD BR M M DD DD DD DD DD DD DD DD DD DD DD DD	M M M L L L L L D M L L L L D M L D L L L L	and Aracana Concade Concade Sanaconana Racan	5 6 4 11 1 5 5 5 2 1 4 11 1 0 0 9 1 3 5 5 5 5 1 4 4 5 5 5 5 5 1 4 5 5 5 5 5 5	138 144 136 138 136 136 126 136 123 130 130 130 130 144 126 137 140 140 136 137 140 140 136 137 139 126 131 139 126 131 139 131 140 140 130 130 130 130 130 130 130 130 130 13	193 196 186 190 199 183 186 190 173 182 184 184 191 188 193 194 183 184 184 182 192 190 193 189 187 187 188 188 188 188 188 188 188	148 155 148 149 150 151 146 134 146 130 141 150 139 144 144 146 141 150 149 144 146 141 150 140 148 153 147 143 146 139 141 141
				1											

XVIII.—Perth District Asylum.

			Fl	EMALES	5.					 FI	EMALES	S.		
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	M M D F M D M M M M R M D	M D D D L M L D D D M M M	ananananan Eurana	5 4 5 2 5 1 5 0 5 1 1 5 0 0 5 2 4 10 5 5 1 5 5 4 10 5 1 5 5 3	135 140 128 134 132 134 131 124 134 128 136 140 128 129 132	189 191 180 181 188 185 181 182 185 190 181 192 180 182 182	145 150 146 142 148 143 141 138 149 156 146 146 134 145 142	16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	D D D M D M F D M D M R D D M R	acamacamanacama	4 10 4 10 5 1 5 1 4 9 5 5 5 1 4 10 5 0 4 8 5 1 5 0 5 0 5 1	132 131 134 139 132 144 129 128 132 124 136 126 130 135 128	182 185 182 195 198 189 182 180 195 178 183 185 191 181	142 143 143 151 147 149 143 143 147 141 143 142 147

				X	////.	-Per	th D	istr	ict .	Asj	/lui	m.			
			F	FEMALE	S.						F	EMALES	5.		
No.	Cole		of Nose.	Stature.		Cranial Characte	r.	No.	Colo Chara		of Nose.	Stature.		Cranial haracte	r.
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 56 67 68 69	M M M F M M D D D D D D D D D D M M D D D D	M D D L D M M M D D M M D D L M D D L M M M D D L M M D D L M M D D L M M M D D L M M M M	Non : sassasasasasasasasasasasasasasasasasa	5 3 1 5 1 1 5 0 4 5 5 1 1 5 5 4 9 9 5 5 4 4 1 1 1 5 5 3 3 5 5 1 1 1 4 9 9 4 1 1 0 5 5 3 3 5 5 1 1 1 5 5 2 2 5 5 2	134 132 127 132 132 127 133 132 135 134 128 135 139 138 132 141 134 134 134 134 134 134 135 131 134 134 136 137 137 138 139 139 139 139 139 139 139 139 139 139	188 186 198 188 188 185 196 187 191 179 183 176 185 184 189 179 181 176 196 182 189 194 191 176 196 182 180 176 185 187	151 147 146 141 152 139 142 149 151 138 147 148 147 148 147 148 146 147 148 146 147 148 146 147 148 147 148 147 148 147 148 147 148 149 157 149 149 157 149 149 157 149 149 157 149 149 157 149 149 157 149 149 157 149 149 149 157 149 149 149 149 149 149 149 149 149 149	70 71 72 73 74 75 76 77 78 80 81 82 83 84 85 86 87 90 91 91 92 93 94 95 100 101 102 103 104 105	D	M M M M D L D M M M D L D M M M M D L D M M M M	and and and and and and and and and and	$\begin{array}{c} 4 \ 11 \\ 5 \ 10 \\ 4 \ 11 \\ 5 \ 3 \\ 5 \ 3 \\ 5 \ 2 \\ 4 \ 11 \\ 5 \ 5 \\ 5 \ 4 \\ 4 \ 11 \\ 5 \ 5 \\ 5 \ 3 \\ 4 \ 10 \\ 5 \ 5 \\ 3 \\ 4 \ 10 \\ 5 \ 5 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 2 \\ 3 \\ 4 \ 10 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 1 \\ 5 \ 2 \\ 3 \\ 4 \ 10 \\ 5 \ 1 \\ 5 $	135 133 134 140 141 135 152 139 131 134 126 132 133 130 135 130 129 140 136 128 133 139 137 138 129 126 140 128	191 189 189 194 184 182 192 192 184 176 185 174 176 185 185 185 185 185 185 185 185 185 185	153 141 149 151 144 150 147 147 150 144 135 144 145 143 141 143 141 145 146 149 141 159 146 154 159 146 154 159 146 154 159 146 159 146 159 146 159 149 149 149 149 149 149 149 149 149 14

XIX.—Roxburgh District Asylum.

		F1	EMALES	ò.						F	EMA	LE:	3.		
1 D D D D D D D D D D D D D D D D D D D	D D L M L L L M	SSS WSC WSCS	5 3 4 10 4 10 5 3 5 0 5 3 5 1 5 2 5 5 5 0	140 124 138 124 141 134 138 133 139 131	191 180 193 184 180 184 188 186 175 185	144 144 148 148 146 138 148 144 147 149	11 12 13 14 15 16 17 18 19 20	M D R D M M D M M D D	L M L D M L L L L	SSESSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	5 5 5 4 5 5 5 5 5 4	2 1 4 11 1 3 0 4 1 9	129 123 133 126 129 132 136 126 135 128	183 190 185 170 182 194 189 180 183 180	148 142 144 137 146 142 148 139 149

			F	EMALES	S.						F	EMALES	S.		
No.	Cole Chara		of Nose.	Stature.	C	Cranial Characte		No.	Colo Chara		of Nose.	Stature.	(Cranial Characte	
	Hair.	Eyes,	Shape	ft. in.	H.	L.	B. mm.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
21 22 23 24 25 26 27 28 29 30 32 33 33 34 41 42 3 44 44 47 50 51 52 55 56 67 77 78 77 77 78 77 78 78 78 78 78 78 78	M M M M M M M D D D M M M	DMLDDMLDMLDDDLLLLLLMMMMLDLMDDDMLDLMLMLDMLLLLLMMLDDDDMLLLLLL		$\begin{array}{c} 3 \\ 5 \\ 1 \\ 1 \\ 3 \\ 8 \\ 0 \\ 2 \\ 3 \\ 3 \\ 1 \\ 0 \\ 2 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 2 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 1 \\ 1 \\ 0 \\ 1 \\ 1$	129 139 127 133 142 126 138 136 129 133 121 134 133 136 139 134 132 126 137 151 129 135 137 151 129 135 137 151 129 135 137 131 136 130 134 136 130 134 135 139 136 137 131 131 136 137 131 137 131 138 138 139 136 138 139 136 138 139 136 138 139 136 138 139 136 138 138 138 139 130 134 134 136 138 138 138 138 138 139 130 134 134 136 138 138 138 138 138 138 138 138 138 138	179 188 183 189 197 190 180 188 186 195 183 189 197 190 184 186 200 183 192 181 193 183 187 190 184 186 189 189 189 189 189 189 189 189 189 189	142 151 144 142 148 149 149 147 142 143 147 148 146 147 148 153 139 150 146 148 149 153 140 149 144 143 147 148 149 140 141 141 142 143 147 148 149 149 140 140 141 140 141 140 140 140 140 141 140 140	79 80 81 82 83 84 85 86 87 88 89 90 91 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 123 124 125 128 129 130 131 132 133 134 135 136	D D D D D D D D D D D D D D D D D D D	L M D M M L L L L M L L D D D M L L L L	mananananananananananananananananananan	$\begin{matrix} 07302435820001740022224424073245308430344221201236592151324 \\ 55555555555555555555555555555555555$	138 140 146 134 133 145 149 136 131 135 137 135 136 141 135 131 138 148 136 123 139 129 140 133 131 139 126	185 177 187 192 187 186 181 188 183 189 182 187 186 185 189 181 189 188 181 189 189 189 189 189	149 148 141 152 150 143 149 146 144 144 143 138 151 142 144 144 144 144 144 144 144 144 14

XX.—Stirling	District	Aculum
AA.—Suriina	DISTRICT	ASVIUM.

}			F1	EMALES							F	EMALES	5.		
No.	Col Chara		Shape of Nose.	Stature.		Cranial Characte		No.	Col Chara		of Nose.	Stature.		Cranial Characte	
-	Hair.	Eyes.	hape		H.	L.	В.		Hair.	Eyes	Shape		Н.	L.	В.
			<u></u>	ft. in.	mm.	mm.	mm.			<u>—</u>		ft. in.	mm.	mm.	mm.
1 22 3 4 4 5 6 6 7 8 9 10 11 12 13 14 15 16 17 18 19 221 223 224 225 227 228 229 331 332 334 335 336 337 338 340 441 442 443 445 55 55 56 57 58 60	M D D M M M M M M M M M M M M D D D D D		Our Assessment and an analysis	$\begin{smallmatrix}2&1&1&2&2&1&9\\4&1&1&2&2&1&9\\5&5&5&5&5&5$	132 142 143 134 135 139 132 145 137 140 144 143 136 128 131 145 134 134 135 144 138 133 118 133 118 134 135 147 130 134 132 134 135 128 131 132 134 135 130 132 134 135 136 137 137 139 139 139 139 139 139 139 139 139 139	176 186 194 176 181 189 186 194 193 193 191 181 182 177 184 194 194 192 187 189 188 187	146 147 157 143 146 143 145 150 142 151 145 147 154 143 139 136 137 146 150 143 145 147 146 129 148 143 151 147 146 129 148 143 151 147 140 137 140 144 144 144 147 141 143 145 140 149 150 148 150 150 160 160 160 160 160 160 160 160 160 16	61 62 63 64 65 66 67 70 71 72 73 74 75 76 77 78 81 82 83 84 85 88 89 90 91 92 93 94 95 100 102 103 104 105 106 107 108 109 110 110 110 110 110 110 110 110 110	M D D D F R D D M D D M M D D D D D M D D D D D D		SSS No Son Control of the Control of	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	132 134 134 132 134 133 136 136 137 131 139 130 128 131 139 130 128 131 132 133 128 136 140 129 128 138 131 132 133 132 136 137 138 139 130 131 131 132 133 133 134 135 136 137 138 139 130 131 131 132 133 133 134 135 136 137 138 139 130 130 131 131 132 133 134 135 136 137 138 139 130 130 130 130 130 130 130 130	183 184 176 187 179 193 182 187 191 176 187 189 190 180 180 180 180 180 180 180 18	144 146 138 154 141 146 141 151 154 143 144 129 140 145 145 145 147 144 147 144 147 144 147 144 147 146 147 146 147 147 146 147 146 147 147 146 147 147 146 147 147 148 149 149 149 149 149 149 149 149

				XX	S	tirlin	g D	istr	ict .	Asy	lui	n.			
			F	EMALES	5.						F	EMALES	5.		
No.	Cole Chara		of Nose.	Stature.	C	Cranial Characte		No.	Col Chara		of Nose.	Stature		Cranial Characte	
	Hair.	Eyes.	Shape	ft. in.	H.	L.	B.		Hair.	Eyes.	Shape	ft. in.	H.	L.	B.
121 122 123 124 125 127 128 129 130 131 132 133 134 135 134 141 142 143 144 145 150 151 152 153 154 155 156 161 161 162 163 164 165 166 167 170 171 172 173 174 174 175 176 177 178 178 178 179 179 179 179 179 179 179 179 179 179	M D D D D D M M D F M D D M M		acananananananananananananacacang canaganang canagang and garagang ananganang ananganang ananganang	$\begin{array}{c} 21231905002299040122700972621123211262301258391311100211119120331112 \\ 555554555554444454555455545554554554554$	136 135 123 136 132 134 137 135 134 131 130 126 136 125 136 124 136 125 136 124 125 136 124 125 136 125 136 121 136 125 136 127 128 139 129 129 129 139 139 139 139 139 139 139 139 139 13	188 189 180 187 187 192 183 191 192 183 199 182 187 187 188 189 198 186 186 186 186 186 186 186 18	140 150 141 144 145 145 142 143 147 141 143 144 144 142 149 143 144 144 142 149 143 146 147 141 148 140 143 147 151 148 140 141 148 149 141 141 148 149 141 141 141 141 141 141 141	181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 229 231 2224 225 224 225 228 229 230 231 232 233 234 235 236 237 238 239 240	F D D D D D D D D D D D D D D D D D D D	LMDMLDLDD ::LLDDDDMMDDLMDLMDLMDLL ::L ::LLLL ::MMMDDDDDLL	acasasasasasasasasasasasasasasasasasasa	$\begin{smallmatrix} 522311333301109012949902117903611101121133122112222381611100071260022011211331221122222381611100071260020011101111111111111111111$	123 131 133 142 125 135 131 141 145 132 124 125 134 137 134 126 143 138 136 125 137 115 122 132 132 133 140 131 130 131 140 141 141 142 145 137 115 127 126 131 131 131 132 133 134 135 137 136 137 137 138 139 130 130 130 130 130 130 130 130	187 189 179 188 187 193 180 193 177 192 183 187 190 191 187 192 190 181 185 192 190 181 186 181 179 183 179 190 181 183 179 190 181 180 181 180 181 185 190 181 180 181 180 181 180 180 18	142 145 149 144 140 142 142 142 140 143 144 145 140 143 144 145 146 125 144 146 125 146 147 148 147 148 149 140 141 141 141 141 145 146 147 148 149 141 149 141 149 149 141 149 149 149

XX	Stirlina	District	Asylum.
$\Lambda\Lambda : -1$	Sui illig	DIGHTOL	MONIMILI.

			F	EMA	LES							F	'EM	ALE	S.		
No.	Cole Chara		of Nose.	Sta	ture.	,C	Cranial Characte		No.	Cole Chara		of Nose.	Sta	ture.		Cranial Characte	
	Hair.	Eyes.	Shape	ft.	in.	H.	L.	B.		Hair.	Eyes.	Shape	ft.	in.	H.	L.	B. mm.
241 242 243 244 245	R M M D D	D L D D M	nnnnn	4 5 5 5 5	11 0 3 0 3	131 142 134 132 131	186 191 186 178 189	145 149 151 132 147	246 247 248 249 25	F M M D M	L M L D	S W C S W	5 5 4 5 5	5 1 8 1 1	135 139 137 139 138	187 193 177 190 179	147 145 140 149 139

XXI.—Greenock Parochial Asylum.

			F	EMALES	5.					F	EMALES	5.		
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XXII.—Paisley Parochial Asylum.

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APPENDIX II.—TABLES OF CLASSIFIED DATA.

			TABL	E I.—	-Tabli	E OF I	FREQU	ENCIE	s.		
		MA	LES.					FEM	ALES.		
Head Height.	Frequency.	Head Breadth.	Frequency.	Head Length.	Frequency.	Head Height.	Frequency.	Head Breadth.	Frequency.	Head Length.	Frequency.
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TABLE II.—TABLE OF HEAD LENGTHS AND HEAD BREADTHS—4436 Male Inmates. Head Length (Millimetres).

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74	1	T	-	T	T	1			1	1	1	C	-		-	I				1	1	1	1	T	~	T	T	Ī	1	- 1				1	1	1	1	1	1	1	1	1	1	T	1	1	J	T	T	T	-
73	1	1	T	T	1	1			1	I	1	1	1	I	-	I		-	4	1	1	1	T	1	1	1	-1	- 1	1					1	1	1	1	1	l	Τ	1	1	1	1	1	i	1	T	-	Î	r
72		t	I	1	1	1		1	1	T	1	1	1	1	-1	_	1			1	1	1	1	1	T	T	T	7	1					1	i	1	1	1	T	T	T	1	T	1	1	Т	1	1	-1	T	r
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63	-	1	T	T	T	1			ī	T	1	1	-	-	1	I				1	T	1	1	1	1	1	1	- 1	- 1	-			_	1	1	T	10	1	T	1	I	T	1	$\overline{\top}$	1	<u> </u>	L	_	T	·	-
62	\top	T	I	1	1	1			1	T	1	1	T	1	1	1	-		-	_	T	T	1	T	-	1	1	- 1	-	_				1	-	T	1	1	T	T	-	1	1	Ť	1	1	T	_		_	┞
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	125	53	3	31	32	33	2	0 1	000	36	37	38	39	40	41	42	43	7	1 1	2	46	47	8	49	50	51	52	30	54	1 10	200	12	0 10	5 5	300	200	19	62	63	64	65	99	67	89	69	20	71	72	75	194	
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TABLE III.—TABLE OF HEAD LENGTHS AND HEAD HEIGHTS—4436 Male Inmates. Head Length (Millimetres).

Totals		98
ote	$\begin{array}{c} -111 \\ -125 \\ -1$	4436
H		_
228		1
222		1
221		
220		2
219		_
$\frac{213}{218}$		2
217		6
216		3
215		2
214		1
213		7
212		12
$\frac{212}{211}$		18
211	N	
210		27
209		30
208	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	49
207	[53
206	;	61
205		94
$\frac{205}{204}$		106
$\frac{204}{203}$	111111111111111111111111111111111111111	$\frac{100}{150}$
202		172
201	111111111111111111111111111111111111111	190
200		214
199		235
$\overline{198}$		262
197		253
196	1 1 1 1 1 1 1 1 1 1	262
$\frac{190}{195}$	111111111111111111111111111111111111111	$\frac{202}{273}$
194	1	263
193	111111111111111111111111111111111111111	261
192		239
191		194
190	1 1 1 1 1 1 1 1 1 1	185
189	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	166
188	111111111111111111111111111111111111111	150
187	11111111111111111111111111111111111111	$\frac{100}{103}$
	——————————————————————————————————————	
186	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	88
185	111211 Magaagaagaataataaaaaaaaaaaaaaaaaaaaaaaa	78
184	1111111100000400040004000411111101111111	50
183	1	42
182	1141111110000000144444000400014441111111	41
181	111111111111111111111111111111111111111	26
180	711511111111111111111111111111111111111	13
179		9
170		
178		11
177		7
176		4
175		6
174		5
173		1
$\frac{172}{172}$		1
171		
		1
170		6
	$a \circ b \circ a \circ a \circ a \circ a \circ a \circ a \circ a \circ a \circ $	Totals
	1116 1117 1117 1117 1117 1117 1117 1117	ote

TABLE IV.—TABLE OF HEAD HEIGHTS AND HEAD BREADTHS—4436 Male Immates. Head Breadth (Millimetres).

1	<u>v:</u> 1		9
1	Tota	411 2 8 8 8 5 8 8 4 4 4 9 9 11 11 18 8 8 1 9 8 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	443
1	196		_
1	195		
1	194		1
29	175	1	
1	172		
1	$\overline{170}$		2
1	$16\overline{9}$		
466 667 668 668 669 669 670 689 689 689 689 689 689 689 689 689 689	168		3
11	167		
1	$1\overline{66}$		
1	165		13
1	$16\tilde{4}$		
50	163		32
60	162		50
60 1 1 1 1 1 1 1 1 1	$16\widetilde{1}$		
1	$1\overline{60}$		
1	159		124
1	$1\overline{58}$		179
1	157	.	188
1	$15\bar{6}$	111111111111111111111111111111111111111	241
1	$15\overline{5}$	11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
1	154		289
1	$\overline{153}$	111111111111111111111111111111111111111	320
48	152	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
48	$1\overline{51}$	1111111100000000014288248825853500000011111111111111111111111111111	330
48	$1\overline{50}$		
46	149	111111111111111111111111111111111111111	294
46	148°	11111100000480500000400912112460601111011111111111	
15 16 17 17 18 19 19 19 10 10 10 10 10	147	1	230
15 16 17 17 18 19 19 19 10 10 10 10 10	146	1 : - -	177
10 1 1 1 1 1 1 1 1 1	145	1 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 2 - 2	151
43 42 41 41 42 43 44 44 44 44 44 44 44 45 46 47 48 48 48 48 48 48 48 48 48 48 48 48 48	144	၂၂၂ ျခချေပါ ၂၀)၀ ၀ လူမှတ်ခုတ်ဆိုပြုသုပ္ပေသမှာမယ္တေသ ၂၂ ခု ၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂၂	103
1	143	1	
41	142		72
40	141		
39	$\overline{140}$	H	43
38	139		18
37	138		15
36 35 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	137		
35	$13\overline{6}$		
34	135		
33	$13\overline{4}$		
32	133		4
$\frac{30}{29}$	132		
29	130		
24	129		
24	125	→	
23	124		
	123		
EFFERNING NOT NOT THE THE THE THE THE THE THE THE THE TH	i		œ
l <u>l</u> ë		@@@@@@@@@@@@#########################	ota
			Ĕ

TABLE V.—TABLE OF HEAD LENGTHS AND HEAD BREADTHS—3951 Female Inmates. Head Length (Millimetres).

S		
Totals	100 100 100 100 100 100 100 100	3951
207		4
206		1
205		2
204		3
203		4
202	111111111111111111111111111111111111111	17
201	111111111111111111111111111111111111111	18
200		25
199	111111111111111111111111111111111111111	30
198	[50
197	11111111111111111111111111111111111111	46
196	1 1 1 1 1 1 1 1 1 1	79
195	1	91
194		113
193	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	136
192	111111111111111111111111111111111111111	159
$\overline{191}$	148826609338138141111111111111111111111111111111	199
190	1	215
189	100110011000000000000000000000000000000	227
188	10 10 10 10 10 10 10 10 10 10 10 10 10 1	259
187	1 1 1 1 1 1 1 1 1 2 20 20 80 4 0 80 20 20 20 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	272
186	111111111111111111111111111111111111111	244
185	1	261
184	111111111111111111111111111111111111111	247
$\overline{183}$	11111111111111111111111111111111111111	235
182	1 1 1 1 1 2 2 2 2 2	207
181		167
180		153
179	1 1 1 1 1 1 1 1 1 1	127
178		96
177		67
176		48
175	1 1 1 1 1 1 1 1 1 1	35
174		23
173		30
$\frac{170}{172}$		18
171	1 1 1 1 1 1 1 1 1 1	13
$\frac{171}{170}$		8
169		6
168		$\frac{3}{4}$
167		2
166	111111111111111111111111111111111111111	$\frac{-2}{2}$
165		$\frac{\overline{2}}{2}$
$\frac{103}{163}$		<u></u>
161		1
158		1
$\frac{108}{154}$		1
		1
152		1
151		
	1123 1124 1125 1125 1125 1125 1125 1125 1125	Totals
		To

Head Breadth (Millimetres).

TABLE VI.—TABLE OF HEAD LENGTHS AND HEAD HEIGHTS-3951 Female Inmates. Head Length (Millimetres).

Totals	100044481000000000000000000000000000000	21
Lot	111122244442222844222284442222888442222888442222888442228884488118888448484848	3951
207		4
206		1
205		2
204		3
203		4
202		17
201	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	18
$\overline{200}$		25
199		30
198	1 1 1 1 1 1 1 1 1 1	50
197	1	46
196		79
195	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	91
194		113
193	1	136
192		159
191		199
190	22	215
$18\overline{9}$		227
188		259
187	1	272
186		244
185	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	261
184		247
183		235
$1\overline{82}$	111111111111111111111111111111111111111	207
181	1 1 1 1 1 1 1 2 3 3 4 3 3 3 4 3 3 4 3 3	167
180		153
$17\overline{9}$		127
178		96
177	[67
176		48
175	111111111111111111111111111111111111111	35
174	1 1 1 1 1 1 1 1 1 1	23
173	111111111111111111111111111111111111111	30
172		18
171		13
170		8
169		6
168		4
167		2
166		2
165		2
163		1
161		1
158		1
154		1
153		1
151		1
	100 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Totals
		Lo
,		-

TABLE VII -TABLE OF HEAD HEIGHTS AND HEAD BREADTHS-3951 Female Inmates. Head Height (Millimetres).

풀 1		
Totals	11112224444875151111111111111111111111111111111	3951
178		1
177		-
176		=
175		
$\frac{174}{173}$		
$\frac{173}{172}$		
171		
170		
169		
168		_
167		_
$\frac{166}{165}$		1
$\frac{163}{164}$		_
163		1
162		3
161		4
160		4
$\frac{159}{158}$		8
157		$\frac{17}{15}$
156	111111111111111111111111111111111111111	27
155		41
154		59
153		86
152		110
$\frac{\overline{151}}{150}$		$\frac{161}{207}$
149	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\frac{207}{244}$
148		291
147	- - - - - - - - - -	281
146	1	321
145	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	340
$\frac{144}{143}$	111111110008841110008841111111111111111	$\frac{319}{286}$
$\frac{143}{142}$		$\frac{286}{276}$
141	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	220
140	11111111111111111111111111111111111111	167
139		131
138	111111111111111111111111111111111111111	106
137		65
$\frac{156}{135}$	111111111111111111111111111111111111111	$\frac{51}{30}$
134		21
133	111111111111111111111111111111111111111	20
132	111411111111111411141114011111111111111	7
131		6
130		7
129		5
$\frac{128}{127}$	<u> </u>	$\frac{5}{1}$
$\frac{127}{126}$	1111111111111111111111111	1
$\frac{120}{125}$		1
124	111111111111111111111111111111111111111	2
123		1
122		1
	100 100 100 100 100 100 100 100 100 100	Totals
		To

Head Breadth (Millimetres).

TABLE VIII.

TABLE OF HAIR AND EYE COLOURS.

4235 Males and 3708 Females.

			MA	LES.			
		Н	AIR C	COLOU	R.		
		Red	Fair	Medium	Dark	Total	Per cent.
UR.	Light	37	175	1345	346	1903	44.94
ΓO	Medium	20	77	788	497	1382	32.63
00	Dark	9	23	389	529	950	22.43
EYE COLOUR.	Total	66	275	2522	1372	4235	100
1	Per cent.	1.56	6:49	59.55	32.40	100	
			FEM	ALES.			
		Н	AIR C	COLOU	R.		
		Red	Fair	Medium	Dark	Total	Per cent.
UR.	Light	28	72	998	347	1445	38 97
[O]	Medium	46	31	642	564	1283	34.60
00	Dark	15	4	369	592	980	26.43
EYE COLOUR.	Total	89	107	2009	1503	3708	100
	Per cent.	2:40	2.89	54.18	40.53	100	-

TABLE IX.

4401 Males.

Head Length (Millimetres).

		$\mathrm{Up}\mathrm{to}I$	173-177	178—182	183—187	188—192	193—197	198—202	203—207	208—212	213217	218 & over	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72 74	1 2 2 2	1 1 3 6 6 6 - 1 1	149182223166	2 1 6 19 56 90 102 60 19 3 	1 1 3 9 19 83 205 280 217 77 25 5	$\begin{array}{c} 2\\ -1\\ 2\\ 4\\ 15\\ 71\\ 195\\ 374\\ 382\\ 168\\ 66\\ 19\\ -\end{array}$	3 8 47 129 297 327 183 67 5				- - 1 1 - - 1 - 2 - 1	5 3 2 7 32 77 299 691 1221 1209 589 220 44 2
	Totals	7	23	100	358	925	1299	1066	462	136	19	6	4401

TABLE X.

4401 Males.

Head Breadth (Millimetres).

		281-821	133—137	138142	143—147	148—152	153—157	158162	163—167	168-172	173 & over	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72 74	- - 1 - 5 - 3 1 - -	3 1 6 8 6 2	1 2 3 12 33 44 51 30 9 6	2 2 7 24 69 152 212 198 61 25 2	$\begin{array}{c} 1\\ -2\\ 1\\ 9\\ 25\\ 93\\ 265\\ 447\\ 410\\ 195\\ 66\\ 18\\ -\end{array}$	1 — 7 11 64 175 355 382 206 78 13 1	1 1 2 3 25 42 127 155 96 33 7	1 2 5 19 28 18 11 3		1	5 3 2 7 32 77 299 691 1221 1209 589 220 44 2
	Totals	10	26	191	756	1532	1293	493	87	11	2	4401

TABLE XL

4401 Males.

Head Height (Millimetres).

		$U_{\rm p}$ to $II7$	118-122	123-127	128—132	133—137	138—142	143—147	148—152	153—157	158—162	163 & over	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72 74 76		1 5 4 3 8 4 — — — — — — — — — — — — — — — — — —	1 4 3 31 44 46 27 7 5	$\begin{array}{c c} 3 \\ 1 \\ - \\ 11 \\ 11 \\ 22 \\ 84 \\ 154 \\ 232 \\ 187 \\ 57 \\ 21 \\ 2 \\ 1 \end{array}$	2 2 3 3 11 28 97 239 434 446 208 68 12	2 3 13 58 188 342 339 187 80	2 2 16 47 125 151 87 29		$\begin{bmatrix} - \\ - \\ 1 \\ 4 \\ 1 \\ 11 \\ 12 \\ 11 \\ 3 \\ 2 \\ - \end{bmatrix}$		1	5 3 2 7 32 77 299 691 1221 1209 589 220 44 2
	Totals	3	25	168	776	1552	1227	469	125	45	10	1	4401

TABLE XII.

3915 Females.

Head Length (Millimetres).

		${ m Up}$ to 172	173-177	178—182	183—187	188—192	193—197	202-861	203-207	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72 74	2 2 1 6 16 12 13 8 —	2 -1 12 44 57 55 23 6 2 -1	3 4 3 23 94 178 251 131 37 12 3	6 2 10 25 102 315 423 265 81 22 1	1 1 15 78 203 348 257 111 31 3 2	3 -1 4 26 73 127 144 65 11	1 6 20 35 39 23 12 3	2 1 7 4	17 9 17 86 366 860 1253 874 327 90 10 4 2
	Totals	60	203	740	1252	1051	456	139	14	3915

TABLE XIII.

3915 Females.

Head Breadth (Millimetres).

		$\mathrm{Up}\ \mathrm{to}\ \mathit{127}$	128—132	133—137	138-142	143—147	148—152	153-157	158—162	163—167	168-172	173 & оvег	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72	1 - 2 1 2 1 - -	1 1 - 5 7 6 7 2 - -	1 2 4 8 35 47 51 29 6 3	6 4 3 30 105 223 294 166 47 12 1 3	6 1 6 28 140 351 499 337 125 37 4	2 1 4 13 64 193 323 264 104 30 3			1 1 		1	17 9 17 86 366 860 1253 874 327 90 10 4 2
	Totals	7	29	186	894	1535	1002	223	36	2		l	3915

TABLE XIV.

3915 Females.

		$\mathrm{Up} \ \mathrm{to} \ II7$	118-122	123—127	128-132	133-137	138—143	143-147	148—152	Totals
Stature (Inches).	Up to 50 52 54 56 58 60 62 64 66 68 70 72 74	1 1 -3 4 10 4 2 - - - 1	1 2 -7 29 48 58 22 6 	5 1 9 28 111 221 271 143 40 11 2 1	4 3 5 33 133 321 438 298 100 28 3 1	5 2 2 12 69 178 352 271 124 23 1	1 -1 3 17 69 104 108 47 20 3	2 11 23 22 9 7	1 2 3 8 1 1 1	17 9 17 86 366 860 1253 874 327 90 10 4 2
	Totals	26	173	843	1368	1041	373	74	17	3915

TABLE XV.—HEAD LENGTH.—INDIVIDUAL ASYLUMS.

		MALES			FEMALES	
Asylums	Mean	Standard Deviation	Coefficient of Variation	Mean	Standard Deviation	Coefficient of Variation
Aberdeen	193·9 ± ·24	6·19 ± ·17	3·20 + ·09	185.8 + .26	6·60 ± ·18	3.55 ± ·10
Dumfries	196.4 ± .47	$7.34 \pm .33$	3.74 ± .17	$187.1 \pm .34$	6·11 ± ·24	3·27 ± ·13
Dundee	$195.1 \pm .39$	6.82 ± .28	3·49 ± ·14	$185.9 \pm .30$	$6.20 \pm .21$	3·33 ± ·11
Edinburgh	194·3 ± ·32	6.26 ± .23	3·22 ± ·12	$185.3 \pm .27$	5.68 ± ·19	$3.06 \pm .10$
Montrose	194.8 ± .28	$6.60 \pm .20$	3·39 ± ·10	$185.5 \pm .33$	5.94 ± .23	3·20 ± ·12
Argyll	$199.3 \pm .33$	6.72 ± 23	$3.37 \pm .12$	189·0 ± ·29	$5.97 \pm .20$	3·16 ± ·11
Ayr	197·7 ± ·25	5.67 ± .18	$2.87 \pm .09$	188.0 ± .26	$6.01 \pm .18$	3·20 ± ·10
Banff	195.6 ± .46	$6.15 \pm .32$	3·14 ± ·17	$185.3 \pm .45$	$5.26 \pm .32$	2·84 ± ·17
Elgin	194·4 ± ·47	5·81 ± ·33	2.99 ± .17	184·8 ± ·43	$5.98 \pm .30$	3·24 ± ·16
Fife	$195.7 \pm .30$	$6.45 \pm .21$	3·30 ± ·11	187·0 ± ·28	5.99 ± .20	3·20 ± ·11
Glasgow (Gartloch)	195·3 ± ·25	6:24 ± :18	$3.19 \pm .09$	$185.6 \pm .31$	5.96 ± .22	3·21 ± ·12
,, (Lenzie)	193.7 ± .23	$6.51 \pm .16$	3.36 ± .08	186.5 ± .22	5.58 ± .16	2·99 ± ·09
Govan	195.8 ± .27	$6.50 \pm .19$	3·32 ± ·10	185.8 ± .28	5.74 ± .20	3.09 ± ·11
Haddington	194·9 ± ·51	6.21 ± .36	3·19 ± ·19	186.7 ± .47	$5.92 \pm .33$	3·17 ± ·18
Inverness	195·9 ± ·25	6.25 ± .18	3·19 ± 09	187·2 ± ·26	$5.95 \pm .18$	3·18 ± ·10
Lanark	196·2 ± ·21	6.05 ± ·15	3.09 ± .08	187·0 ± ·21	5.94 ± ·15	3·18 ± ·08
Midlothian	194·2 ± ·36	6.01 ± .25	3·10 ± ·13	$185.7 \pm .37$	6.45 ± .26	3·47 ± ·14
Perth	195·3 ± ·34	6.54 ± .24	3·35 ± ·12	$186.6 \pm .40$	$6.09 \pm .28$	3·27 ± ·15
Roxburgh	195·2 ± ·37	6.42 ± .26	3·29 ± ·14	186.0 ± .32	5.50 ± .23	2·96 ± ·12
Stirling	195 · 4 ± · 26	6.72 ± .18	3·44 ± ·09	186.5 ± .25	5.83 ± .18	3·13 ± ·10
Greenock	195.6 ± .42	6.70 ± .29	3·43 ± ·15	185·2 ± ·36	5·31 ± ·25	2·87 ± ·14
Paisley	196·7 ± ·49	6·89 ± ·34	3.21 ± .18	187·1 ± ·44	6·24 ± ·31	3:34 ± :17
General Population	195·5 ± ·07	6·55 ± ·05	3·35 ± ·02	186·5 ± ·07	6·04 ± ·05	3·24 ± ·03

TABLE XVI.—HEAD BREADTH.—INDIVIDUAL ASYLUMS.

	· · · · · · · · · · · · · · · · · · ·	MALES			FEMALES	
${f Asylums}$	Mean	Standard Deviation	Coefficient of Variation	Mean	Standard Deviation	Coefficient of Variation
Aberdeen	152·1 ± ·19	4·94 ± ·13	3·25 ± ·09	145·9 ± ·19	4·93 ± ·14	3·38 ± ·09
Dumfries	$151.3 \pm .39$	$6.07 \pm .27$	4·01 ± ·18	$145.5 \pm .28$	4.89 ± ·19	$3.36 \pm .13$
Dundee	$152.1 \pm .30$	$5.30 \pm .21$	3·49 ± ·14	$145.2 \pm .24$	4.99 ± .17	3·44 ± ·12
Edinburgh	$150.9 \pm .27$	$5.24 \pm .19$	$3.47 \pm .13$	144·3 ± ·24	$5.10 \pm .17$	$3.53 \pm .12$
Montrose	$152.5 \pm .22$	5·18 ± ·16	3·40 ± ·10	$146.9 \pm .31$	$5.57 \pm .22$	3·79 ± ·15
Argyll	$153.1 \pm .27$	5.52 ± ·19	3.61 ± .13	145.8 ± .22	4·49 ± ·15	3.08 ± ·11
Ayr	$152.3 \pm .21$	4.71 ± .15	3·10 ± ·10	145.5 ± .23	$5.32 \pm .16$	$3.65 \pm .11$
Banff	153 · 2 ± · 42	5.57 ± .29	3.64 ± .19	147·4 ± ·33	3 ·83 ± ·23	2.60 ± .16
Elgin	152.5 ± .42	5·30 ± ·30	3·48 ± ·20	145.8 ± .34	4.81 ± .24	3·30 ± ·17
Fife	$151.7 \pm .24$	5·12 ± ·17	3·38 ± ·11	145·8 ± ·24	$5.10 \pm .17$	3·50 ± ·12
Glasgow (Gartloch)	$150.5 \pm .21$	5·18 ± ·15	3·44 ± ·10	143·8 ± ·24	4.61 ± .17	$3.20 \pm .12$
,, (Lenzie)	150·0 ± ·20	$5.59 \pm .14$	3.73 ± .09	144.5 ± .17	4·30 ± ·12	2.98 ± .09
Govan	150·8 ± ·23	$5.56 \pm .16$	3.69 ± ·11	144.6 ± .22	4.48 ± .16	3·10 ± ·11
Haddington	151 ·5 ± ·45	5·48 ± ·32	$3.62 \pm .21$	$144.5 \pm .40$	5.04 ± .28	3·49 ± ·20
Inverness	$152.9 \pm .20$	4·93 ± ·14	3·22 ± ·09	146·7 ± ·19	4·36 ± ·13	2·97 ± ·09
Lanark	$151.5 \pm .18$	5·23 ± ·13	3·46 ± ·09	145·2 ± ·17	4·84 ± ·12	3·33 ± ·08
Midlothian	$150.9 \pm .35$	5·86 ± ·25	3.88 ± .16	144·3 ± ·28	4.91 ± .50	3·41 ± ·14
Perth	152.0 ± .28	$5.32 \pm .20$	$3.50 \pm .13$	145·7 ± ·33	4.96 ± .23	3·41 ± ·16
Roxburgh	$151.2 \pm .31$	5·35 ± ·22	3.54 ± .15	$145.0 \pm .29$	4·98 ± ·21	3·43 ± ·14
Stirling	150.9 ± .21	5.53 ± .15	3.67 ± .10	144·9 ± ·21	4.80 ± ·15	$3.31 \pm .10$
Greenock	151·1 ± ·37	5.90 ± .26	3.91 ± .17	$144.5 \pm .34$	4.97 ± .24	3·44 ± ·16
Paisley	151.0 ± .33	4.74 ± .24	3·14 ± ·16	145·8 ± ·33	4.78 ± .24	3·28 ± ·16
General Population	151·5 ± ·06	5·39 ± ·04	3.26 ± .03	145·3 ± ·05	4·91 ± ·04	3.38 ± .03

TABLE XVII.—HEAD HEIGHT.—INDIVIDUAL ASYLUMS.

			MALES			FEMALES	
Asylums		Mean	Standard Deviation	Coefficient of Variation	Mean	Standard Deviation	Coefficient of Variation
Aberdeen		135·8 ± ·20	5·21 ± ·14	3·84 ± ·10	131·2 ± ·25	6·37 ± ·18	4·86 ± ·14
Dumfries		$135.0 \pm .34$	$5.29 \pm .24$	3·92 ± ·18	129·1 ± ·23	4.03 ± .16	3·12 ± ·12
Dundee		$134.0 \pm .25$	$4.31 \pm .17$	3·22 ± ·13	129.9 ± .21	4.48 ± .15	3·45 ± ·12
Edinburgh		139.0 ± .28	$5.58 \pm .20$	4.02 ± .14	133·4 ± ·25	5:31 ± :18	3.98 ± .13
Montrose		139·2 ± ·25	5.84 ± .18	4·19 ± ·13	$132.1 \pm .36$	6:54 ± :25	4.95 ± ·19
Argyll		$135.2 \pm .23$	$4.71 \pm .16$	3·48 ± ·12	130·0 ± ·20	4.24 ± .14	3·26 ± ·11
Ayr		135·9 ± ·19	$4.18 \pm .13$	$3.07 \pm .10$	129·4 ± ·18	4 ·04 ± ·12	3·13 ± ·10
Banff		$136.0 \pm .40$	$5.43 \pm .29$	3.99 ± .51	130·3 ± ·42	4·94 ± ·30	3·79 ± ·23
Elgin		134·5 ± ·49	$6.06 \pm .34$	4.51 ± .26	128·4 ± ·37	$5.19 \pm .26$	4.04 ± .21
Fife		$135.6 \pm .19$	4·14 ± ·14	3.05 ± .10	$129.7 \pm .22$	$4.75 \pm .16$	3.66 ± .12
Glasgow (Gartle	och)	135·2 ± ·18	$4.46 \pm .13$	3.30 ± .09	$128.7 \pm .25$	$4.79 \pm .18$	3·72 ± ·14
,, (Lenzie	e)	135.5 ± .17	4.74 ± .12	3.20 ± .09	130.9 ± ·19	$4.64 \pm .13$	3·55 ± ·10
Govan		135·7 ± ·21	4.96 ± .15	3.66 ± .11	131·5 ± ·20	4·12 ± ·14	3·14 ± ·11
Haddington		137·2 ± ·57	$6.93 \pm .40$	5.06 ± .30	$134.5 \pm .41$	5·20 ± ·29	3·87 ± ·22
Inverness		135·6 ± ·27	6.73 ± .19	4.96 ± .14	128.0 ± .24	$5.67 \pm .17$	4·43 ± ·14
Lanark		138·3 ± ·18	5·19 ± ·13	3.75 ± .09	131.7 ± .18	5·11 ± ·13	3.88 ± .10
Midlothian		$139.5 \pm .32$	5·36 ± ·23	3.84 ± .16	133.6 ± .33	5.85 ± .23	4·38 ± ·18
Perth		$139.6 \pm .34$	6.43 ± .24	4.61 ± .17	133·3 ± ·26	4·17 ± ·19	3·13 ± ·15
Roxburgh		$138.7 \pm .35$	6.00 ± .25	4·33 ± ·18	134.0 ± .34	5.91 ± .24	4·41 ± ·18
Stirling		139·2 ± ·23	5.93 ± .16	4 · 26 ± · 12	133.6 ± .24	5.61 ± .17	4·20 ± ·13
Greenock		133·8 ± ·29	4.64 ± .20	3·47 ± ·15	128.9 ± .30	4·44 ± ·25	3·44 ± ·17
Paisley	•••	137·2 ± ·28	3.93 ± .50	2·87 ± ·14	132·9 ± ·35	4.94 ± .24	3·72 ± ·18
General Populat	tion	136·7 ± ·06	5·58 ± ·04	4·08 ± ·03	131·0 ± ·06	5·43 ± ·04	4·14 ± ·03

TABLE XVIII.—CEPHALIC INDEX.—INDIVIDUAL ASYLUMS.

			MALES			FEMALES	
Asylums		Mean	Standard Deviation	Coefficient of Variation	Mean	Standard Deviation	Coefficient of Variation
Aberdeen		78·5 ± ·10	2·57 ± ·07	3·27 ± ·09	78·6 ± ·11	2·81 ± ·08	3.58 ± ·10
Dumfries		$77.1 \pm .19$	$3.04 \pm .14$	3.94 ± ·18	$77.8 \pm .15$	$2.66 \pm .11$	3·42 ± ·14
Dundee		$78.0 \pm .16$	$2.76 \pm .11$	3.54 ± .14	$78.1 \pm .13$	$2.74 \pm .09$	$3.50 \pm .12$
Edinburgh		$77.7 \pm .13$	$2.64 \pm .10$	$3.40 \pm .12$	$77.9 \pm .13$	$2.67 \pm .09$	3.43 ± .11
Montrose		$78.3 \pm .12$	2.70 ± .08	3·45 ± ·10	$79.2 \pm .16$	2.89 ± ·11	3.64 ± .14
Argyll		76·8 ± ·13	2.73 ± ·10	3.55 ± .12	77.2 ± .12	2·49 ± ·09	3·22 ± ·11
Ayr		$77.1 \pm .10$	2·34 ± ·07	3·04 ± ·10	77·4 ± ·12	$2.75 \pm .08$	3.56 ± .11
Banff		78·4 ± ·20	2.72 ± .14	3·47 ± ·18	79.6 ± .19	2.24 ± .14	2.82 ± .17
Elgin		78·5 ± ·21	2.60 ± .15	3·31 ± ·19	$78.9 \pm .19$	2.67 ± .14	3·38 ± ·17
Fife		77·6±·12	$2.63 \pm .09$	$3.39 \pm .11$	$78.0 \pm .13$	2.71 ± .09	3·47 ± ·12
Glasgow (Gart	(loch)	77·1 ± ·10	$2.61 \pm .07$	3·38 ± ·10	77.5 ± .14	2.56 ± .10	3:31 ±:12
" (Lenz	zie)	77.5 ± ·10	2.80 ± .07	3.61 ± .09	$77.5 \pm .10$	$2.39 \pm .07$	$3.08 \pm .09$
Govan		77·1 ± ·11	$2.75 \pm .08$	3·57 ± ·11	77.9 ± .12	2·49 ± ·09	$3.20 \pm .11$
Haddington		77·8 ± •22	2.70 ± ·16	3·48 ± ·20	77·4 ± ·21	2.67 ± .15	$3.45 \pm .19$
Inverness		78·1 ± ·10	2.54 ± .07	3.25 ± .09	78·5 ± ·11	2.50 ± .08	$3.18 \pm .10$
Lanark		$77.3 \pm .09$	2.58 ± .06	$3.34 \pm .08$	77.7 ± .09	$2.61 \pm .07$	$3.36 \pm .09$
Midlothian		77·7 ± ·17	2.80 ± .12	$3.61 \pm .15$	77·8 ± ·16	$2.77 \pm .11$	$3.56 \pm .14$
Perth		77·9 ± ·14	2.71 ± .10	3·48 ± ·13	78·1 ± ·18	2.70 ± ·13	$3.45 \pm .17$
Roxburgh	• • •	77·5 ± ·16	2.69 ± ·11	3·47 ± ·14	78·0 ± ·15	2.59 ± .11	$3.32 \pm .15$
Stirling		77·3 ± ·11	$2.79 \pm .08$	3·61 ± ·10	77·7 ± ·11	2.59 ± .08	$3.33 \pm .11$
Greenock		77·3 ± ·18	2.90 ± .13	3.75 ± .17	78·1 ± ·17	2.57 ± .12	$3.29 \pm .17$
Paisley	• • • •	76·8 ± ·18	$2.60 \pm .13$	3·39 ± ·17	78·0 ± ·19	2.67 ± ·13	3·42 ± ·18
General Popul	ation	77.6 ± .03	2·72 ± ·02	3.21 ± .03	78·0 ± ·03	2·67 ± ·02	3·42 ± ·03

TABLE XIX.—STATURE.—INDIVIDUAL ASYLUMS.

		MALES		FEMALES				
Asylums	Mean Inches	Standard Deviation	Coefficient of Variation	Mean Inches	Standard Deviation	Coefficient of Variation		
Aberdeen	66·3 ± ·11	2·78 ± ·08	4·19 ± ·12	61·3 ± ·10·	2·52 ± ·07	4·12 ± ·12		
Dumfries	66·0 ± ·17	2·72 ± ·12	4·12 ± ·19	$61.5 \pm .14$	2·43 ± ·10	$3.95 \pm .16$		
Dundee	65.5 ± .15	2.60 ± .11	3.97 ± .16	$60.9 \pm .12$	2·45 ± ·08	4.03 ± .14		
Edinburgh	65.8 ± .15	$3.03 \pm .11$	4.61 ± .16	$61.0 \pm .12$	2.56 ± .09	4·19 ± ·14		
Montrose	$66.3 \pm .11$	2.60 ± .08	3.93 ± .12	$61.0 \pm .14$	2.53 ± ·10	4·15 ± ·16		
Argyll	66.8 ± .14	2.87 ± ·10	4·29 ± ·15	61.6 ± .15	$2.56 \pm .09$	4·15 ± ·14		
Ayr	65·7 ± ·13	2.86 ± .09	4·35 ± ·14	$60.9 \pm .11$	2.66 ± .08	4·37 ± ·13		
Banff	66 · 4 ± · 22	2.96 ± .15	4·46 ± ·23	$62.1 \pm .22$	2.56 ± .16	.4·13 ± ·25		
Elgin	65·7 ± ·24	$2.96 \pm .17$	4.50 ± .26	62·1 ± ·19·	2.51 ± .13	$4.05 \pm .21$		
Fife	$65.9 \pm .10$	2.24 ± .07	3·40 ± ·11	$61.7 \pm .11$	$2.27 \pm .08$	$3.69 \pm .12$		
Glasgow (Gartloch)	65·3 ± ·12	2.92 ± .08	4·47 ± ·13	$60.7 \pm .15$	2.74 ± ·10	4·52 ± ·17		
" (Lenzie)	64·7±·11	$3.03 \pm .08$	4.68 ± .12	$60.3 \pm .10$	2·45 ± ·07	4·06 ± ·12		
Govan	66 · 2 ± · 13	3.02 ± .09	4.56 ± .13	$61.2 \pm .13$	$2.59 \pm .09$	4·23 ± ·15		
Haddington	66.6 ± .25	$3.05 \pm .18$	4.58 ± .27	$61.7 \pm .21$	2.68 ± .15	4·34 ± ·24		
Inverness	66·4 ± ·10	$2.59 \pm .07$	3.90 ± ·11	$62.0 \pm .11$	2.50 ± .08	4·03 ± ·13		
Lanark	$65.7 \pm .09$	2.64 ± .06	4.02 ± ·10	$61.2 \pm .09$	2.62 ± .07	4·29 ± ·11		
Midlothian	66·2 ± ·15	2.51 ± .10	3.80 ± .16	$61.2 \pm .14$	2.51 ± .10	4·11 ± ·17		
Perth	66·2 ± ·14	2·79 ± ·10	4·22 ± ·15	$61.2 \pm .16$	2:37 ±:11	$3.87 \pm .18$		
Roxburgh	66.5 ± .15	2.62 ± ·11	3.95 ± .16	$61.6 \pm .14$	2·41 ± ·10	$3.90 \pm .16$		
Stirling	65.6 ± ·11	2.74 ± .07	4·17 ± ·11	$60.6 \pm .11$	2.65 ± .08	4·37 ± ·13		
Greenock	65·5 ± ·19	$3.04 \pm .13$	4.63 ± .20	$60.3 \pm .17$	2·43 ± ·12	4·03 ± ·19		
Paisley	65·5 ± ·21	3.01 ± .15	4·59 ± ·23	61·5 ± ·17	2·43 ± ·12	3.95 ± .20		
General Population	65·9 ± ·03	2·84 ± ·02	4·31 ± ·03	61·2 ± ·03	2·58 ± ·02	4·22 ± ·03		

TABLE XX.—H.L.B. PRODUCT.—INDIVIDUAL ASYLUMS.

		MA	LES	FEMALES			
Asylums		Mean cm.3=1 unit	Standard Deviation	Mean cm.3=1 unit	Standard Deviation		
Aberdeen		4008 + 12	319.2+ 8.6	3565 + 13	321.1+ 8.9		
Dumfries		4020 ± 23	363.6 ± 16.3	3517 ± 15	262.6 ± 10.4		
Dundee		3981 ± 18	315.3 ± 12.8	3512 ± 13	274.5 ± 9.3		
Edinburgh		4083 ± 17	338.5 ± 12.1	3573 ± 14	288.7 ± 9.6		
Montrose		4141 ± 15	352.2 ± 10.6	3605 ± 18	329.7 ± 12.8		
Argyll		4132 ± 16	$335 \cdot 2 \pm 11 \cdot 7$	3586 ± 13	260.6± 8.9		
Ayr		4094 ± 13	287.0 ± 9.0	3541 ± 12	270.9 ± 8.3		
Banff		4084 ± 25	340.6 ± 17.9	3564 ± 22	251.7 ± 15.3		
Elgin		3992 ± 27	339.7 ± 19.2	3466 ± 20	280.1 ± 14.2		
Fife		4029 ± 14	304·4 ± 10·0	3542 ± 13	280.5 ± 9.3		
Glasgow (Gart	loch)	3977 ± 12	306.7 ± 8.6	3438 ± 14	266.2 ± 9.9		
" (Lenz		3942 ± 11	323.6 ± 8.1	3531 ± 10	256.8 ± 7.3		
Govan		4012 ± 14	331.5 ± 9.7	3535 ± 12	252.3 ± 8.8		
Haddington		4058 ± 31	373.5 ± 21.8	3633 ± 23	292.3 ± 16.3		
Inverness		4068 ± 14	359.5 ± 10.1	3519 ± 12	284.9 ± 8.7		
Lanark		4114±11	328.2 ± 8.0	3580 ± 10	284.1 ± 7.2		
Midlothian		4093 ± 20	343.5 ± 14.5	3584 ± 18	308.3 ± 12.4		
Perth		4149 ± 19	368.3 ± 13.6	3627 ± 18	272.3 ± 12.7		
Roxburgh	• • •	4098 ± 21	354·1 ± 14·5	3618 ± 17	290.0 ± 12.3		
Stirling		4111 ± 14	361.8 ± 9.8	3615 ± 13	294.0 ± 8.9		
Greenock		3960 ± 21	332.0 ± 14.6	3453 ± 17	257.5 ± 12.3		
Paisley	• • •	4077 ± 21	302.0 ± 15.0	3631 ± 20	286.7 ± 14.2		
General Popula	ation	4055 ± 4	345·0 ± 2·5	3555 ± 3	292·2 ± 2·2		

TABLE XXI.

 $\frac{H}{B}$ Index, $\frac{H}{L}$ Index and L.B. Product.—Individual Asylums.—*Males*.

Asylüms	$\frac{H}{B}$ I	ndex	$rac{ ext{H}}{ ext{L}}$ Is	ndex	L.B. Product mm. ² =1 unit		
	Mean	S. D.	Mean	S. D.	Mean	S. D.	
Aberdeen	89·3 ± ·14	3·63 ± ·10	70·1 ± ·11	2·78 ± ·08	29494± 62	1639 ± 44	
Dumfries	89·3 ± ·26	$4.03 \pm .18$	$68.8 \pm .19$	$2.94 \pm .13$	29746 ± 126	1987 ± 89	
Dundee	88·2 ± ·19	3·37 ± ·14	$68.7 \pm .15$	$2.58 \pm .10$	29696 ± 102	1786 ± 72	
Edinburgh	92·2 ± ·20	3.95 ± .14	$71.6 \pm .15$	2·93 ± ·11	29337 ± 86	1692 ± 61	
Montrose	$91.3 \pm .17$	$3.99 \pm .12$	$71.5 \pm .13$	$3.07 \pm .09$	29725 ± 74	1739 ± 52	
Argyll	88·4±·18	$3.57 \pm .12$	$67.9 \pm .13$	$2.60 \pm .09$	30529 ± 90	1837 ± 64	
Ayr	89·3 ± ·14	3·13 ± ·10	$68.8 \pm .10$	$2.29 \pm .07$	30113 ± 69	1550 ± 49	
Banff	88·9 ± ·29	$3.86 \pm .20$	$69.6 \pm .21$	$2.82 \pm .15$	29990 ± 131	1754 ± 92	
Elgin	88·3 ± ·33	4.08 ± .23	69·2 ± ·24	$3.03 \pm .17$	29651 ± 132	1655 ± 94	
Fife	89·5 ± ·15	3·28 ± ·11	$69.4 \pm .11$	$2.46 \pm .08$	29690 ± 79	1709 ± 56	
Glasgow (Gartloch)	89·9 ± ·14	$3.45 \pm .10$	$69.5 \pm .10$	2.52 + .07	29403 ± 67	1685 ± 47	
" (Lenzie)	90·5 ± ·13	$3.72 \pm .09$	70·0 ± ·09	$2.68 \pm .07$	29061 ± 63	1776 ± 44	
Govan	90.1 + .16	$3.76 \pm .11$	$69.4 \pm .11$	$2.71 \pm .08$	29534 ± 74	1785 ± 52	
Haddington	$90.6 \pm .38$	4.60 ± .27	$70.4 \pm .28$	$3.42 \pm .20$	29546 ± 143	1735 ± 101	
Inverness	88·7 ± ·17	$4.32 \pm .12$	69·2 ± ·13	$3.31 \pm .09$	29974 ± 66	1656 ± 47	
Lanark	$91.4 \pm .13$	$3.75 \pm .09$	$70.5 \pm .09$	$2.72 \pm .07$	29728 ± 58	1679 ± 41	
Midlothian	92.6 ± .24	$4.07 \pm .17$	$71.9 \pm .17$	2·81 ± ·12	29311 ± 105	1767 ± 74	
Perth	91·9 ± ·22	$4.32 \pm .16$	$71.5 \pm .17$	$3.26 \pm .12$	29697 ± 91	1753 ± 65	
Roxburgh	$91.8 \pm .24$	$4.15 \pm .17$	71·1 ± ·18	$3.09 \pm .13$	29514 ± 101	1737 ± 71	
Stirling	$92.3 \pm .16$	4·19 ± ·11	71·3 ± ·12	3·11 ± ·08	29498 ± 70	1808 ± 49	
Greenock	88·7 ± ·23	$3.73 \pm .16$	$68.5 \pm .16$	2.64 ± ·12	29567 ± 116	1871 ± 82	
Paisley	90·9 ± ·22	3·11 ± ·16	69:8±·18	2·51 ± ·13	29712 ± 120	1703 ± 85	
General Population	90·3 ± ·04	3·94 ± ·03	70·0 ± ·03	2·94 ± ·02	29637 ± 18	1765 ± 13	

TABLE XXII.

 $\frac{H}{B}$ Index, $\frac{H}{L}$ Index, and L.B. Product.—Individual Asylums.—Females.

Asylums		$\frac{H}{B}$ I	$rac{\mathbf{H}}{\mathrm{B}}$ Index		ndex	L.B. Product mm. ² =1 unit		
		Mean	S. D.	Mean	S. D.	Mean	S. D.	
Aberdeen		90·0 ± ·17	4·42 ± ·12	70·7 ± ·14	3·49 ± ·10	27118 ± 63	1610 ± 45	
Dumfries		88·8 ± ·19	3·33 ± ·13	69·1 ± ·14	$2.53 \pm .10$	27220 ± 74	1312 ± 52	
Dundee		$89.6 \pm .17$	3.56 ± .12	69·9 ± ·13	$2.72 \pm .09$	27012 ± 75	1569 ± 53	
Edinburgh		$92.5 \pm .19$	4·03 ± ·13	72·1 ± ·14	2.96 ± .10	26755 ± 71	1511 ± 50	
Montrose	1.	$90.0 \pm .25$	4.62 ± ·18	$71.2 \pm .19$	3·47 ± ·14	27269 ± 90	1635 ± 63	
Argyll		89·2 ± ·16	3·27 ± ·11	68·8 ± ·12	2.54 ± .09	27578 ± 71	1474 ± 50	
Ayr		$89.0 \pm .15$	$3.51 \pm .11$	$68.9 \pm .11$	2.50 ± .08	27355 ± 69	1606 ± 49	
Banff		88·4 ± ·29	3:38 ± :20	$70.4 \pm .23$	$2.73 \pm .17$	27329 ± 109	1274 ± 77	
Elgin		88·2 ± ·27	$3.77 \pm .19$	$69.5 \pm .21$	2.94 ± .15	26960 ± 108	1510 ± 76	
Fife	•	$89.0 \pm .17$	3.68 ± ·12	69·4 ± ·13	2.74 ± .09	27287 ± 73	1506 ± 52	
Glasgow (Gartlo	och)	$89.6 \pm .19$	3.60 ± .13	69·4 ± ·15	$2.77 \pm .10$	26699 ± 77	1466 ± 55	
" (Lenzie	9)	90·6 ± ·14	3·44 ± ·10	70·2 ± ·11	$2.65 \pm .08$	26960 ± 55	1378 ± 39	
Govan		91·0 ± ·16	3·28 ± ·11	70·8 ± ·12	$2.53 \pm .09$	26871 ± 70	1425 ± 50	
		$93.1 \pm .31$	$3.97 \pm .22$	$72.1 \pm .23$	2.94 ± .16	26997 ± 122	1541 ± 86	
		$87.2 \pm .17$	$3.87 \pm .12$	$68.4 \pm .13$	3.07 ± .09	27475 ± 62	1447 ± 44	
Lanark		90.8 ± .14	$3.80 \pm .10$	$70.5 \pm .10$	2·88 ± ·07	27156 ± 54	1514 ± 38	
		$92.6 \pm .24$	4·23 ± ·17	$72.0 \pm .19$	3·29 ± ·13	26800 ± 90	1581 ± 64	
		$91.6 \pm .23$	3·46 ± ·16	$71.5 \pm .17$	2.62 ± .12	27192 ± 102	1556 ± 72	
		$92.5 \pm .25$	4.25 ± .18	$72.1 \pm .18$	3·16 ± ·13	26984 ± 86	1478 ± 61	
		$92.3 \pm .17$	4.06 ± .12	$71.7 \pm .13$	$3.08 \pm .09$	27036 ± 64	1491 ± 45	
		$89.3 \pm .24$	3.55 ± .17	69·7 ± ·17	$2.54 \pm .12$	26767 ± 98	1449 ± 69	
Paisley	• • •	$91.2 \pm .26$	3·70 ± ·18	71·1 ± ·20	2·89 ± ·14	27295 ± 108	1548 ± 77	
General Populat	ion	90·2 ± ·04	3.96 ± .03	70·3 ± ·03	3.02 ± .02	27108 ± 17	1537±12	

TABLE XXIII.—HAIR AND EYE TABLE.—ASYLUM PERCENTAGES.—Males.

Asylums		H	AIR	EYES			
Asylulus	Red	Fair	Medium	Dark	Light	Medium	Dark
Aberdeen .	3.42	6.84	33.33	56.41	27:35	51.28	21:37
Dumfries .	00	13.27	83.19	3.54	63.72	24.78	11.50
Dundee .	73	5.84	78.83	14.60	61.31	29.20	9.49
Edinburgh .	2.21	9.94	52.49	35.36	51.93	19:34	28.73
Mankana	2.00	29.20	30.00	38.80	31.20	36.40	32.40
Argyll .	1.05	.00	90.53	8.42	46:32	35.26	18.42
A 7770	86	3.86	76.40	18.88	51.50	32.19	16.31
Danff	00	.00	37:31	62.69	1.49	82.09	16.42
Elgin .	4.92	1.64	22.95	70.49	1.64	78.69	19.67
Tric.	47	4.23	80.75	14.55	55.40	27.70	16.90
Glasgow (Gartloch)	34	5.76	76.61	17.29	49.83	24.41	25.76
" (Lenzie) .		2.70	67.92	28.30	43.67	23.45	32.88
Clares '	1.51	1.51	78.49	18.49	53:58	24.91	21.51
Haddington .	00	4.41	64.71	30.88	72.06	16.18	11.76
T	1.87	3.74	27.10	67.29	11.21	72.43	16:36
Lanark .	1.82	4.16	58.96	35.06	55.58	23.64	20.78
Midlothian .	2.25	11.28	51.88	34.59	63.91	21.05	15.04
Perth .	2.35	13.53	30.59	53.53	21.76	37:65	40.59
Roxburgh .	1.45	7.24	65.22	26.09	67:39	20.29	12:32
Chinling	2.61	10.13	40.20	47.06	39.21	33.01	27.78
Crospool	85	.00	75.42	23.73	52.54	27.97	19.49
Daislass	2.15	.00	78.49	19:36	51.61	30.11	18.28
General Population	1:56	6.49	59.55	32.40	44.94	32.63	22:43

TABLE XXIV.—HAIR AND EYE TABLE.—ASYLUM PERCENTAGES.—Females.

		Н	AIR	EYES			
f Asylums	Red	Fair	Medium	Dark	Light	Medium	Dark
Aberdeen	10.19	3.70	20.83	65.28	16.67	51.85	31.48
Dumfries	.69	4.17	74:31	20.83	54.86	24:31	20.83
Dundee	.00	3.52	66.83	29.65	47.24	32.16	20.60
Edinburgh	1.95	2.93	40.97	54.15	49.75	22.93	27.32
Montrose	5.71	2.86	29.52	61.91	13.33	62.86	23.81
Argyll	.00	2.55	78.06	19:39	38.78	35.20	26.02
Ayr	-47	1.63	78.45	19.51	53.66	26.42	19.92
Banff	4.08	2.04	36.74	57.14	4.08	75.51	20.41
Elgin	13.04	4.35	17:39	65.22	4.35	79.71	15.94
Fife	.48	1.91	73.69	23.92	49.76	24.88	25:36
Glasgow (Gartloch)	.62	4.35	73.91	21.12	50.93	26.09	22.98
" (Lenzie)	.71	1.41	56.89	40.99	37.81	28.97	33.22
Govan	1.08	1.61	66.13	31.18	52.69	19.35	27.96
Haddington	2.70	.00	60.81	36.49	39.19	32.43	28:38
Inverness	8.07	3.76	22.58	65.59	13.98	61.83	$24\ 19$
Lanark	0.84	1.68	54.06	43.42	48.74	26.05	25.21
Midlothian	2.11	1.41	38.73	57.75	44.37	32.39	23.24
Perth	2.80	4.67	42.06	50.47	16.82	46.73	36.45
Roxburgh	1.47	1.47	52.94	44.12	50.73	23.53	25.74
Stirling	3.66	6.10	36.58	53.66	23.17	39.43	37.40
Greenock	.00	3.00	70.00	27.00	39.00	32.00	29.00
Paisley	1.09	6.52	69.56	22.83	44.57	34.78	20.65
General Population	2:40	2.89	54.18	40.53	38.97	34.60	26.43

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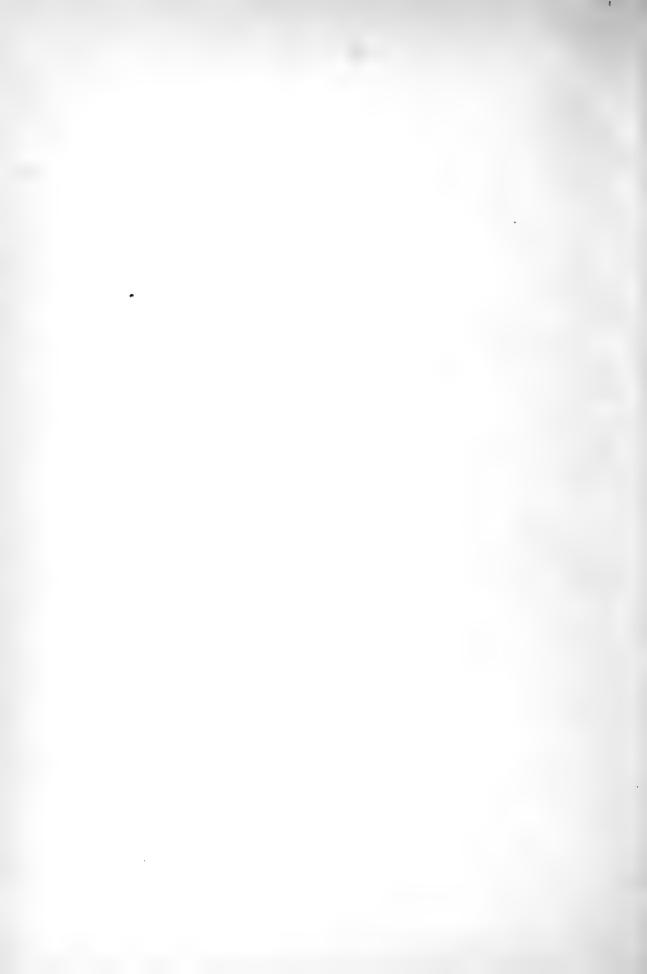
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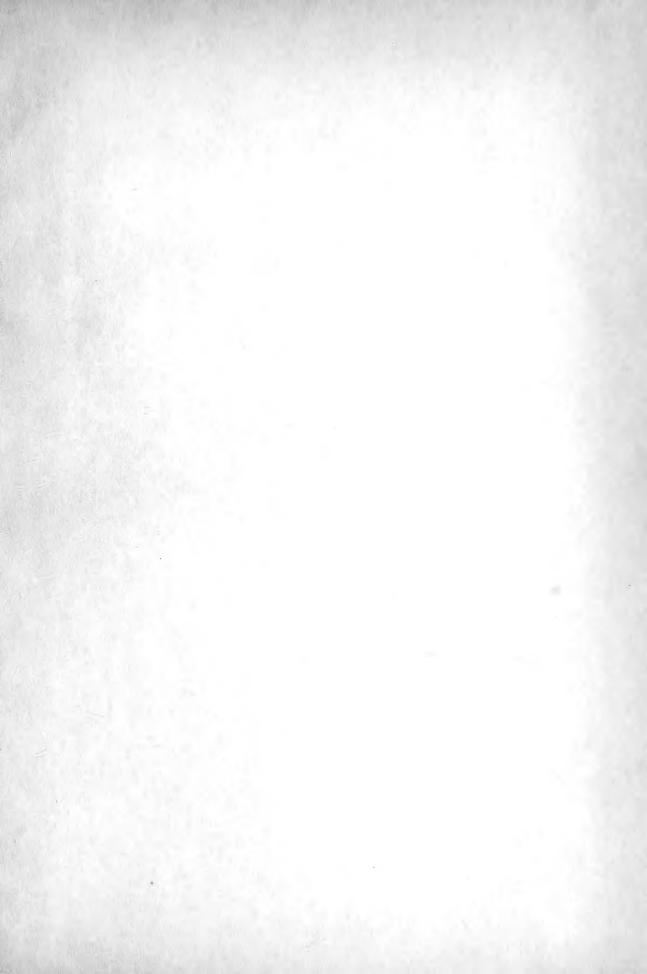
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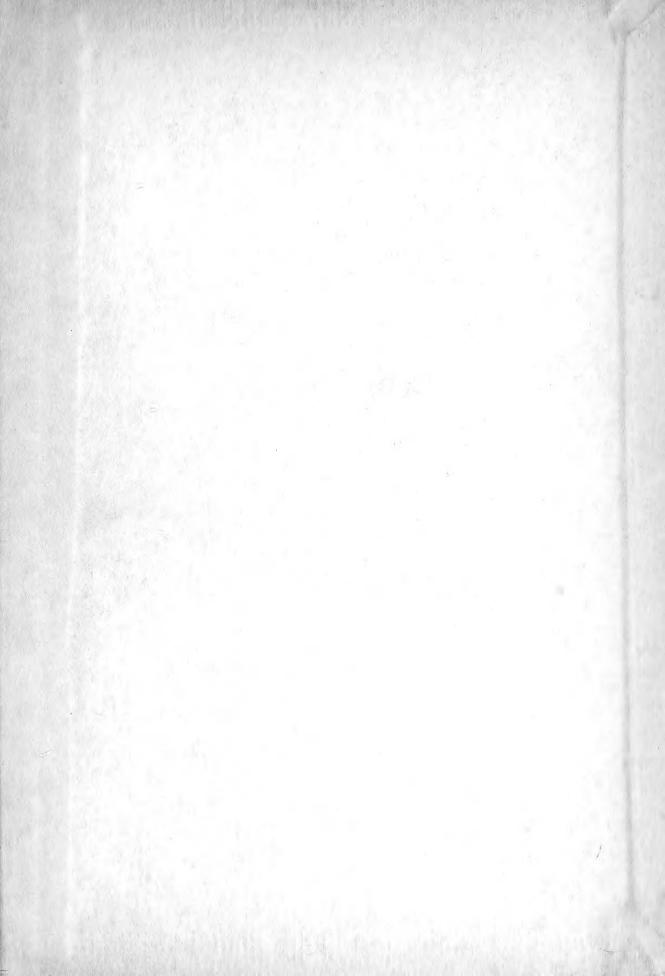
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